

Week 5 COMP90043

RSA Exercise

Q1. RSA Parameter creation: Fill in the blanks:

$$p = 13 \quad q = 7 \quad n = 91 \quad \phi(n) = 72$$

Choose $e = 5$.

Repeat for $e = 7$

How to determine d such that $de = 1 \pmod{n}$? Use Euclid's algorithm

$$\text{GCD}(72, 5)$$

$$\text{GCD}(72, 7)$$

$$72 = 14 \times 5 + 2$$

$$72 = ___ \times 7 + 2___$$

$$5 = 2 \times 2 + 1$$

$$2 = 2 \times 1 + 0$$

Back substitution:

$$1 = 5 - 2 \times 2$$

$$1 = 5 - 2 [72 - 14 \times 5]$$

$$1 = 5 [1 + 28] - 2 \times 72$$

Hence $d = 29$

Show that the RSA encryption and decryption functions are inverse operations by trying with some example messages. You can use the package magma online (<http://magma.maths.usyd.edu.au/calc/>).

Q2. Repeat the steps above another example below:

$$p = 23 \quad q = 37 \quad n = ______ \quad \phi(n) = ______$$

Choose $e = 5$.

Choose $e = 61$

$$\text{GCD}(_, 5)$$

$$\text{GCD}(_, 61)$$