LAMBDA

MODULE LAMBDA

SYNTAX $Val ::= Id$
$\mid \lambda Id.Exp$ [binder]

SYNTAX $Exp ::= Val$
$\mid Exp \;\; Exp$ [strict]
$\mid (Exp)$ [bracket]

SYNTAX $KResult ::= Val$

RULE $\dfrac{(\lambda X{:}Id.E{:}Exp) \;\; V{:}Val}{E[V \;/\; X]}$

SYNTAX $Val ::= Int$
$\mid Bool$

SYNTAX $Exp ::= Exp * Exp$ [strict]
$\mid Exp \;/\; Exp$ [strict]
$\mid Exp + Exp$ [strict]
$\mid Exp \texttt{ <= } Exp$ [strict]

RULE $\dfrac{I1{:}Int * I2{:}Int}{I1 *_{Int} I2}$

RULE $\dfrac{I1{:}Int \;/\; I2{:}Int}{I1 \div_{Int} I2}$

RULE $\dfrac{I1{:}Int + I2{:}Int}{I1 +_{Int} I2}$

RULE $\dfrac{I1{:}Int \texttt{ <= } I2{:}Int}{I1 \leq_{Int} I2}$

SYNTAX $Exp ::= \texttt{if } Exp \texttt{ then } Exp \texttt{ else } Exp$ [strict(1)]

RULE $\dfrac{\texttt{if true then } E \texttt{ else } —}{E}$

RULE $\dfrac{\texttt{if false then } — \texttt{ else } E}{E}$

SYNTAX $Exp ::= \texttt{let } Id \texttt{ = } Exp \texttt{ in } Exp$

RULE $\dfrac{\texttt{let } X \texttt{ = } E \texttt{ in } E'{:}Exp}{(\lambda X.E') \;\; E}$ [macro]

SYNTAX $Exp ::= \texttt{letrec } Id \;\; Id \texttt{ = } Exp \texttt{ in } Exp$
$\mid \mu Id.Exp$ [binder]

RULE $\dfrac{\texttt{letrec } F{:}Id \;\; X \texttt{ = } E \texttt{ in } E'}{\texttt{let } F \texttt{ = } \mu F.\lambda X.E \texttt{ in } E'}$ [macro]

RULE $\dfrac{\mu X.E}{E[(\mu X.E) \;/\; X]}$

END MODULE