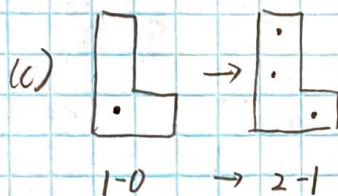
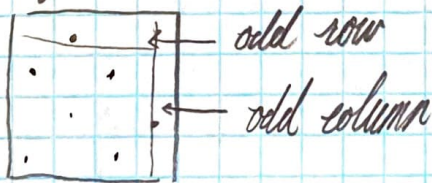


This preserves the parity of the difference between adjacent rows / columns

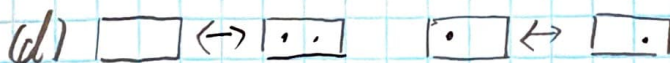
(1)-(2) is odd, so is (3)-(4), but in order to solve the board, they need to be 0 (even). \therefore it is impossible



Similar to (b), this preserves the parity of the diff between adjacent rows / columns.



Once again we have an odd row & an odd column. \therefore It is impossible



This pattern preserves the parity of the points in any row / col.

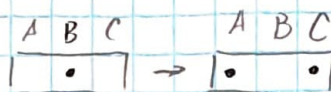
single row. We have a single row and therefore can't solve it.

(e)

A

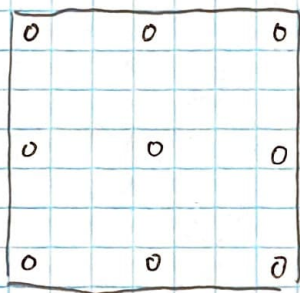
↓

•	B	C	A	B	C	A	B	C	A
B	C	A	B	C	A	B	C	A	B
C	A	B	C	A	B	C	A	B	• ← C



In any operation, the parity of AB , $B \cdot C$, $A \cdot C$ is preserved.
Since we have $1A$, $1C$, $A \cdot B$ is odd, and thus it is not solvable.

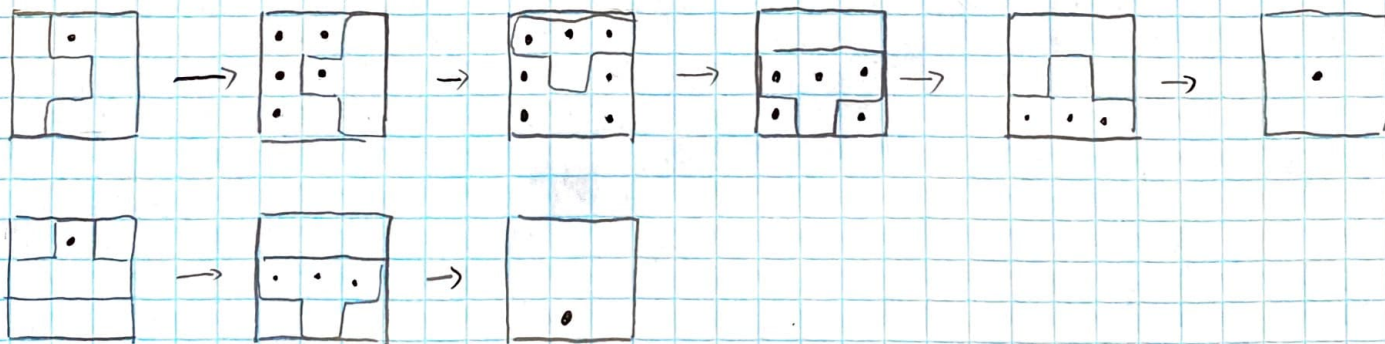
2



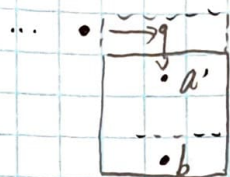
We can remove the marked squares. After removal we just tilt the row horizontally and everything else vertically.

Any other removal cannot be tiled because when we color ~~in~~ it in A, B, C colors, we need to have the board w/ equal numbers of each color. However, any other tile removed would lead to an uneven number when the board is flipped.

Ex 12



In the previous problem we have an algorithm for moving a dot 1 square down. We can rotate it to make it go in any direction. Let the two points be a, b .

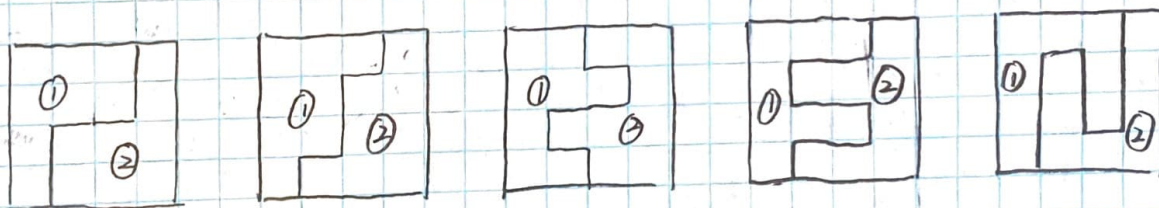


We draw a 3 by 3 grid around b like the one on the left, move a to a' . This is possible because none of the 3x3 boxes around any of the intermediate a' 's contain b .

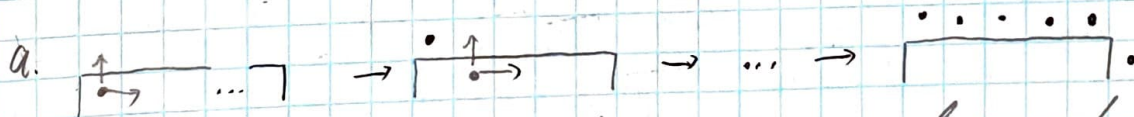


Thus it is solved.

4a.



Fri lec

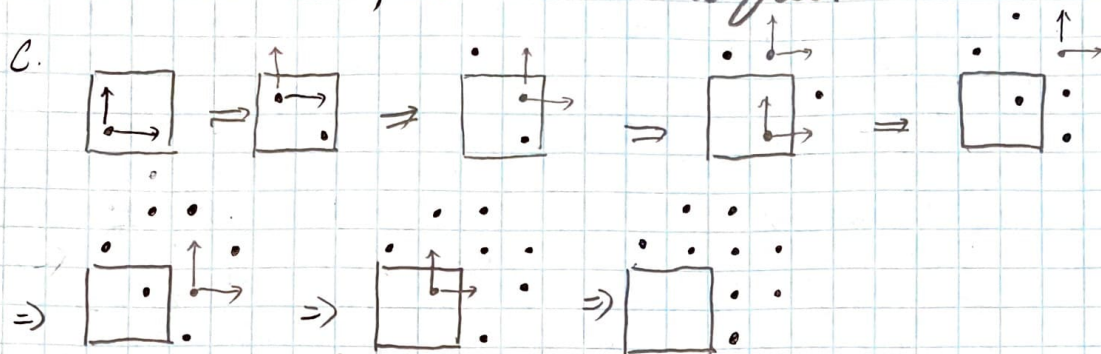


Clone the first man, this creates one above and one to the side. Keep cloning anyone still in the prison. After n moves the prison is now empty.



Clone the first man, then clone the one above. Since there is a clone blocking the right clone, we clone the blocker. Each time the blocker is preventing escape, clone him. After

$n + (n-1) = 2n-1$ moves, the clones are free.



Thus all clones have escaped.

d. Using the weight method we ~~assign~~ assign $\frac{1}{4} \dots$
 $\frac{1}{2} \frac{1}{4} \dots$
 $1 \frac{1}{2} \frac{1}{4} \dots$ to the squares.

$$\text{Total weight} = 2 + 1 + \frac{1}{2} + \dots = 4$$

$$\text{Weight inside box} = 1 + \frac{1}{2} \times 2 + \frac{1}{4} \times 3 + \frac{1}{8} \times 2 + \frac{1}{16} = 3\frac{1}{16}$$

$$\therefore \text{Weight outside} = 4 - 3\frac{1}{16} = \frac{15}{16} < 1$$

of the clones at the end

If it is possible then the square weights must add up to 1. If we have clones in all squares, we would still be $\frac{1}{16}$ short.

\therefore This problem is not solvable.