



$$velocity = \left\| \frac{d\vec{r}}{dt} \right\| = \left\| \vec{v}_s \right\| = \frac{2\pi r}{T}$$

$$acceleration = \left\| \frac{d\vec{v}_s}{dt} \right\| = \left\| \vec{a}_s \right\| = \frac{2\pi \frac{2\pi r}{T}}{T} = 4\pi^2 \frac{r}{T^2}$$

For geostationary orbit:

$$G \frac{m_E}{r_{gs}^2} = 4\pi^2 \frac{r_{gs}}{T^2}$$

Thus the geostationary orbit radius (distance between the satellite and the mass center of earth) is:

$$r_{gs} = \sqrt[3]{\frac{Gm_E T^2}{4\pi^2}} \cong 42000 km$$

Kinetic Energy:

$$\frac{1}{2} m_s \left\| \vec{v}_s \right\|^2$$

Potential Energy:

$$-G \frac{m_E m_s}{\left\| \vec{x}_s \right\|}$$

Energy Conservation:

$$\frac{1}{2}m_s||\vec{v}_s||^2 - G\frac{m_Em_s}{||\vec{x}_s||} = Constant$$