# Lecture 3: Information Inequalities

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# Contents

1	Information Theory Basics		2	
	1.1	Entropy, Relative Entropy, and Mutual Information	2	
2	Info	ormation Inequalities	2	
	2.1	Chain Rules for Entropy, Relative Entropy, and Mutual Information	4	
	2.2	Han's Inequality	2	
	2.3	Sub-Additivity of Entropy and Relative Entropy	2	
	2.4	Duality and Variational Formulas	2	
	2.5	Optimal Transport	2	
	2.6	Pinsker's Inequality	6	
		The Brunn-Minkowski Inequality		

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1.1 Entropy, Relative Entropy, and Mutual Information

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## 2 Information Inequalities

- 2.1 Chain Rules for Entropy, Relative Entropy, and Mutual Information
- 2.2 Han's Inequality
- 2.3 Sub-Additivity of Entropy and Relative Entropy
- 2.4 Duality and Variational Formulas
- 2.5 Optimal Transport
- 2.6 Pinsker's Inequality
- 2.7 The Brunn-Minkowski Inequality