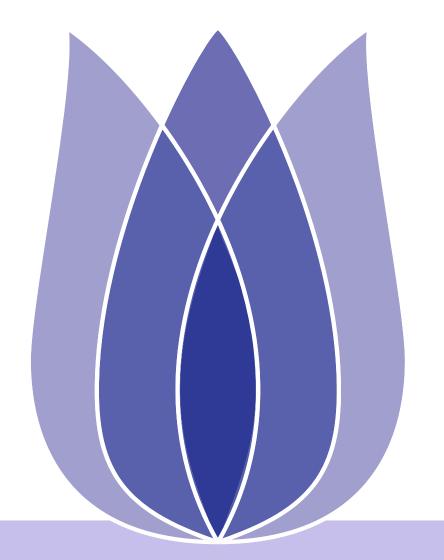
Group Outlying Aspects Mining

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2023-10-22



Overview

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Group Outlying Aspects Mining

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Synthetic Dataset NBA Dataset





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Outlying Aspects Mining

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Outlying Aspects Mining aims to identify the outstanding features of the query object.



- A teacher may be interested in the characteristics that make one student distinctive from others.
- NBA coaches would prefer to find out the strengths and weaknesses of the player (a query object).

Player	3PT%	FTA	FT%	То
P_1	65	4	33	8
P_2	78	1	65	5
P_3	58	6	46	3
P_4	68	1.2	85	6.2
P_5	58	6.2	36	3.4



Outlying Aspects Mining vs Outlier Detection

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Player	3PT%	FTA	FT%	То
P_1	65	4	33	8
P_2	78	1	65	5
P_3	58	6	46	3
P_4	68	1.2	85	6.2
P_5	58	6.2	36	3.4

Outlying Aspects Mining

- Explain the distinctive aspects of the query object.
- The query object may (or may not) be an outlier.

Outlier Detection

- Find out all unusual objects in the whole dataset.
- No explanation on how they are different.



Group Outlying Aspects Mining

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Group Outlying Aspects Mining

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Group outlying aspects mining aims to identify the outstanding features of the group of query object.

- Doctors desire to identify the merits & demerits between a group of cancer patients and normal people.
- NBA coaches are passionate about exploring the obvious advantages & disadvantages of the team.



Figure 1: Medical



Figure 2: NBA-Team



Problem Formalization

Problem Definition

Outlying Aspects Mining

Group Outlying Aspects Mining

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Group outlying aspects mining aims to identify the top-k group outlying subspace $s \subseteq F$ in which the query group G_q is distinctive with other groups.

)efn

- $G = \{G_q, G_2, G_3, ..., G_n\} \Leftrightarrow \text{a set of groups.}$
- $G_q \Leftrightarrow \text{the query group.}$
- Other groups ⇔ comparison groups.
- Each object in the group has d features $F = \{f_1, f_2, ..., f_d\}$.

Group Outlying Aspects Mining



Term Definition

Problem Definition

Outlying Aspects Mining

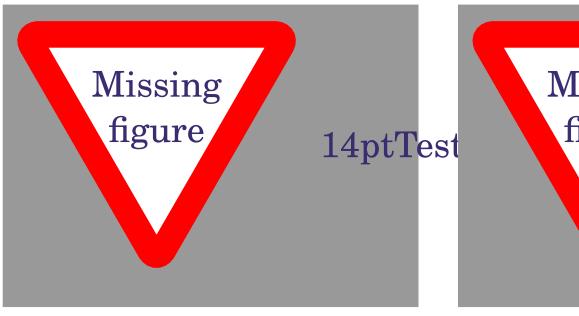
Group Outlying Aspects Mining

Related Work and Challenges

GOAM Algorithm

Evaluation Results

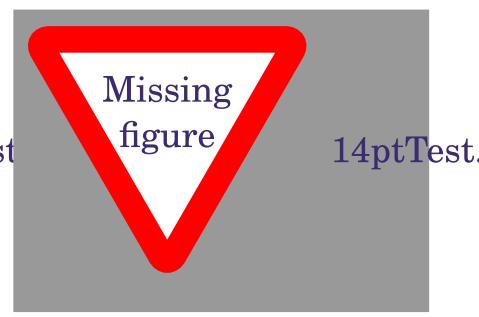
- Top-k group outlying subspaces
 - $\rho_s(\cdot) \Rightarrow$ outlying scoring function.
 - lacktriangle $ho_s(\cdot)$ quantifies the outlying degree of the query group G_q in the subspace s.
 - Order by DESC using scoring function $\rho(\cdot)$ to identify top K group outlying subspaces.







(b) Group Outlying Spaces



(c) Another Subspaces



Term Definition

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Conclusion

- Trivial Outlying Features
 - One-dimension subspaces.
 - G_q 's outlying degree $\rho(\cdot) > \alpha$.

Table 1: $\alpha = 4$

Feature	Outlying Degree
$\{\pmb{F}_1\}$	4.351
$\{\pmb{F}_3,\pmb{F}_4\}$	4.024
$\{\pmb{F}_2,\pmb{F}_4\}$	2.318
$\{\pmb{F}_2\}$	2.002
$\{\pmb{F}_3\}$	1.028

Group Outlying Aspects Mining



Term Definition

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- Non-Trivial Outlying Subspaces
 - Multi-dimension subspaces.
 - G_q 's outlying degree $\rho(\cdot) > \alpha$.

Table 2: $\alpha = 4$

Feature	Outlying Degree
$\{\pmb{F}_1\}$	4.351
$\{\pmb{F}_3,\pmb{F}_4\}$	4.024
$\{\pmb{F}_2,\pmb{F}_4\}$	2.318
$\{\pmb{F}_2\}$	2.002
$\{\pmb{F}_3\}$	1.028

Group Outlying Aspects Mining



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Related Work - Outlying Aspects

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Related Work and Challenges





Related Work - Outlying Aspects Mining

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Related Work - Outlying Aspects Mining

Challenges (1)

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- Existing Methods Feature selection
 - To distinguish two classes: the query point (positive) & rest of data (negative)

Disadvantages

- Positive and negative classes are
 Not balanced.
- Not quantify the outlying degree accurately.
- Not identify group outlying aspects.

Advantages

- **Easy** to operate.
- Resolve dimensionality bias.





Related Work - Outlying Aspects Mining

Problem Definition

Related Work and Challenges
Related Work - Outlying Aspects

Challenges (1)

Mining

GOAM Algorithm

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- Existing Methods Score-and-search
 - Define an outlying score function.
 - Search subspaces.

Disadvantages

- Dimensionality bias.
- Search efficiency is Not high (dataset is large).
- Not identify group outlying aspects.

Advantages

- Quantify the outlying degree correctly.
- ◆ High Comprehensibility.





Problem Definition

Related Work and Challenges

Related Work - Outlying Aspects Mining

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Group Outlying Aspects Mining

- Focus on differences between groups.
- Multiple points.

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Figure 3: Group Outlying Aspects Target

Outlying Aspects Mining

- Concentrates on differences between objects.
- One point.

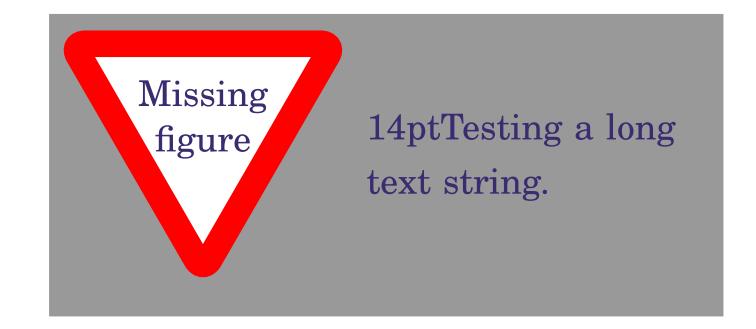


Figure 4: Outlying Aspects Target



Challenges (1)

Problem Definition

Related Work and Challenges
Related Work - Outlying Aspects
Mining

Challenges (1)

GOAM Algorithm

Evaluation Results

- How to represent the group features.
 - Can be affected by outlier values.
 - ◆ Can Not reflect the overall distribution of group features.





Challenges (2)

Problem Definition

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Related Work - Outlying Aspects
Mining

Challenges (1)

GOAM Algorithm

Evaluation Results

- How to evaluate the outlying degree in different aspects.
 - Need design a scoring function when necessary.
 - Adopting an appropriate scoring function (without dimension bias) remains a problem.





Challenges (3)

Problem Definition

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Challenges (1)

GOAM Algorithm

Evaluation Results

- How to improve the efficiency.
 - ◆ When the dimension of the data is high, the candidate subspace grows exponentially.
 - ◆ It will easily go beyond the limits of the computation resources.





Problem Definition

Related Work and Challenges

GOAM Algorithm

Step One - Group Feature Extraction
Step Two - Outlying Degree Scoring
Step Three - Outlying Aspects
Identification

Evaluation Results

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Framework of GOAM algorithm:

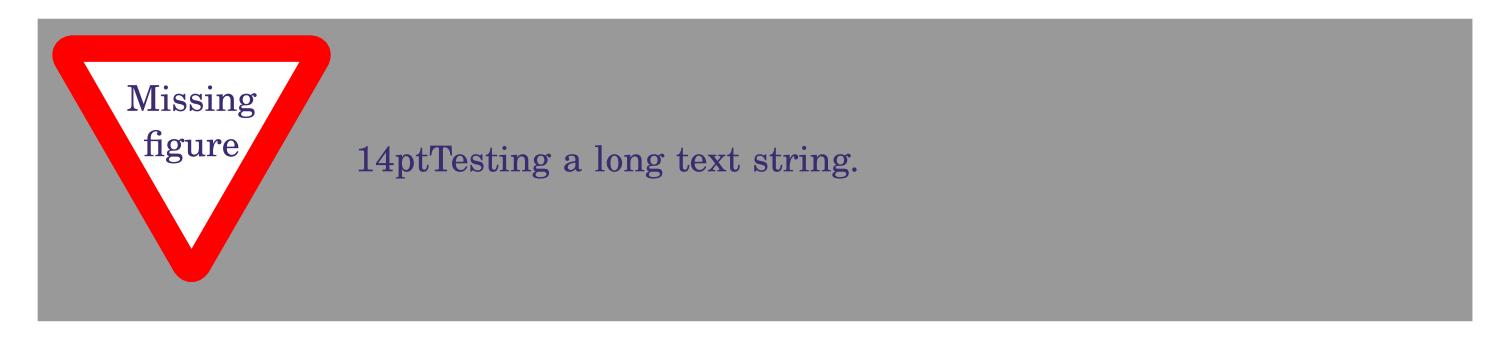


Figure 5: Framework of GOAM Algorithm



Step One - Group Feature Extraction

Problem Definition

Related Work and Challenges

GOAM Algorithm

Step One - Group Feature Extraction

Step Two - Outlying Degree Scoring Step Three - Outlying Aspects Identification

Evaluation Results

Conclusion

Suppose f_1 , f_2 , f_3 are three features of G_q .

$$f_1$$
: { $x_1, x_2, x_3, x_4, x_5, x_2, x_3, x_4, x_1, x_2$ }

$$f_2$$
: { $y_2, y_2, y_1, y_2, y_3, y_3, y_5, y_4, y_4, y_2$ }

$$f_3$$
: { $z_1, z_4, z_2, z_4, z_5, z_3, z_1, z_2, z_4, z_2$ }

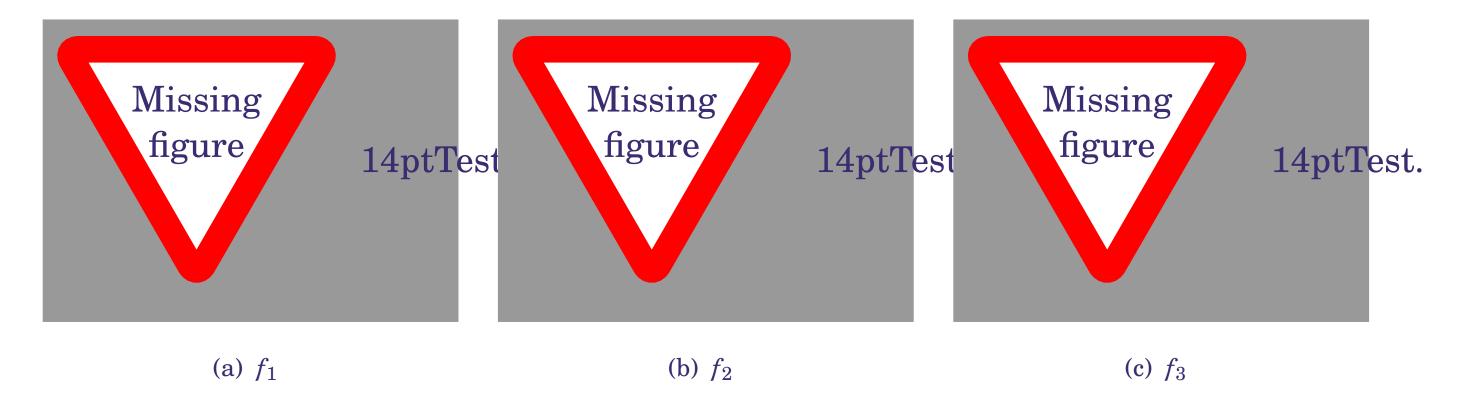


Figure 6: Histogram of G_q on three features



Step Two - Outlying Degree Scoring

Problem Definition

Related Work and Challenges

GOAM Algorithm

Step One - Group Feature Extraction

Step Two - Outlying Degree Scoring

Step Three - Outlying Aspects Identification

Evaluation Results

- Calculate Earth Mover Distance
 - ◆ Represent one feature among different groups
 - ◆ Purpose: calculate the minimum mean distance

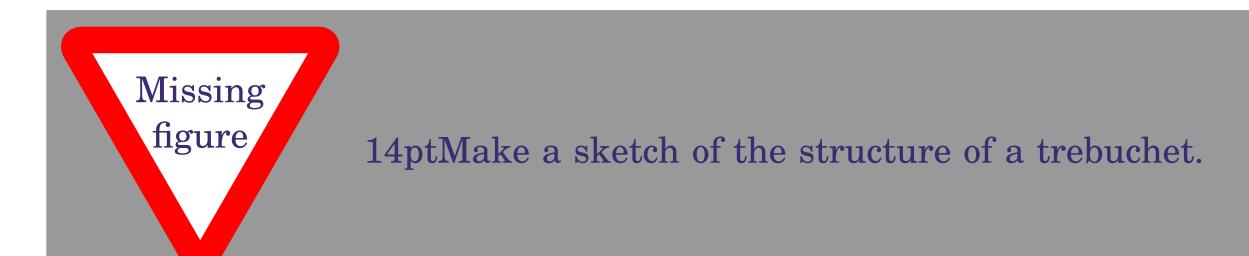


Figure 7: EMD of one feature



Step Two - Outlying Degree Scoring

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Calculate the outlying degree

$$OD(G_q) = \sum_{1}^{n} EDM(h_{q_s}, h_{k_s})$$

- \bullet n \Leftrightarrow the number of contrast groups.
- $h_{k_s} \Leftrightarrow$ the histogram representation of G_k in the subspace s.

Group Outlying Aspects Mining



Step Three - Outlying Aspects Identification

Problem Definition

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Evaluation Results

- Identify group outlying aspects mining based on the value of outlying degree.
- The greater the outlying degree is, the more likely it is group outlying aspect.



Pseudo code

Problem Definition

Related Work and Challenges

GOAM Algorithm

Step One - Group Feature Extraction

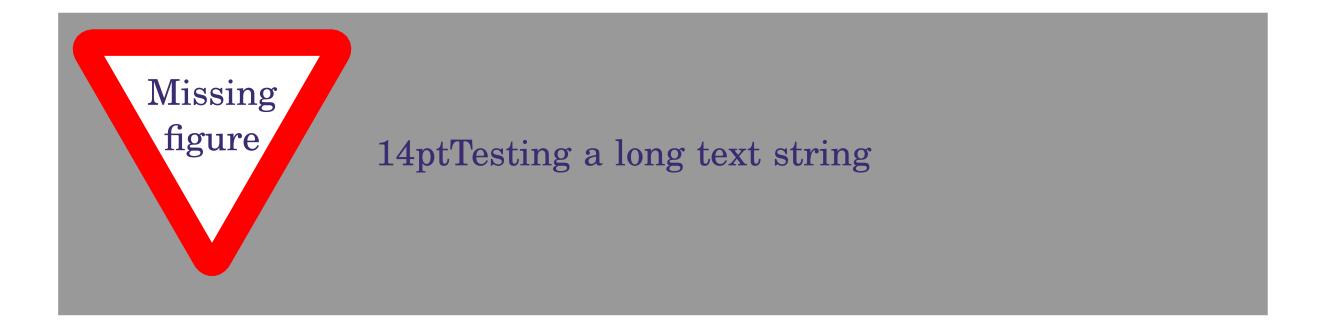
Step Two - Outlying Degree Scoring

Step Three - Outlying Aspects Identification

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Pseudo code of GOAM algorithm







Illustration

Problem Definition

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Step One - Group Feature Extraction

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Identification

Evaluation Results

Table 3: Original Dataset

G_1	F_1	F_2	F_3	F_4	$ig G_2$	F_1	F_2	F_3	F_4
	10	8	9	8		7	7	6	6
	9	9	7	9		8	9	9	8
	8	10	8	8		6	7	8	9
	8	8	6	7		7	7	7	8
	9	9	9	8		8	6	6	7
G_3	F_1	F_2	F_3	$F_{\scriptscriptstyle A}$	G_4	F_1	F_2	F_3	$F_{\scriptscriptstyle A}$
			<u> </u>	- 4				<u> </u>	- 4
	8	10	8	8		9	8	8	8
	8 9								
		10	8	8		9	8	8	8
	9	10 9	8 7	8 9		9	8 7	8 7	8





Illustration

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Table 4: outlying degree of each possible subspaces

Feature	Outlying Degree	Feature	Outlying Degree
$\{\pmb{F}_1\}$	4.351	$\{\pmb{F}_2,\pmb{F}_3\}$	4.023
$\{\pmb{F}_2\}$	2.012	$\{\pmb{F}_3,\pmb{F}_4\}$	4.324
$\{\pmb{F}_3\}$	1.392	$\{\pmb{F}_2,\pmb{F}_4\}$	2.018
$\{\pmb{F_4}\}$	2.207	$\{F_2, F_3, F_4\}$	2.012

Search process:

$$OD(\{F_1\}) > \alpha$$
, save to T_1 .
 $OD(\{F_2\}) < \alpha$, save to C_1 .

$$OD({F_3}) < \alpha$$
, save to C_2 .

$$OD({F_4}) < \alpha$$
, save to C_3 .

$$OD(\{F_2, F_3\}) > \alpha$$
, save to N_1 .

$$OD(\{F_3, F_4\}) > \alpha$$
, save to N_2 .

$$OD(\{F_2, F_4\}) < \alpha$$
, remove.

$$OD(\{F_2, F_3, F_4\}) < \alpha$$
, remove.



Strengths of GOAM Algorithm

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- Reduction of Complexity
 - ◆ Bottom-up search strategy.
 - Reduce the size of candidate subspaces.

Group Outlying Aspects Mining

- Efficiency
 - Before: $O(2^d)$

Now: $O(d * n^2)$





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NBA Dataset

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Evaluation Results

Group Outlying Aspects Mining





Evaluation

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 $Accuracy = \frac{P}{T}$

P: Identified outlying aspects

Group Outlying Aspects Mining

T: Real outlying aspects





Synthetic Dataset

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Synthetic Dataset and Ground Truth

Table 5: Synthetic Dataset and Ground Truth

Query group	\mathbf{F}_1	$\mathbf{F_2}$	F_3	\mathbf{F}_4	F_5	F_6	F_7	F_8
i_1	10	8	9	7	7	6	6	8
i_2	9	9	7	8	9	9	8	9
i_3	8	10	8	9	6	8	7	8
i_4	8	8	6	7	8	8	6	7
i_5	9	9	9	7	7	7	8	8
i_6	8	10	8	8	6	6	8	7
i_7	9	9	7	9	8	8	8	7
i_8	10	9	10	7	7	7	7	7
i_9	9	10	8	8	7	6	7	7
i_{10}	9	9	7	7	7	8	8	8



Synthetic Dataset Results

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Table 6: The experiment result on synthetic dataset

Method	Truth Outlying Aspects	Identified Aspects	Accuracy
GOAM	$\{F_1\},\ \{F_2F_4\}$	$\{{\pmb F}_1\},\ \{{\pmb F}_2{\pmb F}_4\}$	100%
Arithmetic Mean based OAM	$\{{\pmb F}_1\},\ \{{\pmb F}_2{\pmb F}_4\}$	$\{m{F}_4\},\ \{m{F}_2\}$	0%
Median based OAM	$\{m{F}_1\},\ \{m{F}_2m{F}_4\}$	$\{m{F}_2\},\ \{m{F}_4\}$	0%





NBA Dataset

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Data Collection

Source

Yahoo Sports website (http://sports.yahoo.com.cn/nba)

Data

- Extract NBA teams' data until March 30, 2018;
- 6 divisions;
- 12 features (eg: *Point Scored*).





NBA Dataset

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The detail features are as follows:

Table 7: Collected data of Brooklyn Nets Team

Pts	FGA	FG%	3FA	3PT%	6FTA	FT%	Reb	Ass	To	Stl	Blk
18	12	42	2.00	50	7.00	100	0	4	3	0	0
15.7	14.07	41	5.45	32	3.05	75	3.98	5.1	2.98	0.69	0.36
14.5	11.1	47	0.82	26	4.87	78	6.82	2.4	1.74	0.92	0.66
13.5	10.8	42	5.37	37	3.38	77	6.66	2	1.38	0.83	0.42
12.7	10.59	39	5.36	33	3.37	82	3.24	6.6	1.56	0.89	0.31
12.6	10.93	40	6.94	37	1.70	84	4.27	1.5	1.06	0.61	0.44
12.2	10.39	44	3.42	35	2.70	72	3.79	4.1	2.15	1.12	0.32
10.6	7.85	49	4.51	41	1.35	83	3.34	1.6	1.15	0.45	0.24



NBA Dataset

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Data Preprocess

Table 8: The bins that used to discrete data of each feature

Labels	Pts	FGA	FG%	3FA	3PT%	FTA
low	[0,5]	[0,4]	[0,0.35]	[0,1.0]	[0,0.2]	[0,1.0]
medium	(5,10]	(4,7]	(0.35, 0.45]	(1.0,2.5]	(0.2, 0.3]	(1.0, 1.5]
high	(10,15]	(7,10]	(0.45, 0.5]	(2.5, 3.5]	(0.3, 0.35]	(1.5, 2.5]
very high	$(15,+\infty]$	$(10,+\infty]$	(0.5,1]	$(3.5,+\infty]$	(0.35,1]	$(2.5,+\infty]$
Labels	FT%	Reb	Ass	To	Stl	Blk
low	[0,0.6]	[0,2.0]	[0,1.0]	[0,0.6]	[0,0.2]	[0,0.25]
medium	(0.6, 0.65]	(2,5]	(1,2]	(0.6, 0.9]	(0.2, 0.5]	(0.25, 0.5]
high	(0.65, 0.75)	[5,6]	(2,4]	(0.9, 1.7]	(0.6, 0.75]	(0.5, 0.7]
very high	(0.75,1]	$(6,+\infty]$	$(4,+\infty]$	$(1.7,+\infty]$	$(0.75,+\infty]$	$[(0.7,+\infty]]$



NBA Dataset Results

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Table 9: The identified outlying aspects of groups

Teams	Trivial Outlying Aspects	NonTrivial Outlying Aspects
Cleveland Cavaliers	{3FA}	{FGA, FT%}, {FGA, FG%}
Orlando Magic	{Stl}	None
Milwaukee Bucks	{To}, {FTA}	{FGA, FTA}, {3FA, FTA}
Golden State Warriors	$\{FG\%\}$	{FT%, Blk}, {FGA, 3PT%, FTA}
Utah Jazz	${Blk}$	{3FA, 3PT%}
New Orleans Pelicans	{FT%}, {FTA}	{FTA, Stl}, {FTA, To}





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Conclusion

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Evaluation Results

- Formalize the problem of *Group Outlying Aspects Mining* by extending outlying aspects mining;
- Propose a novel method GOAM algorithm to solve the *Group Outlying Aspects Mining* problem;
- Utilize the pruning strategies to reduce time complexity.



Questions?

Problem Definition

Related Work and Challenges

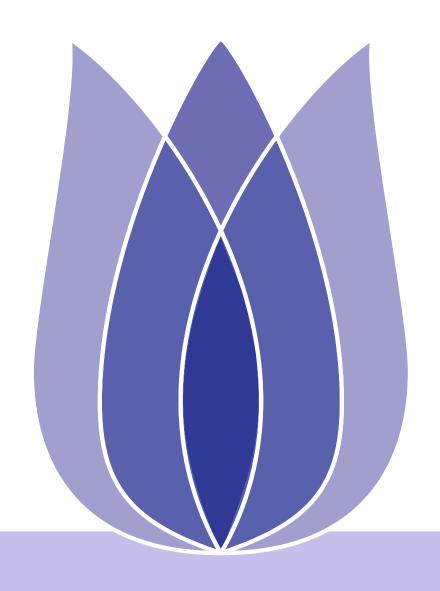
GOAM Algorithm

Evaluation Results





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TEAM FOR UNIVERSAL LEARNING AND INTELLIGENT PROCESSING