

Summary: Part 3

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1 Applications

1.1 U-Statistics

1.2 Kernel-Density Estimation

1.3 Random Graph

1.4 Minimum Weight Spanning Tree

1.5 Rademacher Complexity

1.6 Dimensionality Reduction

2 Self-Bounding Functions

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4.5 Chaining