

Flashcard using combined Leitner-assisted HLR Algorithm

Owen

Problem

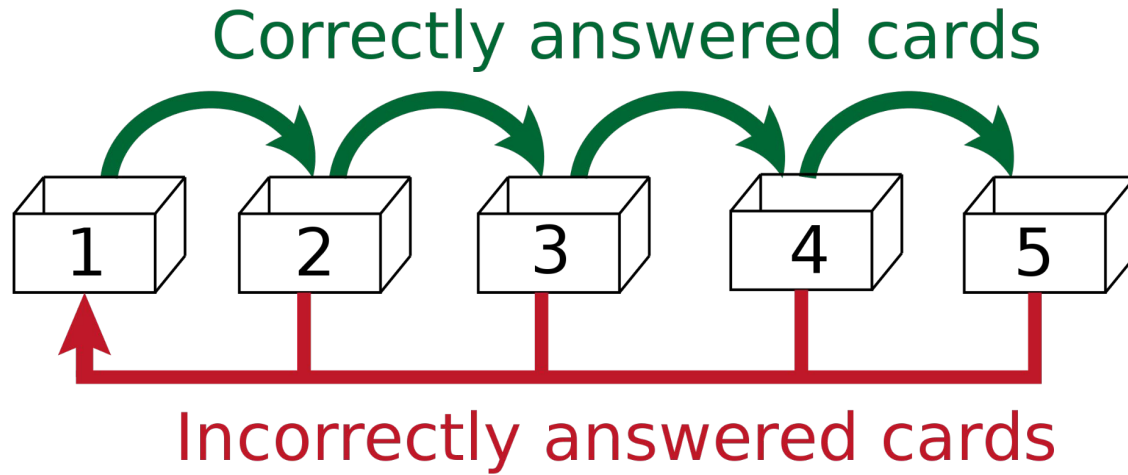
- Not many applications combine an efficient and modular learning-pattern optimization algorithm with a customizable word-list.

Solution

1. Needs an App
 - a. Flutter framework
2. Needs algorithm
 - a. Leitner
 - b. HLR

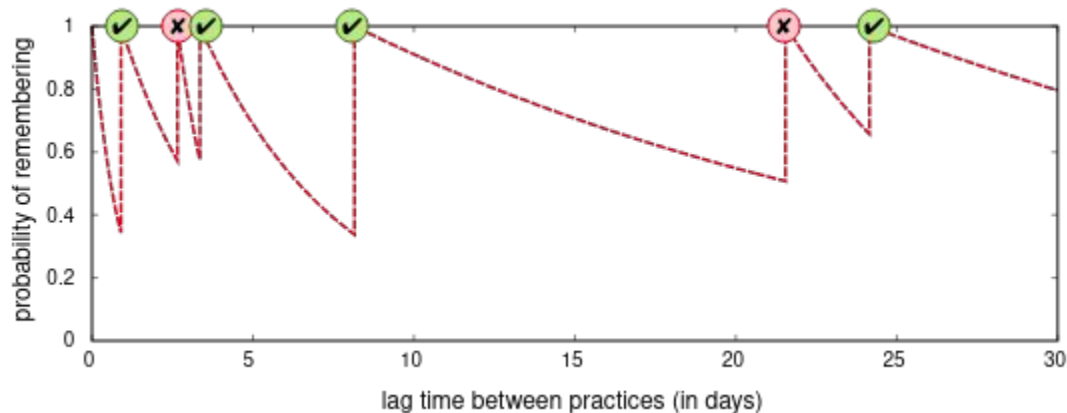


Leitner



Problem: not quite adaptive.

Half Life Regression (HLR) – Duolingo



Memory is assumed to exponentially decay with respect to time — we just need to figure out the rate of decay, and initiate reviews when the retention probability is close to 50%.

Duolingo's Formula

$$\begin{aligned} \ell(\langle p, \Delta, \mathbf{x} \rangle; \Theta) &= (p - \hat{p}_{\Theta})^2 \\ &\quad + \alpha(h - \hat{h}_{\Theta})^2 + \lambda \|\Theta\|_2^2 . \end{aligned}$$

Problem: half-life hard to obtain without accurate-enough probability of memory retention

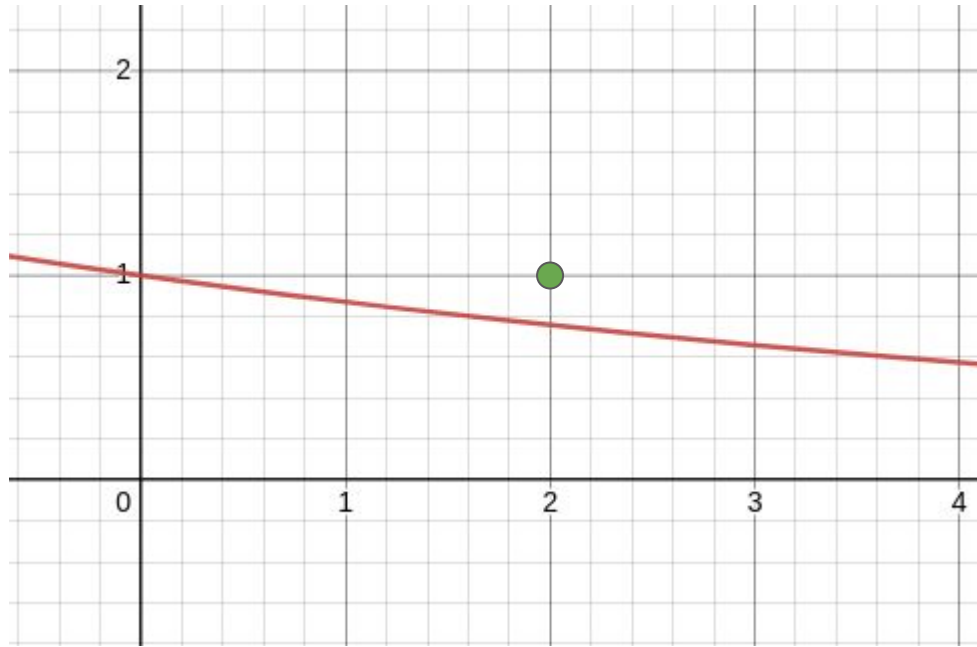
$$\ell(\langle p, \Delta, \mathbf{x} \rangle; \Theta) = (p - \hat{p}_{\Theta})^2 + \alpha(h - \hat{h}_{\Theta})^2 + \lambda \|\Theta\|_2^2 .$$

First attempt: HLR

$$p = \begin{cases} 1.0, \text{ recalled} \\ 0.5, \text{ neutral} \\ 0.0, \text{ forgot} \end{cases}$$

$$\begin{aligned} \ell &= \sum_{i=1}^n (\hat{p}_i - p_i)^2 \\ &= \sum_{i=1}^n \left(\left(\frac{1}{2} \right)^{t_i/\hat{t}} - p_i \right)^2 \\ \frac{d}{d\hat{t}} \ell &= \sum_{i=1}^n 2 \left(\left(\frac{1}{2} \right)^{t_i/\hat{t}} - p_i \right) \cdot \frac{d}{d\hat{t}} \left(\left(\frac{1}{2} \right)^{t_i/\hat{t}} - p_i \right) \\ &= \sum_{i=1}^n 2 \left(\left(\frac{1}{2} \right)^{t_i/\hat{t}} - p_i \right) \cdot \left(\left(\frac{1}{2} \right)^{t_i/\hat{t}} \ln\left(\frac{1}{2}\right) \left(-\frac{t_i}{\hat{t}^2} \right) \right) \end{aligned}$$

Problem: exploding gradient



In an attempt to approximate the forgetting curve when there's a correct answer at $t=2$, the algorithm will try to make half-life infinite.

Solution 1: L2-Regularization

$$p = \begin{cases} 1.0, \text{ recalled} \\ 0.5, \text{ neutral} \\ 0.0, \text{ forgot} \end{cases}$$

$$\begin{aligned}\ell &= \hat{t}^2 + \sum_{i=1}^n (\hat{p}_i - p_i)^2 \\ &= \hat{t}^2 + \sum_{i=1}^n \left(\left(\frac{1}{2} \right)^{t_i/\hat{t}} - p_i \right)^2 \\ \frac{d}{d\hat{t}} \ell &= 2\hat{t} + \sum_{i=1}^n 2 \left(\left(\frac{1}{2} \right)^{t_i/\hat{t}} - p_i \right) \cdot \frac{d}{d\hat{t}} \left(\left(\frac{1}{2} \right)^{t_i/\hat{t}} - p_i \right) \\ &= 2\hat{t} + \sum_{i=1}^n 2 \left(\left(\frac{1}{2} \right)^{t_i/\hat{t}} - p_i \right) \cdot \left(\left(\frac{1}{2} \right)^{t_i/\hat{t}} \ln\left(\frac{1}{2}\right) \left(-\frac{t_i}{\hat{t}^2} \right) \right)\end{aligned}$$

Does not work well in practice!

Leitners Estimation on Success

$$h' = 2h$$

$$\left(\frac{1}{2}\right)^h = \left(\frac{1}{2}\right)^{h'/2} = \sqrt{\left(\frac{1}{2}\right)^{h'}}$$

$$p = \sqrt{p'}$$

when $p = 1/2$, we have $p' \approx 0.7$.

$$p = \begin{cases} 0.7, \text{ recalled} \\ 0.5, \text{ neutral} \\ 0.0, \text{ forgot} \end{cases}$$

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$$\begin{aligned} \ell &= \sum_{i=1}^n (\hat{p}_i - p_i)^2 \\ &= \sum_{i=1}^n \left(\left(\frac{1}{2} \right)^{t_i/\hat{t}} - p_i \right)^2 \\ \frac{d}{d\hat{t}} \ell &= \sum_{i=1}^n 2 \left(\left(\frac{1}{2} \right)^{t_i/\hat{t}} - p_i \right) \cdot \frac{d}{d\hat{t}} \left(\left(\frac{1}{2} \right)^{t_i/\hat{t}} - p_i \right) \\ &= \sum_{i=1}^n 2 \left(\left(\frac{1}{2} \right)^{t_i/\hat{t}} - p_i \right) \cdot \left(\left(\frac{1}{2} \right)^{t_i/\hat{t}} \ln\left(\frac{1}{2}\right) \left(-\frac{t_i}{\hat{t}^2} \right) \right) \end{aligned}$$

Problem: too dependent on history

Rolling Window

$$p = \begin{cases} 0.7, \text{ recalled} \\ 0.5, \text{ neutral} \\ 0.0, \text{ forgot} \end{cases}$$

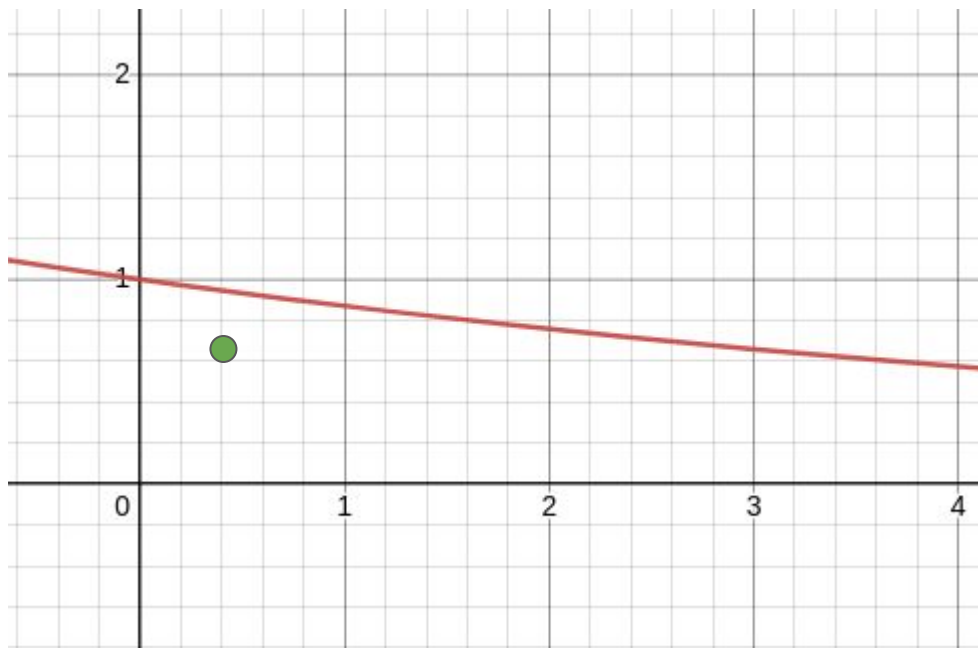
$$\ell = \hat{t}^2 + \sum_{i=n-k+1}^n (\hat{p}_i - p_i)^2$$

$$= \hat{t}^2 + \sum_{i=n-k+1}^n \left(\left(\frac{1}{2} \right)^{t_i/\hat{t}} - p_i \right)^2$$

$$\frac{d}{d\hat{t}} \ell = 2\hat{t} + \sum_{i=n-k+1}^n 2 \left(\left(\frac{1}{2} \right)^{t_i/\hat{t}} - p_i \right) \cdot \frac{d}{d\hat{t}} \left(\left(\frac{1}{2} \right)^{t_i/\hat{t}} - p_i \right)$$

$$= 2\hat{t} + \sum_{i=n-k+1}^n 2 \left(\left(\frac{1}{2} \right)^{t_i/\hat{t}} - p_i \right) \cdot \left(\left(\frac{1}{2} \right)^{t_i/\hat{t}} \ln\left(\frac{1}{2}\right) \left(-\frac{t_i}{\hat{t}^2} \right) \right)$$

Preventing negative feedback from clustered review



One more problem: If user made a correct recall shortly after a previous study session, the algorithm would try to reduce the half-life to fit such datapoint, which is not realistic as clustered learning sessions aren't known to actively make people forget what they learned.

Solution: ditch those cases!

```
// prevents unwanted negative feedback  
// |due to clustered study sessions  
if (time[i] < hl && rate[i] == 2) continue;
```


And that is how I came up with such a version of HLR. Thanks for listening!