复旦大学大数据学院 School of Data Science, Fudan University

Lab 1: Alpha-Beta Pruning & CSPs

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- Python 2.7 Download:
 - https://www.python.org/downloads/release/python-2712/
- Python 2.7 Tutorial:
 - https://docs.python.org/2/tutorial/
- Python IDE:
 - Pycharm https://www.jetbrains.com/pycharm/download/
 - Spyder Python
 http://www.discoversdk.com/products/spyder-python

Outline



- Alpha-beta pruning
 - Submit in class via OJ
- Constraint Satisfaction Problems
 - Take home as an assignment (Homework 2)



α: MAX's best option on path to root

β: MIN's best option on path to root

```
def max-value(state, \alpha, \beta):
    initialize v = -\infty
    for each successor of state:
        v = \max(v, value(successor, \alpha, \beta))
        if v \ge \beta return v
        \alpha = \max(\alpha, v)
    return v
```

```
\begin{aligned} &\text{def min-value(state }, \alpha, \beta): \\ &\text{initialize } v = +\infty \\ &\text{for each successor of state:} \\ &v = \min(v, value(successor, \alpha, \beta)) \\ &\text{if } v \leq \alpha \text{ return } v \\ &\beta = \min(\beta, v) \\ &\text{return } v \end{aligned}
```



```
function ALPHA-BETA-SEARCH(state) returns an action
   v \leftarrow \text{MAX-VALUE}(state, -\infty, +\infty)
   return the action in ACTIONS(state) with value v
function MAX-VALUE(state, \alpha, \beta) returns a utility value
   if TERMINAL-TEST(state) then return UTILITY(state)
   v \leftarrow -\infty
  for each a in ACTIONS(state) do
      v \leftarrow \text{MAX}(v, \text{MIN-VALUE}(\text{RESULT}(s, a), \alpha, \beta))
     if v \geq \beta then return v
     \alpha \leftarrow \text{MAX}(\alpha, v)
   return v
function MIN-VALUE(state, \alpha, \beta) returns a utility value
   if TERMINAL-TEST(state) then return UTILITY(state)
   v \leftarrow +\infty
   for each a in ACTIONS(state) do
      v \leftarrow \text{MIN}(v, \text{MAX-VALUE}(\text{RESULT}(s, a), \alpha, \beta))
     if v < \alpha then return v
      \beta \leftarrow \text{MIN}(\beta, v)
   return v
```

Figure 5.7 The alpha—beta search algorithm. Notice that these routines are the same as the MINIMAX functions in Figure 5.3, except for the two lines in each of MIN-VALUE and MAX-VALUE that maintain α and β (and the bookkeeping to pass these parameters along).

Demo: Alpha-beta pruning



http://inst.eecs.berkeley.edu/~cs61b/fa14/ta-materials/apps/ab_tree_practice/

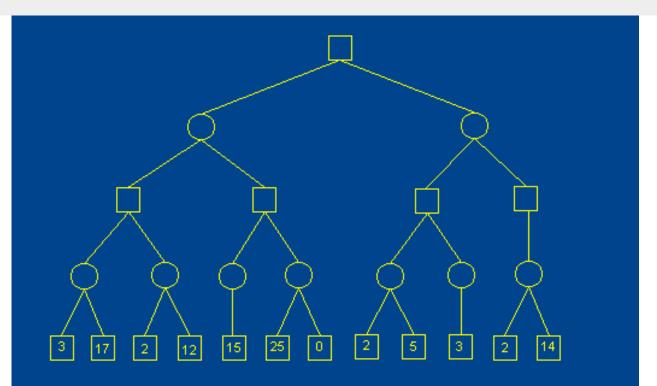
Practice for Alpha-beta Pruning



Problem 1174: http://10.88.12.45/JudgeOnline/problem.php?id=1174

Input Example: Square represents MAX node while circle stands for MIN node. For each test case, it contains two lines. The first line consists of two integers, the role of the root node (1 for MAX node and 0 for MIN node) and the depth of the tree. The second line is a nested list which stands for the game tree. The sample input shows the tree of Fig1

```
1 5 [[[[3,17],[2,12]],[[15],[25,0]]],[[[2,5],[3]],[[2,14]]]]
```



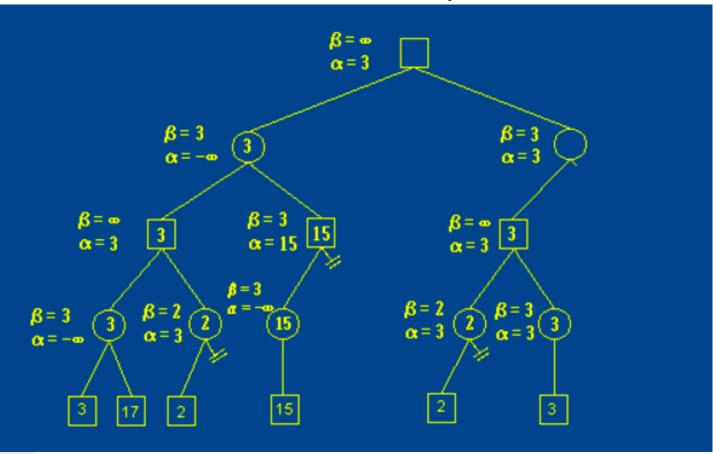
Practice for Alpha-beta Pruning



Problem 1174: http://10.88.12.45/JudgeOnline/problem.php?id=1174

For each test case, the output should include two lines. The first line contains the result for minimax search. The second line should consist of **pruned nodes**

in order.



- Hint()
 - Eval (): Read the string and store it as a python type
 - i.e. tree = eval(raw_input().strip())
 - Mark tree nodes which have been visited
- def value(node, alpha, beta)
 - Choose which function to call
- def maxValue(node, alpha, beta)
- def minValue(node, alpha, beta)



Backtracking is a basic solution for CSP problem

- #problem a
- You can improve the performance of CSP by 3 ways:
- Ordering:
 - Which variable should be assigned next? (MRV)
 - In what order should its values be tried? (LCV)

#problem b

- Filtering: Can we detect inevitable failure early?
 - Arc-consistency checking (AC -3)
- Structure: Can we exploit the problem structure?
 - Tree structure
 - Cutting set conditionning

#problem c

Not this time



- You need to submit your own version of code.
- You are encouraged to discuss with your group members. It might take some time to get familiar with all the supportive codes.
- Homework 2 is due on April 19th, Wednesday, 11:59pm, 2017.
- Download description here.
- Get code here.

class CSP{

```
self.numVars = 0 # number of variables
self.variables = [] # names of variables
self.values = {} # domains for each variable (dictionary)
self.unaryFactors = {} # unary constraints
self.binaryFactors = {} # binary constraints, explicit representation
def add_variable (self, var, domain)
def get_neighbor_vars (self, var)
def add_unary_factor (self, var, factorFunc)
def add_binary_factor (self, var1, var2, factor_func)
```

```
class BacktrackingSearch{
    def solve(self, csp, mcv = False, ac3 = False)
    def backtrack(self, assignment, numAssigned, weight)
    def get_unassigned_variable(self, assignment)
    def arc_consistency_check(self, assignment, var):
}
```



```
def Backtracking (assignment){
    if all variables assigned:
        add current assignment to assignments
    else:
        var <- choose an unassigned variable</pre>
   for value in domain of var:
       add{var = value} to assignment
       Backtracking(assignment)
       delete var from assignment
```



```
def Backtracking:
    if all variables assigned:
        add current assignment to assignments
    else:
        if MRC not implemented:
            randomly choose var from unassigned variables
        else(MRC implemented):
            choose variable by MCV
        for value in domain of var:
            add{var, value} to assignment
            if AC-3 not implemented:
                Backtracking(assignment)
            else(AC-3 implemented):
                localCopy <- store a deep copy for domains</pre>
                arc consistency checking
                Backtracking(assignment)
                use pre-stored localCopy to undo modify on domain
            delete assigned value for var
```



Select a variable with the least number of remaining domain

Hints:

- self.csp.variables gives you all the variables in csp
- given var, self.domains[var] gives you all the possible values
- get_delta_weight(self, assignment, var, val) return the change of weights after assign val to var. In this case , will return 0 for inconsistent, 1 for consistent with assignment
- assignment, a variable, and a proposed value to this variable



 After assigning new value to var, update domain for var's neighbors with AC-3.