Google Analytics Customer Revenue Prediction

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I. Abstract

This report analyzes and predicts customer revenue data of Google store through linear mixed model, logistic model, Censored Regression with Conditional Heteroscedasticy(CRCH) model and Light Gradient Boosting Machine(LGBM) method. From aspect of Root-Mean-Squared-Error(RMSE), LGBM leads to the least of 1.61. From aspect of association, all models help detect relation between revenue and visit information. Then, interpretation and implication are mentioned to show the result of the analysis. In the end, limitation and future discussion are stated to look forward to an improvement in the future for this analysis.

II. Introduction

1. Background

The 80/20 rule has proven true for many businesses—only a small percentage of customers produce most of the revenue. As such, marketing teams are challenged to make appropriate investments in promotional strategies. Thus, the goals are first to figure out association between factors and customer revenue, second to predict the revenue so that marketing teams can make effective investments.

2. Previous work

Several notes have been put on the kernel on Kaggle.com about the customer revenue prediction for Google store. Shivam Bansal [1] discovered missing data in the whole data set and conducted LGBM in python, where RMSE on test set is 1.64. kxx [2]

created various plots for predictors in the data set, and fitted time series model with RMSE 0.34 on train set, linear mixed model with only random intercept by users, LASSO model, neural network and XGBoost with RMSE 1.696 on test set. Erik Bruin [3] grouped data by workday and by month, also used time series model and LGBM model with RMSE 1.72 on test set.

III. Method

1. Data source

The data set is all from kaggle.com (https://www.kaggle.com/c/ga-customer-revenue-prediction), where it contains train dataset, test dataset and submission file. The size of all three file is more than 30GB, so I use Shared Computer Cluster (SCC) to deal with the data. There is one column "hits" in the data which is pretty large, thus I ignore this column when importing the data. Also, there are several columns with subcolumn information in json format, therefore I use "jsonlite" package in r to convert these column into normal columns. Moreover, there are constant columns like "social Engagement Type" and "visits", and I delete them.

2. Model used

I try several different kinds of models, and the best model in that category is displayed below. Then comparison of these models will be in the model choice part.

A. Linear Mixed Model (LMM)

1) Summary

Since the data has repeated observations for one user, I decide to use multilevel models as basic model.

2) Exploratory Data Analysis(EDA)

I group the data by users, and create plots to decide which variables need random intercepts and slopes.

i. Outcome

First, I create plot for revenue, which is the outcome.

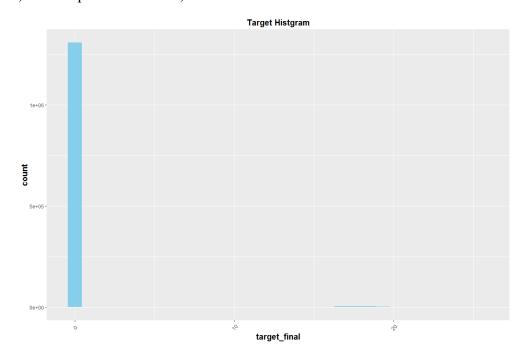


Figure: distribution of all revenue

From the plot, it is clear that most target values are 0, and it is severely right skewed, thus I check the target value without 0s.

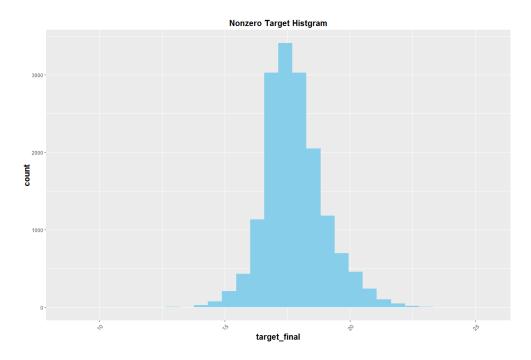


Figure: distribution of nonzero revenue

It seems like a normal distribution, so I create a qqplot.

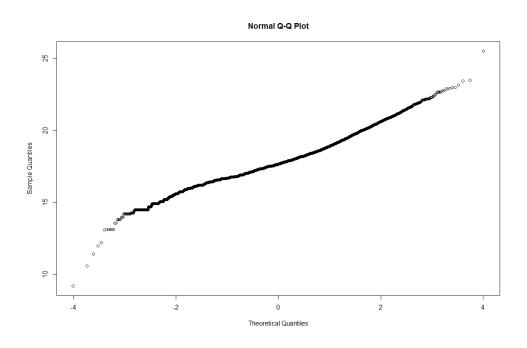


Figure: distribution of nonzero revenue

It seems that except for head and tail, nonzero target values follows a normal distribution approximately.

ii. Predictors and outcome

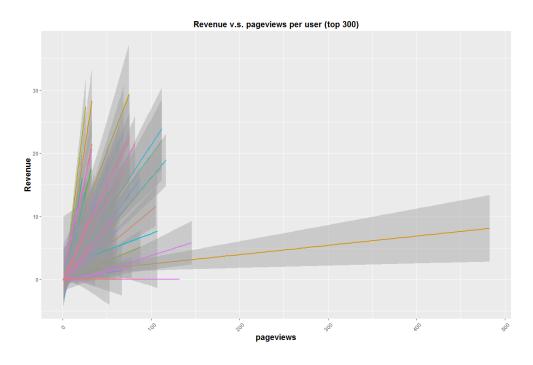
Then, I draw plots between predictors and outcome.

First, I check the correlation between numerical predictors.

Figure: correlation between numerical predictors

From the table we can see that "hits" and "page views" has correlation of 1, thus I select "page views" instead of hits, also correlation between "time on site" and "page views" is more than 0.8. Thus, there may be collinearity. Since the correlation is large as more than 0.8, I choose "page views" instead of "time on site".

Then, I create plots about "page views", "bounces", "new visits" and "visit number". Since there are like more than 1 million users, I choose top 300 users with most visit number.



From this plot, we can see that the slope of "page views" will change a lot between different users, however there are no correlation between intercept and slope. This may indicate adding (0+pageviews|fullVisitorId) in the linear mixed models.

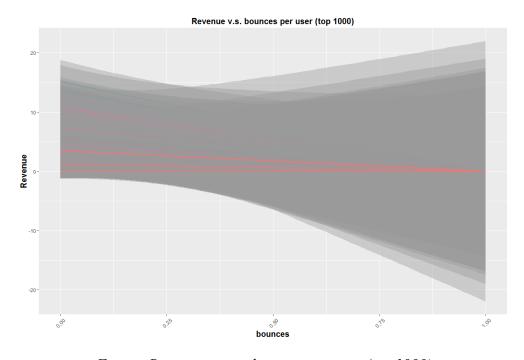


Figure: Revenue versus bounces per user (top 1000)

From the plots of Revenue versus bounces, however, we can see that both slope and intercept don't change a lot between different users. This may indicate no mixed effect for bounces in the linear mixed models. But it can be caused by small sample size, thus this plot is created on 1000 users. As showed in the plot, it still does not change a lot, thus bounces will not be included in mixed effect in the model. Then I check the whole effect of bounces to revenue and it is evident. Thus "bounces" can be fixed effect but not mixed effect.

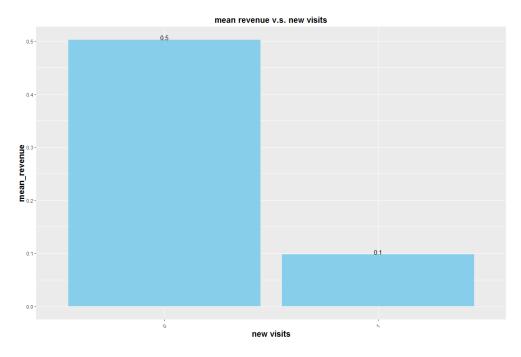


Figure: Revenue versus new visits

From this plot, it is clear that "new visits" has great impact on outcome, thus it should be included in the model.

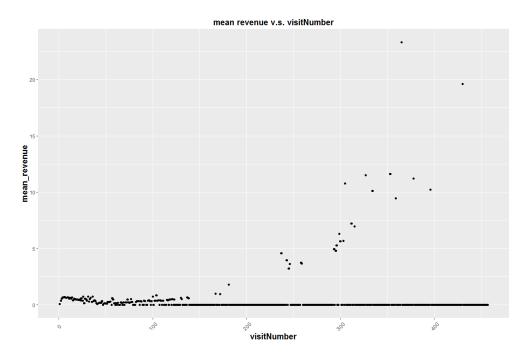


Figure: Revenue versus visit number

It is evident that "visit number" has great impact on revenue.

Next is to deal with "browser", "operating system" and "is mobile". Since there are

too many levels in "browser" and "operating system", I recode them according to the mean outcome. Here are plots after recoding.

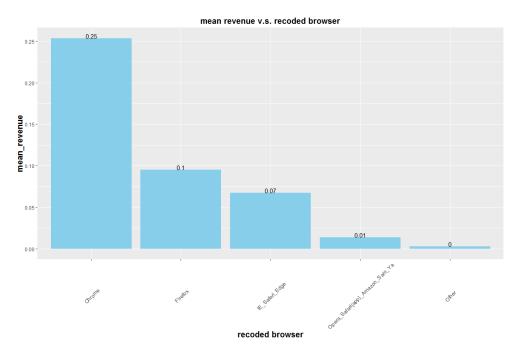


Figure: Revenue versus recoded browsers

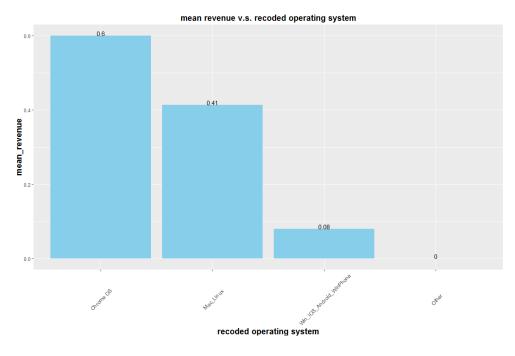


Figure: Revenue versus recoded operating system

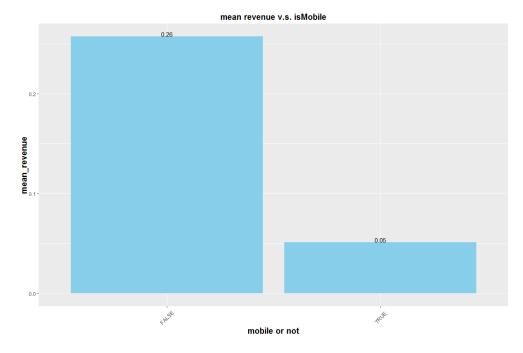


Figure: Revenue versus "is mobile"

From these plots, it is evident that all "browser", "operating system" and "is mobile" have huge impacts on revenue.

Also, for geographical information, we can see that there are huge difference between America and outside America. Thus, I recode continent as "America" and "outside America".

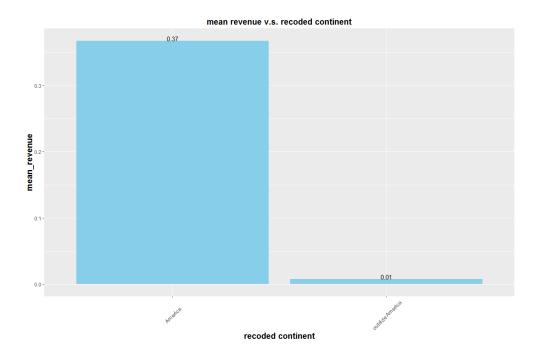


Figure: Revenue versus recoded continent

It is obvious that America has much more revenue than outside America.

Variables of channels like "channel grouping", "medium" and "is true direct" need to be dealt with.

| | channelGrouping <fctr></fctr> | medium <fctr></fctr> | isTrueDirect <int></int> |
|---|----------------------------------|--------------------------------|-----------------------------|
| 1 | Organic Search | organic | 0 |
| 2 | Social | referral | 0 |
| 3 | Social | referral | 0 |
| 4 | Organic Search | organic | 0 |
| 5 | Direct | (none) | 1 |
| 6 | Direct | (none) | 1 |

Figure: variables "channel grouping", "medium" and "is true direct"

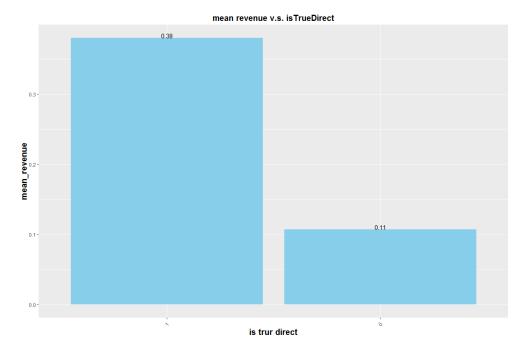


Figure: Revenue versus "is true direct"

From the table, it is clear that the "channel grouping" variable contain similar information with "medium" and "is true direct". From the plot, and also compare it with plots of "channel grouping" and "medium", we can see that direct or not affect revenue significantly. Thus, "is true direct" should be put in the models. (Plots of "channel grouping" and "medium" are in Appendix I)

Finally, I convert date into weekday or not since there are huge difference between revenue on weekdays and on weekends.

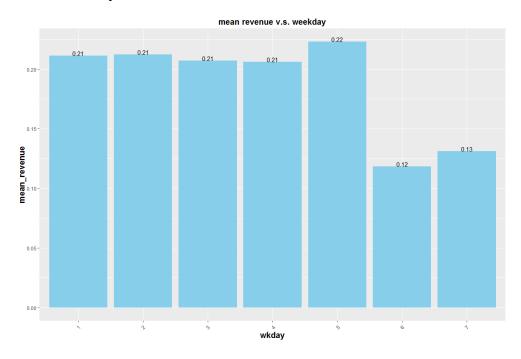


Figure: Revenue versus weekday

3) Modeling

I fit linear mixed model with possible predictors.

```
Linear mixed model fit by REML ['lmerMod']
Formula: log(transactionRevenue + 1) ~ (1 | fullVisitorId) + (0 + pageviews |
   fullVisitorId) + scale(pageviews) + scale(bounces) + factor(newVisits) +
    scale(visitNumber) + factor(browser_n) + factor(operatingSystem_n) +
    factor(isMobile) + factor(continent_n) + factor(isTrueDirect) +
                                                                        factor(wkday n)
  Data: T predictors
REML criterion at convergence: 5237710
Scaled residuals:
    Min
             1Q
                   Median
-22.8633 -0.0443 0.0069 0.0488 23.4878
Random effects:
Groups
                Name
                            Variance Std.Dev.
 fullVisitorId (Intercept) 0.00000 0.0000
 fullVisitorId.1 pageviews 0.02354 0.1534
                            0.95040 0.9749
Residual
Number of obs: 1708337, groups: fullVisitorId, 1323730
Fixed effects:
                                                   Estimate Std. Error t value
(Intercept)
                                                  0.1596383 0.0058360 27.354
scale(pageviews)
                                                  0.6060322 0.0030372 199.538
scale(bounces)
                                                  0.1085692 0.0010301 105.395
                                                 -0.0703168 0.0025497 -27.579
factor(newVisits)1
scale(visitNumber)
                                                  0.0131775 0.0009018 14.613
factor(browser_n)Firefox
                                                  0.0164208 0.0044203
                                                                        3.715
factor(browser_n)IE_Safari_Edge
                                                  0.0310041 0.0021913 14.149
factor(browser_n)Opera_Safari(app)_Amazon_Sam_Ya
                                                 0.0226762 0.0052059
                                                  0.0354069 0.0051255
                                                                        6.908
factor(browser_n)Other
factor(operatingSystem_n)Mac_Linux
                                                 -0.0010539 0.0055540
                                                                        -0.190
factor(operatingSystem_n)Other
                                                  0.0162592 0.0111074
                                                                        1.464
factor(operatingSystem_n)Win_iOS_Android_WinPhone 0.0241365 0.0055019
                                                                        4.387
factor(isMobile)TRUE
                                                 -0.0177673 0.0022772
                                                                        -7.802
factor(continent n)outside America
                                                  0.0275513 0.0017948 15.351
                                                  0.0156247 0.0022582
                                                                         6.919
factor(isTrueDirect)1
factor(wkday_n)weekend
                                                  0.0034554 0.0019933
                                                                         1.734
```

Figure: result of linear mixed model grouped by users

We can see that the residual is 0.95, which is pretty small, and most coefficients are statistically significant. However, the residual plot looks like this:

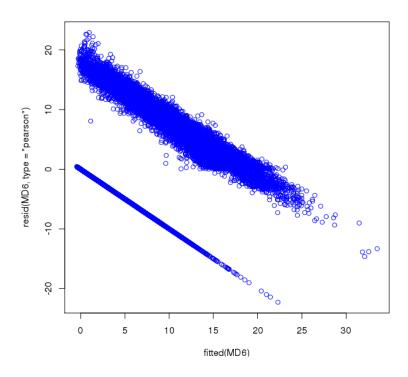


Figure: residual plot of linear mixed model grouped by users

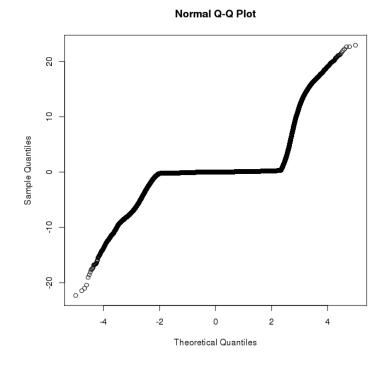


Figure: qq-plot for residuals

The lower straight line in the residual plot is due to too many 0s in the outcome, and the higher one may be due to the violation of normal distribution since the residual plot shows that it does not follow normal distribution.

Also, I predicte revenue on test dataset using this model, the Root Mean Squared Error (RMSE) is 1.97.

B. Linear Mixed Model(LMM) - Grouped by Continent

1) Summary

I also group the data by continent, since there may be similar behavior pattern within one region.

2) EDA

I create plots to see which predictors I should put in the model. According previous plot, different of mean revenue between continents are significant, so there is definitely random intercept. Therefore, I create plots to see if there are random slopes.

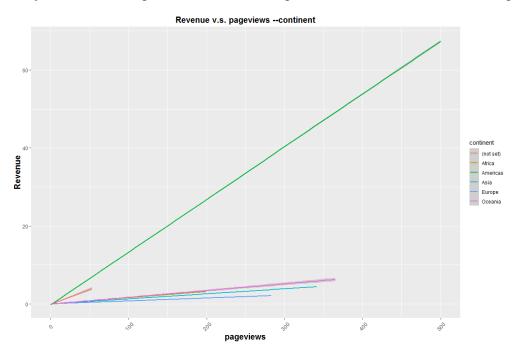


Figure: Revenue versus "page views" --continent

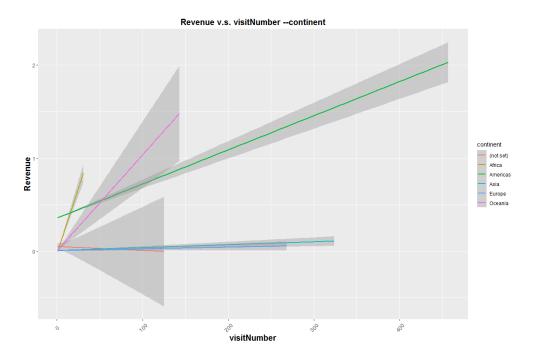


Figure: Revenue versus "visit number" --continent

It is significant that there is random slope of "page views" and "visit number" between continents.

3) Modeling

```
Linear mixed model fit by REML ['lmerMod']
Formula: log(transactionRevenue + 1) \sim (1 | continent) + (0 + pageviews |
    continent) + scale(pageviews) + scale(bounces) + scale(visitNumber) +
    factor(newVisits) + factor(isMobile) + factor(isTrueDirect) +
    factor(browser_n) + factor(operatingSystem_n) + factor(wkday_n)
   Data: T_predictors
REML criterion at convergence: 6591426
Scaled residuals:
    Min 10 Median 30
                                    Max
-41.322 -0.097 0.001 0.059 13.310
Random effects:
 Groups Name
                         Variance Std.Dev.
 continent (Intercept) 0.012300 0.11091
 continent.1 pageviews 0.002437 0.04937
 Residual
                         2.774300 1.66562
Number of obs: 1708337, groups: continent, 6
Fixed effects:
                                                    Estimate Std. Error t value
(Intercept)
                                                    0.334769 0.087774
                                                    0.329438 0.130780
scale(pageviews)
                                                                           2.519
scale(bounces)
                                                    0.088995 0.001447 61.491
                                                   -0.024265 0.001324 -18.334
scale(visitNumber)
factor(newVisits)1
                                                   -0.177700 0.003920 -45.336
factor(isMobile)TRUE
                                                   -0.039066 0.003486 -11.205
                                                   0.074121 0.003509 21.125
-0.018232 0.006866 -2.655
-0.031621 0.003368 -9.389
factor(isTrueDirect)1
factor(browser_n)Firefox
factor(browser_n)IE_Safari_Edge
factor(browser_n)Opera_Safari(app)_Amazon_Sam_Ya 0.032128 0.008255
                                                                         3.892
factor(browser n)Other
                                                   0.055217 0.008374
                                                                         6.594
factor(operatingSystem n)Mac Linux
                                                   -0.021734 0.007784 -2.792
factor(operatingSystem_n)Other -0.149418 0.017478 -8.549 factor(operatingSystem_n)Win_iOS_Android_WinPhone -0.143249 0.007774 -18.427
                                                   factor(wkday_n)weekend
```

Figure: Output for LMM by continents

The residual here is 2.77, which is larger than previous one. Most coefficients are statistically significant since t values are mostly large. Also, the residual plot still look like the previous one:

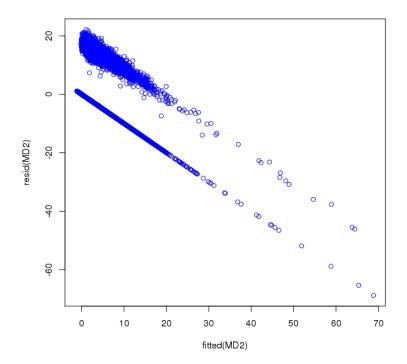


Figure: residual plot

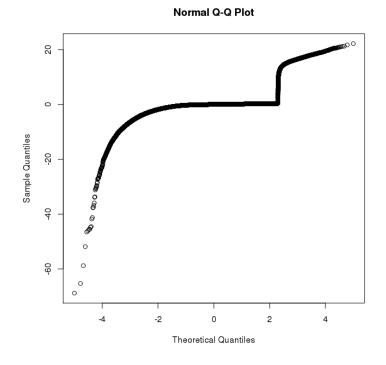


Figure: qq-plot for residuals

Still, the assumption of normal distribution is violated. This may indicate that only mixed linear model here is not enough. Thus, I try first to fit logistic model and then to fit linear mixed model.

Also, RMSE on the test dataset is 1.934, which is a little bit better than before.

C. Logistic & Linear Mixed Model

Since the percentage of nonzero is pretty low in outcome, it may be better to use hurdle model, which is to fit the logistic model first to predict the nonzero value, then fit linear mixed model on the conditional dataset.

Here is the result of the best logistic model:

```
glm(formula = iftransaction ~ scale(pageviews) + scale(bounces) +
    factor(newVisits) + scale(timeOnSite) + factor(browser_n) +
    factor(operatingSystem_n) + factor(isMobile) + factor(continent_n) +
    factor(wkday_n) + factor(isTrueDirect) + scale(visitNumber)
    pageviews * browser_n + visitNumber * operatingSystem_n +
    .
visitNumber * isMobile + visitNumber * isTrueDirect + pageviews *
    operatingSystem_n + timeOnSite * newVisits + timeOnSite *
    isTrueDirect + visitNumber * browser_n, family = binomial(link = "logit"),
    data = T_logis)
Deviance Residuals:
   Min
              1Q
                  Median
                                 30
                                         Max
-8.4904 -0.1025
                  0.0000
                            0.0000
Coefficients: (13 not defined because of singularities)
                                                         Estimate Std. Error z value Pr(>|z|)
(Intercept)
                                                        -1.207e+01 2.358e+01 -0.512 0.608609
                                                        4.774e-01
                                                                    1.226e-02
                                                                               38.939
scale(pageviews)
                                                                                       < 2e-16
                                                                               -0.365 0.714917
scale(bounces)
                                                       -8.439e+00
                                                                    2.310e+01
                                                                                      < 2e-16 ***
factor(newVisits)1
                                                       -8.915e-01
                                                                    3.008e-02 -29.635
                                                                                       < 2e-16 ***
scale(timeOnSite)
                                                        1.328e-01
                                                                    9.957e-03 13.336
factor(browser_n)Firefox
                                                                                5.847 4.99e-09 ***
                                                        4.278e-01
                                                                    7.316e-02
factor(browser_n)IE_Safari_Edge
                                                                    4.623e-02 -6.246 4.22e-10 ***
                                                       -2.887e-01
factor(browser_n)Opera_Safari(app)_Amazon_Sam_Ya
factor(browser_n)Other
                                                                               -2.852 0.004344 **
                                                                    2.781e-01
                                                       -7.932e-01
                                                       -7.157e-03
                                                                    1.077e+00 -0.007 0.994698
                                                                               -6.041 1.54e-09 ***
factor(operatingSystem_n)Mac_Linux
                                                       -2.994e-01
                                                                    4.957e-02
                                                                               -0.009 0.993202
factor(operatingSystem_n)Other
                                                       -1.077e+01
                                                                    1.264e+03
                                                                                       < 2e-16 ***
factor(operatingSystem_n)Win_iOS_Android_WinPhone
                                                                               -9.604
                                                       -5.020e-01
                                                                    5.227e-02
factor(isMobile)TRUE
                                                       -4.491e-01
                                                                    3.790e-02 -11.850
                                                                                       < 2e-16 ***
                                                                                       < 2e-16 ***
                                                       -3.302e+00
                                                                    6.274e-02 -52.632
factor(continent_n)outside America
                                                                                       < 2e-16 ***
factor(wkday_n)weekend
                                                       -2.081e-01
                                                                    2.484e-02
                                                                               -8.379
                                                                                       < 20-16 ***
factor(isTrueDirect)1
                                                        5.562e-01
                                                                    3.0926-02
                                                                               17.987
scale(visitNumber)
                                                       -5.019e-02
                                                                    5.498e-02
                                                                               -0.913 0.361296
pageviews
                                                                NΑ
                                                                           NΑ
                                                                                   NΑ
                                                                                             NΔ
browser_nFirefox
                                                                NΔ
                                                                           NΔ
                                                                                   NA
                                                                                             NA
browser_nIE_Safari_Edge
                                                                NA
                                                                           NA
                                                                                   NA
                                                                                             NΑ
browser_nOpera_Safari(app)_Amazon_Sam_Ya
                                                                NΑ
                                                                           NΑ
                                                                                   NΑ
                                                                                             NΔ
browser_n0ther
                                                                NA
                                                                           NA
                                                                                   NA
                                                                                             NA
visitNumber
                                                                NA
                                                                           NA
                                                                                   NΑ
                                                                                             NA
operatingSystem_nMac_Linux
                                                                NA
                                                                           NΑ
                                                                                   NA
                                                                                             NΑ
operatingSystem_nOther
                                                                NΔ
                                                                           NΔ
                                                                                   NA
                                                                                             NA
operatingSystem_nWin_iOS_Android_WinPhone
                                                                NA
                                                                           NA
                                                                                   NΑ
                                                                                             NA
isMobileTRUE
                                                                NA
                                                                           NA
                                                                                   NA
                                                                                             NA
isTrueDirect
                                                                                   NA
                                                                                             NA
```

```
timeOnSite
                                                              NΑ
                                                                          NA
                                                                                  NΑ
                                                                                           NΑ
newVisits
                                                              NA
                                                                         NA
                                                                                  NA
                                                                                           NA
pageviews:browser_nFirefox
                                                       -4.160e-02
                                                                  2.933e-03 -14.184
                                                                                      < 2e-16 ***
pageviews:browser_nIE_Safari_Edge
                                                       -3.183e-03
                                                                   1.859e-03
                                                                             -1.713 0.086804
pageviews:browser_nOpera_Safari(app)_Amazon_Sam_Ya
                                                       -1.809e-03
                                                                  9.287e-03
                                                                             -0.195 0.845542
                                                                             -6.199 5.67e-10 ***
pageviews:browser_n0ther
                                                       -4.503e-02
                                                                   7.263e-03
.
visitNumber:operatingSystem_nMac_Linux
                                                       -1.535e-02
                                                                   4.670e-03
                                                                              -3.288 0.001010 **
visitNumber:operatingSystem_nOther
                                                        2.409e-01
                                                                   5.495e+02
                                                                               0.000 0.999650
visitNumber:operatingSystem_nWin_iOS_Android_WinPhone 1.791e-03
                                                                   4.254e-03
                                                                              0.421 0.673688
visitNumber:isMobileTRUE
                                                       -8.735e-03
                                                                  6.065e-03
                                                                             -1.440 0.149827
visitNumber:isTrueDirect
                                                       -4.119e-03
                                                                   4.356e-03
                                                                             -0.946 0.344261
pageviews:operatingSystem nMac Linux
                                                       2.432e-02
                                                                   2.020e-03
                                                                             12.043
                                                                                     < 2e-16 ***
pageviews:operatingSystem nOther
                                                       -1.164e+00
                                                                   4.864e+02
                                                                             -0.002 0.998090
pageviews:operatingSystem_nWin_iOS_Android_WinPhone
                                                      -6.961e-03
                                                                  2.061e-03
                                                                              -3.377 0.000732
                                                                                     < 2e-16 ***
                                                                   2.669e-05
timeOnSite:newVisits
                                                       2.321e-04
                                                                              8.698
                                                                                      < 2e-16 ***
                                                                   2.684e-05
                                                                              -8.525
isTrueDirect:timeOnSite
                                                       -2.288e-04
browser_nFirefox:visitNumber
                                                       5.428e-03
                                                                   1.700e-03
                                                                              3.192 0.001412 **
browser_nIE_Safari_Edge:visitNumber
                                                       6.759e-03
                                                                  4.066e-03
                                                                              1.663 0.096402
browser_nOpera_Safari(app)_Amazon_Sam_Ya:visitNumber
                                                      -7.358e-02
                                                                  1.065e-01 -0.691 0.489499
browser_nOther:visitNumber
                                                       -8.598e-01 9.214e-01 -0.933 0.350753
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
(Dispersion parameter for binomial family taken to be 1)
    Null deviance: 204369 on 1708336 degrees of freedom
Residual deviance: 116291 on 1708302 degrees of freedom
AIC: 116361
Number of Fisher Scoring iterations: 21
```

Figure: Logistic model output

The accuracy on train dataset is 98.9% and on test dataset is 98.8%, which seem pretty high. However, it only predict 840 outcome as 1 out of 401590, and in fact there are 4594 outcome should be 1. Then I fit linear mixed model using nonzero outcome observations, the result is as follow:

```
Linear mixed model fit by REML ['lmerMod']
Formula: log(transactionRevenue + 1) \sim (0 + visitNumber | fullVisitorId) +
                                                                       isTrueDirect + continent + wkdav n
   scale(visitNumber) + browser_n + operatingSystem + isMobile +
  Data: T2
REML criterion at convergence: 56634.6
Scaled residuals:
            10 Median
                             3Q
   Min
                                    Max
-7.4213 -0.6202 -0.0677 0.5720 4.6681
Random effects:
              Name
                          Variance Std.Dev.
Groups
fullVisitorId visitNumber 0.005931 0.07701
                          1.146752 1.07087
Number of obs: 18514, groups: fullVisitorId, 16141
Fixed effects:
                                         Estimate Std. Error t value
(Intercept)
                                                     0.46967
scale(visitNumber)
                                          0.47714
                                                     0.04661
                                                               10.24
browser_nFirefox
                                          0.02294
                                                     0.06321
                                                                0.36
browser_nIE_Safari_Edge
                                         -0.33395
                                                     0.03941
                                                               -8.47
browser_nOpera_Safari(app)_Amazon_Sam_Ya -0.72349
                                                     0.18153
                                                               -3.99
browser_n0ther
                                        -0.67686
                                                     0.34225
operatingSystemChrome OS
                                          0.82765
                                                     0.23479
                                                                3.53
                                                                3.06
operatingSystemi0S
                                          0.19664
                                                     0.06423
                                          0.30420
                                                     0.23514
operatingSystemLinux
                                                                1.29
operatingSystemMacintosh
                                          0.73133
                                                     0.23370
operatingSystemWindows
                                          0.53601
                                                     0.23264
                                                                 2.30
operatingSystemWindows Phone
                                          0.01598
                                                     1.11580
                                                                0.01
isMobileTRUE
                                          0.12754
                                                     0.22953
                                                                0.56
isTrueDirect
                                          0.18019
                                                     0.01798
                                                               10.02
continentAfrica
                                          0.76769
continentAmericas
                                         -0.51128
                                                     0.40915
                                                                -1.25
continentAsia
                                         -0.33251
                                                     0.41692
                                                               -0.80
                                                               -1.57
                                                     0.42066
continentEurope
                                         -0.65848
                                                     0.45876
                                          0.22954
                                                                0.50
continentOceania
                                                     0.02328
wkday_nweekend
                                         -0.23507
```

Figure: Linear mixed model output

RMSE on train set is 4.76, and on test set is 13.52, which is not better than before. I think it may be due to the prediction error of the logistic model.

D. Censored Regression with Conditional Heteroscedasticy(CRCH) Model

Since the outcome is mostly zero and the nonzero part approximately follows normal distribution, thus I decide to fit censored(tobit) regression with conditional heteroscedasticy. The result is as follow:

```
Call:
crch(formula = revenue ~ scale(pageviews) + scale(bounces) + factor(newVisits) + scale(timeOnSite) +
    factor(browser_n) + factor(operatingSystem_n) + factor(isMobile) + factor(continent_n) + factor(wkday_n) +
factor(isTrueDirect) + scale(visitNumber), data = T_logis, link.scale = "log", dist = "gaussian",
    left = 0)
Standardized residuals:
                    Median
                                    3Q
                1Q
-13.8117
           2.5254
                     5.7373
                               7.3281 11.3177
Coefficients (location model):
                                                          Estimate Std. Error z value Pr(>|z|)
                                                        -115.94537 160.98204
                                                                                 -0.720
                                                                                           0.4714
(Intercept)
scale(pageviews)
                                                           5.85715
                                                                       0.06212
                                                                                 94.293
                                                                                          < 2e-16 ***
                                                                     157.73173
scale(bounces)
                                                         - 58.91452
                                                                                 -0.374
                                                                                           0.7088
factor(newVisits)1
                                                          -9.29471
                                                                       0.30198 -30.780
                                                                                         < 2e-16 ***
scale(timeOnSite)
                                                           2.22823
                                                                       0.06299
                                                                                35.373
                                                                                         < 2e-16 ***
                                                                                           0.0283 *
factor(browser_n)Firefox
                                                          -1.74694
                                                                       0.79632
                                                                                 -2.194
                                                                                          < 2e-16 ***
factor(browser_n)IE_Safari_Edge
factor(browser_n)Opera_Safari(app)_Amazon_Sam_Ya
factor(browser_n)Other
                                                          -3.70071
                                                                       0.39934
                                                                                 -9.267
                                                        -10.55829
                                                                       1.96595
                                                                                 -5.371 7.85e-08 ***
                                                                                 -5.192 2.08e-07 ***
                                                         -19.88718
                                                                       3.83030
factor(operatingSystem_n)Mac_Linux
                                                           0.34929
                                                                       0.42140
                                                                                  0.829
                                                                                           0.4072
factor(operatingSystem_n)Other
                                                         -92.55234 1041.15583
                                                                                 -0.089
                                                                                           0.9292
factor(operatingSystem_n)Win_iOS_Android_WinPhone
                                                         -8.38142
                                                                       0.46935 -17.857
                                                                                          < 2e-16 ***
                                                                       0.42904 -12.784 < 2e-16 ***
factor(isMobile)TRUE
                                                          -5.48486
                                                                                         < 2e-16 ***
factor(continent n)outside America
                                                         -35.73143
                                                                       0.65869 -54.246
factor(wkday n)weekend
                                                          -2.23156
                                                                       0.31420
                                                                                -7.102 1.23e-12 ***
                                                                       0.29242 17.553 < 2e-16 ***
factor(isTrueDirect)1
                                                           5.13302
scale(visitNumber)
                                                          -1.51633
                                                                       0.10410 -14.567
                                                                                         < 2e-16 ***
Coefficients (scale model with log link):
             Estimate Std. Error z value Pr(>|z|) 3.408021 0.006652 512.4 <2e-16 ***
(Intercept) 3.408021
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
Distribution: gaussian
Log-likelihood: -1.301e+05 on 18 Df
Number of iterations in BFGS optimization: 78
```

Figure: CRCH model output

From the regression table, we can see that coefficients are all statistically significant.

RMSE on train set is 1.8 and on test set is 1.87, which are better than before. The residual plot looks like this:

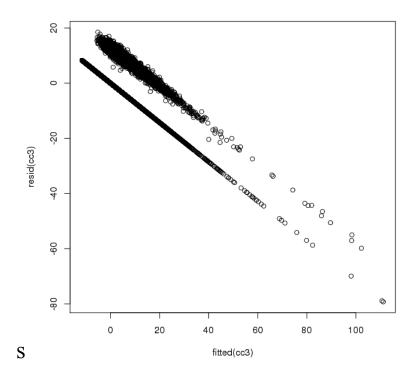


Figure: Residual plot of CRCH model

We can still see the trend of the residual plot, and I think it is due to the unbalanced outcome.

E. Light Gradient Boosting Machine(LGBM)

Since there are previous work using LGBM that lead to great result, I decide to use LGBM to fit on the dataset with recoded predictors. LGBM is a mothod of machine learning. Specifically, it is a gradient boosting framework that uses tree based learning algorithm. Also, unlike other boosting algorithm, LGBM is much faster in that it grows tree leaf-wise while other algorithm grows tree level-wise. Thus, it is a suitable method for this dataset. Here is the result of LGBM:

```
[LightGBM] [Warning] learning_rate is set=0.01, learning_rate=0.01 will be ignored. Current value: learning_rate=0.01 [LightGBM] [Info] Total Bins 814 [LightGBM] [Info] Number of data: 1708337, number of used features: 13 [LightGBM] [Info] Start training from score 0.192588 [11: val's rmse:1.88999 [101]: val's rmse:1.67385 [201]: val's rmse:1.63353 [301]: val's rmse:1.62244 [401]: val's rmse:1.61811 [501]: val's rmse:1.61633 [601]: val's rmse:1.61526 [801]: val's rmse:1.61474 [901]: val's rmse:1.61447 [1000]: val's rmse:1.61401
```

Figure: Light GBM output

It is evident that through iteration, RMSE on test set is reduced to 1.61, which is much better than previous ones. Also, it can calculate the importance of each predictor:

Feature Importance

pageviews

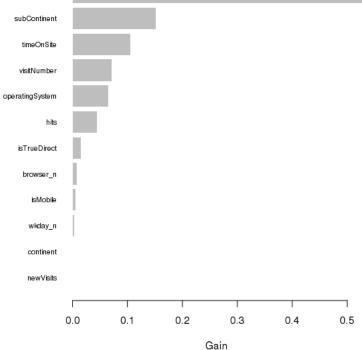


Figure: Light GBM predictors' importance

From the importance plot, we can see that "page views" is the most significant predictor for customer revenue, and then "sub-continent", "time on site", "visit number", "operating system" are also important for prediction of customer revenue. However, predictors like "continent" and "new visits" are not important for prediction.

IV. Result

1. Model choice

| Model | RMSE on test set | |
|---------------------|------------------|--|
| LMM (by users) | 1.97 | |
| LMM (by continents) | 1.93 | |
| Logistic & LMM | 13.52 | |
| CRCH Model | 1.87 | |
| LGBM | 1.61 | |

Table: Comparison of models

According to RMSE on test set, it is clear that LGBM is the best model, then the CRCH model, and next the LMM models.

2. Interpretation

Although LGBM is the best model, different models explain things through different aspects. I combine results of all models to lead to the result of the whole data analysis process.

A. Important predictors for revenue prediction (every visit)

1) Here are the importance of predictors in LGBM, CRCH and LMM models ordered by importance from high to low:

| LGBM | | CRCH | | | |
|--------------|-------|-----------------------------|------|----------|--|
| Feature | Gain | predictors | sign | estimate | |
| page views | 0.526 | page views | + | 5.86 | |
| subcontinent | 0.15 | continent_n-outside America | - | 35.73 | |
| time on site | 0.107 | time on site | + | 2.23 | |
| visit number | 0.072 | new visits | - | 9.29 | |

| operating system | 0.065 | operating system- Win_iOS_Android_WinPhone | - | 8.38 |
|------------------|-------|--|---|------|
| hits | 0.046 | is true direct-1 | + | 5.13 |
| is true direct | 0.015 | visit number | - | 1.52 |

Table: importance of predictors in LGBM and CRCH models

| LMMby users | | s | LMMby continents | | | |
|------------------------------|------|----------|--|------|----------|--|
| predictors | sign | estimate | predictors | sign | estimate | |
| pageviews | + | 0.61 | bounces | + | 0.089 | |
| bounces | + | 0.11 | newVisits-1 | - | 0.18 | |
| Newvisits-1 | - | -0.07 | isTrueDirect-1 | + | 0.074 | |
| Continent_n- outside America | + | 0.027 | visitNumber | - | 0.024 | |
| visitNumber | + | 0.013 | operatingSystem_n-win_iOS_Android_WinPhone | - | 0.143 | |
| Browser_n- IE_Safari_Edge | + | 0.031s | | | | |
| isMobile-True | - | 0.018 | | | | |

Table: importance of predictors in LMM models

From the tables, we can see that "page views" is the most frequent predictor that shows on the top of the list, which means it is the most important predictor to predict customer revenue. Also, all of its signs are positive, which means higher

revenue is expected when there are more "page views". Also, impact of "page views" to prediction of revenue may change between users and continents, thus it is the most indispensable predictor through all predictors.

Geography is also a critical predictor for revenue. Combined with previous EDA part and the result here, we can find out that revenue in America is expected to be higher than which in other continents.

Also, "visit number" is a significant predictor for revenue. Most of its signs are negative, thus more "visit number" may lead to lower expectation of customer revenue.

Next, "operating system" is another crucial predictor. Since the baseline here is "Chrome OS", thus users with "windows", "iOS", "Android" and "WinPhone" are expected to have higher revenue than users with "Chrome OS".

Finally, "is true direct" is also essential when predicting customer revenue. The baseline is "0", which means that users are not direct to the store, thus direct users correspond to higher customer revenue than indirect users.

3. Model Checking

I have already done the checking part before.

V. Discussion

1. Implication

The implication of the analysis could be used to maximize effectiveness of marketing investment. For every visit, based on its information like continent, operating system, page views and if it is true direct to the store, an expected

revenue could be predicted. Then a weight according to the expected revenue can be decided so that it can determine how much investment would be made on the visit. Ideally, higher expected revenue would lead to higher investment of marketing, thus users who are going to have transaction revenue will purchase more.

2. Limitation

Due to time limit, customer files have not been built yet. The largest column "hits", which is also the most interesting column, has not been analyzed. It contains much customer information like users' favorite product and their interested fields, and these can assist marketing strategies a lot. Also, for every user, there may be a purchase pattern, which can also be a great source of probability prediction for users to purchase things at time level. However, I ran out of time to finish these analysis.

3. Future direction

The whole process to analyze data for customer revenue prediction can be divided into two levels:

A. User level: This includes individual information from three aspects. Firstly, in general, whether it is easy for user to generate revenue. This could be summarized by previous revenue versus visit times. Secondly, from aspect of time, purchase pattern of every user may indicate probability of generating revenue for one visit of a user. Finally, history hits records of a user can show interested products of the user, which could help marketing strategies.

B. Visit level: This includes association between predictors of every visit like hits, page views, is true direct and so forth. Revenue for every visit can be predicted through this analysis, which is what this report mostly about. However, though LGBM may be a great method for prediction, I just give a try due to limit time. Parameters like learning rate can be tuned to improve the performance of the method.

To sum up, future direction of customer revenue prediction is to analyze data on user level, and improve methods in this report on visit level.

VI. Acknowledgement

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VIII. Appendix

Appendix I

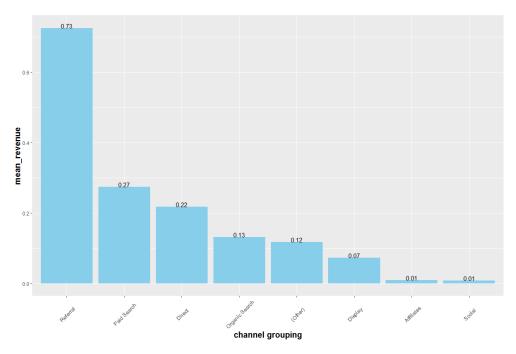


Figure: Revenue versus "channel grouping"

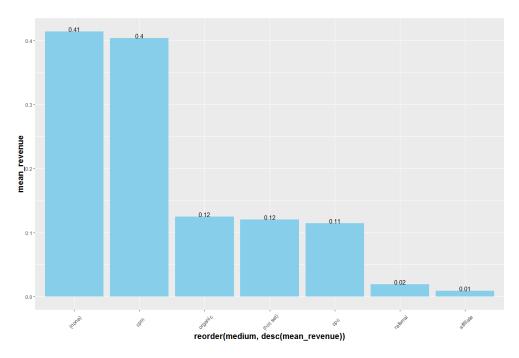


Figure: Revenue versus "medium"