

(a) In this case $x(t)$ must be
an error value this means

$$\text{sign}(w^T(t)x(t)) \neq y(t)$$

sign as an activation function:

if $x \leq 0$ return -1

if $x = 0$ return 0 (No zero in this case)

if $x > 0$ return 1

This means if $y(t) = 1$, ~~$x(t)$~~

$$w^T(t)x(t) < 0$$

$$y(t)w^T(t)x(t) < 0$$

If $y(t) = -1$, ~~$w^T(t)x(t)$~~ $x(t)w^T(t) > 0$

$$y(t)w^T(t)x(t) < 0$$

(b) If the data's linearly separable
There will be no error, this means
if $y(t) = 1$, $w^T(t)x(t) > 0$

$$w^T(t)x(t) * y(t) > 0$$

if $y(t) = -1$, $w^T(t)x(t) < 0$

$$w^T(t)x(t) * y(t) > 0$$

(c) First of all, in terms of $w(t+1)$, it means
it must be based on some error value
that not correct yet.

$$y(t)w^T(t+1)x(t)$$

$$= y(t)(w(t) + y(t)x(t))^T x(t)$$

As for $w(t) + y(t)x(t)$

Because they can do addition, they

$w(t)$ and $y(t)x(t)$ must have same

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~~10~~ columns and rows so can be written

$$w^T(t) + y^T(t) x^T(t)$$

Also see additional information for further explanation!

So we can write

$$\begin{aligned} & y(t) (w^T(t) + y^T(t) x^T(t)) \cdot x(t) \\ &= y(t) x(t) \cdot w^T(t) + y^T(t) y(t) x^T(t) x(t) \end{aligned}$$

→ Based on further information

$$x(t) y(t) = \begin{bmatrix} \text{Updater 0} \\ \text{Updater 1} \\ \text{Updater 2} \end{bmatrix}$$

$$\text{So } x^T(t) y^T(t) = [V_{p0}, V_{p1}, V_{p2}]$$

$$x^T(t) x(t) y^T(t) y(t)$$

$$= \cancel{V_{p0} \cdot V_{p0}} V_{p0}^2 + V_{p1}^2 + V_{p2}^2$$

Updater (whatever)'s square must be a positive number.

$$\text{So } V_{p1}^2 + V_{p2}^2 + V_{p0}^2 > 0, \quad \begin{matrix} x^T(t) y(t) \\ x(t) y^T(t) \end{matrix} > 0$$

$$\text{So } y(t) w^T(t+1) x(t)$$

$$= y(t) x(t) w^T(t) + \text{a positive num}$$

$$> y(t) x(t) w^T(t)$$

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$$= [w_0, w_1, w_2] \times \begin{bmatrix} 1 \\ x_1 \\ x_2 \end{bmatrix}$$

$$= w_0 + w_1 x_1 + w_2 x_2 = 0$$

$$w_2 x_2 = (w_0 + w_1 x_1) \times -1$$

$$x_2 = -\frac{w_1}{w_2} x_1 - \frac{w_0}{w_2}$$

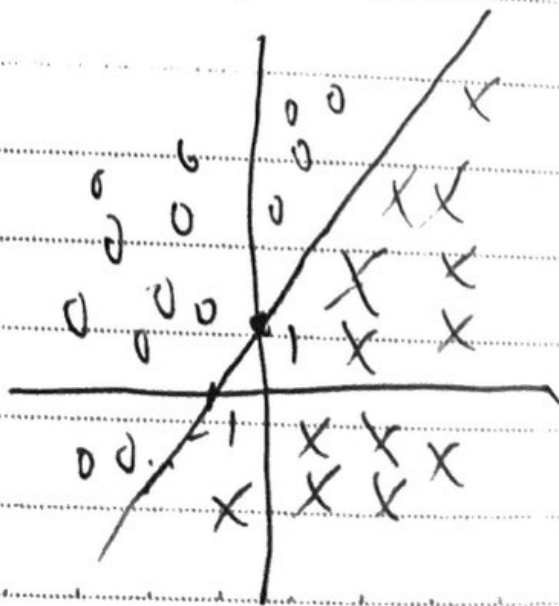
$$m = -\frac{w_1}{w_2}$$

$$c = -\frac{w_0}{w_2}$$

(2)

(a) $w_0 = 1 \quad w_1 = 1 \quad w_2 = -1$

$m = 1 \quad c = 1$



(b)

$$w_0 = -1$$

$$w_1 = -1$$

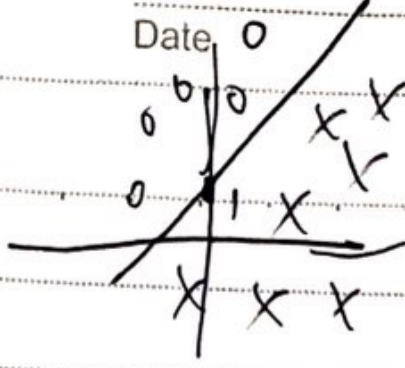
$$w_2 = 1$$

$$M = 1$$

$$C = 1$$

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$$\begin{bmatrix} \text{No.} & X_{11} & X_{12} \\ \text{gate} & X_{21} & X_{22} \\ 1 & X_{31} & X_{32} \\ 1 & X_{41} & X_{42} \\ 1 & \vdots & \vdots \\ 1 & X_{n1} & X_{n2} \end{bmatrix} \begin{bmatrix} w_0 \\ w_1 \\ w_2 \end{bmatrix} = \begin{bmatrix} y_1 \\ y_2 \\ y_3 \\ \vdots \\ y_n \end{bmatrix}$$

$$y(t) x(t) = \begin{bmatrix} y_1 + y_2 + y_3 + y_4 + \dots + y_n \\ x_{11}y_1 + x_{21}y_2 + x_{31}y_3 + \dots + x_{n1}y_n \\ x_{12}y_1 + x_{22}y_2 + x_{32}y_3 + \dots + x_{n2}y_n \end{bmatrix}$$

$$= \begin{bmatrix} \text{Updater 0} \\ \text{Updater 1} \\ \text{Updater 2} \end{bmatrix} \times \text{learning rate}$$

Additional Information

$$W(t+1) = \begin{bmatrix} w_0 + \text{Updater 0} \\ w_1 + \text{Updater 1} \\ w_2 + \text{Updater 2} \end{bmatrix} \xrightarrow{\text{learning rate}} \rightarrow 1A$$

$$W^T(t+1) = [w_0 + v_{p0}, w_1 + v_{p1}, w_2 + v_{p2}]$$

$$= W^T(t) + (y(t) \otimes z(t))^T$$

$$= [w_0, w_1, w_2] + [v_{p0}, v_{p1}, v_{p2}]$$