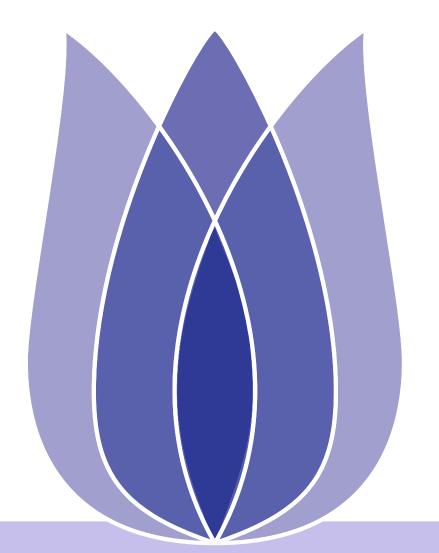
# **Group Outlying Aspects Mining**

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## **Overview**

**Problem Definition** 

Related Work and Challenges

GOAM Algorithm

**Evaluation Results** 

Conclusion

#### **Problem Definition**

Outlying Aspects Mining
Group Outlying Aspects Mining

#### **Related Work and Challenges**

Related Work - Outlying Aspects Mining Challenges (1)

## **GOAM Algorithm**

Step One - Group Feature Extraction
Step Two - Outlying Degree Scoring
Step Three - Outlying Aspects Identification

#### **Evaluation Results**

Synthetic Dataset NBA Dataset





#### **Problem Definition**

Outlying Aspects Mining
Group Outlying Aspects Mining

Related Work and Challenges

GOAM Algorithm

**Evaluation Results** 

Conclusion

# **Problem Definition**

**Group Outlying Aspects Mining** 





# **Outlying Aspects Mining**

**Problem Definition** 

#### Outlying Aspects Mining

**Group Outlying Aspects Mining** 

Related Work and Challenges

**GOAM Algorithm** 

**Evaluation Results** 

Conclusion

Outlying Aspects Mining aims to identify the outstanding features of the query object.



- A teacher may be interested in the characteristics that make one student distinctive from others.
- NBA coaches would prefer to find out the strengths and weaknesses of the player (a query object).

Player	3PT%	FTA	FT%	То
$P_1$	65	4	33	8
$P_2$	78	1	65	5
$P_3$	58	6	46	3
$\boldsymbol{P_4}$	68	1.2	85	6.2
$P_5$	58	6.2	36	3.4



# **Outlying Aspects Mining vs Outlier Detection**

**Problem Definition** 

#### Outlying Aspects Mining

**Group Outlying Aspects Mining** 

Related Work and Challenges

**GOAM** Algorithm

**Evaluation Results** 

Conclusion

Player	3PT%	FTA	FT%	То
$P_1$	65	4	33	8
$P_2$	78	1	65	5
$P_3$	58	6	46	3
$P_4$	68	1.2	85	6.2
$P_5$	58	6.2	36	3.4

## Outlying Aspects Mining

- Explain the distinctive aspects of the query object.
- The query object may (or may not) be an outlier.

## Outlier Detection

- Find out all unusual objects in the whole dataset.
- No explanation on how they are different.



# **Group Outlying Aspects Mining**

**Problem Definition** 

**Outlying Aspects Mining** 

Group Outlying Aspects Mining

Related Work and Challenges

GOAM Algorithm

**Evaluation Results** 

Conclusion

Group outlying aspects mining aims to identify the outstanding features of the group of query object.

- Doctors desire to identify the merits & demerits between a group of cancer patients and normal people.
- NBA coaches are passionate about exploring the obvious advantages & disadvantages of the team.



Figure 1: Medical



Figure 2: NBA-Team



#### **Problem Formalization**

**Problem Definition** 

**Outlying Aspects Mining** 

Group Outlying Aspects Mining

Related Work and Challenges

GOAM Algorithm

**Evaluation Results** 

Conclusion

Group outlying aspects mining aims to identify the top-k group outlying subspace  $s \subseteq F$  in which the query group  $G_q$  is distinctive with other groups.

Defr

- $G = \{G_q, G_2, G_3, ..., G_n\} \Leftrightarrow \text{a set of groups.}$
- $\blacksquare$   $G_q \Leftrightarrow ext{the query group.}$
- Other groups ⇔ comparison groups.
- Each object in the group has d features  $F = \{f_1, f_2, ..., f_d\}$ .



## **Term Definition**

**Problem Definition** 

**Outlying Aspects Mining** 

#### Group Outlying Aspects Mining

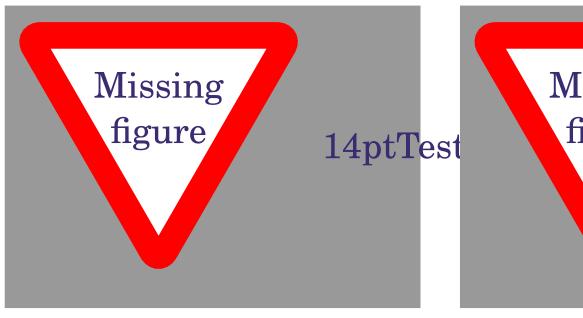
Related Work and Challenges

GOAM Algorithm

**Evaluation Results** 

Conclusion

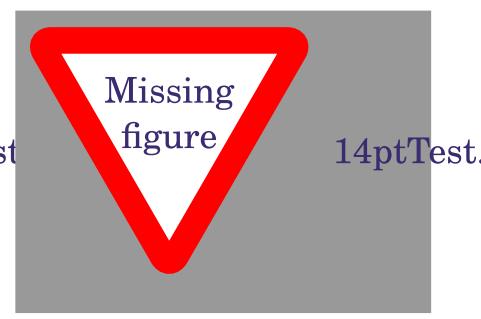
- Top-k group outlying subspaces
  - $\rho_s(\cdot) \Rightarrow$  outlying scoring function.
  - lacktriangle  $ho_s(\cdot)$  quantifies the outlying degree of the query group  $G_q$  in the subspace s.
  - Order by DESC using scoring function  $\rho(\cdot)$  to identify top K group outlying subspaces.







(b) Group Outlying Spaces



(c) Another Subspaces



# **Term Definition**

**Problem Definition** 

**Outlying Aspects Mining** 

#### Group Outlying Aspects Mining

Related Work and Challenges

GOAM Algorithm

**Evaluation Results** 

Conclusion

- Trivial Outlying Features
  - One-dimension subspaces.
  - $G_q$ 's outlying degree  $\rho(\cdot) > \alpha$ .

Table 1:  $\alpha = 4$ 

Feature	Outlying Degree
$\{\pmb{F}_1\}$	4.351
$\{\pmb{F}_3, \pmb{F}_4\}$	4.024
$\{\pmb{F}_2,\pmb{F}_4\}$	2.318
$\{\pmb{F}_2\}$	2.002
$\{\pmb{F}_3\}$	1.028

**Group Outlying Aspects Mining** 



# **Term Definition**

**Problem Definition** 

**Outlying Aspects Mining** 

#### Group Outlying Aspects Mining

Related Work and Challenges

GOAM Algorithm

**Evaluation Results** 

- Non-Trivial Outlying Subspaces
  - Multi-dimension subspaces.
  - $G_q$ 's outlying degree  $\rho(\cdot) > \alpha$ .

Table 2:  $\alpha = 4$ 

Feature	Outlying Degree
$\{\pmb{F}_1\}$	4.351
$\{\pmb{F}_3,\pmb{F}_4\}$	4.024
$\{\pmb{F}_2,\pmb{F}_4\}$	2.318
$\{\pmb{F}_2\}$	2.002
$\{\pmb{F}_3\}$	1.028



**Problem Definition** 

#### Related Work and Challenges

Related Work - Outlying Aspects

Mining

Challenges (1)

GOAM Algorithm

**Evaluation Results** 

Conclusion

# Related Work and Challenges





# Related Work - Outlying Aspects Mining

**Problem Definition** 

Related Work and Challenges

Related Work - Outlying Aspects Mining

Challenges (1)

GOAM Algorithm

**Evaluation Results** 

Conclusion

- Existing Methods Feature selection
  - ◆ To distinguish two classes: the query point (positive) & rest of data (negative)

## Disadvantages

- Positive and negative classes are
   Not balanced.
- Not quantify the outlying degree accurately.
- Not identify group outlying aspects.

## Advantages

- ◆ Easy to operate.
- Resolve dimensionality bias.





# Related Work - Outlying Aspects Mining

**Problem Definition** 

Related Work and Challenges

Related Work - Outlying Aspects
Mining

Challenges (1)

GOAM Algorithm

**Evaluation Results** 

Conclusion

- Existing Methods Score-and-search
  - Define an outlying score function.
  - Search subspaces.

#### Disadvantages

- Dimensionality bias.
- Search efficiency is Not high (dataset is large).
- Not identify group outlying aspects.

## Advantages

- Quantify the outlying degree correctly.
- ◆ High Comprehensibility.





**Problem Definition** 

Related Work and Challenges

Related Work - Outlying Aspects Mining

Challenges (1)

GOAM Algorithm

**Evaluation Results** 

Conclusion

### Group Outlying Aspects Mining

- Focus on differences between groups.
- Multiple points.

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Figure 3: Group Outlying Aspects Target

#### Outlying Aspects Mining

- Concentrates on differences between objects.
- One point.

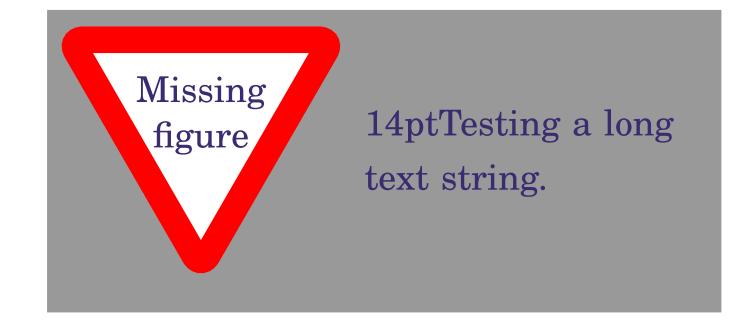


Figure 4: Outlying Aspects Target



# Challenges (1)

**Problem Definition** 

Related Work and Challenges
Related Work - Outlying Aspects
Mining

Challenges (1)

GOAM Algorithm

**Evaluation Results** 

- How to represent the group features.
  - ◆ Can be affected by outlier values.
  - ◆ Can Not reflect the overall distribution of group features.





# Challenges (2)

**Problem Definition** 

Related Work and Challenges
Related Work - Outlying Aspects
Mining

Challenges (1)

GOAM Algorithm

**Evaluation Results** 

- How to evaluate the outlying degree in different aspects.
  - Need design a scoring function when necessary.
  - Adopting an appropriate scoring function (without dimension bias) remains a problem.





# Challenges (3)

**Problem Definition** 

Related Work and Challenges
Related Work - Outlying Aspects
Mining

Challenges (1)

GOAM Algorithm

**Evaluation Results** 

- How to improve the efficiency.
  - ◆ When the dimension of the data is high, the candidate subspace grows exponentially.
  - ◆ It will easily go beyond the limits of the computation resources.





Problem Definition

Related Work and Challenges

#### GOAM Algorithm

Step One - Group Feature Extraction
Step Two - Outlying Degree Scoring
Step Three - Outlying Aspects
Identification

**Evaluation Results** 

Conclusion

# **GOAM Algorithm**





**Problem Definition** 

Related Work and Challenges

GOAM Algorithm

Step One - Group Feature Extraction
Step Two - Outlying Degree Scoring
Step Three - Outlying Aspects
Identification

**Evaluation Results** 

Conclusion

## Framework of GOAM algorithm:

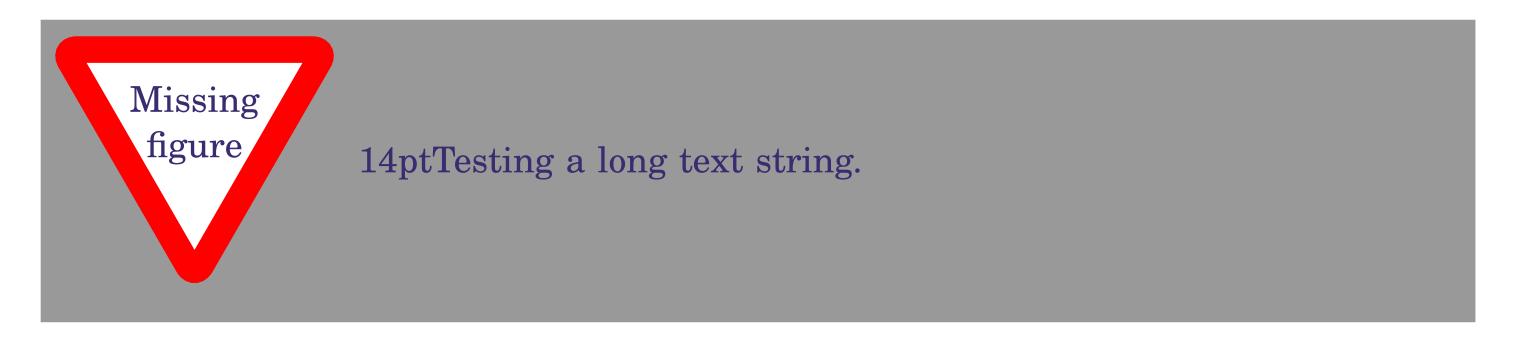


Figure 5: Framework of GOAM Algorithm



# **Step One - Group Feature Extraction**

**Problem Definition** 

Related Work and Challenges

GOAM Algorithm

#### Step One - Group Feature Extraction

Step Two - Outlying Degree Scoring Step Three - Outlying Aspects Identification

**Evaluation Results** 

Conclusion

Suppose  $f_1$ ,  $f_2$ ,  $f_3$  are three features of  $G_q$ .

$$f_1$$
: { $x_1, x_2, x_3, x_4, x_5, x_2, x_3, x_4, x_1, x_2$ }

$$f_2$$
: { $y_2, y_2, y_1, y_2, y_3, y_3, y_5, y_4, y_4, y_2$ }

$$f_3$$
: { $z_1, z_4, z_2, z_4, z_5, z_3, z_1, z_2, z_4, z_2$ }

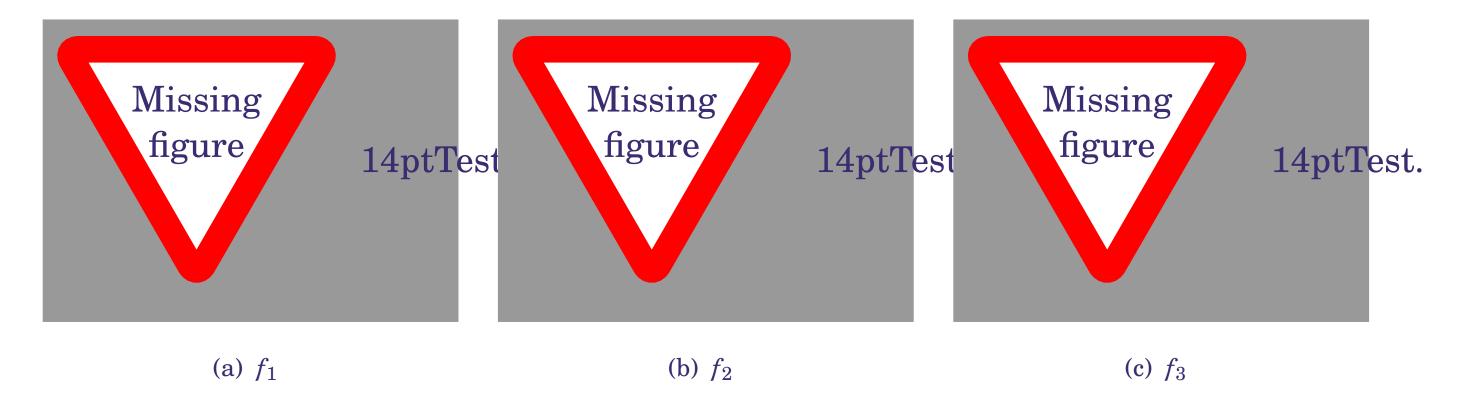


Figure 6: Histogram of  $G_q$  on three features



# **Step Two - Outlying Degree Scoring**

Problem Definition

Related Work and Challenges

GOAM Algorithm

Step One - Group Feature Extraction

#### Step Two - Outlying Degree Scoring

Step Three - Outlying Aspects Identification

**Evaluation Results** 

- Calculate Earth Mover Distance
  - ◆ Represent one feature among different groups
  - ◆ Purpose: calculate the minimum mean distance

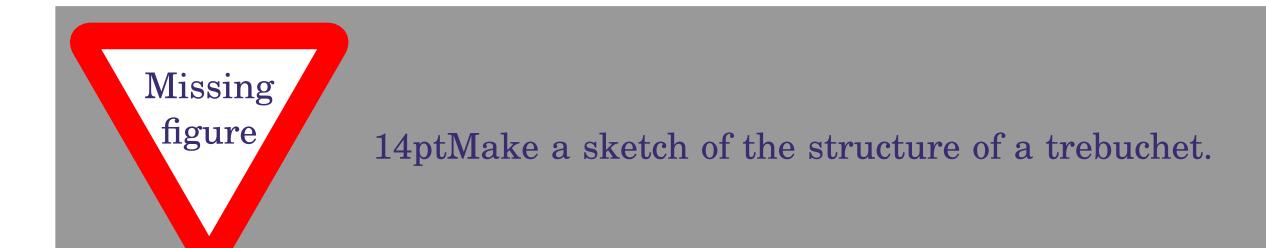


Figure 7: EMD of one feature



# **Step Two - Outlying Degree Scoring**

**Problem Definition** 

Related Work and Challenges

GOAM Algorithm

Step One - Group Feature Extraction

#### Step Two - Outlying Degree Scoring

Step Three - Outlying Aspects Identification

**Evaluation Results** 

Conclusion

Calculate the outlying degree

$$OD(G_q) = \sum_{1}^{n} EDM(h_{q_s}, h_{k_s})$$

- $\bullet$  n  $\Leftrightarrow$  the number of contrast groups.
- $h_{k_s} \Leftrightarrow$  the histogram representation of  $G_k$  in the subspace s.



# **Step Three - Outlying Aspects Identification**

**Problem Definition** 

Related Work and Challenges

GOAM Algorithm

Step One - Group Feature Extraction

Step Two - Outlying Degree Scoring

Step Three - Outlying Aspects
Identification

**Evaluation Results** 

- Identify group outlying aspects mining based on the value of outlying degree.
- The greater the outlying degree is, the more likely it is group outlying aspect.



# Pseudo code

**Problem Definition** 

Related Work and Challenges

GOAM Algorithm

Step One - Group Feature Extraction

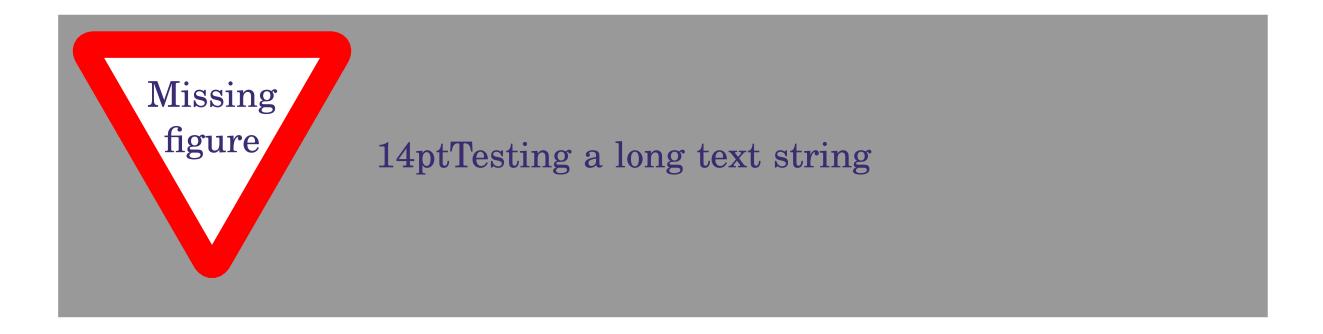
Step Two - Outlying Degree Scoring

Step Three - Outlying Aspects Identification

**Evaluation Results** 

Conclusion

Pseudo code of GOAM algorithm







# Illustration

**Problem Definition** 

Related Work and Challenges

GOAM Algorithm

Step One - Group Feature Extraction

Step Two - Outlying Degree Scoring

Step Three - Outlying Aspects
Identification

**Evaluation Results** 

Table 3: Original Dataset

$G_1$	$F_1$	$F_2$	$F_3$	$F_4$	$G_2$	$F_1$	$F_2$	$F_3$	$F_4$
	10	8	9	8		7	7	6	6
	9	9	7	9		8	9	9	8
	8	10	8	8		6	7	8	9
	8	8	6	7		7	7	7	8
	9	9	9	8		8	6	6	7
$G_3$	$F_1$	$F_2$	$F_3$	$F_4$	$ig G_4$	$F_1$	$F_2$	$F_3$	$F_4$
	8	10	8	8		9	8	8	8
	9	9	7	9		7	7	7	9
	10	9	10	7		8	6	6	8
	9	10	8	6		9	8	8	7
	9	9	7	9		8	7	9	8



## Illustration

**Problem Definition** 

Related Work and Challenges

GOAM Algorithm

Step One - Group Feature Extraction

Step Two - Outlying Degree Scoring

Step Three - Outlying Aspects Identification

**Evaluation Results** 

Conclusion

Table 4: outlying degree of each possible subspaces

Feature	Outlying Degree	Feature	Outlying Degree
$\{\pmb{F}_1\}$	4.351	$\{\pmb{F}_2,\pmb{F}_3\}$	4.023
$\{\pmb{F}_2\}$	2.012	$\{\pmb{F}_3,\pmb{F}_4\}$	4.324
$\{\pmb{F}_3\}$	1.392	$\{\pmb{F}_2,\pmb{F}_4\}$	2.018
$\{\pmb{F}_4\}$	2.207	$\{F_2, F_3, F_4\}$	2.012

#### Search process:

$$OD(\{F_1\}) > \alpha$$
, save to  $T_1$ .  
 $OD(\{F_2\}) < \alpha$ , save to  $C_1$ .  
 $OD(\{F_3\}) < \alpha$ , save to  $C_2$ .

$$OD({F_4}) < \alpha$$
, save to  $C_3$ .

$$OD(\{F_2, F_3\}) > \alpha$$
, save to  $N_1$ .

$$OD(\{F_3, F_4\}) > \alpha$$
, save to  $N_2$ .

$$OD(\{F_2, F_4\}) < \alpha$$
, remove.

$$OD(\{F_2, F_3, F_4\}) < \alpha$$
, remove.



# Strengths of GOAM Algorithm

**Problem Definition** 

Related Work and Challenges

GOAM Algorithm

Step One - Group Feature Extraction

Step Two - Outlying Degree Scoring

Step Three - Outlying Aspects Identification

**Evaluation Results** 

Conclusion

- Reduction of Complexity
  - ◆ Bottom-up search strategy.
  - Reduce the size of candidate subspaces.

**Group Outlying Aspects Mining** 

- Efficiency
  - Before:  $O(2^d)$

Now:  $O(d * n^2)$ 





**Problem Definition** 

Related Work and Challenges

GOAM Algorithm

#### **Evaluation Results**

Synthetic Dataset

NBA Dataset

Conclusion

# **Evaluation Results**





# **Evaluation**

**Problem Definition** 

Related Work and Challenges

GOAM Algorithm

**Evaluation Results** 

Synthetic Dataset

**NBA** Dataset

Conclusion

 $Accuracy = \frac{P}{T}$ 

P: Identified outlying aspects

T: Real outlying aspects





# **Synthetic Dataset**

**Problem Definition** 

Related Work and Challenges

GOAM Algorithm

**Evaluation Results** 

#### Synthetic Dataset

**NBA** Dataset

Conclusion

Synthetic Dataset and Ground Truth

Table 5: Synthetic Dataset and Ground Truth

Query group	$\mathbf{F}_1$	$\mathbf{F_2}$	$F_3$	$\mathbf{F}_4$	$F_5$	$F_6$	$F_7$	$F_8$
$i_1$	10	8	9	7	7	6	6	8
$i_2$	9	9	7	8	9	9	8	9
$i_3$	8	<b>10</b>	8	9	6	8	7	8
$i_4$	8	8	6	7	8	8	6	7
$i_5$	9	9	9	7	7	7	8	8
$i_6$	8	10	8	8	6	6	8	7
$i_7$	9	9	7	9	8	8	8	7
$i_8$	10	9	10	7	7	7	7	7
$i_9$	9	10	8	8	7	6	7	7
$i_{10}$	9	9	7	7	7	8	8	8



# **Synthetic Dataset Results**

**Problem Definition** 

Related Work and Challenges

GOAM Algorithm

**Evaluation Results** 

Synthetic Dataset

**NBA** Dataset

Conclusion

Table 6: The experiment result on synthetic dataset

Method	Truth Outlying Aspects	Identified Aspects	Accuracy
GOAM	$\{\pmb{F}_1\},\ \{\pmb{F}_2\pmb{F}_4\}$	$\{{\pmb F}_1\},\ \{{\pmb F}_2{\pmb F}_4\}$	100%
Arithmetic Mean based OAM	$\{m{F}_1\},\ \{m{F}_2m{F}_4\}$	$\{m{F}_4\},\ \{m{F}_2\}$	0%
Median based OAM	$\{{\pmb F}_1\},\ \{{\pmb F}_2{\pmb F}_4\}$	$\{\pmb{F}_2\},\ \{\pmb{F}_4\}$	0%

**Group Outlying Aspects Mining** 





## **NBA Dataset**

**Problem Definition** 

Related Work and Challenges

GOAM Algorithm

**Evaluation Results** 

Synthetic Dataset

**NBA** Dataset

Conclusion

**Data Collection** 

Source

Yahoo Sports website (http://sports.yahoo.com.cn/nba)

Data

- Extract NBA teams' data until March 30, 2018;
- 6 divisions;
- 12 features (eg: *Point Scored*).





# **NBA Dataset**

**Problem Definition** 

Related Work and Challenges

GOAM Algorithm

**Evaluation Results** 

Synthetic Dataset

NBA Dataset

Conclusion

The detail features are as follows:

Table 7: Collected data of Brooklyn Nets Team

Pts	FGA	FG%	3FA	3PT%	6FTA	FT%	Reb	Ass	To	Stl	Blk
18	12	42	2.00	50	7.00	100	0	4	3	0	0
15.7	14.07	41	5.45	32	3.05	75	3.98	5.1	2.98	0.69	0.36
14.5	11.1	47	0.82	26	4.87	78	6.82	2.4	1.74	0.92	0.66
13.5	10.8	42	5.37	37	3.38	77	6.66	2	1.38	0.83	0.42
12.7	10.59	39	5.36	33	3.37	82	3.24	6.6	1.56	0.89	0.31
12.6	10.93	40	6.94	37	1.70	84	4.27	1.5	1.06	0.61	0.44
12.2	10.39	44	3.42	35	2.70	72	3.79	4.1	2.15	1.12	0.32
10.6	7.85	49	4.51	41	1.35	83	3.34	1.6	1.15	0.45	0.24



# **NBA Dataset**

**Problem Definition** 

Related Work and Challenges

GOAM Algorithm

**Evaluation Results** 

Synthetic Dataset

NBA Dataset

Conclusion

## Data Preprocess

Table 8: The bins that used to discrete data of each feature

Labels	Pts	FGA	FG%	3FA	3PT%	FTA
low	[0,5]	[0,4]	[0,0.35]	[0,1.0]	[0,0.2]	[0,1.0]
medium	(5,10]	(4,7]	(0.35, 0.45]	(1.0,2.5]	(0.2, 0.3]	(1.0, 1.5]
high	(10,15]	(7,10]	(0.45, 0.5]	(2.5, 3.5]	(0.3, 0.35]	(1.5, 2.5]
very high	$(15,+\infty]$	$(10,+\infty]$	(0.5,1]	$(3.5,+\infty]$	(0.35,1]	$(2.5,+\infty]$
Labels	FT%	Reb	Ass	To	Stl	Blk
low	[0,0.6]	[0,2.0]	[0,1.0]	[0,0.6]	[0,0.2]	[0,0.25]
medium	(0.6, 0.65]	(2,5]	(1,2]	(0.6, 0.9]	(0.2, 0.5]	(0.25, 0.5]
high	(0.65, 0.75]	[5,6]	(2,4]	(0.9, 1.7]	(0.6, 0.75]	(0.5, 0.7]
very high	(0.75,1]	$(6,+\infty]$	$(4,+\infty]$	$(1.7,+\infty]$	$(0.75,+\infty]$	$(0.7,+\infty]$



# **NBA Dataset Results**

Problem Definition

Related Work and Challenges

GOAM Algorithm

**Evaluation Results** 

Synthetic Dataset

**NBA** Dataset

Table 9: The identified outlying aspects of groups

Teams	Trivial Outlying Aspects	NonTrivial Outlying Aspects
Cleveland Cavaliers	{3FA}	{FGA, FT%}, {FGA, FG%}
Orlando Magic	{Stl}	None
Milwaukee Bucks	{To}, {FTA}	{FGA, FTA}, {3FA, FTA}
Golden State Warriors	$\{FG\%\}$	{FT%, Blk}, {FGA, 3PT%, FTA}
Utah Jazz	${Blk}$	{3FA, 3PT%}
New Orleans Pelicans	{FT%}, {FTA}	{FTA, Stl}, {FTA, To}





Problem Definition

Related Work and Challenges

GOAM Algorithm

**Evaluation Results** 

Conclusion





## Conclusion

Problem Definition

Related Work and Challenges

GOAM Algorithm

Evaluation Results

- Formalize the problem of *Group Outlying Aspects Mining* by extending outlying aspects mining;
- Propose a novel method GOAM algorithm to solve the *Group Outlying Aspects Mining* problem;
- Utilize the pruning strategies to reduce time complexity.



# **Questions?**

Problem Definition

Related Work and Challenges

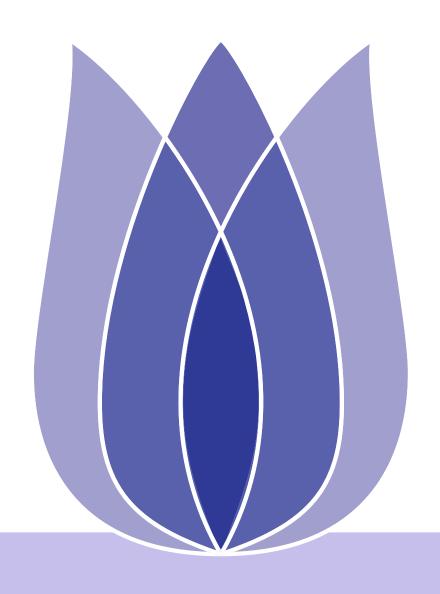
GOAM Algorithm

**Evaluation Results** 





# **Contact Information**



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