

Exercise 1.a – b)

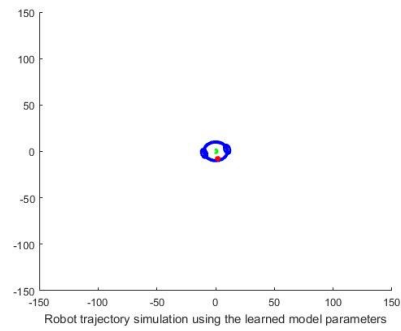
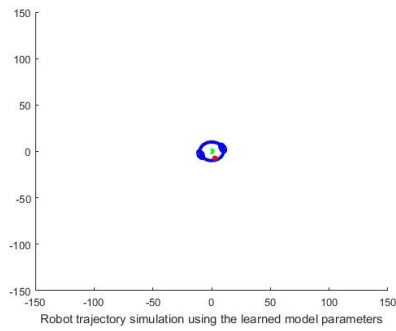
$k = 5$ ($p_1 = 4, p_2 = 1$)	$k = 2$ ($p_1 = 5, p_2 = 3$)
$a_{1,1} = 0.0025$	$a_{1,1} = 0.0022$
$a_{1,2} = 0.9198$	$a_{1,2} = 0.9217$
$a_{1,3} = -0.0029$	$a_{1,3} = 0.0066$
$a_{1,4} = -0.0007$	$a_{1,4} = -0.0016$
$a_{1,5} = -0.0010$	$a_{1,5} = -9.9158 \text{ e-}04$
$a_{1,6} = 0.0014$	$a_{1,6} = 0.0025$
$a_{1,7} = 0.0025$	$a_{1,7} = 0.0023$
$a_{1,8} = 0.0001$	$a_{1,8} = -1.1665 \text{ e-}05$
$a_{1,9} = -0.0003$	$a_{1,9} = -0.0130$
$a_{1,10} = 6.6926 \text{ e-}05$	$a_{1,10} = 1.2268 \text{ e-}04$
$a_{1,11} = 1.3061 \text{ e-}05$	$a_{1,11} = 1.2836 \text{ e-}05$
$a_{1,12} = -0.0043$	$a_{1,12} = -0.0045$
$a_{1,13} = 4.5174 \text{ e-}05$	$a_{1,13} = -4.3099 \text{ e-}05$
	$a_{1,14} = 1.6696 \text{ e-}06$
	$a_{1,15} = 0.0026$
	$a_{1,16} = -4.0239 \text{ e-}07$
$a_{2,1} = -0.0043$	$a_{2,1} = -0.0027$
$a_{2,2} = -0.0010$	$a_{2,2} = -0.0014$
$a_{2,3} = 0.0014$	$a_{2,3} = -0.0115$
$a_{2,4} = 0.4680$	$a_{2,4} = 0.4730$
$a_{2,5} = 5.6850 \text{ e-}04$	$a_{2,5} = 2.4454 \text{ e-}04$
$a_{2,6} = -0.0025$	$a_{2,6} = -0.0083$
$a_{2,7} = -0.0010$	$a_{2,7} = 7.4693 \text{ e-}05$
$a_{2,8} = 1.9246 \text{ e-}05$	$a_{2,8} = 4.3810 \text{ e-}05$
$a_{2,9} = -0.0017$	$a_{2,9} = 0.0164$
$a_{2,10} = 6.7254 \text{ e-}04$	$a_{2,10} = -9.7700 \text{ e-}04$
$a_{2,11} = -7.8462 \text{ e-}06$	$a_{2,11} = -5.2889 \text{ e-}06$
$a_{2,12} = 0.0035$	$a_{2,12} = 0.0043$
$a_{2,13} = 8.7155 \text{ e-}06$	$a_{2,13} = -4.4187 \text{ e-}06$
	$a_{2,14} = -2.6911 \text{ e-}07$
	$a_{2,15} = -0.0038$
	$a_{2,16} = 2.1016 \text{ e-}06$
$a_{3,1} = 8.0784 \text{ e-}04$	$a_{3,1} = -5.9515 \text{ e-}04$
$a_{3,2} = -3.1902 \text{ e-}04$	$a_{3,1} = -1.7107 \text{ e-}04$
$a_{3,3} = 0.9987$	$a_{3,1} = 0.9997$
$a_{3,4} = 3.2142 \text{ e-}04$	$a_{3,1} = 8.3936 \text{ e-}04$
	$a_{3,1} = 1.2687 \text{ e-}04$
	$a_{3,1} = 0.0018$
	$a_{3,1} = -1.4105 \text{ e-}04$
	$a_{3,1} = -4.5223 \text{ e-}06$
	$a_{3,1} = -6.2224 \text{ e-}04$
	$a_{3,1} = -1.3221 \text{ e-}05$

Exercise 1.c)

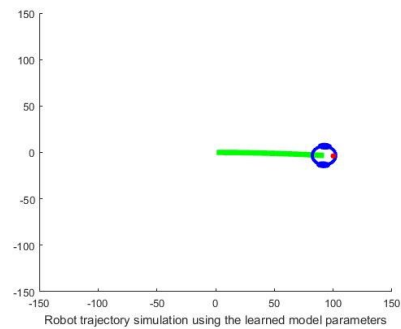
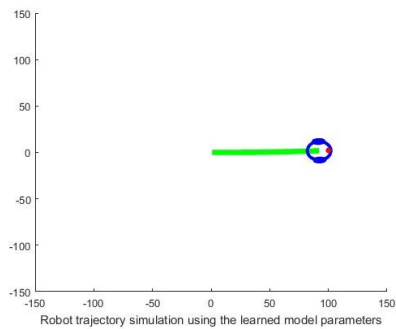
$k = 5$

$k = 2$

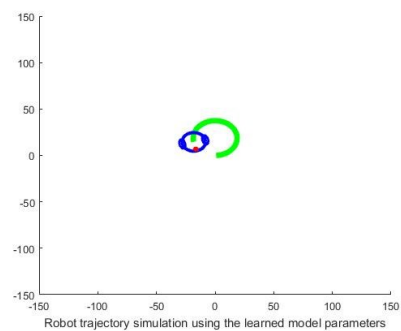
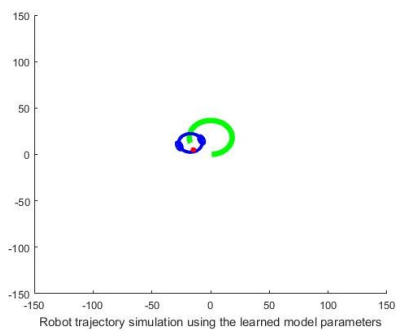
$(v, w) = (0, 0.05)$



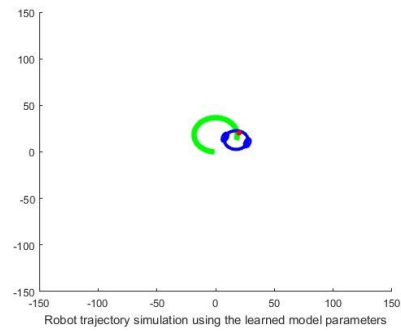
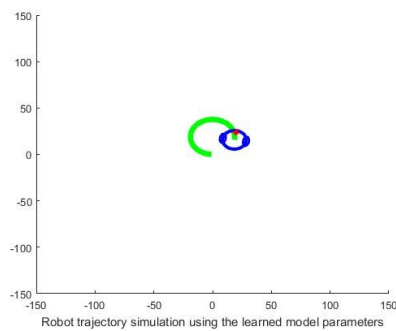
$(v, w) = (1, 0)$



$(v, w) = (1, 0.05)$

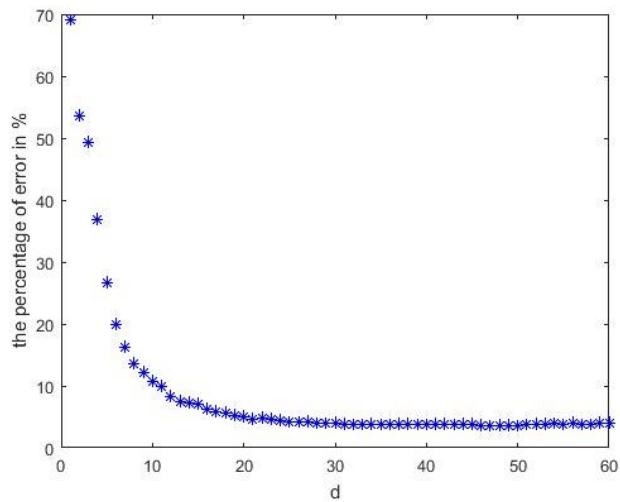


$(v, w) = (-1, -0.05)$



Exercise 2

- The optimal value of d is 48 and its classification error is 3.62%.
- The plot of classification error when varying d from 1 to 60



- The confusion matrix of the optimal d is:

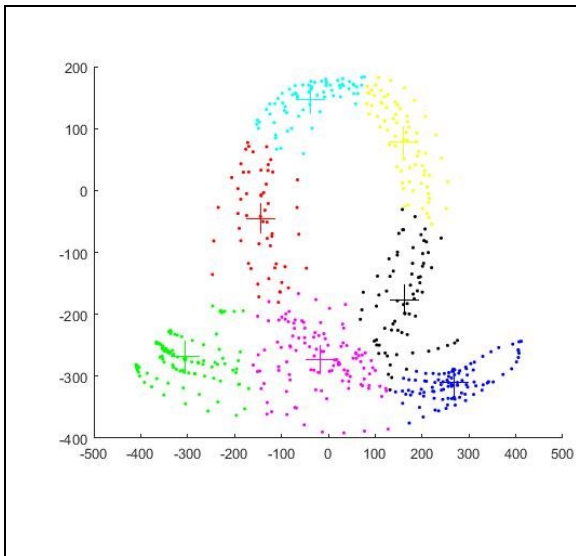
970	0	3	2	1	2	8	1	3	5
0	1098	0	0	0	0	1	2	0	1
1	11	1001	8	3	1	1	31	7	10
0	1	3	972	0	18	0	1	10	7
0	2	3	0	964	0	3	2	1	10
2	1	0	5	0	859	13	3	5	2
1	1	2	0	3	2	924	0	1	0
1	0	1	2	2	0	0	956	1	6
5	21	18	17	3	10	8	13	941	15
0	0	1	4	6	0	0	19	5	953

- The percentage form of this confusion matrix is:

digit	0	1	2	3	4	5	6	7	8	9
0	0.97	0.00	0.00	0.00	0.00	0.00	0.01	0.00	0.00	0.01
1	0.00	1.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00
2	0.00	0.01	0.93	0.01	0.00	0.00	0.00	0.03	0.01	0.01
3	0.00	0.00	0.00	0.96	0.00	0.02	0.00	0.00	0.01	0.01
4	0.00	0.00	0.00	0.00	0.98	0.00	0.00	0.00	0.00	0.01
5	0.00	0.00	0.00	0.01	0.00	0.97	0.01	0.00	0.01	0.00
6	0.00	0.00	0.00	0.00	0.00	0.00	0.99	0.00	0.00	0.00
7	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.99	0.00	0.01
8	0.00	0.02	0.02	0.02	0.00	0.01	0.01	0.01	0.90	0.01
9	0.00	0.00	0.00	0.00	0.01	0.00	0.00	0.02	0.01	0.96

Exercise 3

k-means



NUBS

