

$$X_1 = \beta_0 + \beta_2 X_2 + \beta_3 X_3 + \cdots + \beta_p X_p + \epsilon$$

$$Y = \beta_0 + \textcolor{red}{\beta_1 X_1} + \beta_2 X_2 + \beta_3 X_3 + \cdots + \beta_p X_p + \epsilon$$

$$\widehat{Var}(\textcolor{red}{\beta_1}) = \frac{s^2}{(n-1)\widehat{Var}(X_1)} \times \frac{1}{\textcolor{red}{1 - R_1^2}}$$

$$\textcolor{red}{X_1} = \beta_0 + \beta_2 X_2 + \beta_3 X_3 + \cdots + \beta_p X_p + \epsilon$$

$$\begin{aligned}\widehat{Var}(\textcolor{red}{\beta_1}) &= \frac{s^2}{(n-1)\widehat{Var}(X_1)} \times \frac{1}{\textcolor{red}{1 - R_1^2}} \\ &= \frac{s^2}{(n-1)\widehat{Var}(X_1)} \times \frac{1}{\textcolor{red}{Tolerance}}\end{aligned}$$

$$Y = \beta_0 + \textcolor{red}{\beta_1 X_1} + \beta_2 X_2 + \beta_3 X_3 + \cdots + \beta_p X_p + \epsilon$$

$$\textcolor{red}{X_1} = \beta_0 + \beta_2 X_2 + \beta_3 X_3 + \cdots + \beta_p X_p + \epsilon$$

$$\Sigma u_i = \lambda_i u_i$$

$$\lambda_1, \lambda_2, \cdots, \lambda_p$$

$$u_1, u_2, \cdots, u_p$$

$$\textcolor{blue}{\hat{a}_i} = u_i$$

$$\textcolor{blue}{Var}(Y_i) = \lambda_i$$

$$\phi_i = u_i$$