Ejercicios Clasificaci?n

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Ejercios Clasificación

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0.1.1 Ejercicio 1

Probar diferentes valores para k y compararlos. Hacer un plot con los resultados.

```
In [2]: # Primero leemos el archivo que contiene el dataset de breast cancer
        wbcd = read.csv("wisc_bc_data.csv",stringsAsFactors = FALSE)
        str(wbcd)
        head(wbcd)
'data.frame':
                    569 obs. of 32 variables:
```

```
$ id
                  : int 87139402 8910251 905520 868871 9012568 906539 925291 87880 862989 8
                         "B" "B" "B" "B" ...
$ diagnosis
                 : chr
$ radius_mean
                         12.3 10.6 11 11.3 15.2 ...
                  : num
$ texture_mean
                 : num
                         12.4 18.9 16.8 13.4 13.2 ...
$ perimeter_mean
                         78.8 69.3 70.9 73 97.7 ...
                 : num
$ area_mean
                  : num
                         464 346 373 385 712 ...
                         0.1028 0.0969 0.1077 0.1164 0.0796 ...
$ smoothness_mean : num
$ compactness_mean : num
                         0.0698 0.1147 0.078 0.1136 0.0693 ...
$ concavity_mean
                         0.0399 0.0639 0.0305 0.0464 0.0339 ...
                  : num
$ points_mean
                         0.037 0.0264 0.0248 0.048 0.0266 ...
                  : num
$ symmetry_mean
                         0.196 0.192 0.171 0.177 0.172 ...
                  : num
$ dimension_mean
                 : num
                         0.0595 0.0649 0.0634 0.0607 0.0554 ...
$ radius_se
                         0.236 0.451 0.197 0.338 0.178 ...
                  : num
                  : num
$ texture_se
                         0.666 1.197 1.387 1.343 0.412 ...
$ perimeter_se
                         1.67 3.43 1.34 1.85 1.34 ...
                  : num
                         17.4 27.1 13.5 26.3 17.7 ...
$ area_se
                  : num
$ smoothness_se
                         0.00805 0.00747 0.00516 0.01127 0.00501 ...
                  : num
                         0.0118 0.03581 0.00936 0.03498 0.01485 ...
$ compactness_se
                 : num
$ concavity_se
                         0.0168 0.0335 0.0106 0.0219 0.0155 ...
                  : num
$ points_se
                  : num
                         0.01241 0.01365 0.00748 0.01965 0.00915 ...
$ symmetry_se
                         0.0192 0.035 0.0172 0.0158 0.0165 ...
                  : num
$ dimension_se
                         0.00225 0.00332 0.0022 0.00344 0.00177 ...
                  : num
$ radius_worst
                         13.5 11.9 12.4 11.9 16.2 ...
                  : num
$ texture_worst
                         15.6 22.9 26.4 15.8 15.7 ...
```

: num

```
$ perimeter_worst : num 87 78.3 79.9 76.5 104.5 ...
$ area_worst : num 549 425 471 434 819 ...
$ smoothness_worst : num 0.139 0.121 0.137 0.137 0.113 ...
$ compactness_worst : num 0.127 0.252 0.148 0.182 0.174 ...
$ concavity_worst : num 0.1242 0.1916 0.1067 0.0867 0.1362 ...
$ points_worst : num 0.0939 0.0793 0.0743 0.0861 0.0818 ...
$ symmetry_worst : num 0.283 0.294 0.3 0.21 0.249 ...
$ dimension_worst : num 0.0677 0.0759 0.0788 0.0678 0.0677 ...
```

id	diagnosis	radius_mean	texture_mean	perimeter_mean	area_mean	smoothness_mean
87139402	В	12.32	12.39	78.85	464.1	0.10280
8910251	В	10.60	18.95	69.28	346.4	0.09688
905520	В	11.04	16.83	70.92	373.2	0.10770
868871	В	11.28	13.39	73.00	384.8	0.11640
9012568	В	15.19	13.21	97.65	711.8	0.07963
906539	В	11.57	19.04	74.20	409.7	0.08546

```
In [3]: # Quitamos el id ya que no nos sirve de nada para predecir.
     wbcd = wbcd[,-1]

# Transformamos los datos de la variable diagnosis a un factor.
```

Benign Malignant 357 212

```
In [6]: library(class)
     wbcd_test_pred <- knn(train = wbcd_train, test = wbcd_test, cl = wbcd_train_labels, k=
     wbcd_test_pred</pre>
```

1. Malignant 2. Benign 3. Malignant 4. Benign 5. Benign 6. Benign 7. Benign 8. Malignant 9. Malignant 10. Benign 11. Malignant 12. Benign 13. Benign 14. Malignant 15. Benign 16. Benign 17. Malignant 18. Malignant 19. Malignant 20. Malignant 21. Benign 22. Benign 23. Benign 24. Malignant 25. Malignant 26. Malignant 27. Malignant 28. Benign 29. Benign 30. Benign 31. Benign 32. Malignant 33. Benign 34. Benign 35. Benign 36. Benign 37. Benign 38. Benign 39. Malignant 40. Malignant 41. Benign 42. Malignant 43. Benign 44. Benign 45. Benign 46. Malignant 47. Malignant 48. Benign 49. Benign 50. Malignant 51. Malignant 52. Malignant 53. Benign 54. Benign 55. Malignant 56. Malignant 57. Benign 58. Benign 59. Malignant 60. Benign 61. Benign 62. Benign 63. Benign 64. Malignant 65. Malignant 66. Benign 67. Benign 68. Malignant 69. Malignant 70. Benign 71. Malignant 72. Malignant 73. Benign 74. Benign 75. Benign 76. Benign 77. Benign 78. Malignant 79. Malignant 80. Benign 81. Malignant 82. Malignant 83. Malignant 84. Benign 85. Benign 86. Malignant 87. Benign 88. Malignant 89. Benign 90. Benign 91. Benign 92. Benign 93. Malignant 94. Benign 95. Malignant 96. Benign 97. Benign 98. Benign 99. Benign 100. Malignant 101. Benign 102. Benign 103. Benign 104. Benign 105. Malignant 106. Malignant 107. Benign 108. Benign 109. Malignant 110. Benign 111. Benign 112. Malignant 113. Benign 114. Malignant

Levels: 1. 'Benign' 2. 'Malignant'

```
In [7]: # Evaluating model performance
        table(wbcd test pred,wbcd test labels)
              wbcd_test_labels
wbcd_test_pred Benign Malignant
    Benign
                   64
    Malignant
                    1
                             46
In [8]: require(caret)
        knnModel <- train(x = wbcd_train, y = wbcd_train_labels, method = "knn")
        class(knnModel)
        knnModel
Loading required package: caret
Loading required package: lattice
Loading required package: ggplot2
  'train'
k-Nearest Neighbors
455 samples
30 predictor
  2 classes: 'Benign', 'Malignant'
No pre-processing
Resampling: Bootstrapped (25 reps)
Summary of sample sizes: 455, 455, 455, 455, 455, 455, ...
Resampling results across tuning parameters:
```

```
5 0.9521769 0.8951747
 7 0.9587139 0.9094152
 9 0.9563613 0.9042244
Accuracy was used to select the optimal model using the largest value.
The final value used for the model was k = 7.
In [9]: knnModel <- train(wbcd_train, wbcd_train_labels, method="knn", metric="Accuracy", tune</pre>
       knnModel
       knnModel$results
k-Nearest Neighbors
455 samples
30 predictor
 2 classes: 'Benign', 'Malignant'
No pre-processing
Resampling: Bootstrapped (25 reps)
Summary of sample sizes: 455, 455, 455, 455, 455, 455, ...
Resampling results across tuning parameters:
    Accuracy
                Kappa
  1 0.9478945 0.8847191
  2 0.9463138 0.8812730
  3 0.9488789 0.8871577
  4 0.9502554 0.8900188
  5 0.9535576 0.8969792
  6 0.9570826 0.9046823
  7 0.9574269 0.9051750
  8 0.9546111 0.8986517
  9 0.9563040 0.9024635
  10 0.9550870 0.8998954
  11 0.9557871 0.9015039
  12 0.9562668 0.9023992
  13 0.9566278 0.9027401
  14 0.9557234 0.9008844
  15 0.9545654 0.8983665
Accuracy was used to select the optimal model using the largest value.
```

k Accuracy

Kappa

The final value used for the model was k = 7.

```
k | Accuracy
                  Kappa
                            AccuracySD
                                         KappaSD
       0.9478945 0.8847191
                            0.01275406
                                         0.03034491
    1
    2
       0.01458878
                                         0.03233081
       0.9488789 0.8871577
    3
                            0.01617309
                                         0.03435837
       0.9502554 0.8900188
                            0.01726663
    4
                                         0.03745958
    5
       0.9535576  0.8969792
                            0.01453045
                                         0.03136439
       0.9570826 0.9046823
                            0.01526867
                                         0.03360832
    7
       0.9574269 0.9051750
                            0.01347818
                                         0.02965065
       0.9546111  0.8986517
                            0.01476031
                                         0.03378720
       0.9563040 0.9024635
                            0.01260454
                                         0.02787252
   10
       0.9550870 0.8998954
                            0.01298011
                                         0.02822099
       0.9557871 0.9015039
                            0.01359157
                                         0.02961247
   11
       0.9562668 0.9023992
                            0.01347443
                                         0.02935660
   13
       0.9566278 0.9027401
                            0.01222972
                                         0.02813461
       0.9557234 0.9008844
   14
                            0.01200884
                                         0.02611681
   0.01153953
                                         0.02477225
In [10]: require(caret)
```

knnModel <- train(x = wbcd[shuffle_ds[1:eightypct],-1], y = wbcd[shuffle_ds[1:eightypct]]</pre> class(knnModel)

knnModel

'train'

k-Nearest Neighbors

```
455 samples
30 predictor
```

2 classes: 'Benign', 'Malignant'

Pre-processing: centered (30), scaled (30)

Resampling: Bootstrapped (25 reps)

Summary of sample sizes: 455, 455, 455, 455, 455, 455, ...

Resampling results across tuning parameters:

```
k Accuracy
             Kappa
```

5 0.9548653 0.9003593

7 0.9563098 0.9035668

0.9589189 0.9090480

Accuracy was used to select the optimal model using the largest value. The final value used for the model was k = 9.

```
In [11]: knnPred <- predict(knnModel, newdata = wbcd[shuffle_ds[(eightypct+1):dim(wbcd_n)[1]],</pre>
         knnPred
```

1. Malignant 2. Benign 3. Malignant 4. Benign 5. Benign 6. Benign 7. Benign 8. Malignant 9. Malignant 10. Benign 11. Malignant 12. Benign 13. Benign 14. Malignant 15. Benign 16. Benign 17. Malignant 18. Malignant 19. Malignant 20. Malignant 21. Benign 22. Benign 23. Benign 24. Malignant 25. Malignant 26. Malignant 27. Malignant 28. Benign 29. Benign 30. Benign 31. Benign 32. Malignant 33. Benign 34. Benign 35. Benign 36. Benign 37. Benign 38. Benign 39. Malignant 40. Malignant 41. Benign 42. Malignant 43. Benign 44. Benign 45. Benign 46. Malignant 47. Malignant 48. Benign 49. Benign 50. Malignant 51. Malignant 52. Malignant 53. Benign 54. Benign 55. Malignant 56. Malignant 57. Benign 58. Benign 59. Malignant 60. Benign 61. Benign 62. Benign 63. Benign 64. Malignant 65. Malignant 66. Benign 67. Benign 68. Malignant 69. Malignant 70. Benign 71. Malignant 72. Malignant 73. Benign 74. Benign 75. Benign 76. Benign 77. Benign 78. Malignant 79. Malignant 80. Benign 81. Malignant 82. Malignant 83. Malignant 84. Benign 85. Malignant 86. Malignant 87. Benign 88. Malignant 89. Benign 90. Benign 91. Benign 92. Benign 93. Malignant 94. Benign 95. Malignant 96. Benign 97. Benign 98. Benign 99. Benign 100. Malignant 101. Benign 102. Benign 103. Benign 104. Benign 105. Malignant 106. Malignant 107. Benign 108. Benign 109. Malignant 110. Benign 111. Benign 112. Malignant 113. Benign 114. Malignant

Levels: 1. 'Benign' 2. 'Malignant'

Accuracy

Kappa

k

```
In [12]: postResample(pred = knnPred, obs = wbcd[shuffle_ds[(eightypct+1):dim(wbcd_n)[1]], 1])
  Accuracy
                      0.973684210526316 Kappa
                                                        0.946175637393768
In [13]: # Ejercicio, probar con diferentes valores de k y
         # dibujar un plot con los resultados.
         # Primero crearemos una lista con los nivesles de k que nos interesan
         # para ello iremos desde 1 hasta 20, quedandonos solamente con los valores
         # impares, ya que con valores impares podría darse empates con knn.
         ks = 1:20
         ks = ks[ks\%2 != 0]
         # Ahora crearemos un modelo que utilice esta lista de puntos y nos devuelva
         # los valores de accuracy para cada k
         knnModel <- train(wbcd_train, wbcd_train_labels, method="knn", metric="Accuracy", tun-
         knnModel
         # Obtenemos los resultados del modelo.
         resultados = knnModel$results[,c("k","Accuracy")]
         resultados
k-Nearest Neighbors
455 samples
30 predictor
  2 classes: 'Benign', 'Malignant'
No pre-processing
Resampling: Bootstrapped (25 reps)
Summary of sample sizes: 455, 455, 455, 455, 455, 455, ...
Resampling results across tuning parameters:
```

```
1 0.9484865 0.8870499
3 0.9517521 0.8937340
5 0.9536736 0.8974576
7 0.9553670 0.9007900
9 0.9544674 0.8986978
11 0.9561944 0.9024569
13 0.9556020 0.9008999
15 0.9529198 0.8944641
17 0.9534857 0.8958782
19 0.9559035 0.9010304
```

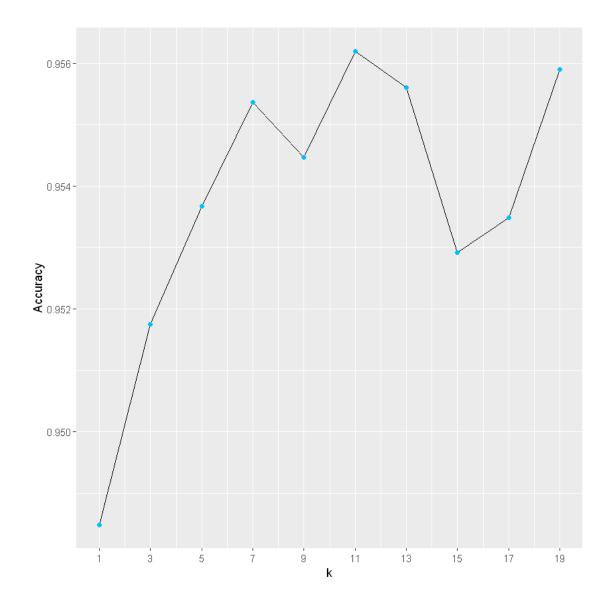
In

Accuracy was used to select the optimal model using the largest value. The final value used for the model was k = 11.

1.	A
k	Accuracy
1	0.9484865
3	0.9517521
5	0.9536736
7	0.9553670
9	0.9544674
11	0.9561944
13	0.9556020
15	0.9529198
17	0.9534857
19	0.9559035
[14]	: library(ggplot2)
	<pre>ggplot(resultados,aes(x=k,y=Accuracy))+geom_line()+</pre>

geom_point(col="deepskyblue")+

scale_x_continuous(breaks=resultados\$k)



Según lo que se puede ver en la gráfica, el mejor valor para k es 5 para este conjunto de datos, ya que obtiene mejores resultados que todos los otros k. Otros valores cercanos como 3,7 o 9 obtienen también resultados buenos (Además son valores usuales para knn). Para valores grandes, se puede ver que los resultados son peores, por ello no se suelen elegir normalmente. (Con otras ejecuciones los resultados de la gráfica pueden ser diferentes)

0.1.2 Ejercicio 2

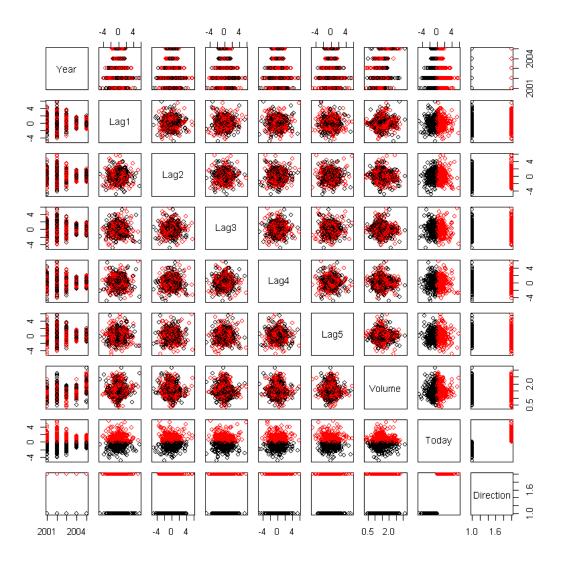
Hacer un 10 fold-cv con una regressión logística

```
In [15]: # Leemos el dataset
    library(ISLR)
    names(Smarket)
    summary(Smarket)
```

1. 'Year' 2. 'Lag1' 3. 'Lag2' 4. 'Lag3' 5. 'Lag4' 6. 'Lag5' 7. 'Volume' 8. 'Today' 9. 'Direction'

Year	Lag1	Lag2	Lag3				
Min. :2001	Min. $:-4.922000$	Min. $:-4.922000$	Min. $:-4.922000$				
1st Qu.:2002	1st Qu.:-0.639500	1st Qu.:-0.639500	1st Qu.:-0.640000				
Median :2003	Median : 0.039000	Median : 0.039000	Median : 0.038500				
Mean :2003	Mean : 0.003834	Mean : 0.003919	Mean : 0.001716				
3rd Qu.:2004	3rd Qu.: 0.596750	3rd Qu.: 0.596750	3rd Qu.: 0.596750				
Max. :2005	Max. : 5.733000	Max. : 5.733000	Max. : 5.733000				
Lag4	Lag5	Volume	Today				
Min. $:-4.922$	000 Min. :-4.922	00 Min. :0.3561	Min. $:-4.922000$				
1st Qu.:-0.640	000 1st Qu.:-0.640	000 1st Qu.:1.2574	1st Qu.:-0.639500				
Median : 0.038	Median : 0.038500						
Mean : 0.001	636 Mean : 0.005	61 Mean :1.4783	Mean : 0.003138				
3rd Qu.: 0.596	750 3rd Qu.: 0.597	00 3rd Qu.:1.6417	3rd Qu.: 0.596750				
Max. : 5.733	000 Max. : 5.733	00 Max. :3.1525	Max. : 5.733000				
Direction							
Down:602							
Up :648							

In [16]: pairs(Smarket, col=Smarket\$Direction)



```
"glm.fit: fitted probabilities numerically 0 or 1 occurred"Warning message:
"glm.fit: fitted probabilities numerically 0 or 1 occurred"Warning message:
"glm.fit: fitted probabilities numerically 0 or 1 occurred"Warning message:
"glm.fit: fitted probabilities numerically 0 or 1 occurred"Warning message:
"glm.fit: fitted probabilities numerically 0 or 1 occurred"
Generalized Linear Model
1250 samples
  8 predictor
  2 classes: 'Down', 'Up'
Pre-processing: centered (8), scaled (8)
Resampling: Cross-Validated (10 fold)
Summary of sample sizes: 1125, 1125, 1124, 1124, 1125, 1125, ...
Resampling results:
 Accuracy
             Kappa
  0.9936062 0.9871929
```

0.1.3 Ejercicio 3

Probar LDA con todas la variables. Comparar con Regresión Logística y LDA. Por último, probar con QDA, comparar los resultados y pintarlos.

```
Shapiro-Wilk normality test
data: Smarket$Lag2
W = 0.97217, p-value = 8.798e-15
Shapiro-Wilk normality test
data: Smarket$Lag3
W = 0.9724, p-value = 1.035e-14
Shapiro-Wilk normality test
data: Smarket$Lag4
W = 0.97242, p-value = 1.049e-14
Shapiro-Wilk normality test
data: Smarket$Lag5
W = 0.97011, p-value = 2.149e-15
In [19]: var(Smarket$Lag1)
         var(Smarket$Lag2)
         var(Smarket$Lag3)
         var(Smarket$Lag4)
         var(Smarket$Lag5)
         # Como se puede ver, las varianzas de las variables son parecidas, menos para
         # el caso de la variable 'Laq5', esto afectará a los resultados del LDA
  1.29117506222642
  1.2911328189265
  1.29664442448359
  1.29680562160128
  1.31687148397502
In [20]: # Ahora aplicamos LDA.
         lda.fit = lda(Direction~Lag1+Lag2+Lag3+Lag4+Lag5, data=Smarket, subset=Year<2005)</pre>
         lda.fit
```

```
Call:
```

```
lda(Direction ~ Lag1 + Lag2 + Lag3 + Lag4 + Lag5, data = Smarket,
    subset = Year < 2005)</pre>
```

Prior probabilities of groups:

Down Up 0.491984 0.508016

Group means:

 Lag1
 Lag2
 Lag3
 Lag4
 Lag5

 Down
 0.04279022
 0.03389409
 -0.009806517
 -0.010598778
 0.0043665988

 Up
 -0.03954635
 -0.03132544
 0.005834320
 0.003110454
 -0.0006508876

Coefficients of linear discriminants:

LD1

Lag1 -0.63046918

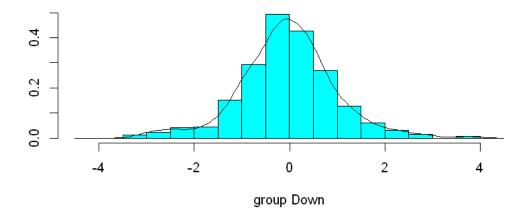
Lag2 -0.50221745

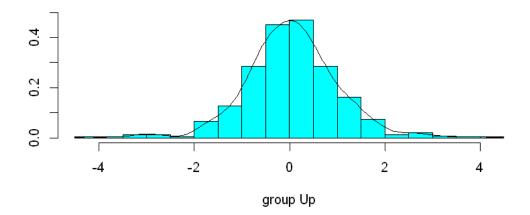
Lag3 0.10142974

Lag4 0.09725317

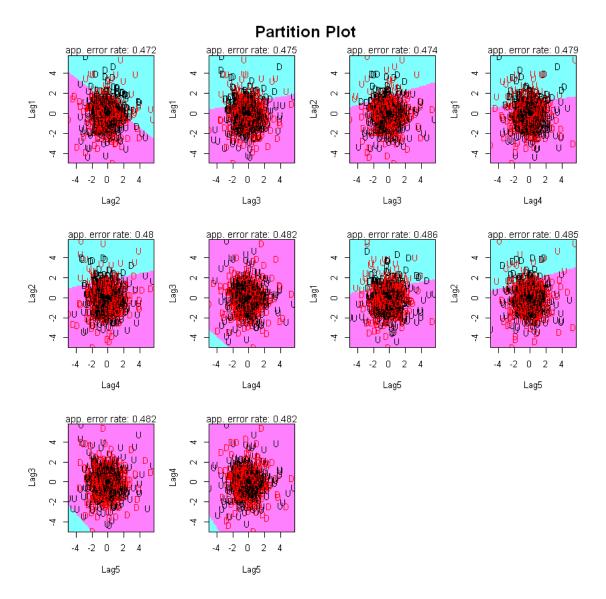
Lag5 -0.03685767

In [21]: plot(lda.fit, type="both", xlab="LD1", ylab="Normalized frecuency")



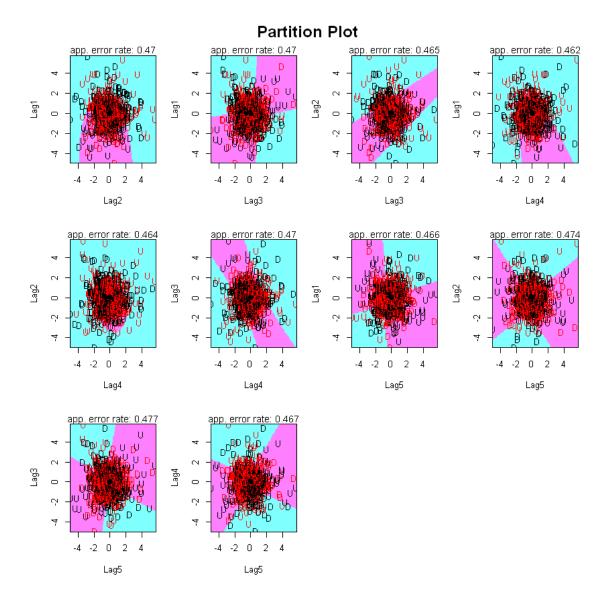


```
print("Tabla de resultados para lda")
         table(lda.pred$class,Smarket.2005$Direction)
         mean(lda.pred$class==Smarket.2005$Direction)
         \# Para estos datos y para las variables elegidas el error es el mismo.
         # Por lo cual ninguno de los dos es buen predictor.
[1] "Tabla de resultados para glm"
       Down Up
 Down
         37 30
 Uр
         74 111
   0.587301587301587
[1] "Tabla de resultados para lda"
       Down Up
 Down
         37 30
 Uр
         74 111
   0.587301587301587
In [23]: library(klaR)
         partimat(Direction~Lag1+Lag2+Lag3+Lag4+Lag5,data=Smarket, method="lda")
```



1.27913706688038

```
1.24717074806801
  1.30204143704291
  1.33905195969342
  1.27785074789389
  1.22092377886303
  1.31893272233984
  1.38060525375758
  1.36348271540061
  1.26880333331491
In [25]: # Ejecutamos el algoritmo de QDA.
         qda.fit = qda(Direction~Lag1+Lag2+Lag3+Lag4+Lag5, data=Smarket,
                      subset=Year<2005)</pre>
         qda.fit
Call:
qda(Direction ~ Lag1 + Lag2 + Lag3 + Lag4 + Lag5, data = Smarket,
    subset = Year < 2005)</pre>
Prior probabilities of groups:
    Down
0.491984 0.508016
Group means:
            Lag1
                        Lag2
                                      Lag3
                                                   Lag4
                                                                  Lag5
Down 0.04279022 0.03389409 -0.009806517 -0.010598778 0.0043665988
Up -0.03954635 -0.03132544 0.005834320 0.003110454 -0.0006508876
In [26]: # Predecimos los datos para qda.
         qda.pred = predict(qda.fit, Smarket.2005)
         table(qda.pred$class, Smarket.2005$Direction)
         mean(qda.pred$class==Smarket.2005$Direction)
         # Como se puede ver, aunque el resultado no sea mucho mejor que para LDA
         # o para Regresión Lineal.
       Down Up
         37
             35
  Down
  Uр
         74 106
  0.567460317460317
In [27]: # Ahora mostrarermos los resultados de cada uno de los modelos.
         partimat(Direction~Lag1+Lag2+Lag3+Lag4+Lag5,data=Smarket, method="qda")
```



0.1.4 Ejercicio 4

Usando la información del dataset 'clasif_train_alumnos.csv' * Comparar lda y qda usando Wilcoxon. * Hacer una comparación múltiple usando Friedman. * Usando Holm, mirar si hay algún algoritmo ganador.

```
appendicitis
                 0.8834602
                                0.8815461
                                              0.8690241
       australian
                 0.7277419
                                0.8605475
                                              0.8072464
         balance
                 0.9072122
                                0.8791122
                                              0.9167999
           bupa
                 0.7405521
                                0.7024224
                                              0.6447628
    contraceptive
                 0.6168944
                                0.5236485
                                              0.5314180
       haberman | 0.7795116
                                0.7519934
                                              0.7567115
'data.frame':
                     20 obs. of 4 variables:
 $ X
                : chr "appendicitis" "australian" "balance" "bupa" ...
 $ out_train_knn: num   0.883  0.728  0.907  0.741  0.617  ...
 $ out train lda: num 0.882 0.861 0.879 0.702 0.524 ...
 $ out_train_qda: num   0.869 0.807 0.917 0.645 0.531 ...
In [29]: # Realizamos el test de wilcoxon.
         QDAvsLDA = wilcox.test(alum$out_train_lda,alum$out_train_qda,
                                 alternative="two.sided", paired=TRUE)
         Rmas = QDAvsLDA$statistic
         pvalue = QDAvsLDA$p.value
         QDAvsLDA = wilcox.test(alum$out_train_qda,alum$out_train_lda,
                                 alternative="two.sided",paired=TRUE)
         Rmenos = QDAvsLDA$statistic
         Rmas
         Rmenos
         pvalue
         # Según el valor del p-value, podemos decir que los algoritmos son diferentes
         # con un 82.31% ((1-pvalue)*100) de confianza.
   V: 68
   V: 142
  0.176853179931641
In [30]: # Realizamos el test de Friedman para todos los dataset.
         test_friedman = friedman.test(as.matrix(alum))
         test_friedman
         # Según el resultado del test de friedman, podemos decir que al menos hay
         # diferencias significativas entre un par de algortimos.
Friedman rank sum test
data: as.matrix(alum)
Friedman chi-squared = 36.78, df = 3, p-value = 5.122e-08
```

out_train_qda

out_train_knn out_train_lda

Según los resultados obtenidos por el test de Holm, no hay diferencias significativ # entre los diferentes algoritmos y por lo tanto no podemos concluir si un algoritmo # es mejor que los demás.

	out_train_knn	out_train_lda	out_train_qda
appendicitis	0.8834602	0.8815461	0.8690241
australian	0.7277419	0.8605475	0.8072464
balance	0.9072122	0.8791122	0.9167999
bupa	0.7405521	0.7024224	0.6447628
contraceptive	0.6168944	0.5236485	0.5314180
haberman	0.7795116	0.7519934	0.7567115

1. 1 2. 1 3. 1 4. 1 5. 1 6. 1 7. 1 8. 1 9. 1 10. 1 11. 1 12. 1 13. 1 14. 1 15. 1 16. 1 17. 1 18. 1 19. 1 20. 1 21. 2 22. 2 23. 2 24. 2 25. 2 26. 2 27. 2 28. 2 29. 2 30. 2 31. 2 32. 2 33. 2 34. 2 35. 2 36. 2 37. 2 38. 2 39. 2 40. 2 41. 3 42. 3 43. 3 44. 3 45. 3 46. 3 47. 3 48. 3 49. 3 50. 3 51. 3 52. 3 53. 3 54. 3 55. 3 56. 3 57. 3 58. 3 59. 3 60. 3

Pairwise comparisons using Wilcoxon signed rank test

data: as.matrix(tablatst) and groups

1 2 2 0.65 -3 0.59 0.53

 ${\tt P}$ value adjustment method: holm