# **ECO208Y Macroeconomics Notes**

# **Chapter 2 Measurements**

- Product
  - $\circ$  GNP = GDP + NFP
  - Real GDP
    - Using base year prices.
    - Chain-weighted real GDP. (Rolling base year)
  - $RGDPod = GDP_t \times (1 + g_c)$  where  $g_c$  is the geometric average of growth rate using previous year and current year variable.

□ Disposable Income

$$1 + g_c = \sqrt{(1 + g_t) \times (1 + g_{t+1})}$$

- Price Level
  - $\circ$  GDP Deflator =  $\frac{Nominal\ GDP}{Real\ GDP} \times 100$
  - $\begin{array}{ll}
    \circ & CPI = \frac{Q_{base} \cdot P_{new}}{Q_{base} \cdot P_{base}} \times 100 \\
    \circ & Inflation = \frac{P_{t+1} P_{t}}{P_{t}}
    \end{array}$
- National Accounts

$$Y^d = \underbrace{Y}_{GDP} + \underbrace{NFP}_{net\ factor\ payments} + \underbrace{TR}_{gov't\ transfers} + \underbrace{INT}_{interest\ on\ gov't\ debt} - \underbrace{T}_{taxes}$$

- 0
- $\circ$  CA = NX + NFP $\circ$  S = I + CA
- Labor Markets
  - Unemployment rate := #Unemployed Labor Force Labor Force Labor Force

  - O Participation rate := \(\frac{Labor roce}{Working Age Population}\)

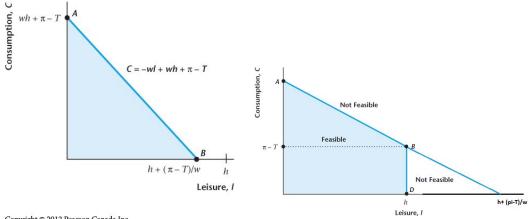
    \[
    \frac{\participation rate}{\participation rate} := \(\frac{\participation rate}{\participation rate} := \(\frac{\part  $\circ$  Employment/Population rate :=  $\frac{\#Employmen}{Working Age Population}$

# Chapter 4 Consumer-Firm One Period

# **CONSUMERS**

Consumer Setups

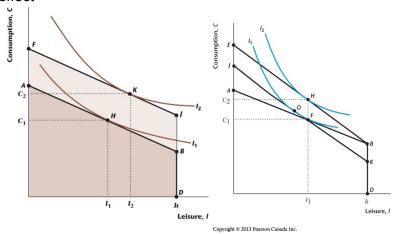
- $max_{c,l} \ u(c, l)$ 
  - Abstract normal good(C) against normal leisure(l)
  - Assumptions on preference
    - Monotonicity.
    - Convexity.
- $\circ \quad \text{s.t. } w(h-l) + \pi T = C$



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# **Experiment on Consumers**

Pure income effect



- Labor Supply: Assumed to be upwards sloping (SE dominates IE)
- $L = ln(c) + \eta ln(l) + \lambda [w(h-l) + \pi T C]$
- Comparative Statistics on  $C^*$ ,  $l^*$ 
  - T,  $\pi$  (Pure income)
  - w (IE + SE)

# **FIRMS**

# Firm Setup

- $max_{N^d} \{ \pi = zF(\overline{K}, N^d) \times p w \times N^d \}$ 
  - $\circ$  Take p=1
  - Take cost on K as LR, sunk
  - $\circ$   $\overline{K}$  exogenous
- Assumptions on technology.
  - CRS

- o Positive 1st ord. Der.
- Negative self 2nd ord. Der.
- o Positive cross 2nd ord. Der.
- FOC.  $MP_N = w$

# Experiments on $N^d$

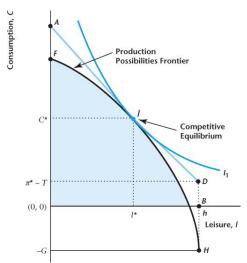
- z,  $\overline{K}$ , Tax on REVENUE  $(1-\tau)$
- w, Tax on labor  $w(1 + \tau_N)$

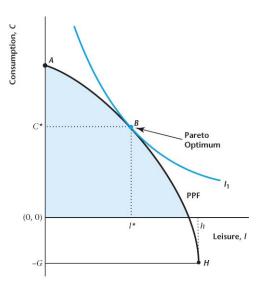
# Chapter 5 Closed Economy One-Period General Equilibrium Model

# Competitive Equilibrium

- All Market (Good/Labor) Clearing:  $C^* + \overline{G} = Y^* \wedge N^{s*} = N^{d*}$
- Agents take price as given and optimize.
  - Consumer:  $MRS_{l, C} = w$
  - Firm:  $MRT_{l,C} = w$
- Only price here is w, price for C is normalized to 1.
- Exo Var: *G*, *z*, *K*
- Endo Var: C,  $N^s$ ,  $N^d$ , T,  $\pi$ , Y
- Walras' Law
- Production Possibility Frontier

$$\circ \quad C = zF(K, h-l) - G$$





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- Government
  - $\circ$   $\overline{G} = T$
  - $\circ Y = C + G$

#### **Economic Efficiency**

- Pareto efficient: there is no way to do Pareto improvement
- Pareto optimal 
   ← Perfect Information + No friction.
- Solve Social Planner's Optimization: Choosing N to maximize consumption Y G
  - o Utilitarian Social Welfare Function:  $\sum_{i} U_i(C_i)$
  - Rawlsian Social Welfare Function:  $min\{U_i(C_i)\}\$

#### Welfare Theorems

- First welfare theorem: Competitive equilibrium ⇒ Pareto optimal.
- **Second welfare theorem**: Pareto optimal ⇒ Competitive equilibrium by redistribution.
- Economic inefficiencies

  - · Distortionary taxes.
  - · Market power.
  - Information Asymmetries.

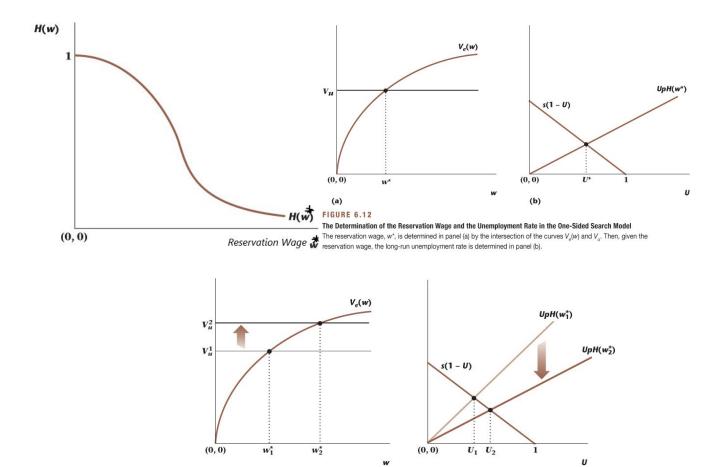
#### **Experiments**

- Change *G*
- Change *z*
- Lump-sum Tax: parallel shift, same as  $\Delta G$
- Income Tax: Effective a reduce in real wage

# Chapter 6a One-side Model of Job Search

## Setup

- *N* := working age population.
- *Q* := labor force.
- *U* := <u>fraction</u> of unemployment.
- $V_e(w) := \text{utility from employment as a function of } w$ .
- *s* := job separation rate.
- $V_u$  := value from unemployment. (e.g. unemployment benefit b, prob of getting job offer)
- p := prob. Of receiving job offer.
- $w^*$  := reservation wage: cutoff for accepting job offer.
- $H(w^*)$ := fraction of unemployed workers who receive a wage offer greater than their reservation wage  $(w > w^*)$ . Offer Acceptance Rate
- Job creation flow  $:= U \times p \times H(w^*)$
- Job destroy flow :=  $s \times (1 U)$



(b)

# Chapter 6b Two-side Model of Job Search

# Setup

- $\circ$  A := aggregate number of vacancies posted by firms.
- $\circ$  Q := people looking for job.
- $\circ$  Q-U := currently employed.

(a)

- Vacancy rate =  $\frac{A}{A+O-U}$
- Each firm post one vacancy.
- Consumer choose to search for work or not.
  - Heterogeneous in home production payoff.
  - Same in expected payoff from searching for jobs.
- $\circ$  v(Q) expected payoff from searching for job.
- $\circ$  Firms pay k to post vacancy.
- $\circ$  Total A firms posting vacancy.

#### Measurements

$$\circ \quad v = \frac{{}^{A(1-p_f)}}{{}^{A}} = 1 - p_f \text{ vacancy rate}$$

$$\circ \quad u = \frac{Q(1-p_c)}{Q} = 1-p_c$$
 unemployment rate

$$\circ$$
  $Y = zM = zem(Q, A)$  total output

# **Matching Function**

$$\circ \quad M = em(Q, A)$$

■ CRS 
$$\Rightarrow$$
  $M = Qem(1, j)$ 

- Increasing func.
- Neg. 2nd ord. Der.
- All argument essential.
- $M = eO^{\alpha}A^{1-\alpha}$
- All job seekers share the same probability to be matched.
  - $j := \frac{A}{O}$  labor market tightness
  - $p_c = \frac{M}{Q} = em(1, j)$

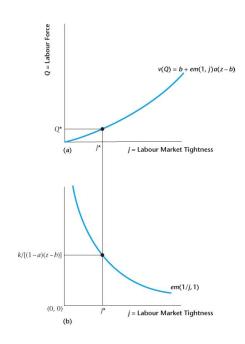
# **Consumer Optimization**

- Choose between <u>home production</u> and <u>searching for work</u>
  - v(Q) = b + em(1, j) (w b)

# Firm Optimization

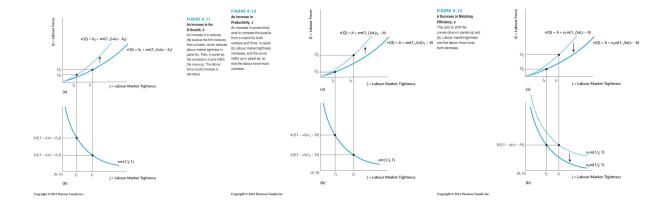
$$o p_f = \frac{M}{A} = em(\frac{1}{i}, 1)$$

- $\circ$  If matched, a worker and a firm produce output z
  - ightharpoonup ightharpoonup Profit := z w
- Net gain from posting job  $p_f(z-w)-k=0$  at equilibrium (the free entry condition)
- Nash Bargaining
  - Total surplus z b
  - $v(Q) = b + em(1,j) \times a \times (z b)$   $p_f = em(\frac{1}{j}, 1) = \frac{k}{(1-a)(z-b)}$   $j = \frac{A}{Q}$



## **Experiments**

- Change in b
- Change in z
- Change in e



# Chapter 7 Economic Growth

## Setup

- Production function Y = zF(K, N)
  - $\circ$  *K* := Assets, at their purchase prices.
  - $\circ$  N := # of total hours worked.
  - $\circ$  z := Residual
    - Solow Residual  $\hat{z} = \frac{\hat{Y}}{\hat{K}^a \hat{N}^{1-a}}$
- Economic Growth ⇒ Growth in output per capita.
- Solow Growth Model setup

$$\circ N' = (1+n)N$$

$$\circ$$
  $C = (1 - s)Y$ 

$$\circ$$
 CRS  $F(K, N) \Rightarrow y = zf(k)$ 

$$\circ K' = (1 - \delta)K + I$$

$$\circ \quad Y = C + I$$

## Equilibrium & Steady State

Steady state: all endogeneous variables are growing at a constant rate.

$$\circ$$
 Solve  $k' = k := k^2$ 

o Solve 
$$k' = k := k^*$$
  
o  $k' = \frac{K'}{N}, = \frac{1}{1+n} \frac{(1-\delta)K + szF(K,N)}{N} = \frac{K}{N}$   
o  $\Rightarrow (1-\delta)k + szf(k) = (1+n)k$ 

$$\circ \Rightarrow (1-\delta)k + szf(k) = (1+n)k$$

$$\circ \Rightarrow szf(k^*) = (n+\delta) \times k^*$$

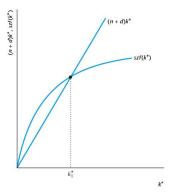


FIGURE 7.14 Determination of the Steady State Quantity of The steady state quantity of capital,  $k_1^*$  is determined by the intersection of the curve  $szf(k^*)$  with the line  $(n + d)k^*$ .

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# **Experiments**

#### Increase s

- $g_Y = g_N + g_y$
- $g_{v} > 0 \in \text{transition}$  to new steady state.

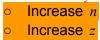


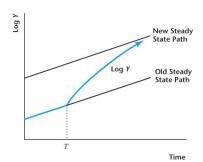
FIGURE 7.15 Effect of an Increase in

Effect of an Increase in the Savings Rate on the Steady State Quantity of Capital per Worker
An increase in the savings rate shifts the curve szf(k²) up, resulting in an increase in the quantity of capital per worker from k², to k².

#### FIGURE 7.16 Effect of an Increase in the

growth path.

Savings Rate at Time T The figure shows the natural logarithm of aggregate output. Before time T, the economy is in a steady state. At time T, the savings rate increases, and output then converges in the long run to a new higher steady state



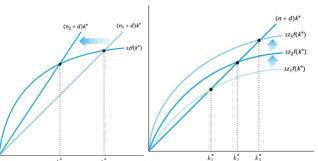
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#### FIGURE 7.19 Steady State Effects of an Increase in the Labour Force Growth Rate

An increase in the labour force growth rate from  $n_1$  to  $n_2$  causes a decrease in the steady state quantity of capital per worker.

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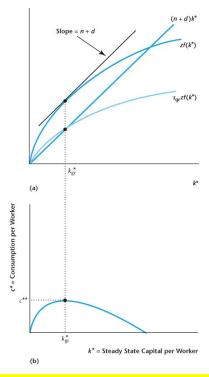
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FIGURE 7.20 Increases in Total Factor Productivity in the Solow

**Growth Model** Increases in total factor productivity from  $z_1$  to  $z_2$ , and from  $z_2$  to  $z_3$ , cause increase in the quantity of capital per worker from  $k_1^*$  to  $k_2^*$ , and from  $k_2^*$  to  $k_3^*$ . Thus, increases in total factor productivity lead to increases in output

Golden Rule Level of Capital per Worker / Golden Rule of Saving

- $k_{GR}^* = argmax_{k^*} \{c^* = (1-s) \times zf(k^*)\}$   $s_{GR}^* = argmax_s \{c^* = (1-s) \times zf(k^*)\}$

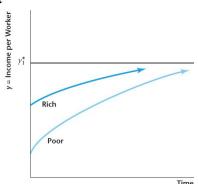


• **Conclusion**: z is thought to be the main driver of per capita GDP growth in developed countries.

# Chapter 8 Convergence in the Solow Model

- Steady State:  $\Delta y = \Delta c = \Delta k = 0$  defined over <u>per capita</u> values.
- Different initial  $k_0$  converge to the same  $k^*$

FIGURE 8.2
Convergence in Income per
Worker across Countries in
the Solow Growth Model
Two otherwise identical
countries, one with lower
income per worker (the poor
country) than the other (the
rich country), converge in
the long-run steady state to
the same level of income per
worker, y\*,.

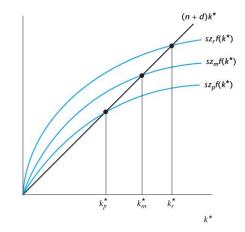


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• Different TFP z converges to different  $k^*$ 

#### FIGURE 8.4

Differences in Total Factor
Productivity Can Explain
Disparity in Income per
Worker across Countries
If countries have different
levels of total factor
productivity because
of differing barriers to
technology adoption, then
capital per worker and
income per worker differ
across countries in the
steady state.



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- Causes of different TFP across countries.
  - Technology adoption.
  - Trade liberalization.
  - Market imperfections.
  - o Institutions: private property.
  - o Education.
  - Misallocation.

# Chapter 9 Two-Period Model: Consumption-Saving Decision and Credit Markets. Exogenous Income y - t

# Setup

- Preference  $\max_{c, c'} \{u(c) + \beta u(c')\}$ 
  - Assumptions
    - Monotonicity
      - c, c' are normal goods
      - Convexity ⇒ Consumption smoothing
- Budget
  - c + s = y t P.1
  - $c' = y' t' + (1 + r) \times s \text{ P.2}$
  - $c + \frac{c'}{1+r} = y t + \frac{y'-t'}{1+r}$  Life-time PDV.
- $\circ$   $c > y t \Rightarrow Borrower.$
- $\circ$   $c < y t \Rightarrow \text{Lender}$ .
- $o we := y t + \frac{y' t'}{1 + r}$

## **Model Solution**

$$max_{c,c'}\{ln(c)+eta ln(c')\},\; s.t.\; c+rac{c'}{1+r}=y-t+rac{y'-t'}{1+r}$$

Solve.

$$\mathcal{L} = ln(c) + eta ln(c') + \lambda (y - t + rac{y' - t'}{1 + r} - c - rac{c'}{1 + r})$$

FOC.

$$\frac{\partial \mathcal{L}}{c} = \frac{1}{c} - \lambda = 0$$

$$\frac{\partial \mathcal{L}}{c'} = \frac{\beta}{c'} - \lambda \frac{1}{1+r} = 0$$

$$rac{\partial \mathcal{L}}{\lambda} = y - t + rac{y' - t'}{1 + r} - c - rac{c'}{1 + r} = 0$$

=>

$$\frac{c'}{c} = (1+r)\beta$$

Plut in to constraint

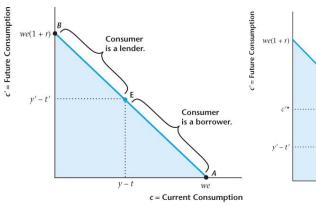
Solve...

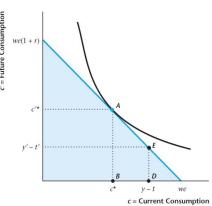
$$c^*=rac{1}{1+eta}(y-t+rac{y'-t'}{1+r})$$

And

$$c'^* = rac{eta(1+r)}{1+eta}(y-t+rac{y'-t'}{1+r})$$

# Graphics





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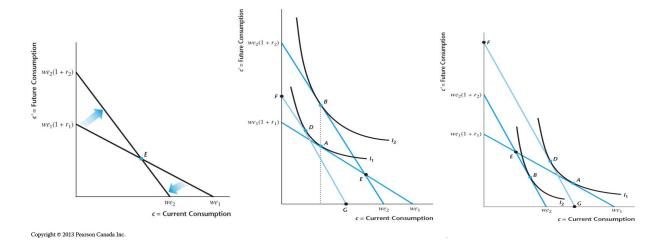
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# Experiment

- Increase  $y, y', t, t' \Rightarrow Pure IE$
- Increase  $r \Rightarrow IE + SE$ 
  - $\circ$  SE: more c' and less c

o IE:

- Positive for lenders
- Negative for borrowers



# Permanent Income Hypothesis

- o main determinant of consumption is **permanent income**, which is closely related to lifetime wealth *we*.
- o Permanent increase in income leads to a **small** increase in saving.

## Ricardian Equivalence Theorem

- o <u>Holding government spending</u> (G, G') <u>fixed</u> (equivalently, hold PDV of taxation fixed), change in T, T' will leave r, c, c' unchanged. (<u>Timing of the taxes do not matter</u>)
- Rational expectations (<u>Lucas Critique</u>): foreseeing the future tax and reduction in lifetime wealth ⇒ adapt saving.
- o Proof.

By government budget constraints in both period,

as (G, G') is exogenous and unchanged, then

$$\Delta t + \frac{\Delta t'}{1+r} = 0$$

$$m\Delta t + \frac{m\Delta t'}{1+r} = 0$$

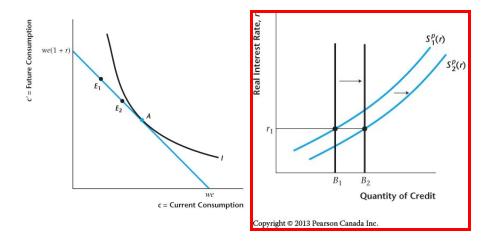
$$\Delta T + \frac{\Delta T'}{1+r} = 0$$

Therefore, if above equations hold, there would be **no change** 

In consumers' PDV of life time wealth and therefore the consumptions

 $(C^*, C'^*)$  Will be **unchanged** with tax change  $\Delta t$  in current period.

- Lifetime budget constraint:  $c + \frac{c'}{1+r} = y + \frac{y'}{1+r} \frac{1}{m} \left[ G + \frac{G'}{1+r} \right]$
- o Change in timing of taxation
  - ⇒ Effective moving the endowment along the original budget line
  - ⇒ No change in lifetime wealth.
  - Implications: no free lunch in tax cut.



## Martingales

- $\circ$   $E[p_{t+1}|p_t, p_{t-1}, \cdots, p_{t-n}] = p_t$
- o Prove by contradiction, self-fulfilling hypothesis.
- o Implication: consumers assume that any changes in the value of stocks is **permanent**.

### Ricardian Equivalence Failure

- Individuals may not paying the same taxes ⇒ Redistribute lifetime wealth among individuals. (INTRA-generational redistribution)
- INTER-generational redistribution of wealth.
- Distortionary taxation. (i.e. not lump-sum tax).
- Credit market imperfection.

# Chapter 11 Two Periods model with Leisure-Consumption choice

# Real intertemporal model with investment

- Markets.
  - Current Labor Market ⇒ Output Supply Curve
  - Current Good Market ⇒ Output <u>Demand</u> Curve

# Representative Consumer

- Budget
  - P1.  $C + S^P = w \times (h l) + \pi T$
  - P2.  $C' = w' \times (h l') + \pi' T' + (1 + r) \times S^P$
  - Life-time  $C + \frac{C'}{1+r} = w \times (h-l) + \pi T + \frac{w' \times (h-l') + \pi' T'}{1+r}$
- Solution

■ S.t. 
$$C + \frac{C'}{1+r} = w \times (h-l) + \pi - T + \frac{w' \times (h-l') + \pi' - T'}{1+r}$$

C: 
$$\frac{1}{C} - \lambda = 0$$
C': 
$$\frac{\beta}{C'} - \frac{\lambda}{1+r} = 0$$
I: 
$$\frac{\eta}{I} - \lambda w = 0$$
I': 
$$\frac{\beta \eta}{I'} - \frac{\lambda w'}{1+r} = 0$$

$$\lambda: w(h-I) + \pi - T + \frac{w'(h-I') + \pi' - T'}{1+r} - C - \frac{C^{L}}{1+r} = 0$$

#### Current period labor supply

- Assumptions
  - Increase in w
  - Decrease in we
  - Increase in r

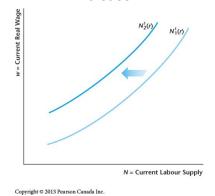
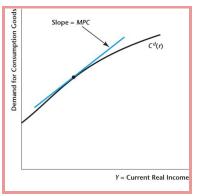


FIGURE 11.3
Effects of an Increase in
Lifetime Wealth
More leisure is consumed
in the present, because of
the income effect, and the
current labour supply curve
shifts to the left.



#### Consumption demand

- Assumptions
  - o Increase in lifetime wealth we
  - Decrease in *r*

# Representative firms.

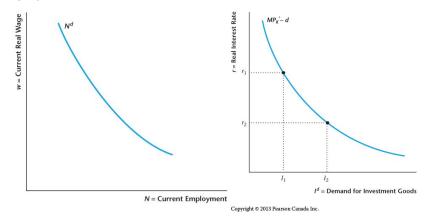
#### Firm Setup

- Maximize PDV of lifetime profit  $V = \pi + \frac{\pi'}{1+r}$  by choosing N, N', K'
- Setup:
  - Capital Transition:  $K' = (1 \delta)K + I$
  - $\circ$  P1:  $\pi = z F(\overline{K}, N) wN I$
  - o P2:  $\pi' = z' F(K', N') w' N' + (1 \delta)K'$
  - $\bullet \quad \mathsf{LT} : \ V = zF(\overline{K}, N) wN K' + (1 \delta)\overline{K} + \frac{z'F(K', N') w'N' + (1 \delta)K'}{1 + r}$
- Solution
  - o FOC
    - $\blacksquare MP_N = w$

$$MP_{N'} = w'$$

$$MP_{K'} = r + \delta$$

#### **Current Labor Demand**



- Decrease in w
- Increase in z
- Increase in  $\overline{K}$

#### Firm's investment scheme

- Final  $K'^*$  s.t.  $r = MP_K' \delta$  And  $I^* = K'^* (1 \delta) \times \overline{K}$
- $I^*$  decreases in r
- Increases in z'
- Decrease in  $\overline{K}$

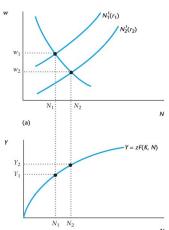
#### Government

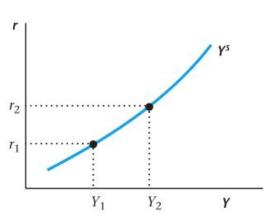
$$\circ \quad G + \frac{G'}{1+r} = T + \frac{T'}{1+r}$$

# Competitive Equilibrium

- 1. All markets clear.
- 2. PDV of government budget balanced.
- 3. All agents optimize.

Output Supply Curve

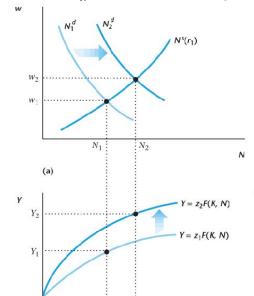




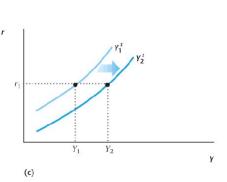
Experiments on output supply

Ν

- Increase in z or K
  - $MP_N$  rises  $\Rightarrow N^d$  shifts right  $\Rightarrow Y^s$  shifts right



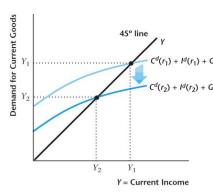
 $N_2$ 

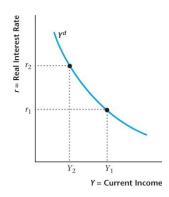


Current good demand curve

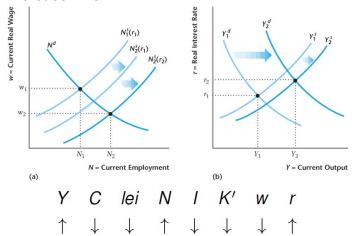
$$\circ Y^d = C^d(r) + I^d(r) + G$$

(b)





- Experiments on output demand
  - Increasing in G
    - G increases and  $C^d(r)$  falls  $\Rightarrow$  by consumption smoothing mechanism  $\Rightarrow$  increase in G is greater than falling in  $C^d \Rightarrow Y^d$  increases.
- Complete Model
  - $\circ$  Labor market clearing at  $r \Rightarrow Y^s(r)$
  - $\circ Y^d = C^d(r) + I^d(r) + G \text{ holds at } r \Rightarrow Y^d(r)$
- Experiments with the Complete Model
  - $\circ$  Temporal increase in G



- Assume smaller change in Y<sup>s</sup> since ΔG is temporal.
- $\circ$  Government Multiplier  $\frac{\Delta Y}{\Delta G} < 1$  since temporal shocks have small income effect.

# Chapter 12 Money & Monetary Policy

- Functions.
  - Medium of exchange
  - Store of value
  - Unit of account
- Cash in advance model: money is necessary for exchange.
- Classical ⇒ Neutrality of money
- Inflation  $i = \frac{P'-P}{P}$
- Fisher's relation:  $r \approx R i$

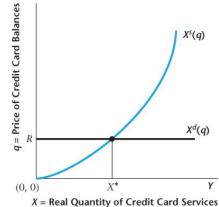
• Assume zero inflation  $\Rightarrow R > 0 \Rightarrow$  rate of return on nominal bonds dominates the rate of return on money.

## Model setup

#### Banks

- · Quantity of credit card balances
- Credit card costs q per nominal unit of credits
- Credit card market
  - o  $X^{s}(q)$ : supply of credit card services.
  - $\circ$   $X^d$ : q == R: perfectly elastic credit card service demand.

FIGURE 12.3
Equilibrium in the Market for Credit Card Services
The demand curve for credit balances is horizontal at the price q = R, the equilibrium price of credit card services is q = R and the quantity is  $X^*$ .



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#### **Demand for Money**

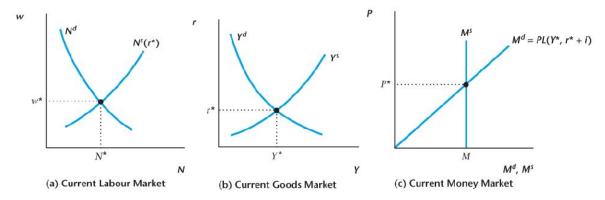
- $\bullet \quad M^d = P[Y X^*(R)]$
- $\bullet \quad M^d = P \times L(Y, R)$ 
  - $\circ$   $L(\cdot)$  real demand for money, increases in Y and decreases R.

#### Representative consumer/firm

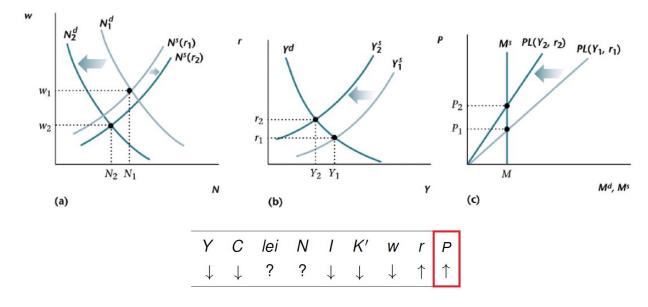
- Transaction Constraint  $P(C+I+T) + B^d = M^- + (1+R^-)B^- + PX^d$
- Budget Constraint  $P(C+I+T) + B^d + M^d + qPX^d = M^- + (1+R^-)B^- + PY$

#### Government

- Budget  $PG + (1 + R^{-})B^{-} = PT + B + (M M^{-})$
- Seigniorage Revenue: revenue from direct money supply.
- Increase Money supply
  - Reduce *T* (Helicopter drop)
  - Increase *G* (Seigniorage)
  - Reduce *B* (Open market operation)



- Classical Dichotomy: Equilibrium in the money market does not affect <u>real</u> macroeconomic variables.
- Experiment: temporary exogenous decrease in z
  - Empirically N falls and lei increases.

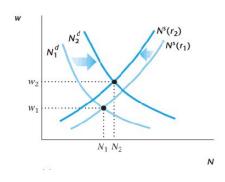


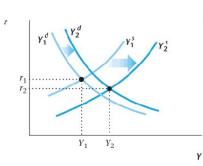
# Chapter 13 Business Cycle Models

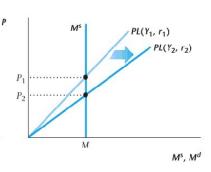
# Standard Real Business Cycle Model

- Agent respond optimally to <u>real</u> productivity shocks.
- No Government intervention (Central bank still works).
- Productivity shocks
  - Persistent shock (both z and z')
- Positive productivity shocks z ↑, z'↑
  - 1.  $N^d$  increases (Larger as the primary shock source).
  - 2. Y<sup>s</sup> increases (Direct result from primary shock)

- 3.  $Y^d$  increases as  $I \uparrow$ ,  $C \uparrow$  from positive wealth effect.
- 4. **Overall**: Positive expansionary shocks.  $r \downarrow (empirically) Y \uparrow$







Data ⇒ Higher employment level ⇒ Higher labor productivity (average) ⇒ N\* should increase
in positive productivity shock.

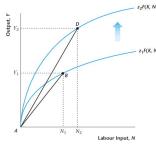
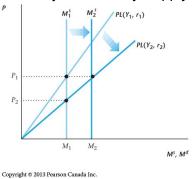


FIGURE 13.3 Average Labour Productivity with Total Factor Productivity Shocks When output and employment are high, average labour productivity is also high, as in data.

Policies:

• Endogeneous Procyclical Money Supply: Central Bank targeting price level.



Procyclical Money Supply in the Real Business Cycle Model with Endogenous Money
A persistent increase in total factor productivity increases aggregate real income and reduces the real interest rate, causing money demand to increase. If the central bank attempts to stabilize the price level, this will increase the money supply in response to the total factor productivity shock.

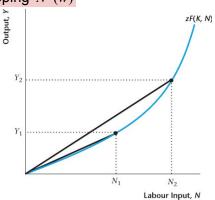
- Assessment
  - Misleading Solow Residual z measurement.
  - Labour Hoarding: sticky labor market.
  - Capital Utilization: change in capital utilization during different sessions.

# Keynesian Coordination Failure Model (Multiple Equilibria)

## Setup

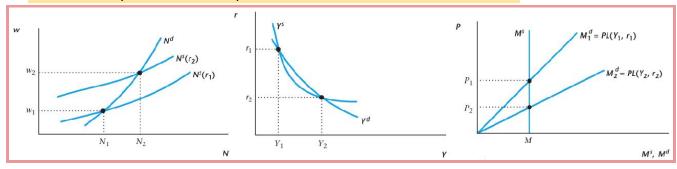
• (Firm outputs) **Strategic complementarities**  $\Rightarrow$  increasing return to scale (<u>At the aggregate level</u>) production function.  $\Rightarrow$  Upward-sloping  $N^d(w)$ 





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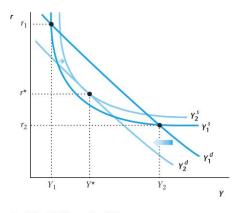
- Self-fulfilling perception ⇒ Animal Spirits
- $N^d$  is steeper than  $N^s$  is required for coordination failure model to work.



• Both equilibria are steady, the movement between is determined by sunspot.

#### Government

- Indirect ⇒ Sunspot ⇒ Announcement.
- Alter government expenditure G to affect  $Y^d \downarrow But$  the new equilibrium outcome is **not** necessarily better.



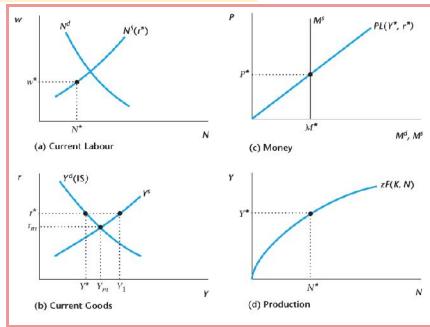
Stabilizing Fiscal Policy in the Coordination Failure Model Fiscal policy can stabilize output in the coordination failure model by eliminating multiple equilibria. Here, with a decrease in government spending, the output demand curve shifts to the left and the output supply curve shifts to the right, and this can produce a unique equilibrium where Y = Y\* and r = r\*.

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# Chapter 14 New Keynesian Sticky Price Model

## Model Setup

- Sticky Prices real and nominal prices w, r, P do not adjust to clear the markets in the short run.
  - o Firms produce however much output is demanded at given prices.
  - Workers must work the exact hours demanded by firms although we will allow the real wage to vary.
  - Consumer side matters (N<sup>s</sup> and Y<sup>d</sup>(IS)).



- $Y^d(IS)$  and  $r^*$  determines the actual output.
- Output gap

#### Natural rate of interest

#### **Government Policies**

#### Central bank:

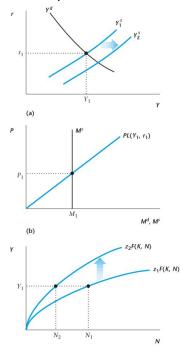
- Announce interest rate *r*\*
- $\circ$  Support it by setting money supply  $M^s$  so that  $\overline{P}$  is unchanged. ( $\overline{P}$  does not change by our assumption).

#### Process

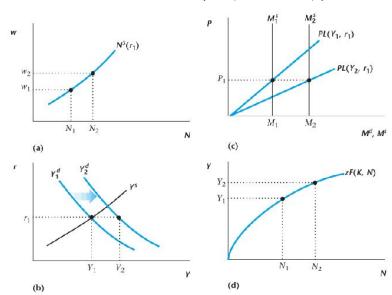
- 1. Central bank <u>claim</u> new interest rate.
- 2.  $Y^*$ ,  $N^*$  changes.
- 3.  $N^s$  changes,  $w^*$  changes.
- 4. Central bank adjust  $M^s$  to keep  $\overline{P}$ .
- Keynesians and all orthodox agree that money is natural in the long-run. (Since price stickiness is released in the long run)

# Current period TFP Shocks $z\ \uparrow$

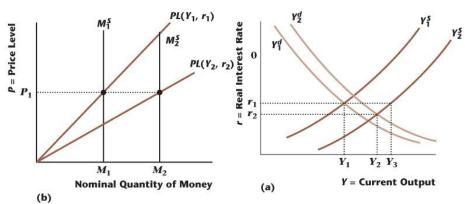
- $Y^s$  changes and leaves  $Y^d$  unchanged.
- The main determination is left unchanged.
- $N^*$  falls as production function shifts up.



Demand shock from Future TFP Shocks  $(z' \uparrow \Rightarrow I^d \uparrow)$ 



Persistent TFP Shocks  $(z \uparrow z' \uparrow \Rightarrow I^d \uparrow)$ 

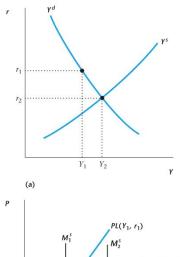


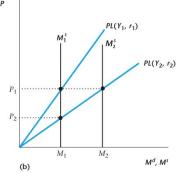
- (In persistent TFP shocks) If the central bank cut the interest rate to  $r_2$  and increase  $M^s$  it can eliminate the output gap.
- The outcome in a Neo-Keynesian model with the central bank eliminating output gaps gives the same result as the RBC model with a central bank targeting the price level.

# Government Policy

Monetary Policy: claiming  $r_{new}$  and adjust  $M^s$ 

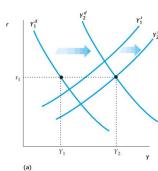
- Indirect change in *C*, *I* (others constant)
- (Keep price level  $\overline{P}$  constant)

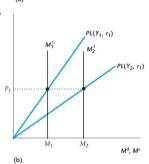




# Fiscal Policy

- Direct change in G (others constant)  $G \uparrow \Rightarrow Y^d \uparrow$  and negative wealth effect  $\Rightarrow N^s \uparrow Y^s \uparrow$   $M^s \uparrow$  to keep price level constant  $\overline{P}$ .





### Claims of New Keynesians (from sticky price model)

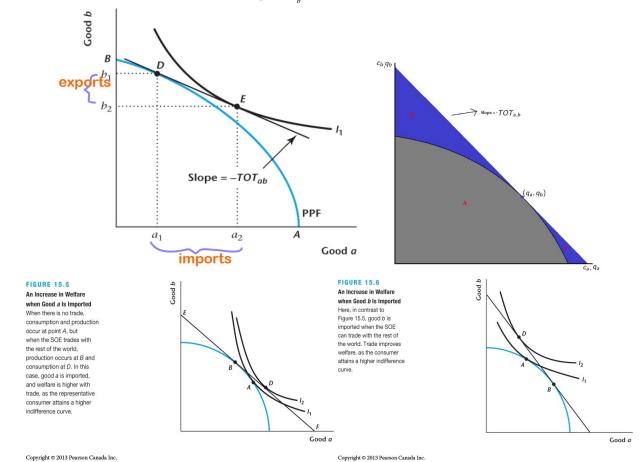
- In the short-run private markets do not always work efficiently on their own (price stickiness).
- **Demand(IS)** is an important determinant of output.

# Chapter 16 International Trade in Goods and Assets

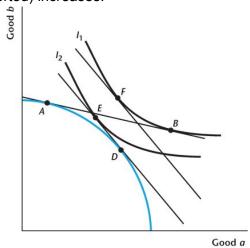
# Topic 1: SOE w/ two goods (Single Period)

- **Autarky**
- $TOT_{a,b} = \frac{P_a^T}{P_b^T}$  exogenous international prices

  Budget constraints  $P_a^T \times c_a + P_b^T \times c_b = P_a^T \times q_a + P_b^T \times q_b$ 
  - Markets clear on international scale
- Opening to trade makes the economy weakly better than Autarky.
  - Special case where  $TOT_{a,b} = \frac{\overline{P_a}}{\overline{P_b}}$   $\Rightarrow$  the economy is indifferent between two.



- Substitution Effects and Income Effects when *TOT* changes.
  - Draw SE hypothetical on the **original** indifference curve.
  - (Intuition) Beneficial if international (relative) price for the products with comparative advantages (exported) increases.



# Topic 2: the Current Account in the Two Goods SOE Model

- Assuming NFP = 0
- CA = NX = 0
  - With single period, there's no borrowing/saving.
  - SOE consumers pay all consumption in single period.
  - Value of imports = value of exports.

# Topic 3: SOE with two periods with no investment. (Single good)

#### Simply substitute saving to CA (using the international credit market)

- Assume  $TFP = 0 \Rightarrow S = CA = NX$
- World credit market clears and gives exogeneous r.
- Representative consumer budget  $C + \frac{C'}{1+r} = Y T + \frac{Y' T'}{1+r}$  Government budget  $G + \frac{G'}{1+r} = T + \frac{T'}{1+r}$
- $\bullet \quad S^p = Y T C$
- $S^g = T G$

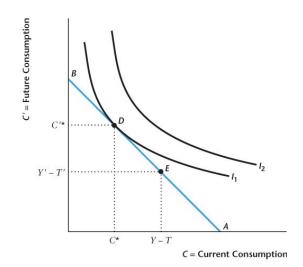
$$\Rightarrow S^p + S^g = Y - G - C = CA$$

- $G \uparrow \Rightarrow C, C' \downarrow (Consumption smoothing, normal consumption goods.)$
- $T \uparrow \Rightarrow$  No Effect on C, C' (Ricardian Equivalence)

#### FIGURE 15.9

The Two-Period Small Open Economy Model

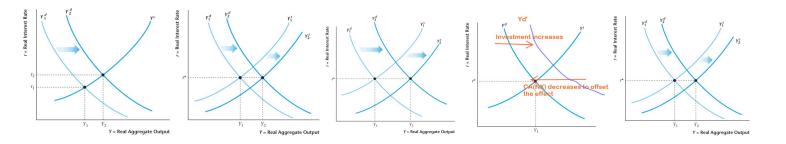
The representative consumer's budget constraint is *AB*, the endowment point is *E*, and the consumer chooses point *D*.



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# Topic 4: SOE with production and investment

- World credit market clears and gives exogeneous  $r^*$ .
- Output demand  $Y^{d}(r^{*}) = C^{d}(r^{*}) + I^{d}(r^{*}) + G + NX(r^{*})$ 
  - CA and NX always adjust to clear output market.
- Experiment 1: r\* ↑
  - $\circ$   $NX \uparrow C \downarrow I \downarrow$
- Experiment 2 G ↑
  - $\circ$   $T \uparrow \Rightarrow we \downarrow, N^s \uparrow$  (negative lifetime income effect)  $\Rightarrow Y^s \uparrow$
  - $\circ$   $C \downarrow$  and  $\Delta C < \Delta G$  due to consumption smoothing
  - NX/CA ↓ (Cannot see from the model) <u>Some of government spending was financed</u> from the originally exported economic surplus(production), therefore NX falls.
- Experiment 3 z ↑
  - $\circ$   $N^d \uparrow \Rightarrow Y^s \uparrow$
  - $\circ$  C  $\uparrow$  for small magnitude due to consumption smoothing
  - $\circ$  CA/NX  $\uparrow$
- Experiment 4 : z' ↑
  - $\circ$  I, C  $\uparrow$
  - $\circ$  Borrow from the rest of the world, and  $NX/CA \downarrow$  to clear market.
- Experiment 5: K ↑
  - $\circ$   $N^d \uparrow Y^s \uparrow$
  - $\circ$  I  $\downarrow$  since less investment needed to achieve target K'
  - $\circ$   $NX \uparrow Y^d \uparrow$  to clear market



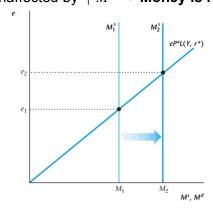
# Chapter 17 Small Open Economy

#### **Definitions**

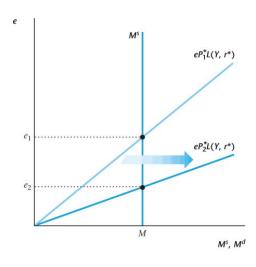
- P domestic price
- P\* foreign price
- *e* exchange rate
- $\frac{eP^*}{P}$  real exchange rate / terms of trade
- Purchasing Power Parity
  - $\circ$   $eP^* = P$  # Real Interest Rate = 1

# Monetary SOE with flexible exchange rate

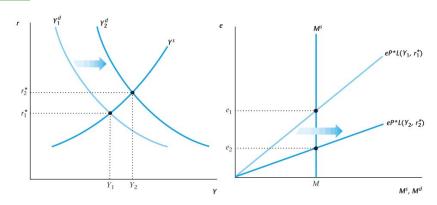
- Setup
  - Exogenous  $r^* \in \text{world credit market}$
  - Assume PPP holds  $P = eP^*$
- Money market: devaluation by increasing M<sup>s</sup>
  - o *e* and *P* increase proportionally since  $P^* = \frac{P}{e}$  is unchanged.
  - Real variables are unaffected by  $\uparrow M^s \Rightarrow$  Money is Neutral



- Experiment 1  $P^* \uparrow$  (Nominal foreign shock)
  - o P unchanged and other real variables unaffected.
  - ⇒ Insulate economy/ domestic price from nominal foreign shocks.

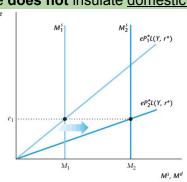


- Experiment 2  $r^* \uparrow$  (Real foreign shock)
  - ⇒ Flexible exchange rate **does not** insulate the <u>domestic prices</u> from **real** foreign shocks.

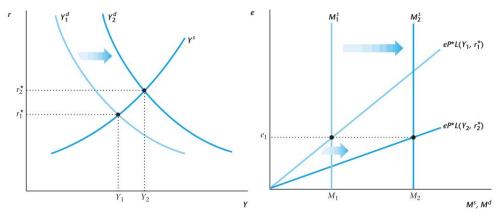


# Monetary SOE with fixed exchange rate

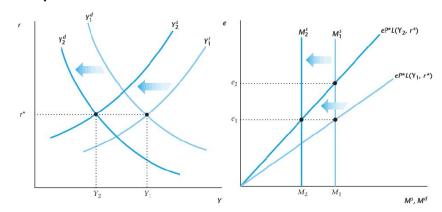
- Setup: Central bank target exchange rate  $\overline{e}$  by adjusting  $M^s \Rightarrow \underline{\text{endogenous}} M^s$ .
- Experiment 1 P\* ↑ (Nominal foreign shock)
  - Domestic price  $P = \overline{e} \times P^* \uparrow$
  - ⇒ Fixed exchange rate does not insulate domestic prices from nominal foreign shocks.



- Experiment 2 *r*\* ↑ (Real foreign shock)



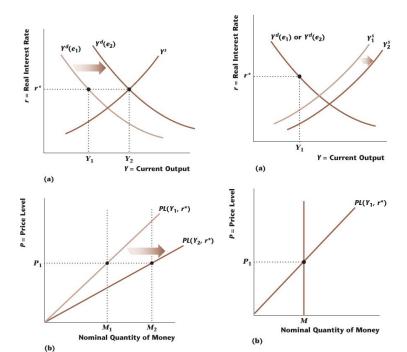
- Experiment 3  $z \downarrow$ 
  - Notice  $C \downarrow$  for a little bit due to wealth effect.
  - $\circ$  NX/CA  $\downarrow$



- Central bank choose to **devalues** currency in response to *z* shocks.
  - $\circ$  Central bank does not change  $M^s$  and reset exchange rate target to  $e_2$ .
  - $\circ$   $P \uparrow$
  - But the shocks to real variables (as <u>primary shock absorber</u>) **cannot** be prevented.

# New Keynesian Sticky Price with Flexible exchange rate

- Output determined by the output demand curve.
- $r^*$  exogenous from international credit market.
- $(P, P^*)$  fixed  $\Rightarrow$  PPP does not hold.
- $M^s \uparrow$ 
  - Oppreciation of money  $e \uparrow$ , since  $(P, P^*)$  does not change, real exchange rate  $\frac{eP^*}{P}$  also depreciate.
  - Real Depreciation  $\Rightarrow EX \uparrow \Rightarrow Y^d(e) \uparrow$
  - Money is **not** neutral



- $G^s \uparrow$  fiscal policy no use.

  - o Increase demand (domestic cash)
  - ⇒ Real Appreciation  $e_1 \downarrow to e_2 \Rightarrow NX \downarrow \Rightarrow Y^d \downarrow$  Government spending crowds out an equal quantity of net exports. Therefore  $Y^d$  is unchanged.