CONTENTS

Final Project Code

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Contents

1	Dat	Data Import					
2	Dat	Oata partition					
3	Prin 3.1 3.2	mary Analysis Exploratory analysis and data visualization 3.1.1 Data Frame Summary Model Training 3.2.1 Linear Model 3.2.2 LASSO 3.2.3 Ridge	4 5 11 11 12 14				
		3.2.4 Elastic Net 3.2.5 Principal components regression (PCR) 3.2.6 Partial Least Squares (PLS) 3.2.7 Generalized Additive Model (GAM) 3.2.8 Multivariate Adaptive Regression Splines (MARS) 3.2.9 K-Nearest Neighbour (KNN)	16 18 20 22 24 26				
	3.3 3.4	3.2.10 Bagging	27 29 31 33 35 38				
4	4.1	Exploratory analysis and data visualization	39 39				
	4.2	Model Training	43 44 46 48 51 51 51				
	4.3 4.4	4.2.9 Random Forest 4.2.10 Boosting . 4.2.11 Classification Trees 4.2.12 Support Vector Machine (SVM) Model Selection Training / Testing Error	51 51 51 51 52 53 53				

```
library(tidyverse)
library(summarytools)
library(corrplot)
library(caret)
library(vip)
library(rpart.plot)
library(ranger)
```

1 Data Import

```
# import data
load("./recovery.RData")
set.seed(3196)
lts.dat <- dat[sample(1:10000, 2000),]</pre>
set.seed(2575)
lincole.dat <- dat[sample(1:10000, 2000),]</pre>
set.seed(5509)
amy.dat <- dat[sample(1:10000, 2000),]</pre>
dat1 <- lts.dat %>%
  merge(lincole.dat, all = TRUE) %>%
  na.omit() %>%
  select(-id) %>%
  mutate(
    gender = as.factor(gender),
    race = as.factor(race),
    smoking = as.factor(smoking),
    hypertension = as.factor(hypertension),
    diabetes = as.factor(diabetes),
    vaccine = as.factor(vaccine),
    severity = as.factor(severity),
    study = as.factor(study))
dat2 <- lts.dat %>%
  merge(amy.dat, all = TRUE) %>%
  na.omit() %>%
  select(-id) %>%
  mutate(
    gender = as.factor(gender),
    race = as.factor(race),
    smoking = as.factor(smoking),
    hypertension = as.factor(hypertension),
    diabetes = as.factor(diabetes),
    vaccine = as.factor(vaccine),
    severity = as.factor(severity),
    study = as.factor(study))
dat3 <- lincole.dat %>%
  merge(amy.dat, all = TRUE) %>%
  na.omit() %>%
  select(-id) %>%
```

```
mutate(
    gender = as.factor(gender),
   race = as.factor(race),
    smoking = as.factor(smoking),
   hypertension = as.factor(hypertension),
   diabetes = as.factor(diabetes),
   vaccine = as.factor(vaccine),
   severity = as.factor(severity),
    study = as.factor(study))
dat <- dat1
summary(dat)
##
                    gender
                                      smoking
                                                   height
                                                                   weight
         age
                             race
                                                                      : 56.70
##
  Min.
          :45.00
                    0:1842
                             1:2372
                                      0:2223
                                                      :151.2
                                               Min.
                                                               Min.
   1st Qu.:57.00
                    1:1781
                             2: 172
                                      1:1034
                                               1st Qu.:166.2
                                                               1st Qu.: 75.40
## Median :60.00
                             3: 716
                                      2: 366
                                               Median :170.2
                                                               Median: 80.20
   Mean
           :60.06
                             4: 363
                                                      :170.2
                                                                      : 80.13
                                               Mean
                                                               Mean
##
   3rd Qu.:63.00
                                               3rd Qu.:174.2
                                                               3rd Qu.: 84.80
##
  Max.
          :77.00
                                               Max.
                                                     :188.6
                                                               Max.
                                                                      :103.40
##
        bmi
                    hypertension diabetes
                                               SBP
                                                               LDL
                                                                          vaccine
## Min.
         :19.70
                    0:1891
                                 0:3065
                                          Min.
                                                 :102.0
                                                          Min.
                                                                 : 28.0
                                                                          0:1469
   1st Qu.:25.80
                    1:1732
                                 1: 558
                                          1st Qu.:125.0
                                                          1st Qu.: 97.0
                                                                          1:2154
## Median :27.60
                                          Median :130.0
                                                          Median :110.0
## Mean
          :27.73
                                                :130.2
                                          Mean
                                                          Mean
                                                                :110.5
## 3rd Qu.:29.40
                                          3rd Qu.:136.0
                                                          3rd Qu.:124.0
## Max.
          :39.80
                                          Max.
                                                 :158.0
                                                          Max. :174.0
  severity study
##
                      recovery_time
##
   0:3289
            A: 728
                      Min. : 3.00
  1: 334
##
           B:2171
                      1st Qu.: 28.00
##
             C: 724
                      Median : 38.00
##
                           : 42.87
                      Mean
##
                      3rd Qu.: 49.00
##
                      Max.
                             :365.00
bin.dat1 <- dat1 %>%
  mutate(recovery_time = ifelse(recovery_time > 30, "gt30", "lt30")) %>%
  mutate(recovery_time = factor(recovery_time, levels = c("lt30", "gt30")))
bin.dat2 <- dat2 %>%
  mutate(recovery_time = ifelse(recovery_time > 30, "gt30", "lt30")) %>%
  mutate(recovery_time = factor(recovery_time, levels = c("lt30", "gt30")))
bin.dat3 <- dat3 %>%
 mutate(recovery_time = ifelse(recovery_time > 30, "gt30", "lt30")) %>%
  mutate(recovery_time = factor(recovery_time, levels = c("lt30", "gt30")))
bin.dat <- bin.dat1</pre>
summary(bin.dat)
##
                    gender
                                                   height
                                                                   weight
                             race
                                      smoking
         age
## Min.
           :45.00
                    0:1842
                             1:2372
                                      0:2223
                                               Min.
                                                      :151.2
                                                               Min.
                                                                      : 56.70
## 1st Qu.:57.00
                    1:1781
                             2: 172
                                      1:1034
                                               1st Qu.:166.2
                                                               1st Qu.: 75.40
## Median :60.00
                             3: 716
                                               Median :170.2
                                                               Median: 80.20
                                      2: 366
```

```
## Mean
          :60.06
                           4: 363
                                             Mean
                                                    :170.2
                                                            Mean
                                                                   : 80.13
## 3rd Qu.:63.00
                                             3rd Qu.:174.2
                                                            3rd Qu.: 84.80
## Max.
          :77.00
                                                  :188.6 Max. :103.40
                                             SBP
                                                            LDL
##
        bmi
                   hypertension diabetes
                                                                       vaccine
## Min.
          :19.70
                   0:1891
                               0:3065
                                        Min.
                                               :102.0
                                                       Min.
                                                              : 28.0
                                                                       0:1469
  1st Qu.:25.80
                   1:1732
                                1: 558
                                        1st Qu.:125.0
                                                        1st Qu.: 97.0
##
                                                                       1:2154
## Median :27.60
                                        Median :130.0
                                                       Median :110.0
          :27.73
                                        Mean :130.2
## Mean
                                                       Mean
                                                             :110.5
## 3rd Qu.:29.40
                                        3rd Qu.:136.0
                                                       3rd Qu.:124.0
## Max.
          :39.80
                                        Max.
                                              :158.0
                                                       Max.
                                                             :174.0
## severity study
                     recovery_time
## 0:3289
           A: 728
                     1t30:1102
                     gt30:2521
## 1: 334
          B:2171
##
            C: 724
##
##
##
```

2 Data partition

```
# data partition
dat.matrix <- model.matrix(recovery_time ~ ., dat)[ ,-1]

set.seed(2023)
trainRows <- createDataPartition(y = dat$recovery_time, p = 0.8, list = FALSE)

train.dat <- dat[trainRows,]
train.bin.dat <- bin.dat[trainRows,]

train.dat.matrix <- model.matrix(~., train.dat)[, -1]
train.bin.dat.matrix <- model.matrix(~., train.bin.dat)[, -1]

train.x <- dat.matrix[trainRows,]
train.y <- dat$recovery_time[trainRows]

test.x <- dat.matrix[-trainRows,]
test.y <- dat$recovery_time[-trainRows]
test.y <- dat$recovery_time[-trainRows]
test.y <- dat$recovery_time[-trainRows]</pre>
```

3 Primary Analysis

3.1 Exploratory analysis and data visualization

3.1.1 Data Frame Summary

 ${\bf train.dat}$

 $\textbf{Dimensions:}\ \ 2900 \ x\ 15$

Duplicates: 0

NI -	Vaniak 1-	Ctata / Val	Freqs (% of	Charle		M:
No	Variable	Stats / Values	Valid)	Graph	Valid	Missing
1	age	Mean (sd) : 60.1	33 distinct	:	2900	0
	[numeric]	(4.5)	values	:	(100.0%)	(0.0%)
		$\min < \max < \max$.::		
		45 < 60 < 77		:::.		
2	gender	IQR (CV) : 6 (0.1) 1. 0	1468 (50.6%)	.::::. IIIIIIIII	2900	0
2	[factor]	2. 1	1432 (49.4%)	IIIIIIIII	(100.0%)	(0.0%)
3	race	1. 1	1909 (65.8%)	IIIIIIIIIIIII	2900	0.070)
0	[factor]	2. 2	132 (4.6%)	1111111111111	(100.0%)	(0.0%)
	[Idetor]	3. 3	568 (19.6%)	III	(100.070)	(0.070)
		4. 4	291 (10.0%)	II		
4	smoking	1. 0	1763 (60.8%)	IIIIIIIIIII	2900	0
	[factor]	2. 1	845 (29.1%)	IIIII	(100.0%)	(0.0%)
	. ,	3. 2	292 (10.1%)	II	(' ' ' ' ' ' ' ' ' ' ' ' ' ' ' ' ' ' '	(/
5	height	Mean (sd) : 170.2 (6)	312 distinct	::	2900	0
	[numeric]	$\min < \max < \max$	values	::	(100.0%)	(0.0%)
		151.2 < 170.1 <		.::.		
		188.6		::::		
		IQR (CV) : 8 (0)		.::::.		
6	weight	Mean (sd) : 80.2 (7)	361 distinct	.:	2900	0
	[numeric]	$\min < \max < \max$:	values	.::	(100.0%)	(0.0%)
		57.1 < 80.3 < 103.4		::::		
		IQR (CV) : 9.5 (0.1)		.::::.		
_		25 (1) 25 2	4.00 14	.:::::.		
7	bmi	Mean (sd) : 27.8	160 distinct	: .	2900	0
	[numeric]	(2.7)	values	::	(100.0%)	(0.0%)
		$\min < \max < \max$:::.		
		19.7 < 27.7 < 39.8		::::		
0	1	IQR (CV) : 3.6 (0.1)	1514 (50.007)	::::::	0000	0
8	hypertension	1. 0 2. 1	1514 (52.2%)	IIIIIIIII IIIIIIIII	2900 (100.0%)	$0 \\ (0.0\%)$
9	[factor] diabetes	1. 0	1386 (47.8%) 2446 (84.3%)		2900	(0.076)
9	[factor]	2. 1	454 (15.7%)	III	(100.0%)	(0.0%)
10	SBP	Mean (sd) : 130.2	54 distinct	:	2900	0.070)
10	[numeric]	(8.1)	values	· :.	(100.0%)	
	[Humerie]	$\min < \max < \max$	varues	:::.	(100.070)	(0.070)
		104 < 130 < 158		.::::		
		IQR (CV) : 11 (0.1)		. : : : : :		
11	LDL	Mean (sd): 110.3	116 distinct	.:	2900	0
	[numeric]	(19.9)	values	:::	(100.0%)	(0.0%)
	J	$\min < \max < \max$:::.	()	('*/
		32 < 110 < 174		:::::		
		IQR (CV) : 27 (0.2)		.:::::		
12	vaccine	1. 0	1192 (41.1%)	IIIIIIII	2900	0
	[factor]	2. 1	1708 (58.9%)	IIIIIIIIII	(100.0%)	(0.0%)
	- *		, ,		. /	. ,

No	Variable	Stats / Values	Freqs (% of Valid)	Graph	Valid	Missing
13	severity [factor]	1. 0 2. 1	2619 (90.3%) 281 (9.7%)	IIIIIIIIIIIIIIIIII	2900 (100.0%)	0 (0.0%)
14	study	1. A	580 (20.0%)	IIII	2900 (100.0%)	0
	[factor]	2. B 3. C	1750 (60.3%) 570 (19.7%)	IIIIIIIIIIIIIIIIIIIIIIIIIIIIIIIIIIIIII	,	(0.0%)
15	recovery_time [numeric]	Mean (sd): 43 (30.5) min < med < max:	144 distinct values	: ::	$2900 \ (100.0\%)$	$0 \\ (0.0\%)$
		3 < 38 < 365 IQR (CV) : 21 (0.7)		::		
				::.		

skimr::skim_without_charts(train.dat)

Table 2: Data summary

Name	train.dat
Number of rows	2900
Number of columns	15
Column type frequency:	
factor	8
numeric	7
Group variables	None

Variable type: factor

skim_variable	n_missing	$complete_rate$	ordered	n_unique	top_counts
gender	0	1	FALSE	2	0: 1468, 1: 1432
race	0	1	FALSE	4	1: 1909, 3: 568, 4: 291, 2: 132
smoking	0	1	FALSE	3	0: 1763, 1: 845, 2: 292
hypertension	0	1	FALSE	2	0: 1514, 1: 1386
diabetes	0	1	FALSE	2	0: 2446, 1: 454
vaccine	0	1	FALSE	2	1: 1708, 0: 1192
severity	0	1	FALSE	2	0: 2619, 1: 281
study	0	1	FALSE	3	B: 1750, A: 580, C: 570

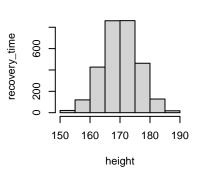
Variable type: numeric

skim_variable	n_missing	complete_rate	mean	sd	p0	p25	p50	p75	p100
age	0	1	60.07	4.51	45.0	57.0	60.00	63.0	77.0
height	0	1	170.17	6.04	151.2	166.1	170.15	174.1	188.6
weight	0	1	80.20	7.00	57.1	75.4	80.30	84.9	103.4
bmi	0	1	27.76	2.73	19.7	25.9	27.70	29.5	39.8
SBP	0	1	130.19	8.08	104.0	125.0	130.00	136.0	158.0
LDL	0	1	110.27	19.87	32.0	97.0	110.00	124.0	174.0
${\tt recovery_time}$	0	1	43.02	30.51	3.0	28.0	38.00	49.0	365.0

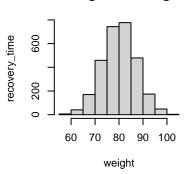
```
## Remember to edit the next chunk if you do any modification here:)
cts_var = c("age", "height", "weight", "bmi", "SBP", "LDL")
fct_var = c("gender", "race", "smoking", "hypertension", "diabetes", "vaccine", "severity", "study")
# scatter plot of continuous predictors
par(mfrow=c(2, 3))
for (i in 1:length(cts_var)){
  var = cts_var[i]
  plot(recovery_time~train.dat[,var],
       data = train.dat,
       ylab = "recovery time",
       xlab = var,
       main = str_c("Scatter Plot of ", var))
  lines(stats::lowess(train.dat[,var], train.dat$recovery_time), col = "red", type = "l")
}
        Scatter Plot of age
                                     Scatter Plot of height
                                                                    Scatter Plot of weight
                                      ത്യാത ര
                                                                               <u>റത്താത്താ</u>
                                                                 300
    300
                                  300
recovery time
                              recovery time
                                                             recovery time
   00
                                  100
                                                                 100
       45
            55
                  65
                       75
                                         160
                                                   180
                                                                     60
                                                                         70
                                                                             80
                                                                                 90
                                                                                    100
                                     150
                                              170
                                                       190
                                             height
                                                                            weight
               age
        Scatter Plot of bmi
                                                                     Scatter Plot of LDL
                                      Scatter Plot of SBP
   300
                                  300
                                                                 300
ecovery time
                               ecovery time
                                                             recovery time
   100
                                                                 100
                                  100
    0
                                  0
                                                                 0
                                                                          80
                                                                               120
       20
           25
                30
                    35
                         40
                                       110
                                              130
                                                    150
                                                                     40
                                                                                    160
               bmi
                                              SBP
                                                                             LDL
for (i in 1:length(cts_var)){
  var = cts_var[i]
  hist(train.dat[,var],
       ylab = "recovery_time",
       xlab = var,
       main = str_c("Histogram of ", var))
}
```

Histogram of age

Histogram of height



Histogram of weight



Histogram of bmi

30

bmi

recovery_time

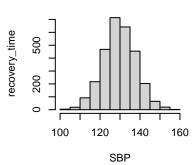
900

200

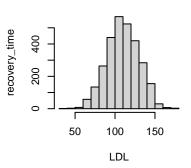
20 25

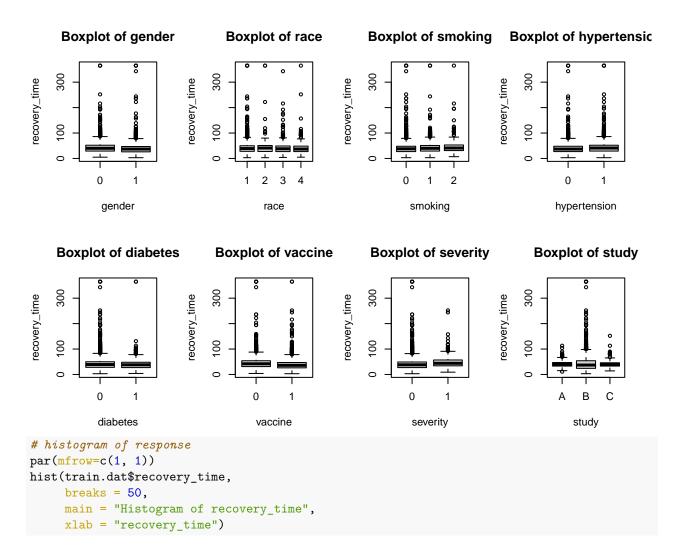


Histogram of SBP

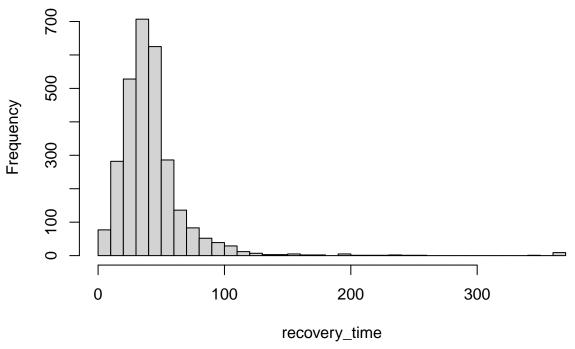


Histogram of LDL

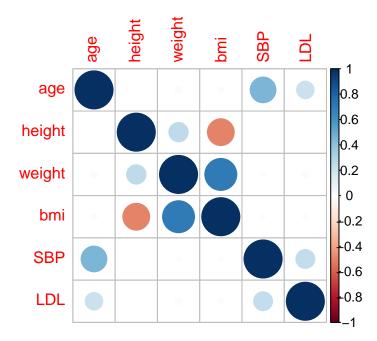




Histogram of recovery_time



Correlation plot of continuous variables

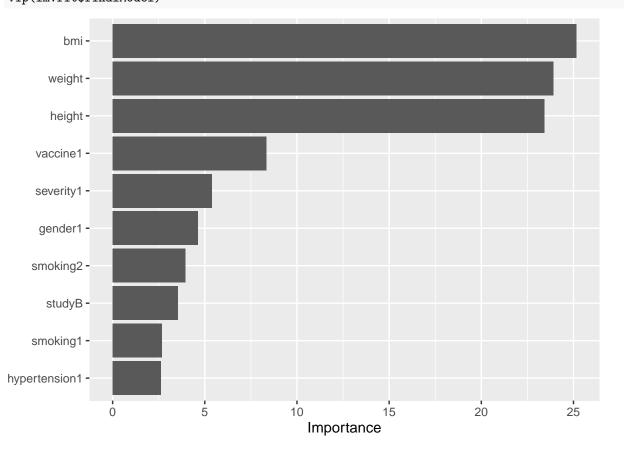


3.2 Model Training

```
ctrl1 <- trainControl(method = "cv", number = 5)</pre>
```

3.2.1 Linear Model

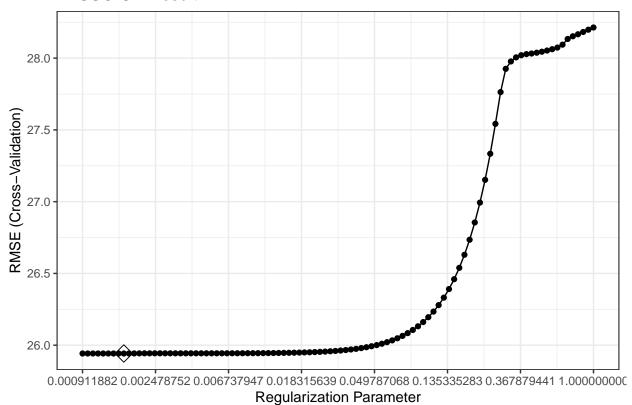
```
set.seed(2023)
lm.fit <- train(train.x, train.y,</pre>
               method = "lm",
               trControl = ctrl1)
coef(lm.fit$finalModel)
     (Intercept)
                                     gender1
                                                     race2
                           age
## -3.190120e+03 1.163953e-01 -4.443893e+00 2.189010e+00 -6.599719e-01
##
                      smoking1
                                    smoking2
                                                    height
           race4
## -1.156806e+00 2.905693e+00 6.427376e+00 1.866280e+01 -2.014323e+01
##
             bmi hypertension1
                                   diabetes1
                                                       SBP
##
  6.056969e+01 4.165589e+00 -1.152370e+00 -7.863399e-02 -4.215262e-02
##
        vaccine1
                     severity1
                                      studyB
## -8.133542e+00 8.747096e+00 4.368587e+00 -6.869681e-01
vip(lm.fit$finalModel)
```



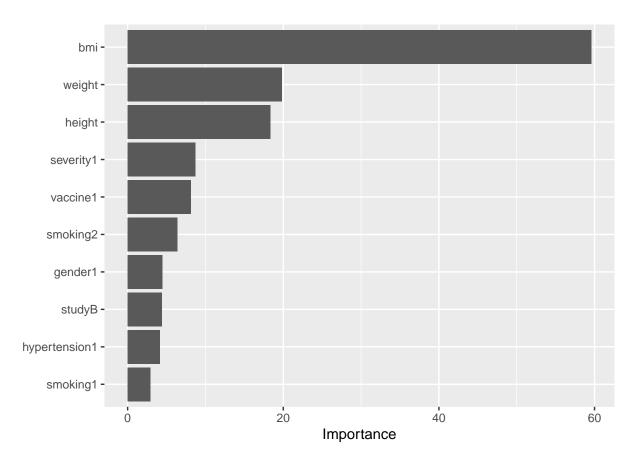
3.2.2 LASSO

```
set.seed(2023)
lasso.fit <- train(train.x, train.y,</pre>
                  method = "glmnet",
                  tuneGrid = expand.grid(
                    alpha = 1,
                    lambda = exp(seq(0, -7, length=100))),
                  trControl = ctrl1)
lasso.fit$bestTune
## alpha
               lambda
## 9
        1 0.001605462
coef(lasso.fit$finalModel, s = lasso.fit$bestTune$lambda)
## 19 x 1 sparse Matrix of class "dgCMatrix"
##
                           s1
## (Intercept) -3.134172e+03
## age
                1.153955e-01
## gender1
                -4.441866e+00
## race2
                2.191861e+00
## race3
               -6.681255e-01
## race4
                -1.149670e+00
## smoking1
                2.901232e+00
               6.400802e+00
## smoking2
## height
                1.833161e+01
## weight
                -1.979266e+01
## bmi
                 5.956877e+01
## hypertension1 4.150461e+00
## diabetes1
             -1.160249e+00
## SBP
                -7.746419e-02
## LDL
                -4.212203e-02
## vaccine1
              -8.147730e+00
## severity1
               8.730928e+00
## studyB
                 4.369356e+00
## studyC
                -6.781352e-01
ggplot(lasso.fit, highlight = TRUE) +
 labs(title="LASSO CV Result") +
 scale_x_continuous(trans='log',n.breaks = 10) +
 theme_bw()
```

LASSO CV Result



ggsave("./figure/lasso_cv.jpeg", dpi = 500)
vip(lasso.fit\$finalModel)

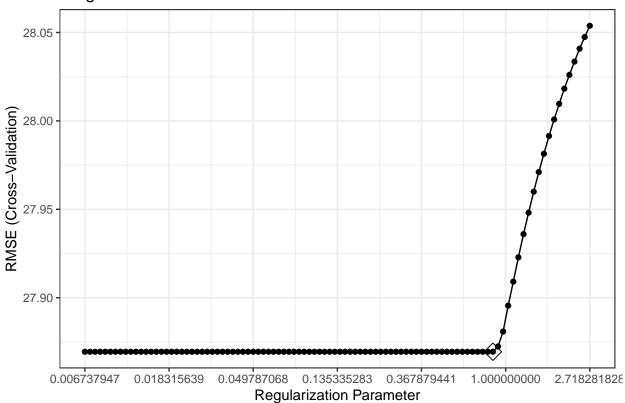


3.2.3 Ridge

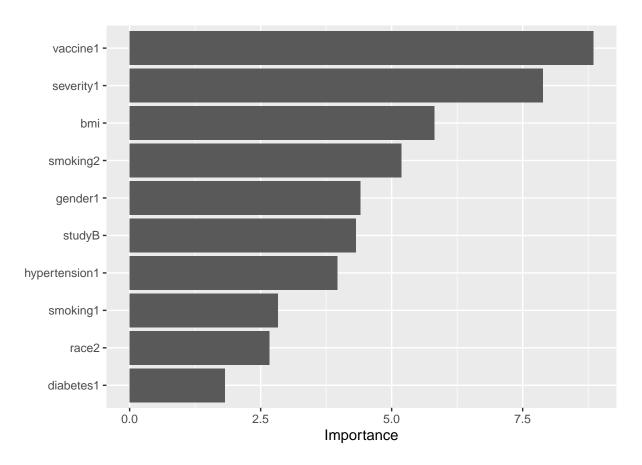
```
## 19 x 1 sparse Matrix of class "dgCMatrix"
                -131.33806374
## (Intercept)
                   0.09731228
## age
## gender1
                   -4.40320528
## race2
                   2.66527141
## race3
                  -1.32710400
## race4
                  -1.12570977
## smoking1
                   2.82624366
## smoking2
                   5.18400128
## height
                   0.60404463
```

```
## weight
                   -1.01341715
## bmi
                    5.81922510
## hypertension1
                   3.96367066
## diabetes1
                   -1.81677375
## SBP
                   -0.06303616
## LDL
                   -0.04440780
## vaccine1
                   -8.84608080
## severity1
                   7.88676978
## studyB
                    4.32156225
## studyC
                   -0.51357417
ggplot(ridge.fit,highlight = TRUE) +
  scale_x_continuous(trans='log', n.breaks = 6) +
  labs(title="Ridge CV Result") +
  theme_bw()
```

Ridge CV Result



```
ggsave("./figure/ridge_cv.jpeg", dpi = 500)
vip(ridge.fit$finalModel)
```

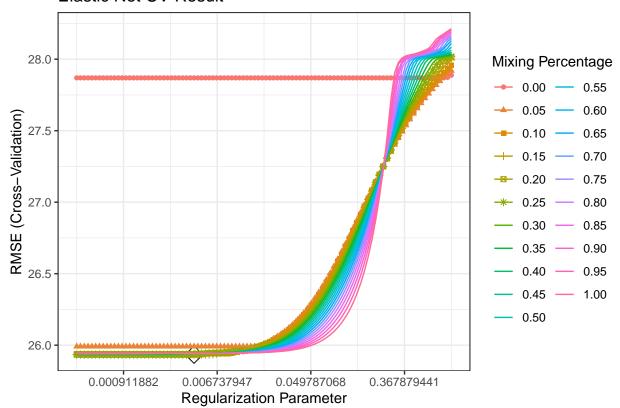


3.2.4 Elastic Net

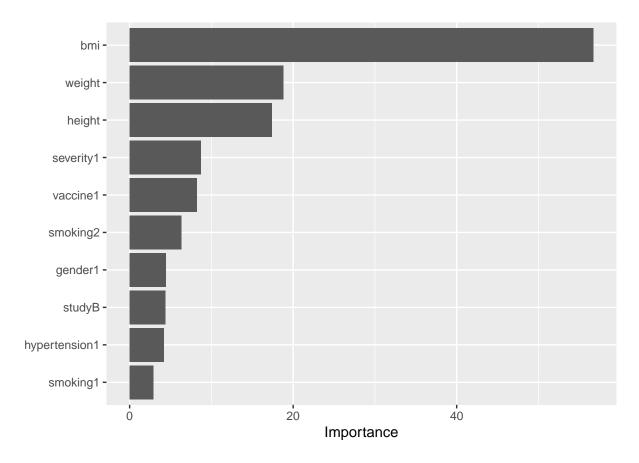
```
## 19 x 1 sparse Matrix of class "dgCMatrix"
##
## (Intercept)
                -2.973365e+03
                 1.150907e-01
## age
## gender1
                -4.447763e+00
## race2
                 2.221991e+00
## race3
                -7.070056e-01
## race4
                -1.153498e+00
## smoking1
                2.906092e+00
## smoking2
                 6.349675e+00
```

```
## height
                  1.738293e+01
## weight
                 -1.878818e+01
## bmi
                  5.669617e+01
## hypertension1 4.168257e+00
                -1.199482e+00
## diabetes1
## SBP
                 -7.836707e-02
## LDL
                 -4.236166e-02
## vaccine1
                 -8.201080e+00
## severity1
                  8.701657e+00
## studyB
                  4.377894e+00
## studyC
                 -6.636602e-01
ggplot(enet.fit, highlight = TRUE) +
  scale_x_continuous(trans='log', n.breaks = 6) +
 labs(title ="Elastic Net CV Result") +
 theme_bw()
```

Elastic Net CV Result

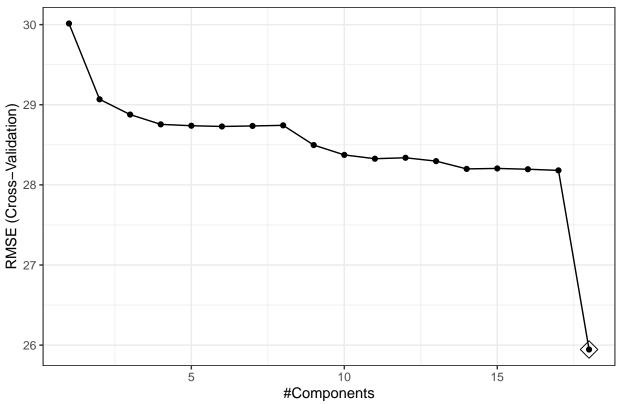


```
ggsave("./figure/enet_cv.jpeg", dpi = 500)
vip(enet.fit$finalModel)
```



3.2.5 Principal components regression (PCR)

PCR CV Result



```
ggsave("./figure/pcr_cv.jpeg", dpi = 500)
pcr.fit$bestTune
```

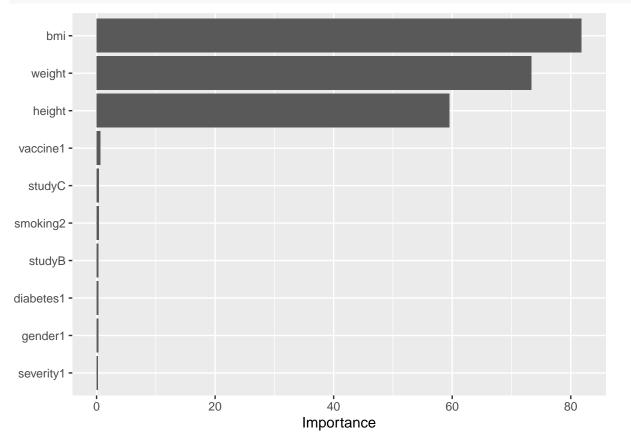
ncomp ## 18 18

coef(pcr.fit\$finalModel)

```
## , , 18 comps
##
##
                     .outcome
                    0.5252538
## age
## gender1
                   -2.2221586
## race2
                   0.4563464
## race3
                   -0.2619635
## race4
                   -0.3476329
## smoking1
                   1.3205684
## smoking2
                    1.9344423
## height
                  112.6936931
## weight
                 -141.0001175
                  165.1518985
## bmi
## hypertension1
                   2.0811234
                   -0.4188178
## diabetes1
## SBP
                   -0.6356938
## LDL
                  -0.8376686
## vaccine1
                  -4.0025673
## severity1
                  2.5879846
```

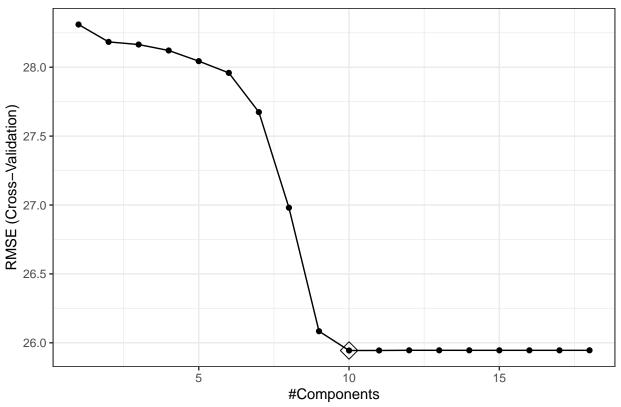
```
## studyB 2.1374000
## studyC -0.2730416
```

vip(pcr.fit\$finalModel)



3.2.6 Partial Least Squares (PLS)

PLS CV Result



```
ggsave("./figure/pls_cv.jpeg", dpi = 500)
pls.fit$bestTune
```

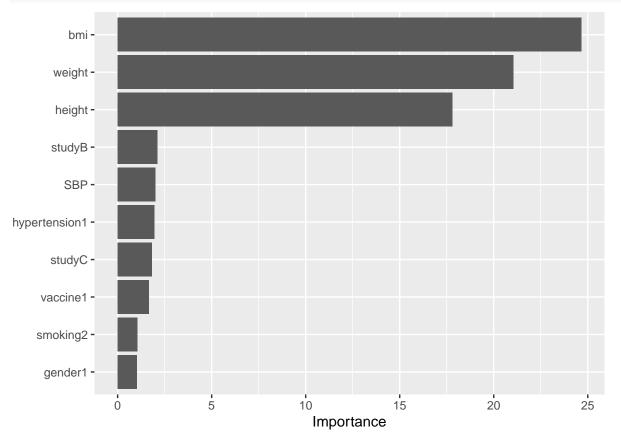
ncomp ## 10 10

coef(pls.fit\$finalModel)

```
## , , 10 comps
##
##
                     .outcome
                    0.2557655
## age
                   -2.2288535
## gender1
## race2
                    0.4448161
## race3
                   -0.1161982
## race4
                   -0.4146309
## smoking1
                    1.3626057
## smoking2
                    1.8793373
## height
                  112.5738962
## weight
                 -140.9034395
## bmi
                  165.0235495
## hypertension1
                    2.1927025
## diabetes1
                   -0.4588377
## SBP
                   -0.6092501
## LDL
                   -0.7129796
## vaccine1
                   -4.0284909
## severity1
                   2.5664367
```

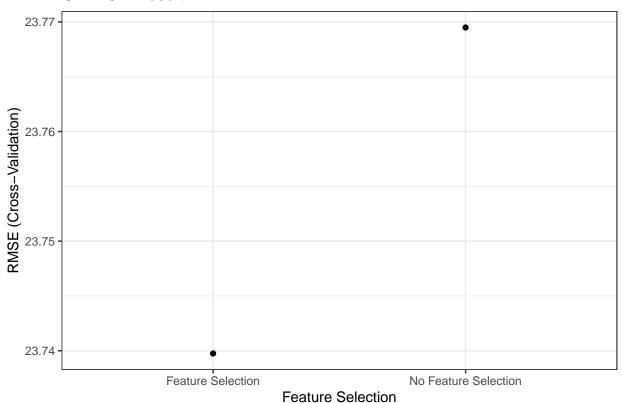
```
## studyB 2.1234056
## studyC -0.2961257
```

vip(pls.fit\$finalModel)



3.2.7 Generalized Additive Model (GAM)

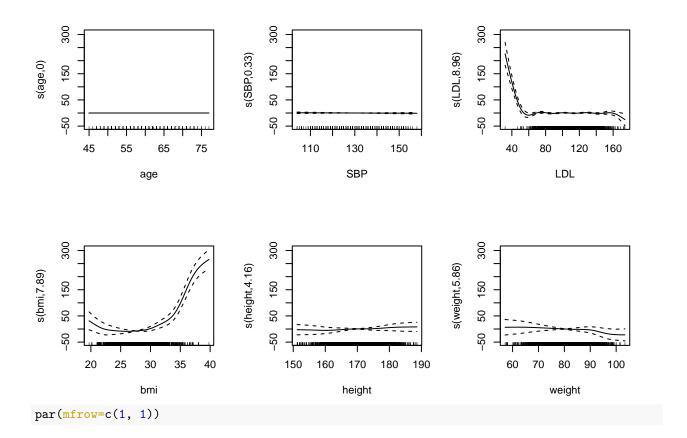
GAM CV Result



```
ggsave("./figure/gam_cv.jpeg", dpi = 500)
gam.fit$bestTune
```

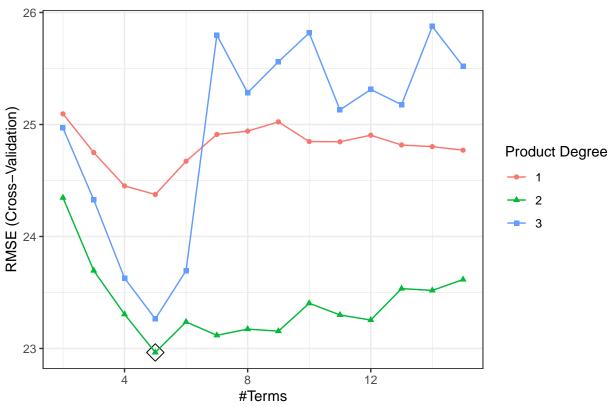
```
## select method
## 2 TRUE GCV.Cp
# coef(gam.fit$finalModel)
gam.fit$finalModel
```

```
## Family: gaussian
## Link function: identity
##
## Formula:
   .outcome ~ gender1 + race3 + race4 + smoking1 + smoking2 + hypertension1 +
##
       diabetes1 + vaccine1 + severity1 + studyB + studyC + s(age) +
##
       s(SBP) + s(LDL) + s(bmi) + s(height) + s(weight)
##
## Estimated degrees of freedom:
## 0.000 0.329 8.959 7.893 4.163 5.856 total = 39.2
##
## GCV score: 524.051
par(mfrow=c(2, 3))
plot(gam.fit$finalModel)
```



3.2.8 Multivariate Adaptive Regression Splines (MARS)





```
ggsave("./figure/mars_cv.jpeg", dpi = 500)
mars.fit$bestTune
```

nprune degree ## 18 5 2

coef(mars.fit\$finalModel)

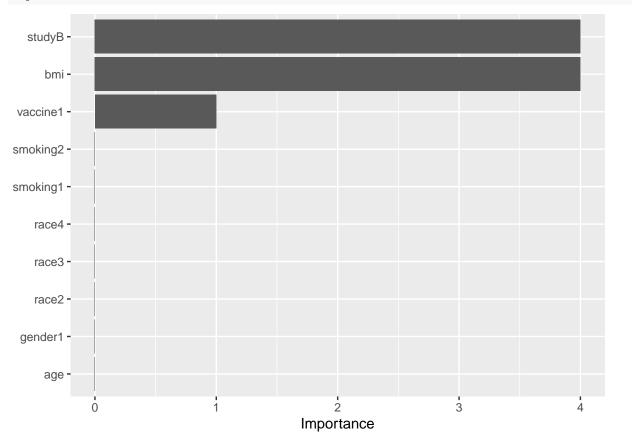
##	(Intercept)	h(31.7-bmi)	h(bmi-31.7) * studyB
##	19.366730	3.705371	34.383832
##	h(bmi-26.8)	vaccine1	
##	6.695655	-7.788338	

summary(mars.fit\$finalModel)

```
## Call: earth(x=matrix[2900,18], y=c(40,34,31,50,3...), keepxy=TRUE, degree=2,
               nprune=5)
##
##
                        coefficients
##
## (Intercept)
                           19.366730
## vaccine1
                           -7.788338
## h(bmi-26.8)
                            6.695655
## h(31.7-bmi)
                            3.705371
## h(bmi-31.7) * studyB
                           34.383832
##
## Selected 5 of 25 terms, and 3 of 18 predictors (nprune=5)
## Termination condition: Reached nk 37
## Importance: bmi, studyB, vaccine1, age-unused, gender1-unused, ...
```

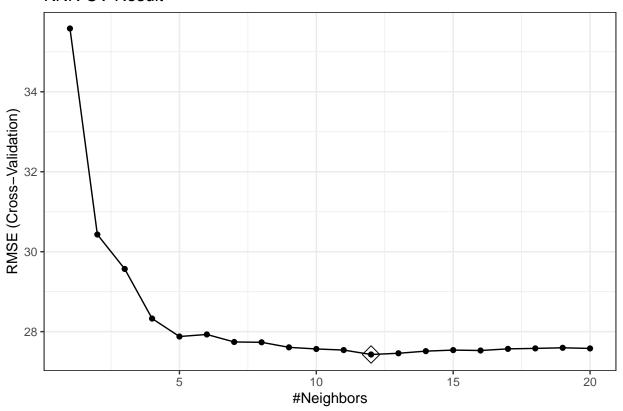
```
## Number of terms at each degree of interaction: 1 3 1   
## GCV 491.1694    RSS 1413606    GRSq 0.4723714    RSq 0.4760052
```

vip(mars.fit\$finalModel)



3.2.9 K-Nearest Neighbour (KNN)

KNN CV Result



```
ggsave("./figure/knn_cv.jpeg", dpi = 500)
knn.fit$bestTune
```

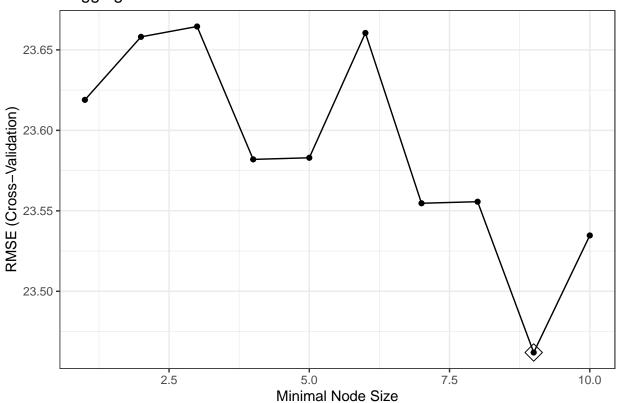
k ## 12 12

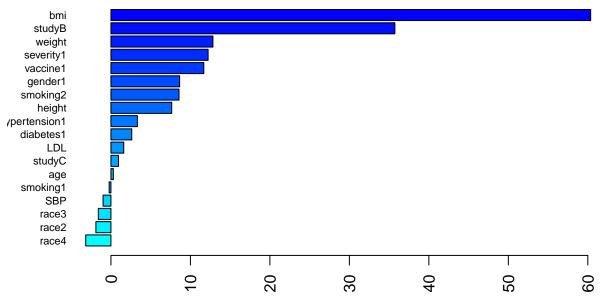
3.2.10 Bagging

```
## mtry splitrule min.node.size
## 9 18 variance 9
```

```
ggplot(bag.fit, highlight = TRUE) +
labs(title = "Bagging CV Result") +
theme_bw()
```

Bagging CV Result

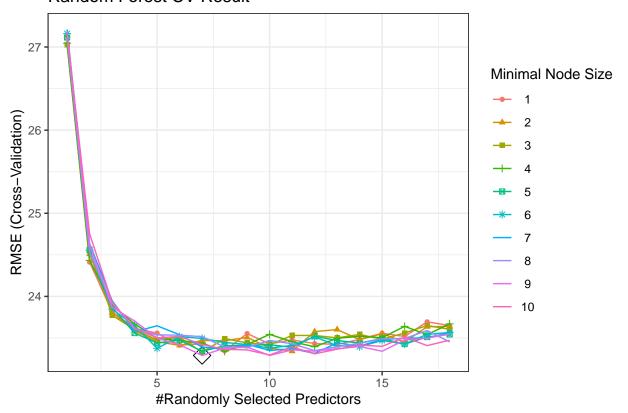


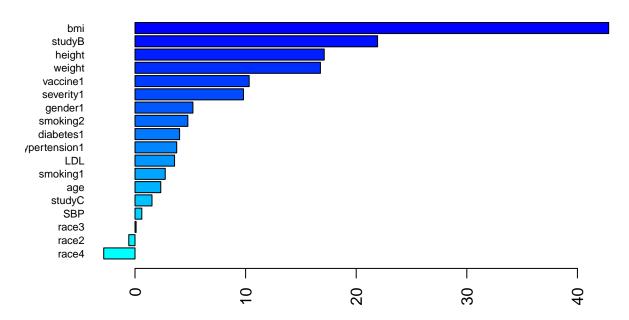


```
# p1 <- pdp::partial(</pre>
 bag.fit,
   pred.var = "Lot_Area",
#
  grid.resolution = 20
#
  ) %>%
#
  autoplot()
# p2 <- pdp::partial(
  bag.fit,
  pred.var = "Lot_Frontage",
  grid.resolution = 20
  ) %>%
  autoplot()
# gridExtra::grid.arrange(p1, p2, nrow = 1)
```

3.2.11 Random Forest

Random Forest CV Result

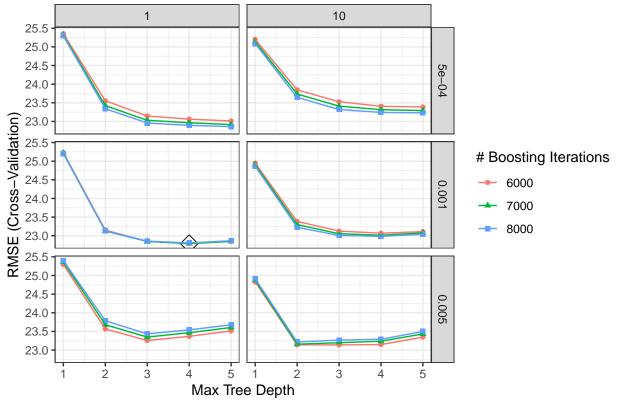




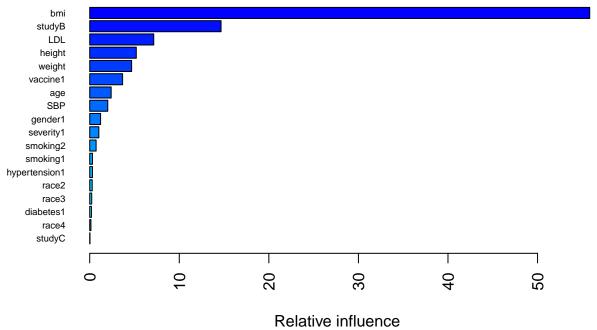
3.2.12 Boosting

```
ggplot(bst.fit, highlight = TRUE) +
  labs(title = "Boosting CV Result") +
  theme_bw()
```





ggsave("./figure/boosting_cv.jpeg", dpi = 500)
Variable Importance
summary(bst.fit\$finalModel, las = 2, cBars = ncol(train.x), cex.names = 0.6)

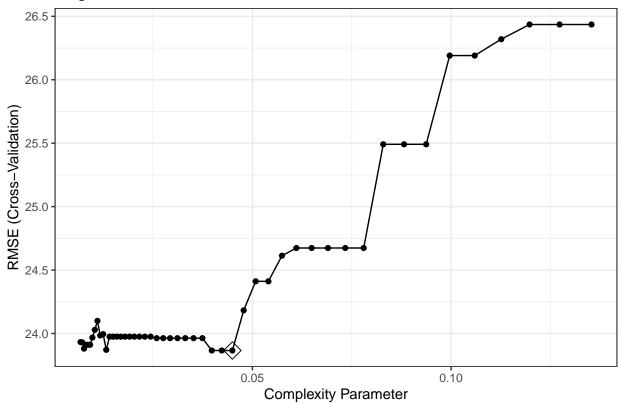


var rel.inf

```
bmi 55.82435579
## bmi
## studyB
                    studyB 14.66082079
## LDL
                      LDL 7.14824322
## height
                    height 5.20099563
## weight
                     weight 4.67820774
## vaccine1
                  vaccine1 3.66997663
                         age 2.39369807
## age
## SBP
                         SBP 2.01391839
                    gender1 1.21406824
## gender1
## severity1
                 severity1 1.01825404
## smoking2
                   smoking2 0.71254465
                    smoking1 0.30551973
## smoking1
## hypertension1 hypertension1 0.30244396
## race2
                      race2 0.28011065
## race3
                       race3 0.22397720
## diabetes1
                   diabetes1 0.19176667
## race4
                       race4 0.13327971
## studyC
                      studyC 0.02781888
```

3.2.13 Regression Trees

Regression Tree CV Result

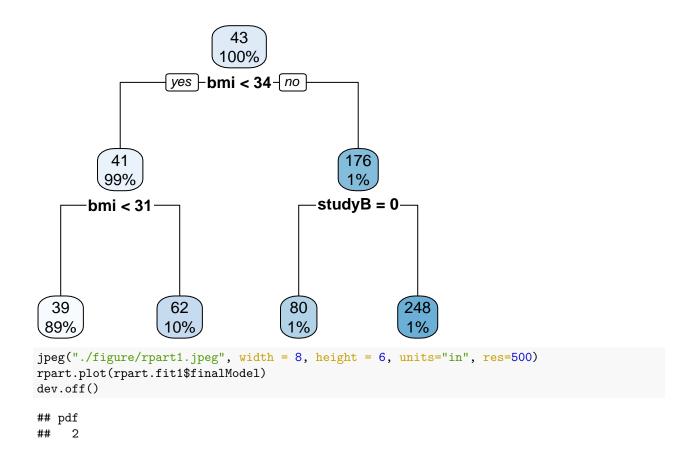


```
ggsave("./figure/rpart1_cv.jpeg", dpi = 500)
rpart.fit1$bestTune
```

cp ## 32 0.04495736

rpart.plot(rpart.fit1\$finalModel)

3.3 Model Selection 35



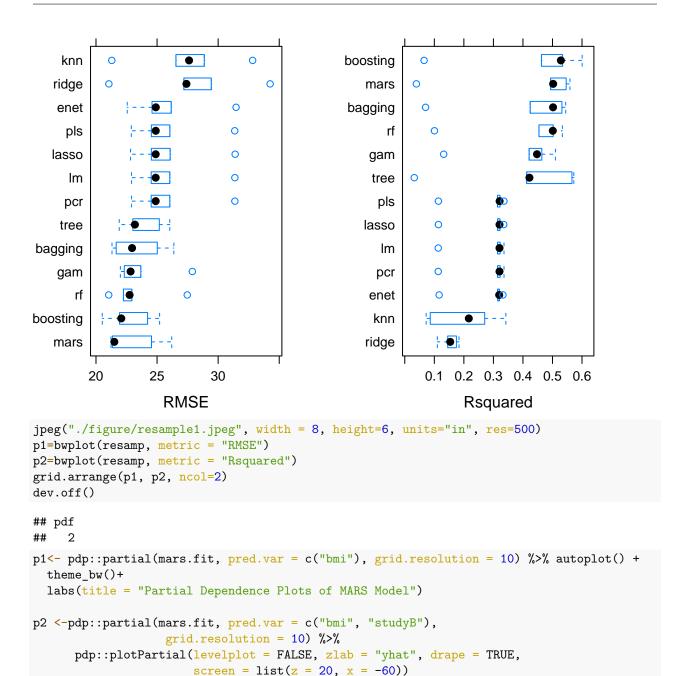
3.3 Model Selection

```
##
## Call:
## summary.resamples(object = resamp)
##
## Models: lm, lasso, ridge, enet, pcr, pls, gam, mars, knn, bagging, rf, boosting, tree
## Number of resamples: 5
##
## MAE
```

3.3 Model Selection 36

```
##
                Min. 1st Qu.
                                Median
                                            Mean 3rd Qu.
## lm
            16.23173 16.30828 16.52868 16.61900 16.59544 17.43085
## lasso
            16.21044 16.29219 16.49725 16.58977 16.53867 17.41030
            15.98311 16.49651 16.70285 16.85431 17.12329 17.96581
## ridge
                                                                      0
## enet
            16.16042 16.24960 16.36222 16.51089 16.42530 17.35693
## pcr
            16.23173 16.30828 16.52868 16.61900 16.59544 17.43085
            16.21851 16.31098 16.52109 16.60977 16.57408 17.42418
## pls
            14.96149 15.31743 15.35347 15.37421 15.37746 15.86122
## gam
## mars
            14.48861 14.54724 14.58285 15.06219 15.81591 15.87632
## knn
            15.16105 15.73142 15.79086 16.13709 16.38626 17.61583
## bagging 14.58743 14.76587 15.07453 15.19909 15.69039 15.87722
            14.26815 14.67895 14.92547 14.98461 15.22321 15.82726
                                                                      0
## boosting 14.09554 14.53527 14.69015 14.71165 15.03535 15.20193
                                                                      0
## tree
            14.91705 15.21864 15.45248 15.51302 15.91231 16.06462
##
## RMSE
##
                     1st Qu.
                                Median
                                            Mean 3rd Qu.
                                                              Max. NA's
                Min.
## lm
            22.91150 24.51831 24.88597 25.94526 26.04242 31.36808
            22.82812 24.53373 24.88628 25.94219 26.07031 31.39252
                                                                      0
## lasso
## ridge
            21.05565 27.19445 27.40378 27.86946 29.43813 34.25528
## enet
            22.55834 24.58644 24.89736 25.93351 26.15765 31.46776
            22.91150 24.51831 24.88597 25.94526 26.04242 31.36808
## pcr
            22.89214 24.53226 24.89142 25.94392 26.04558 31.35821
## pls
            21.99363 22.31575 22.83368 23.73975 23.66851 27.88718
## gam
            21.22944 21.34499 21.50208 22.96420 24.54460 26.19988
## mars
## knn
            21.29395 26.54338 27.61785 27.42866 28.86421 32.82391
            21.31058 21.65291 22.95364 23.46197 25.01913 26.37361
## bagging
                                                                      0
            21.04171 22.24775 22.75182 23.28937 22.93423 27.47134
                                                                      0
## boosting 20.51403 21.92962 22.07191 22.78917 24.22341 25.20691
## tree
            21.90520 23.01458 23.18530 23.86591 25.18408 26.04041
##
## Rsquared
##
                          1st Qu.
                                     Median
                                                  Mean
                                                         3rd Qu.
                  Min.
## lm
            0.11319560 0.31401617 0.3206204 0.2813453 0.3229742 0.3359202
            0.11386516 0.31421662 0.3206286 0.2811877 0.3221851 0.3350431
## lasso
            0.11015851 0.14523321 0.1538663 0.1535189 0.1747868 0.1835499
## ridge
                                                                              0
## enet
            0.11628655 0.31442226 0.3195815 0.2805479 0.3202588 0.3321902
            0.11319560\ 0.31401617\ 0.3206204\ 0.2813453\ 0.3229742\ 0.3359202
## pcr
                                                                               0
            0.11377107 0.31374985 0.3210112 0.2812813 0.3222148 0.3356594
## pls
            0.13171077 \ 0.42087488 \ 0.4475492 \ 0.3948083 \ 0.4638793 \ 0.5100272
## gam
            0.03921635 0.49381643 0.5023136 0.4281672 0.5463545 0.5591351
## mars
            0.07225895 0.08613868 0.2166700 0.1975252 0.2704826 0.3420757
## knn
                                                                              0
## bagging
           0.07033870 0.42448137 0.5019016 0.4146791 0.5319576 0.5447161
                                                                               0
            0.10049299 0.45424922 0.5011111 0.4183419 0.5024069 0.5334491
                                                                               0
## boosting 0.06532432 0.46267491 0.5284672 0.4382426 0.5343027 0.6004439
                                                                               0
            0.03210038 0.41264371 0.4220056 0.4009682 0.5659027 0.5721886
## tree
                                                                               0
p1=bwplot(resamp, metric = "RMSE")
p2=bwplot(resamp, metric = "Rsquared")
grid.arrange(p1, p2 ,ncol=2)
```

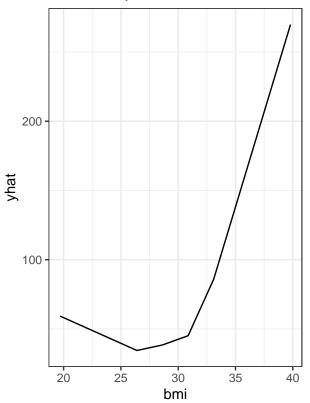
3.3 Model Selection 37

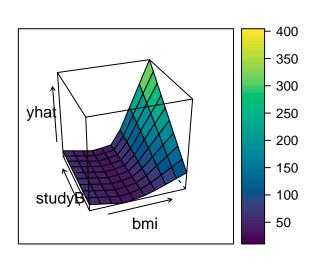


jpeg("./figure/partial_dependence.jpeg", width = 8, height=6, units="in", res=500)

gridExtra::grid.arrange(p1, p2, ncol = 2)

Partial Dependence Plots of MARS Model





dev.off()

Important variables

varImp(mars.fit\$finalModel)

0veral1 ## bmi 100.00000 ## studyB 100.00000 ## vaccine1 17.78457

3.4 Training / Testing Error

```
# training error
mars.train.pred = predict(mars.fit, newdata = train.x)
RMSE(train.y, mars.train.pred)
```

```
## [1] 22.07828
```

```
# testing error
mars.pred = predict(mars.fit, newdata = test.x)
RMSE(test.y, mars.pred)
```

[1] 22.1712

4 Secondary Analysis

4.1 Exploratory analysis and data visualization

4.1.1 Data Frame Summary

train.bin.dat

Dimensions: 2900×15

Duplicates: 0

Missing
0
0%) (0.0%)
(0.070)
0
0%) (0.0%)
0
0%) (0.0%)
770) (0.070)
0
0%) (0.0%)
770) (0.070)
0
0%) (0.0%)
770) (0.070)
0
0%) (0.0%)
770) (0.070)
0
0%) (0.0%)
770) (0.070)
0
0%) (0.0%)
0
0%) (0.0%)

No	Variable	Stats / Values	Freqs (% of Valid)	Graph	Valid	Missing
10	SBP	Mean (sd): 130.2	54 distinct	:	2900	0
	[numeric]	(8.1)	values	:.	(100.0%)	(0.0%)
		$\min < \max < \max$:		:::.		
		104 < 130 < 158		.::::		
		IQR (CV) : 11 (0.1)		.:::::		
11	LDL	Mean (sd) : 110.3	116 distinct	.:	2900	0
	[numeric]	(19.9)	values	:::	(100.0%)	(0.0%)
		$\min < \max < \max$:::.		
		32 < 110 < 174		:::::		
		IQR (CV) : 27 (0.2)		.:::::		
12	vaccine	1. 0	1192 (41.1%)	IIIIIIII	2900	0
	[factor]	2. 1	1708 (58.9%)	IIIIIIIIII	(100.0%)	(0.0%)
13	severity	1. 0	2619 (90.3%)	IIIIIIIIIIIIIIII	2900	0
	[factor]	2. 1	281 (9.7%)	I	(100.0%)	(0.0%)
14	study	1. A	580 (20.0%)	IIII	2900	0
	[factor]	2. B	1750 (60.3%)	IIIIIIIIIII	(100.0%)	(0.0%)
		3. C	570 (19.7%)	III	, ,	, ,
15	recovery_time	1. lt30	887 (30.6%)	IIIIII	2900	0
	[factor]	2. gt30	2013~(69.4%)	IIIIIIIIIII	(100.0%)	(0.0%)

skimr::skim_without_charts(train.bin.dat)

Table 6: Data summary

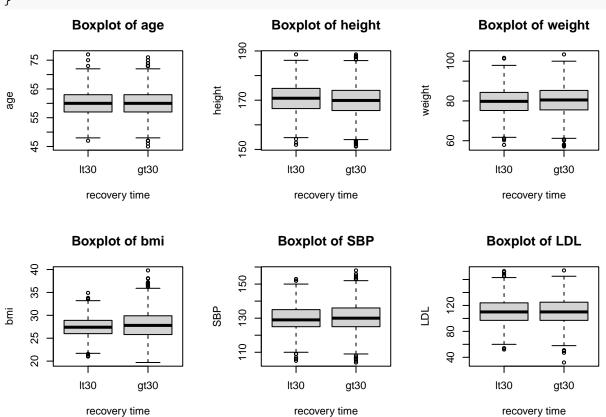
Name Number of rows	train.bin.dat
Number of columns	15
Column type frequency:	
factor	9
numeric	6
Group variables	None

Variable type: factor

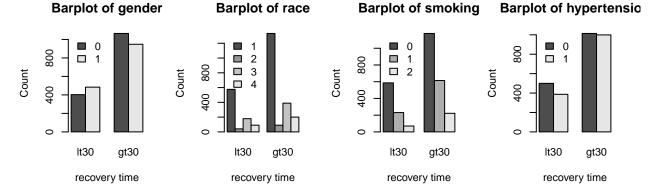
skim_variable	n_missing	$complete_rate$	ordered	n_unique	top_counts
gender	0	1	FALSE	2	0: 1468, 1: 1432
race	0	1	FALSE	4	1: 1909, 3: 568, 4: 291, 2: 132
smoking	0	1	FALSE	3	0: 1763, 1: 845, 2: 292
hypertension	0	1	FALSE	2	0: 1514, 1: 1386
diabetes	0	1	FALSE	2	0: 2446, 1: 454
vaccine	0	1	FALSE	2	1: 1708, 0: 1192
severity	0	1	FALSE	2	0: 2619, 1: 281
study	0	1	FALSE	3	B: 1750, A: 580, C: 570
recovery_time	0	1	FALSE	2	gt3: 2013, lt3: 887

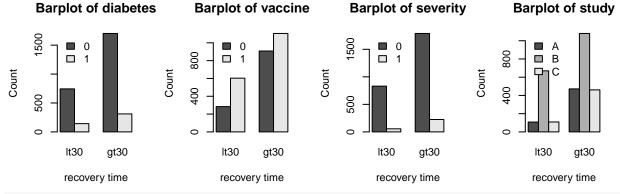
Variable type: numeric

skim_variable	n_missing	complete_rate	mean	sd	p0	p25	p50	p75	p100
age	0	1	60.07	4.51	45.0	57.0	60.00	63.0	77.0
height	0	1	170.17	6.04	151.2	166.1	170.15	174.1	188.6
weight	0	1	80.20	7.00	57.1	75.4	80.30	84.9	103.4
bmi	0	1	27.76	2.73	19.7	25.9	27.70	29.5	39.8
SBP	0	1	130.19	8.08	104.0	125.0	130.00	136.0	158.0
LDL	0	1	110.27	19.87	32.0	97.0	110.00	124.0	174.0

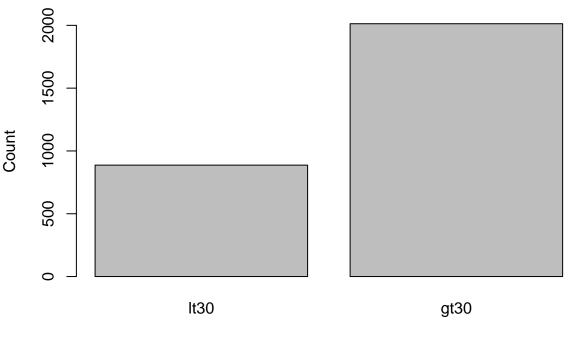


```
# barplot of categorical predictors
par(mfrow=c(2, 4))
for (i in 1:length(fct_var)){
```





Barplot of binary recovery_time



recovery time

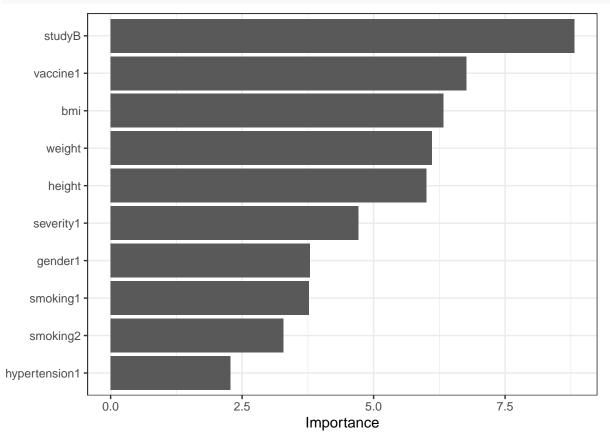
4.2 Model Training

4.2.1 Logistic Regression

```
## -85.313351100
                   0.014271893 -0.323467202 -0.104376256
                                                            -0.039351201
           race4
##
                      smoking1
                                    smoking2
                                                    height
                                                                  weight
     0.003550318
                                               0.502637208
##
                   0.367190652
                                 0.502782618
                                                            -0.545510559
##
             bmi hypertension1
                                   diabetes1
                                                       SBP
                                                                     LDL
##
     1.634689792
                   0.325697328 -0.070567897
                                              -0.005832901
                                                            -0.001829020
##
        vaccine1
                     severity1
                                                    studyC
                                      studyB
```

-0.600151829 0.761039467 -1.066825060 -0.031460504

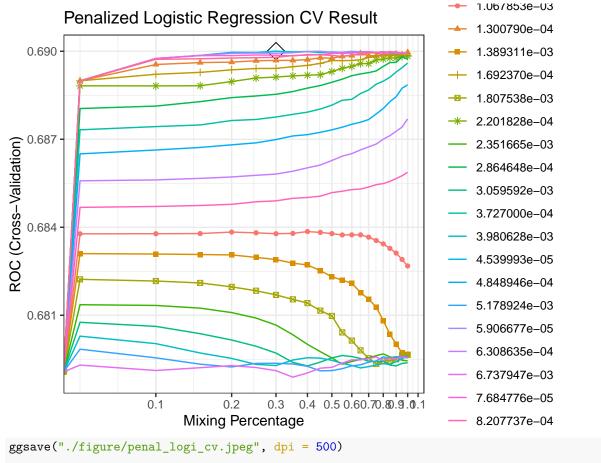
vip(glm.fit\$finalModel) + theme_bw()



4.2.2 Penalized Logistic Regression

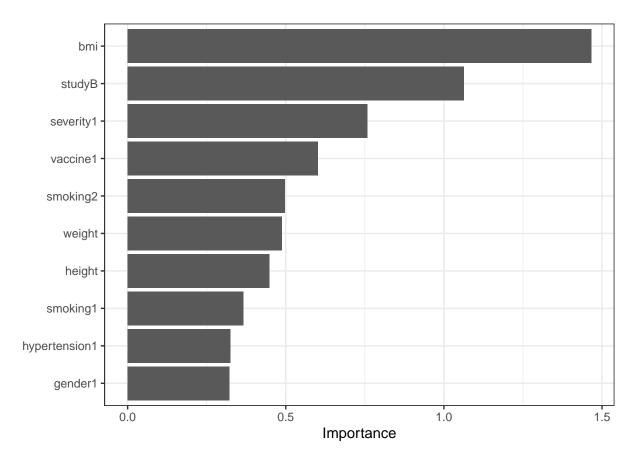
lambda

alpha



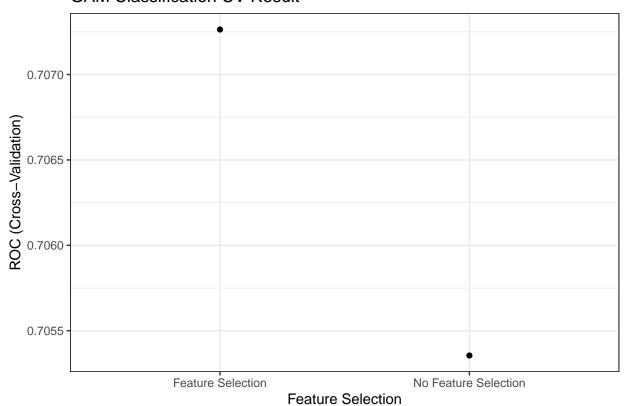
#coef(glmn.fit\$finalModel)

vip(glmn.fit\$finalModel) + theme_bw()



4.2.3 Generalized Additive Model (GAM) for classification

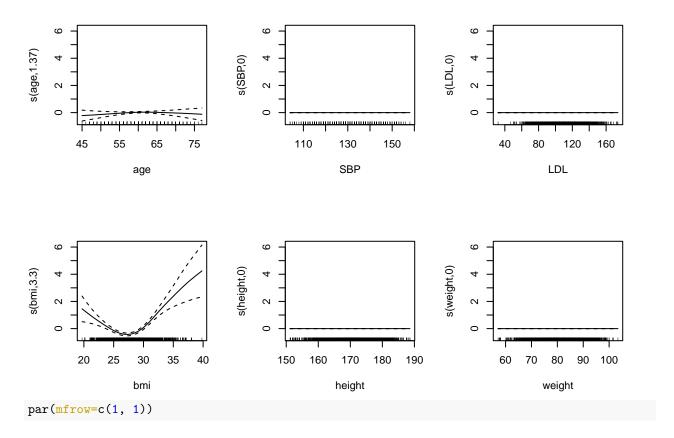
GAM Classification CV Result



```
ggsave("./figure/gam_binned_cv.jpeg", dpi = 500)
gam.bin.fit$bestTune
```

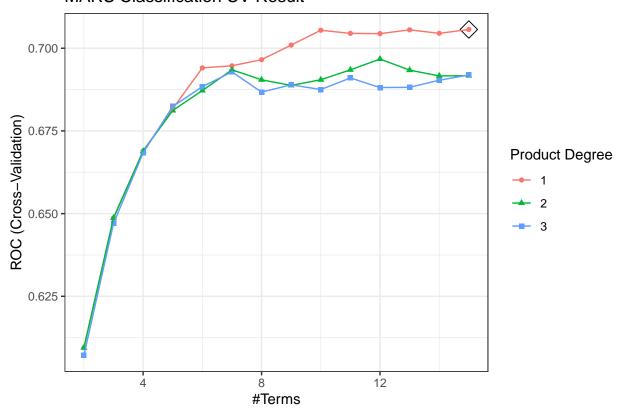
```
## select method
## 2 TRUE GCV.Cp
# coef(gam.fit$finalModel)

par(mfrow=c(2, 3))
plot(gam.bin.fit$finalModel)
```



4.2.4 Multivariate Adaptive Regression Splines (MARS) for classification

MARS Classification CV Result



ggsave("./figure/mars_binned_cv.jpeg", dpi = 500)

mars.bin.fit\$bestTune

nprune degree ## 14 15 1

coef(mars.bin.fit\$finalModel) %>%

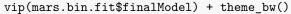
broom::tidy() %>%
knitr::kable()

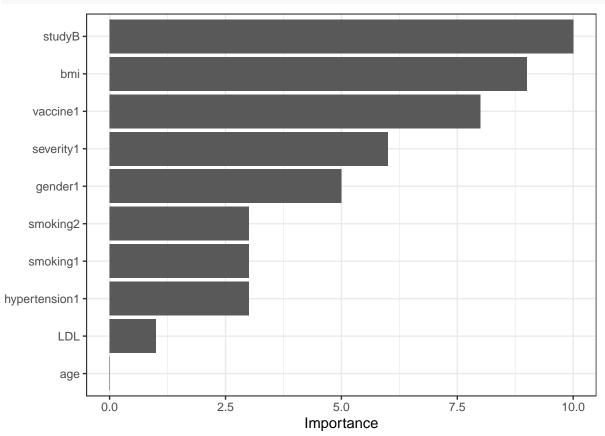
names	X
(Intercept)	1.1011705
studyB	-1.0779091
h(bmi-26.9)	0.2900212
h(26.9-bmi)	0.2935615
vaccine1	-0.6217928
severity1	0.7969230
gender1	-0.3261333
hypertension1	0.3099788
smoking1	0.3912885
smoking2	0.5358382
h(LDL-157)	-0.1512777

summary(mars.bin.fit\$finalModel)

Call: earth(x=matrix[2900,18], y=factor.object, keepxy=TRUE,

```
glm=list(family=function.object, maxit=100), degree=1, nprune=15)
##
##
## GLM coefficients
##
                       gt30
## (Intercept)
                  1.1011705
## gender1
                 -0.3261333
## smoking1
                  0.3912885
## smoking2
                  0.5358382
## hypertension1 0.3099788
## vaccine1
                 -0.6217928
## severity1
                  0.7969230
## studyB
                 -1.0779090
## h(26.9-bmi)
                  0.2935615
## h(bmi-26.9)
                  0.2900212
## h(LDL-157)
                 -0.1512777
##
## GLM (family binomial, link logit):
  nulldev
             df
                       dev
                             df
                                  devratio
                                                AIC iters converged
##
  3571.35 2899
                   3204.42 2889
                                     0.103
                                               3226
                                                        4
##
## Earth selected 11 of 14 terms, and 9 of 18 predictors (nprune=15)
## Termination condition: RSq changed by less than 0.001 at 14 terms
## Importance: studyB, bmi, vaccine1, severity1, gender1, smoking1, smoking2, ...
## Number of terms at each degree of interaction: 1 10 (additive model)
## Earth GCV 0.1906834
                          RSS 545.0022
                                          GRSq 0.1024844
                                                             RSq 0.1148255
```



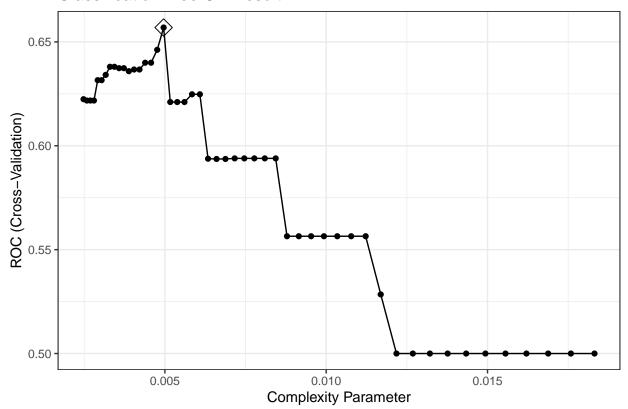


- 4.2.5 Linear Discriminant Analysis (LDA)
- 4.2.6 Quadratic Discriminant Analysis (QDA)
- 4.2.7 Naive Bayes (NB)
- 4.2.8 Bagging
- 4.2.9 Random Forest
- 4.2.10 Boosting
- 4.2.11 Classification Trees

```
## cp
## 18 0.004961126
```

```
ggplot(rpart.fit2, highlight = TRUE) +
labs(title = "Classification Tree CV Result") +
theme_bw()
```

Classification Tree CV Result



```
ggsave("./figure/rpart2_cv.jpeg", dpi = 500)
rpart.plot(rpart.fit2$finalModel)
```

```
jpeg("./figure/rpart2.jpeg", width = 8, height = 6, units="in", res=500)
rpart.plot(rpart.fit2$finalModel)
```

pdf ## 2

dev.off()

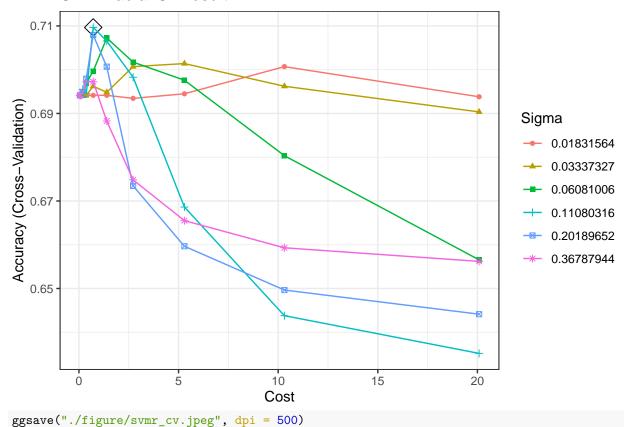
4.2.12 Support Vector Machine (SVM)

```
svmr.grid \leftarrow expand.grid(C = \exp(seq(-3, 3, len = 10)),
                           sigma = exp(seq(-4, -1, len = 6)))
set.seed(2023)
svmr.fit <- train(train.x,</pre>
                   train.bin.y,
                   method = "svmRadialSigma",
                   tuneGrid = svmr.grid,
                   trControl = ctrl1)
svmr.fit$bestTune
                          С
##
           sigma
## 28 0.1108032 0.7165313
myCol<- rainbow(25)</pre>
myPar <- list(superpose.symbol = list(col = myCol),</pre>
               superpose.line = list(col = myCol))
```

4.3 Model Selection 53

```
ggplot(svmr.fit, highlight = TRUE, par.settings = myPar) +
labs(title = "SVM Radial CV result") +
theme_bw()
```

SVM Radial CV result



4.3 Model Selection

4.4 Training / Testing Error