

4. (1342) (123) = (14132) $(1534269)^{-1} = (9624351)$ 50. The order of a permutation Pio the smallest interger south that P'= I (February).
Let P: P. P. ... Pn, x, & P, UP. UPn. If x. &P., & must be a multiple of 1P.1, the zame is true for all Ps. Ps. Pn. Smult be a multiple of 1Ps.1. Pn) to ensure that P' maps x to t. Therefore IPI= lcm (Pi. Pn). DIS WED 6b. (13674810) => (32685741091) =) (13) (16) (17) (14) (18) (110) Wen 9e. (25) = (5 2) [(25)(63)] = (36)(52) [(25)(256)] = (652)(52) (153429) - = (924351) [(1342)(123)]= (321)(2431) $(\frac{1}{3}, \frac{2}{5}, \frac{3}{7}, \frac{4}{7}, \frac{5}{7}, \frac{7}{8})^{-1} = \overline{L}(3571)(468)\overline{J}^{-1} = (864)(1753)$

6. Since block 16 1 the engly block I is at the same spot, and shifts can be written as a product of Transposition any shift up must have a shift cloure. The same of lift and right. Thus the Total coloring must be 1 2 3 4 is the identity, reachobbe 5678 9 10 11 12 13 14 15 = (14)(23)
= (9/2)(10/1) 4321 even permedicions, recenable 5678 1211/09 13 14 15 987 1121 = (1 10 3 8 .6 2 9 /2 5 11 4 12 3 4 5 zing 12 tycle => told # of lunspositions, not suchaple 13 14 15 8 14 11 3 = (189621410431113715512) 12 2 15 9 4 13 1 213e 15 eyell => even # 20licable 16 Assuming that the rest of the ruggle is complete. 1 2 3 4 5 6 7 8 We know that the only even permutation, 13 14 15, 14 15 13, 13 13 14. One is to 9 10 11 12 7 7 7 for the rest we do the following 1 2 3 4 1 2 3 4 5 6 7 8 5 6 7 8 => 14 9 16 11 => 14 13 9 11 => 1234 1 2 3 4 1234 5 6 7 8 5678 9 10 11 12 13/19/11 => 13 9 10 11 15 13 12 15 10 12 14 15 10 12 14 15 /- 17 14 15 B =) 1 2 3 4 9 10 11 12

Sinil (15 13 14) = (14, 15, 13), applying this algorithm times quilds the desired result. Mon Lec Consider as group of size 4, since it is a group, it is eleved and Each element has to appear in a now of lel + e, then lb or l'i must be e in this case it is the soldier grayn since it is nomorphic to n mod 4, the numbers votate like on a wheel. thelf is the cilentity and ler-b since neither is the celestiby and it is has always appeared thus it must be use morphic to the sock gazyr