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Supplementary Information for

- Cooking Beyond Your Front Door: Novel Fusion Recipe Generation
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- 7 This PDF file includes:
- 8 Tables S1 to S2

1. CulinaryDB: A Critical Eye

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CulinaryDB contains 45,772 recipes comprised of 1,033 ingredients from 22 defined regions globally taken from multiple websites. Ignoring controversial region names, such as Britain and Ireland being classified under the outdated label of British Isles, there are downfalls to the data set. Firstly, the data set restricts itself to English speaking sites which leads to a better representation of the USA and western Europe than the rest of the world. Secondly, due to the large list of ingredients that had to be classified there is the occasional wrong or debated classification of an ingredient. A collection of such classifications are lised in Table S1.

Thirdly, in order to simplify the data's complexity, the ingredients in recipes are reduced to be contained in one of the 1,033 ingredients previously mentioned. This allows for easier to run code but has resulted in some unusual decisions. Included in Table S2, we see a sample of unusual choices in regards the labelling of ingredients. Many oils, such as olive oil, are relabelled by what they are made from, like olives. While this reduces the pool of possible ingredients, even the most professional chef would be stumped trying to deep fry doughnuts in a vat of sunflower seeds.

When classifying recipes by region there is no explanation as to how this was done, leading to question whether the region classification can be relied upon fully. Especially with websites such as AllRecipes.co.uk, where anyone can post a recipe.

Table S1. Sample of unexpected ingredient classifications.

File	Row	Ingredient Name	Classification
02_Ingredients	333	Oregano	Spice
02_Ingredients	424	Mexican Oregano	Herb
03_Compound_Ingredients	58	Ranch Dressing	Spice

Table S2. Sample of unexpected ingredient labels contained within 04 Recipe-Ingredients Aliases.csv.

Row	Original Ingredient	Labelled
17138	Olive Oil	Olive
5808	Sesame Oil	Sesame
26726	Taco Seasoning	Taco
56824	Burrito Seasoning	Burrito

2. Project Code

```
#Loading in required modules
                                                               59
                                                                   ingCode = {}
    import pandas as pd
                                                                   ingredients = ing['Entity ID']
24
                                                               60
    import numpy as np
                                                                   for i in range(ingShape[0]):
                                                               61
   import networkx as nx
                                                                       ingCode[ingredients[i]] = i
                                                               62
    from matplotlib import pyplot as plt
                                                                   ingredientsComp = compIng['entity_id']
                                                               63
    import math
                                                                   for i in range(compIngShape[0]):
                                                                       ingCode[ingredientsComp[i]] = ingShape[0] + i
                                                               65
    #Load in CulinaryDB database
    recipeDetails = pd.read_csv(filepath_or_buffer='./Data 67
                                                                   #Quick map from node number to ingredient name
31
        /01_Recipe_Details.csv', sep=',', encoding='latin'68
                                                                   labels = {}
32
                                                                   for j in range(totIng):
33
                                                                       if (j < 930):
    ing = pd.read_csv(filepath_or_buffer='./Data/02
    _Ingredients.csv', sep=',', encoding='latin')
compIng = pd.read_csv(filepath_or_buffer='./Data/03
                                                                           labels[j] = ing['Aliased Ingredient Name'][j]
35
37
         _Compound_Ingredients.csv', sep=',', encoding=
                                                                           labels[j] = compIng['Compound Ingredient Name'
                                                                       ][j-930]
        latin')
38
39
    recipeIng = pd.read_csv(filepath_or_buffer='./Data/04
        _Recipe-Ingredients_Aliases.csv', sep=',',
                                                                   #Create adjacency matrix for each region
40
                                                               76
41
        encoding='latin')
                                                               77
                                                                   adjMx = []
                                                                   for i in range(regions):
42
                                                               78
43
    #Record number of ingredients (compound and simple)
                                                               79
                                                                       adjMx.append(np.zeros([totIng,totIng]))
   ingShape = ing.shape
compIngShape = compIng.shape
44
                                                               80
                                                                   #Store dist of ingredient list length
45
                                                               81
    totIng = ingShape[0] + compIngShape[0]
                                                                   ingDist = []
46
                                                               82
47
                                                                   for i in range(regions):
                                                               83
    #Record Number of Regions
                                                                       ingDist.append([])
48
                                                               84
    regionList = np.unique(recipeDetails['Cuisine'].values.85
49
        tolist())
                                                                   #Record number of recipes and length of ingredient file
50
                                                                   fileLength = recipeIng.shape[0]
    regions = regionList.shape[0]
51
                                                               87
                                                                   recipeCount = recipeDetails.shape[0]
52
                                                               88
    #Quick map from region name to layer of matrix
                                                                   startPoint = 0:
53
                                                               89
    areaCode = {}
54
                                                               90
    for i in range(regions):
                                                                   #Iterate through each recipe
55
                                                               91
        areaCode[regionList[i]] = i
56
                                                               92
                                                                   for i in range(recipeCount):
                                                                       #Find which ingredients are in the recipe
57
                                                               93
   #Quick map from ingredient code to node number
                                                               94
                                                                       ingredientList = []
```

```
ingLength = 0:
95
                                                                  175
         while (recipeIng.iloc[startPoint,0] == i+1):
96
                                                                  176
             #Add ingredient to ingredient list and update 177
97
98
         number of ingredients
99
             ingredientList.append(ingCode[recipeIng.iloc[
100
          startPoint,3]])
             startPoint = startPoint + 1
ingLength = ingLength + 1
101
102
103
             #Stop once we are at a new recipe
             if (startPoint == fileLength):
104
105
                  break
106
         #Check region
107
         region = areaCode[recipeDetails.iloc[i,3]]
108
         \# Add recipe ingredient list length to distribution _{186}
109
110
         ingDist[region].append(ingLength)
111
                                                                  188
112
         #For each ingredient add one to frequency of
                                                                  189
         occurrence together in adj mx
113
                                                                  190
114
         count = len(ingredientList)
115
         for j in range(count):
                                                                  192
              for k in range(count):
116
                                                                  193
117
                  adjMx[region][ingredientList[j]][
                                                                  194
118
          ingredientList[k]] += 1
                                                                  195
                                                                  196
    G = [] #List of graphs
120
                                                                  197
121
                                                                  198
122
    #Create Weights
                                                                  199
    for i in range(regions):
                                                                  200
124
         #Remove all self-loops
                                                                  201
125
         for j in range(totIng):
126
              adjMx[i][j][j] = 0
127
         #Create Weighted graph
                                                                  202
129
         G.append(nx.from_numpy_matrix(adjMx[i]))
130
131
    #Save Properly for MATLAB WSBM code
                                                                  205
    for i in range(len(G)):
132
                                                                  206
         A = nx.adjacency_matrix(G[i])
133
         np.savetxt(".\\adjMx\\adjMx" + str(i) + ".txt", A.<sub>208</sub>
134
         todense(),delimiter= " ")
135
                                                                  209
                                                                  211
```

Listing 1. Constructing network and storing useful information.

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```
function [labels, model] = saveAdjMx(regions, alpha, beta)14
    %Construct adjacency matrix
    number = length(regions);
adjMx = zeros(1033*number);
    for i = 1:number
                                                           219
                                                           220
        for j=1:number
            adjMx((1 + 1033*(i-1)):(1033*(i)),(1 +
                                                           221
     1033*(j-1):(1033*(j))) = beta .* eye(1033);
                                                           223
                                                           224
                                                           225
                                                           226
    %Load in matrix from saved files
    for i = 1:number
                                                           227
        newMx = readmatrix(strcat('..\adiMx\adiMx'.
                                                           228
     string(regions(i)),'.txt'));
                                                           229
        adjMx((1 + 1033*(i-1)):(1033*(i)),(1 + 1033*(i^{230}))
    -1)):(1033*(i))) = newMx;
                                                           231
                                                           232
                                                           233
    %Set non-edges to "NaN"
                                                           234
    adjMx(adjMx == 0) = nan;
                                                           235
    %Subtract one from each edge weight
                                                           236
    adjMx = adjMx - 1;
                                                           237
                                                           238
    %Run WSBM
                                                           239
    [labels,model] = wsbm(adjMx ,10,'W_Distr','Poisson<sup>240</sup>
     ,'alpha',alpha,'numTrials',12,'parallel',1);
                                                           241
                                                           242
                                                           243
    %Save data
                                                           244
    thetaW = reshape(model.Para.tau_w(:,1),10,10);
    thetaE = reshape(model.Para.theta_e,10,10);
    writematrix(thetaW, strcat('..\params\thetaW',
    string(beta),'.txt'))
    writematrix(thetaE, strcat('..\params\thetaE',
    string(beta),'.txt'))
    writematrix(labels, strcat('..\params\z', string(bet248
    ),'.txt'))
```

```
writematrix(regions, strcat('..\params\regions',
string(beta),'.txt'))
```

Listing 2. MATLAB function to construct multilayer network and run WSBM model.

```
#Construct new graph from MATLAB data
totIng = 1033
Gnew = []
#Load in blockstructure data
thetaE = np.loadtxt(".\params\\thetaE10.txt",delimiter
thetaW = np.loadtxt(".\params\\thetaW10.txt", delimiter
z = np.loadtxt(".\params\\z10.txt",dtype = int,
    delimiter = ",")
#Generate each layer
for k in range(int(len(z) / totIng)):
   Gnew.append(nx.Graph())
   Gnew[k].add_nodes_from(range(totIng))
   for i in range(totIng):
       for j in range(i+1,totIng):
           edge = np.random.random_sample()
           if (edge < thetaE[z[i]-1][z[j]-1]):</pre>
               Gnew[k].add_edge(i,j,weight = np.random
    .poisson(thetaW[z[i]-1][z[j]-1]) + 1)
```

Listing 3. Generating new network using block structure information.

```
#Pick layer or "region"
region = 0
#collect nodes by their group
group = [[],[],[],[],[],[],[],[],[],[]]
for i in range(1033):
    group[z[i+1033*region]-1].append(i)
blockStructure = []
#Construct order for nodes based on block structure
for g in group:
    blockStructure = blockStructure + g
#List of all unused nodes
remove = [node for node,degree in dict(G[newRegionList[
    region]].degree()).items() if degree == 0]
#Default order
defaultStructure = list(range(1033))
#Remove unused nodes from both orders
for i in remove:
    blockStructure.remove(i)
    defaultStructure.remove(i)
#Load both adjacency matrices
adjNew = nx.adjacency_matrix(G[newRegionList[region]],
    nodelist=blockStructure, weight='weight')
adjOld = nx.adjacency_matrix(G[newRegionList[region]],
    nodelist=defaultStructure, weight='weight')
#Plot results
fig = plt.figure(figsize=(20,40))
ax1 = fig.add_subplot(121)
ax1.imshow(adjOld.todense(), cmap="copper r")
ax2 = fig.add_subplot(122)
ax2.imshow(adjNew.todense(), cmap="copper_r")
plt.savefig('block' + str(region) + '10.png',
    bbox_inches='tight')
plt.show()
```

Listing 4. Python code to display the adjacency matrix for each layer.

```
#Modified Random Walk Proposed
def modRdmWalkPort(G,region,x0,maxIng,gamma,delta):
    #x is an ingredient list
   x = [x0]
```

```
#storing info on nerby ingredients as well as
                                                          312
weights of edges for each ingredient in list \boldsymbol{x}
                                                          313
ing = [[] for _ in range(len(G))]
weight = [[] for _ in range(len(G))]
total = [[] for _ in range(len(G))]
invWeight = [[] for _ in range(len(G))]
                                                          314
                                                          315
                                                          316
                                                          317
                                                          318
#Adding ingredients to our list
                                                          319
for i in range(maxIng-1):
                                                          320
                                                          321
    #Deciding whether to choose randomly, change
                                                          322
region or just pick an ingredient
                                                          323
    choice = np.random.choice([0,1,2],p=[gamma,
                                                          324
delta, 1-gamma-delta])
                                                          325
                                                          326
    #For the new ingredient added we have to store 327
the information found
    for j in range(len(G)):
         #Getting adjacent ingredient and edge
weight info for region j
         nextIng = []
         nextWeight = []
                                                          328
                                                          329
         for u,v,w in G[j].edges(x[i],data=True):
                                                          330
              nextWeight.append(w['weight'])
                                                          331
              nextIng.append(v)
                                                          332
         #Storing all information
                                                          333
                                                          334
         total[j].append(sum(nextWeight))
                                                          335
         ing[j].append(nextIng)
         weight[j].append(nextWeight)
                                                          336
                                                          337
         \#Storing inverted total weight (making sur e^{38}
 to account for when the weight sums to zero)
                                                          339
         if (total[j][i] < pow(10,-6)):</pre>
                                                          340
              invWeight[j].append(0)
                                                          341
                                                          342
         else:
                                                          343
             invWeight[j].append(1/total[j][i])
                                                          344
    #Updating region (if applicable)
                                                          345
                                                          346
    if choice == 1:
         newRegion = np.random.choice(range(len(G) 347
                                                          348
 -1))
                                                          349
         if newRegion < region:
                                                          350
             region = newRegion
                                                          351
         else:
                                                          352
             region = newRegion +1
                                                          353
                                                          354
    if choice == 0:
         #Choosing random ingredient if applicable 355
         x.append(np.random.choice(G[region].nodes()56
))
                                                          358
    else:
                                                          359
         #Summing all inverted weights
         totInvWeight = sum(invWeight[region])
                                                          360
         if totInvWeight == 0:
                                                          361
                                                          362
             x.append(np.random.choice(G[region].
nodes()))
                                                          364
             \hbox{\tt\#Picking an ingredient from list $x$ with}\\
 probability proportional to inverse of
             #sum of weights on edges leaving it
             prob = [w/totInvWeight for w in
```

Listing 5. Python function to perform the modified random walk proposed in **Recipe Generation Strategy, Materials and Methods**.

```
#Function to run through layer G of the graph for
    recipes of length L for a chosen gamma
def recipeLenDist(G,L,iterNo,gamma):
    lengthDist = []
    for j in range(iterNo):
        x = rdmWalkPort(G,np.random.choice(G.
    number_of_nodes()),L,gamma)
        #if len(set(x)) > 1:
        lengthDist.append(len(set(x)))
    return lengthDist
#Variables to change in order to match histogram to
   preferred region
gamma = 0.1
length = 30
region = 5
#Run function
lengthDist = recipeLenDist(Gnew[region],length,10000,
    gamma)
#Plot results
plt.hist(ingDist[newRegionList[region]],len(set(ingDist
    [newRegionList[region]])), density=True, facecolor
    ='b', alpha=0.5, label='True Distribution')
plt.hist(lengthDist, len(set(lengthDist)), density=True
     , facecolor='r', alpha=0.5,label='Distribution')
plt.xlabel('Recipe Ingredient List Length', fontsize
    =16)
plt.ylabel('Probability', fontsize=16)
plt.title('Historgram showing the Distribution of
    Number of \nUnique Nodes Visited over 10,000 Random Walks\nof length ' + str(length) + ' with $\
    gamma$ =' + str(gamma), fontsize=20)
plt.legend(prop={"size":16})
bbox_inches='tight')
plt.show()
```

Listing 6. Python code to generate recipe ingredient list length distribution for modified random walk

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