

**COMP90043: Cryptography and security**  
**Week 3: Workshop Questions**

**Preparation:**

- (1) Please revise the Extended Euclid's algorithm before going to the workshop (ExtendedEuclid.pdf).

**Questions: Part A**

- (1) What is a cipher? What does it do? And, in general, how does it go about doing this?
- (2) What is a block cipher and a stream cipher?
- (3) What is a one time pad? Discuss the practical applicability of the scheme in security?
- (4) Now that we have defined our definitions, lets apply this in a more practical setting:
  - (a) What is a symmetric cipher? What are the essential components of a symmetric cipher?
  - (b) What is an asymmetric cipher? How does it differ from a symmetric cipher? Cite at least two differences.
- (5) Lets consider cryptographic keys.
  - (a) What is it and why do we need one?
  - (b) List some of the different types of cryptographic keys used in practice?
  - (c) What are some of the security requirements for storing keys? How is this different when considering both symmetric ciphers and asymmetric ciphers?

**Questions: Part B**

- (1) Solve the following problems using Extended Euclid's algorithm using first principles. Make sure that you understand the process.
  - (a)  $3^{-1} \bmod 7 = \dots\dots\dots$
  - (b)  $5^{-1} \bmod 13 = \dots\dots\dots$
  - (c)  $1473^{-1} \bmod 1562 = \dots\dots\dots$
  - (d)  $73^{-1} \bmod 127 = \dots\dots\dots$
- (2) Try the above questions using any online Extended GCD function (XGCD on magma).  
(<http://magma.maths.usyd.edu.au/calc/>)

- (3) Any number  $a \geq 1$  has a unique factorization given by:  $a = p_1^{a_1} p_2^{a_2} \cdots p_n^{a_n}$ , where  $p_1, p_2, \cdots p_n$  are the first  $n$  primes in the representation of  $a$ . Give an expression for the gcd of two numbers using the above representation of numbers.
- (4) Classical Ciphers
- (a) What is a Caesar Cipher?
  - (b) Explain differences between mono and poly alphabetic ciphers.
  - (c) If you have a Caesar Cipher with key  $k = 4$ . Encrypt "MELBOURNE" using the key.
  - (d) Consider the affine Caesar cipher defined as follows. The encryption function is defined as:  $C = E_{[a,b]}(p) = (ap + b) \bmod 26$ , where  $p$  is the plain text and the tuple  $[a, b]$  is the key.
    - (i) How many different keys are possible with the system?
    - (ii) Derive a decryption function and determine what values of  $a$  and  $b$  are allowed, if this function exists.

### Part C: Homework

The following are a list of questions for students to attempt at home to get a better grasp of the concepts discussed during the workshop.

- (1) Complete any questions which were not completed during the workshop.
- (2) List at least six vulnerabilities listed in [www.cert.org](http://www.cert.org).
- (3) There are also a number of Internet sites dedicated to information security, including [www.cert.org](http://www.cert.org), [www.securityfocus.com](http://www.securityfocus.com), and others. Using these sites, find one vulnerability of each of the following types:
  - (a) Buffer overflow
  - (b) Unintended program function caused by unexpected input
  - (c) Cryptographic weakness
  - (d) Back door / trojan programs
- (4) What is a CVE number?