

ProblemSet2_ANSWER

May 15, 2019

0.0.1 Problem Set 2

MACS 30250, Dr. Evans

Due Wednesday, May. 15 at 1:30pm

Tianxin Zheng

1. Stochastic i.i.d. cake eating problem

```
In [1]: import numpy as np
import scipy.optimize as opt
import scipy.interpolate as intpl
import matplotlib.pyplot as plt
%matplotlib notebook
```

(a)

```
In [2]: # Set up the parameters
beta = 0.9
gamma = 2.2
W_min = 0.1
W_max = 10.0
W_size = 30
W_vec = np.linspace(W_min, W_max, W_size)
V_t = np.log(W_vec)

def util_CRRA(W, W_pr, gamma):
    # Define CRRA utility function
    c = W - W_pr
    util = (c ** (1 - gamma) - 1) / (1 - gamma)

    return util

eps_vec = np.array([-1.40, -0.55, 0.00, 0.55, 1.4])
eps_prob = np.array([0.1, 0.2, 0.4, 0.2, 0.1])
eps_size = eps_vec.shape[0]
```

```

def neg_V_iid(W_pr, *args):
    W_init, eps, util, EXP_V_t_interp, gamma, beta = args
    Vtp1 = np.exp(eps) * util(W, W_pr, gamma) + beta * EXP_V_t_interp(W_pr)
    neg_Vtp1 = -Vtp1

    return neg_Vtp1

In [3]: V_init = np.zeros((W_size, eps_size))
        V_new = V_init.copy()

        VF_iter = 0
        VF_dist = 10
        VF_maxiter = 200
        VF_mindist = 1e-8

        while (VF_iter < VF_maxiter) and (VF_dist > VF_mindist):
            VF_iter += 1
            V_init = V_new.copy()
            V_new = np.zeros((W_size, eps_size))
            psi_vec = np.zeros((W_size, eps_size))

            # Intergrate out eps_pr from V_init
            Exp_V = V_init @ eps_prob.reshape((eps_size, 1))

            # Interpolate ? value function
            Exp_V_interp = interp1d(W_vec, Exp_V.flatten(), kind='cubic',
                                    fill_value='extrapolate')

            for eps_ind in range(eps_size):
                for W_ind in range(W_size):
                    W = W_vec[W_ind]
                    eps = eps_vec[eps_ind]
                    V_args = (W, eps, util_CRRA, Exp_V_interp, gamma, beta)
                    results_all = opt.minimize_scalar(neg_V_iid, bounds=(1e-10, W - 1e-10),
                                                    args=V_args, method='bounded')

                    V_new[W_ind, eps_ind] = -results_all.fun
                    psi_vec[W_ind, eps_ind] = results_all.x

            VF_dist = ((V_init - V_new) ** 2).sum()
            print('VF_iter=', VF_iter, ', VF_dist=', VF_dist)

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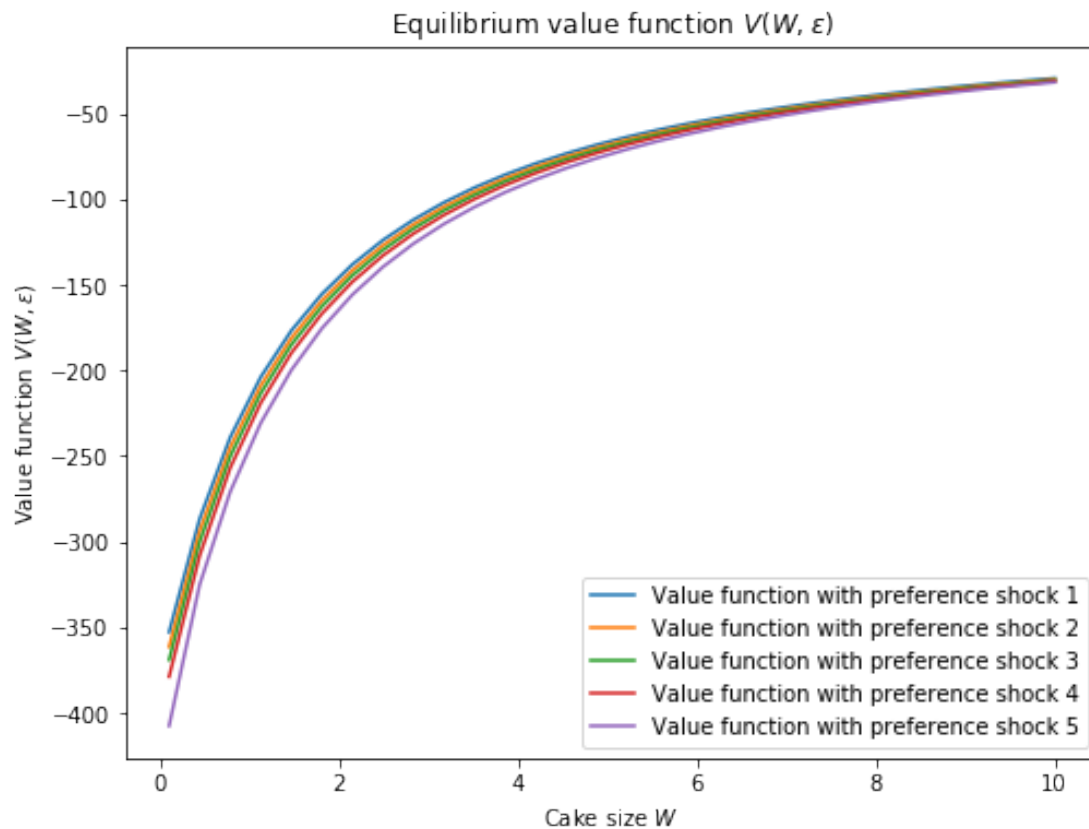
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(b)

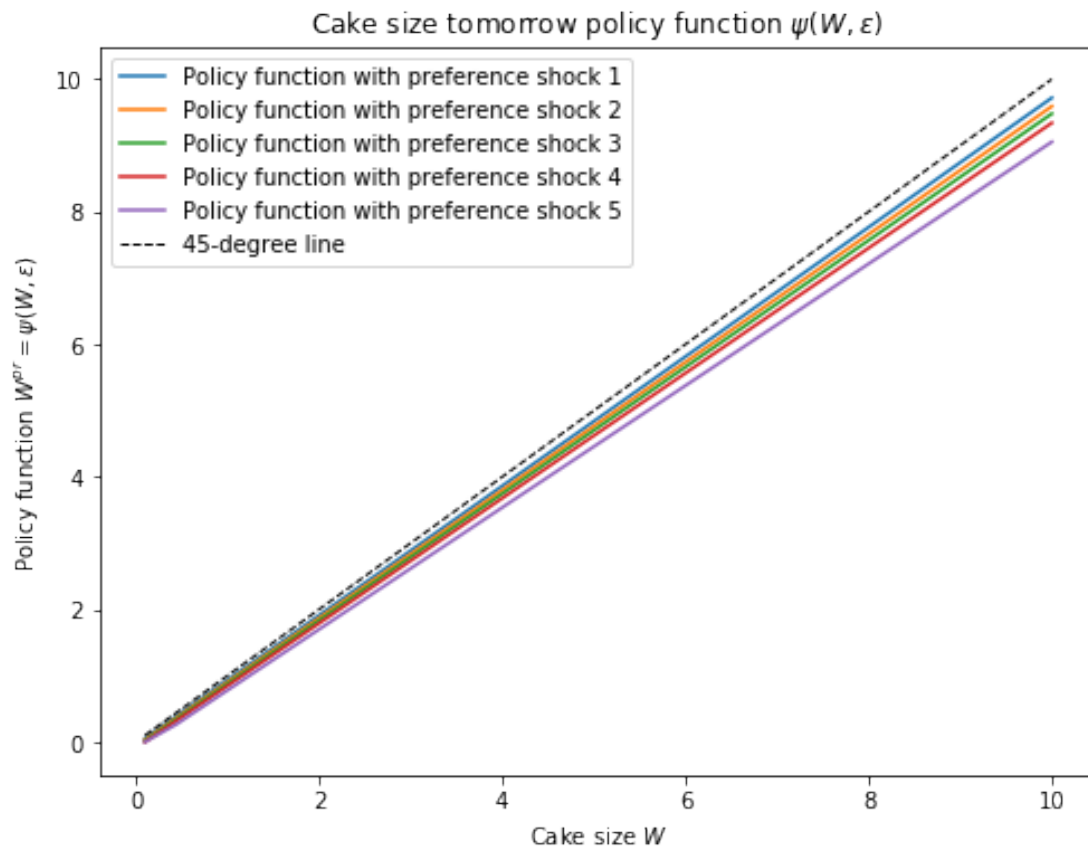
```
In [4]: plt.figure(figsize=(8,6))
        for i in range(5):
            plt.plot(W_vec, V_new[:,i], label='Value function with preference shock {}'.format(i))
        plt.title('Equilibrium value function  $V(W, \epsilon)$ ')
        plt.xlabel('Cake size  $W$ ')
        plt.ylabel('Value function  $V(W, \epsilon)$ ')
        plt.legend()
```

Out[4]: <matplotlib.legend.Legend at 0x1108c5198>



```
In [5]: plt.figure(figsize=(8,6))
        for i in range(5):
            plt.plot(W_vec, psi_vec[:,i], label='Policy function with preference shock {}'.format(i))
        plt.plot(W_vec, W_vec, color = 'black', linewidth=1, linestyle='--',
                 label='45-degree line')
        plt.title('Cake size tomorrow policy function  $\psi(W, \epsilon)$ ')
        plt.xlabel('Cake size  $W$ ')
        plt.ylabel('Policy function  $W^{\{pr\}} = \psi(W, \epsilon)$ ')
        plt.legend()
```

Out [5]: <matplotlib.legend.Legend at 0x1109dd748>



2. Persistent AR(1) stochastic cake eating problem

(a)

```
In [6]: trans_mat=np.array([[0.40, 0.28, 0.18, 0.10, 0.04],
                             [0.20, 0.40, 0.20, 0.13, 0.07],
                             [0.10, 0.20, 0.40, 0.20, 0.10],
                             [0.07, 0.13, 0.20, 0.40, 0.20],
                             [0.04, 0.10, 0.18, 0.28, 0.40]])
```

```
In [7]: V_init = np.zeros((W_size,eps_size))
```

```
V_new = V_init.copy()
```

```
VF_iter = 0
```

```
VF_dist = 10
```

```
VF_maxiter = 200
```

```
VF_mindist = 1e-8
```

```

while (VF_iter < VF_maxiter) and (VF_dist > VF_mindist):
    VF_iter += 1
    V_init = V_new.copy()
    V_new = np.zeros((W_size,eps_size))
    psi_mat = np.zeros((W_size,eps_size))
    for eps_ind in range(eps_size):
        eps = eps_vec[eps_ind]
        eps_prob = trans_mat[eps_ind,:]
        Exp_V = V_init @ eps_prob.reshape((eps_size,1))
        Exp_V_interp = interp1d(W_vec, Exp_V.flatten(), kind='cubic',
                                fill_value='extrapolate')
        for W_ind in range(W_size):
            W = W_vec[W_ind]
            V_args = (W, eps, util_CRRA, Exp_V_interp, gamma, beta)
            results1 = opt.minimize_scalar(neg_V_iid, bounds=(1e-10, W - 1e-10),
                                           args=V_args, method='bounded')
            V_new[W_ind, eps_ind] = -results1.fun
            psi_mat[W_ind, eps_ind] = results1.x

    VF_dist = ((V_init - V_new) ** 2).sum()
    print('VF_iter=', VF_iter, ', VF_dist=', VF_dist)

VF_iter= 1 , VF_dist= 3494.416552492849
VF_iter= 2 , VF_dist= 4874.985394413625
VF_iter= 3 , VF_dist= 5656.12392067181
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VF_iter= 121 , VF_dist= 3.6353327310852107e-06

```

VF_iter= 122 , VF_dist= 2.943998810995179e-06
VF_iter= 123 , VF_dist= 2.3841295554757415e-06
VF_iter= 124 , VF_dist= 1.9307333682581294e-06
VF_iter= 125 , VF_dist= 1.5635662339836826e-06
VF_iter= 126 , VF_dist= 1.2662309477630227e-06
VF_iter= 127 , VF_dist= 1.0254469301659195e-06
VF_iter= 128 , VF_dist= 8.304583962909381e-07
VF_iter= 129 , VF_dist= 6.725547457491646e-07
VF_iter= 130 , VF_dist= 5.446819406192471e-07
VF_iter= 131 , VF_dist= 4.4112761496225405e-07
VF_iter= 132 , VF_dist= 3.5726599797105377e-07
VF_iter= 133 , VF_dist= 2.8935128587648305e-07
VF_iter= 134 , VF_dist= 2.3435026815796068e-07
VF_iter= 135 , VF_dist= 1.8980678277275483e-07
VF_iter= 136 , VF_dist= 1.5373192912320232e-07
VF_iter= 137 , VF_dist= 1.245151713786484e-07
VF_iter= 138 , VF_dist= 1.0085235263566314e-07
VF_iter= 139 , VF_dist= 8.168739194090008e-08
VF_iter= 140 , VF_dist= 6.616508779991977e-08
VF_iter= 141 , VF_dist= 5.359289518903287e-08
VF_iter= 142 , VF_dist= 4.340998180457873e-08
VF_iter= 143 , VF_dist= 3.51621655905898e-08
VF_iter= 144 , VF_dist= 2.8481629018835357e-08
VF_iter= 145 , VF_dist= 2.3070489617555775e-08
VF_iter= 146 , VF_dist= 1.868749732046429e-08
VF_iter= 147 , VF_dist= 1.5137265955297337e-08
VF_iter= 148 , VF_dist= 1.2261547883836958e-08
VF_iter= 149 , VF_dist= 9.93217479503226e-09

```

(b)

```

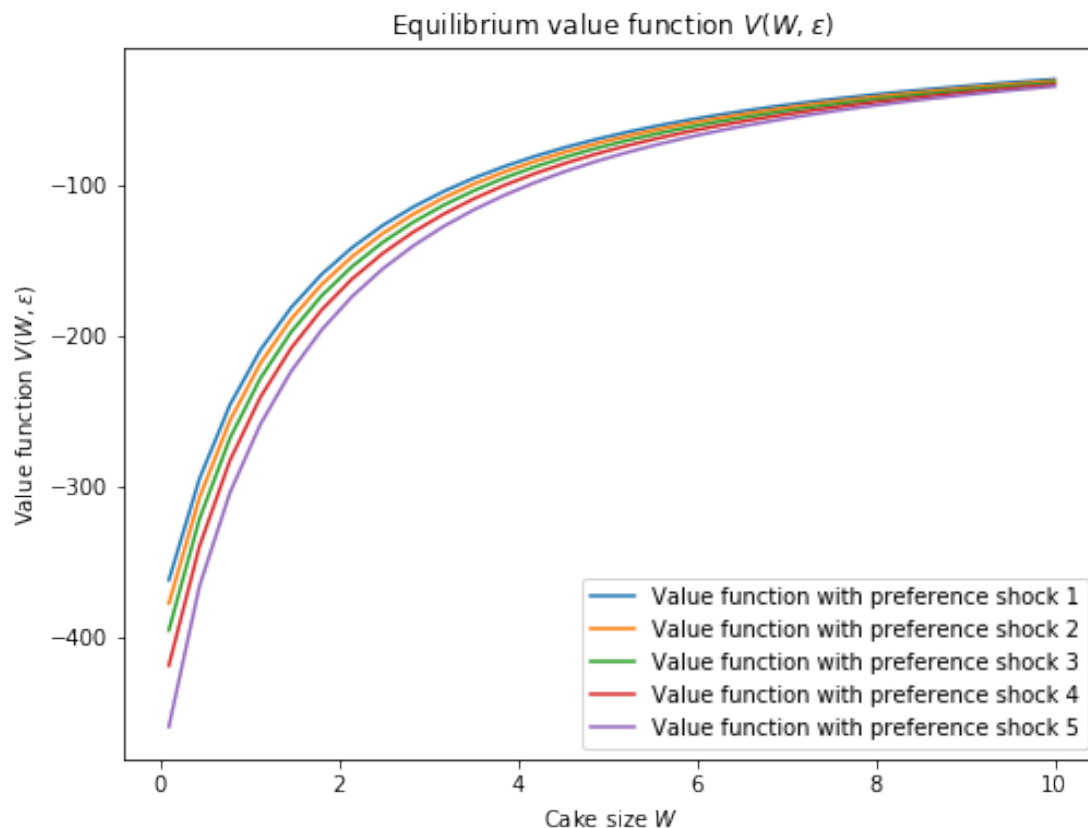
In [8]: plt.figure(figsize=(8,6))
        for i in range(5):
            plt.plot(W_vec, V_new[:,i], label='Value function with preference shock {}'.format(i))
        plt.title('Equilibrium value function $V(W, \epsilon)$')
        plt.xlabel('Cake size $W$')
        plt.ylabel('Value function $V(W, \epsilon)$')
        plt.legend()

```

```

Out[8]: <matplotlib.legend.Legend at 0x110b046a0>

```



(c)

```
In [9]: plt.figure(figsize=(8,6))
        for i in range(5):
            plt.plot(W_vec, psi_mat[:,i], label='Policy function with preference shock {}'.format(i))
        plt.plot(W_vec, W_vec, color = 'black', linewidth=1, linestyle='--',
                 label='45-degree line')
        plt.title('Cake size tomorrow policy function  $\psi(W, \epsilon)$ ')
        plt.xlabel('Cake size  $W$ ')
        plt.ylabel('Policy function  $W^{\text{pr}} = \psi(W, \epsilon)$ ')
        plt.legend()
```

Out[9]: <matplotlib.legend.Legend at 0x110c7aa20>

