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ii Tieway59

## 1 基础

### 1.1 fastpower.cpp

```
./code/基础/fastpower.cpp
//
// Created by acm-33 on 2019/9/19.
//
template<typename var= long long>
var fpow(var a, var b, var m) {
    var ret = 1;
    while (b) {
        if (b & 1)ret = ret * a % m;
        a = a * a % m;
        b >>= 1;
    return ret;
}
long long fpow(long long a, long long b, long long m) {
    long long ret = 1;
    while (b) {
        if (b & 1)ret = ret * a % m;
        a = a * a % m;
        b >>= 1;
    }
    return ret;
}
```

#### 1.2 prime sieve 素数筛.cpp

```
./code/基础/prime sieve 素数筛.cpp
//单纯求素数, 本地 60ms+
const <u>int</u> MAXN = -1;//10000005
int prime[MAXN], pnum;
bool is_composite[MAXN];
void sieve(const int &n) {
    // 1 is exception
    for (int i = 2; i < n; ++i) {
        if (!is_composite[i]) prime[++pnum] = i;
        for (int j = 1; j <= pnum && i * prime[j] < n; ++j) {</pre>
            is_composite[i * prime[j]] = true;
            if (i % prime[j] == 0) break;
        }
    }
}
//求素数和最小素因子, 本地 90ms+
const int MAXN = -1;//10000005
int prime[MAXN], pnum;
int min_composite[MAXN];
void sieve(const int &n) {
    // 1 is exception
    for (int i = 2; i < n; ++i) {
        if (!min_composite[i]) {
            prime[++pnum] = i;
            min_composite[i] = i;
        for (int j = 1; j \le pnum)
            && prime[j] <= min_composite[i]
            && i * prime[j] < n; ++j) {
            min_composite[i * prime[j]] = prime[j];
```

## 2 字符串

#### 2.1 Aho-Corasick AC 自动机 统计次数 拓扑序优化.cpp

```
./code/字符串/Aho-Corasick AC 自动机 统计次数 拓扑序优化.cpp
#include <bits/stdc++.h>
#define _debug(x) cerr<<#x<<" = "<<x<<endl</pre>
using namespace std;
// Aho-Corasick algorithm, finite-state machine
template < const int NODEsetsize, const int CHARsetsize, const int

→ STRsetsize>

struct Aho_Corasick_FSM {
    int root;
    int cntNd;
    int trie[NODEsetsize][CHARsetsize];
    int fail[NODEsetsize];
    int end[NODEsetsize]; //number of strings ends at node i
    int tag[NODEsetsize]; //times of visit j-th end.
    int ind[NODEsetsize]; //save for topo order
    int strNum;
    int strEnd[STRsetsize]; //the i-th pattern's end node is

    strEnd[i];

    inline int newNd() {
        for (int i = 0; i < CHARsetsize; ++i)</pre>
            trie[cntNd][i] = -1;
```

```
end[cntNd] = 0;
    tag[cntNd] = 0;
    return cntNd++;
}
// hash char to a proper int ID;
inline int hashChar(const char &c) { return c - 'a'; }
// what will be changed when reaching an end node;
inline void endOperation(const int &id) {
    end[id]++;
    strEnd[strNum++] = id;
}
inline void init() {
    cntNd = 0;
    strNum = 0;
    root = newNd();
}
// insert pattern, ensure p[len-1]==0
inline void insert(const char p[]) {
    int cur = root;
    for (int j = 0, i; p[j]; ++j) {
        i = hashChar(p[j]);
        cur = (~trie[cur][i]) ? trie[cur][i] : trie[cur][i] =
newNd();
    endOperation(cur);
}
inline void build() {
    int cur = root;
    fail[root] = root;
    queue<int> que;
    for (int i = 0; i < CHARsetsize; ++i) {</pre>
        if (~trie[cur][i]) {
             fail[trie[cur][i]] = root;
```

```
ind[root]++;
                             //+ topo
            que.push(trie[cur][i]);
        } else {
            trie[cur][i] = root;
        }
    }
    while (!que.empty()) {
        cur = que.front();
        que.pop();
        for (int i = 0; i < CHARsetsize; ++i) {</pre>
            if (~trie[cur][i]) {
                 fail[trie[cur][i]] = trie[fail[cur]][i];
                 ind[trie[fail[cur]][i]]++; //+ topo
                 que.push(trie[cur][i]);
            } else {
                trie[cur][i] = trie[fail[cur]][i];
            }
        }
    }
}
// dictionary-matching target, differs by problem
inline void query(const char t[]) {
    int cur = root;
    for (int j = 0, i, rec; t[j]; ++j) {
        i = hashChar(t[j]);
        cur = trie[cur][i];
        tag[cur]++; //+ topo
    }
    queue<<u>int</u>> topo;
    for (<u>int</u> i = 0; i < cntNd; ++i)
        if (!ind[i])topo.emplace(i);
    while (!topo.empty()) {
        int u = topo.front();
        topo.pop();
```

```
tag[fail[u]] += tag[u];
             if (!--ind[fail[u]])
                 topo.emplace(fail[u]);
        }
        for (<u>int</u> i = 0; i < strNum; ++i) {
             cout << tag[strEnd[i]] << '\n';</pre>
        }
    }
//
      void printAllNode() {
           for (int i = 0; i < cntNd; i++) {</pre>
//
//
               printf("fail[%d] = %02d\nend[%d] = %02d\nchi[%d] = [",
    i, fail[i], i, end[i], i);
//
               for (int j = 0; j < CHARsetsize; j++)
//
                   printf("%d%c", trie[i][j], ", "[j == CHARsetsize -
    1]);
\hookrightarrow
//
               printf("]\n");
//
           }
      }
//
};
typedef long long ll;
const int MOD = 1e9 + 7;
const int INF = 1e9 + 59;
const int MAXP = 2e5 + 59; //Pattern
const int MAXT = 2e6 + 59; //Target
typedef Aho_Corasick_FSM<MAXP, 26, MAXP> ACFSM;
ACFSM ac;
int kase, Kase;
int n, k;
char p[MAXP];
char t[MAXT];
/*
```

```
* https://www.luogu.org/problem/P5357
 * print the times of appearance of all patterns in target.
 */
int main() {
    ios_base::sync_with_stdio(0);
    cin.tie(0);
    cin >> n;
    ac.init();
    for (int i = 1, j; i <= n; i++) {</pre>
        cin >> p;
        ac.insert(p);
    }
    ac.build();
    cin >> t;
    ac.query(t);
    return 0;
}
/*
 а
 aa
 aaa
 aaaa
 aaaaa
 */
```

#### 2.2 Levenshtein-Distance 编辑距离.py

```
./code/字符串/Levenshtein-Distance 编辑距离.py
import math
```

```
# https://www.jianshu.com/p/a617d20162cf
def Levenshtein_Distance(str1, str2):
    11 11 11
    计算字符串 str1 和 str2 的编辑距离
    :param str1
    :param str2
    :return:
    matrix = [[i + j for j in range(len(str2) + 1)] for i in
   range(len(str1) + 1)]
    for i in range(1, len(str1) + 1):
        for j in range(1, len(str2) + 1):
            if (str1[i - 1] == str2[j - 1]):
                d = 0
            else:
                d = 1
            matrix[i][j] = min(matrix[i - 1][j] + 1, matrix[i][j - 1]
 \rightarrow + 1, matrix[i - 1][j - 1] + d)
    return matrix[len(str1)][len(str2)]
# num's bit format.
def bindigits(num, bits):
    s = bin(num & int("1"*bits, 2))[2:]
    return ("{0:0>%s}" % (bits)).format(s)
if __name__ == "__main__":
    for i in range(0,255):
        if(Levenshtein_Distance("1010", bindigits(i, 4))>2):
            print(bindigits(i, 4))
            print(Levenshtein_Distance("10101010", bindigits(i, 4)))
```

#### 2.3 manacher 双数组马拉车.cpp

```
./code/字符串/manacher 双数组马拉车.cpp
/**
   @Source: https://codeforces.com/blog/entry/12143
 *
    @Complexity: O(n)
    @Description: length of largest palindrome centered at each
        character of string and between every consecutive pair
        二维数组分别表示第 i 个位置偶数长度和奇数长度的回文半径(不含中心位置)。
 *
 *
    @Example:
        s = "123321"
        [p[0], p[1]] := \{0, 0, 0, 3, 0, 0\} \{0, 0, 0, 0, 0, 0\}
        s = "12321"
        [p[0], p[1]] := \{0, 0, 0, 0, 0\} \{0, 0, 2, 0, 0\}
    @Verification:
        https://codeforces.com/contest/1326/submission/73742092
 */
void manacher(const string &s, vector<vector<int>> &p) {
    int n = s.size();
    p.assign(2, vector<int>(n, 0));
    for (int z = 0, l = 0, r = 0; z < 2; z++, l = 0, r = 0) {
        for (int i = 0; i < n; i++) {
           if (i < r) p[z][i] = min(r - i + !z, p[z][l + r - i + !z]);</pre>
            int L = i - p[z][i], R = i + p[z][i] - !z;
            while (L - 1 >= 0 \&\& R + 1 < n \&\& s[L - 1] == s[R + 1])
                p[z][i]++, L--, R++;
            if (R > r) l = L, r = R;
        }
    }
}
/**
    @Source: https://cp-algorithms.com/string/manacher.html
    @Complexity: O(n)
    @Description: length of largest palindrome centered at each
        character of string and between every consecutive pair
        两个数组分别表示第 i 个位置偶数长度和奇数长度的回文半径(含中心位置)。
```

```
@Example:
        s = "123321"
        [d1, d2] := \{1, 1, 1, 1, 1, 1\} \{0, 0, 0, 3, 0, 0\}
        s = "12321"
        [d1, d2] := \{1, 1, 3, 1, 1\} \{0, 0, 0, 0, 0\}
    @Verification:
        https://codeforces.com/contest/1326/submission/73715067
 */
void manacher(const string &s, vint &d1, vint &d2) {
    int n = s.size();
    d1.assign(n, 0);
    for (int i = 0, l = 0, r = -1; i < n; i++) {
        \underline{int} k = (i > r) ? 1 : min(d1[l + r - i], r - i + 1);
        while (0 \le i - k \& i + k \le n \& s[i - k] == s[i + k]) {
             k++;
        }
        d1[i] = k--;
        if (i + k > r) {
            l = i - k;
             r = i + k;
        }
    }
    d2.assign(n, 0);
    for (int i = 0, l = 0, r = -1; i < n; i++) {
        \underline{int} k = (i > r) ? 0 : min(d2[l + r - i + 1], r - i + 1);
       while (0 \le i - k - 1 \& k i + k \le n \& k s[i - k - 1] == s[i + k]) {
             k++;
        }
        d2[i] = k--;
        if (i + k > r) {
             l = i - k - 1;
             r = i + k;
        }
    }
}
```

#### 2.4 Aho-Corasick AC 自动机 多模式匹配.cpp

```
./code/字符串/Aho-Corasick AC 自动机 多模式匹配.cpp
#include <bits/stdc++.h>
using namespace std;
typedef long long ll;
const ll \mod = 1e9 + 7;
const int MAXN = 500000 + 59;
const int inf = 1e9 + 5;
// Aho-Corasick algorithm, finite-state machine
template < const int NODEsetsize, const int CHARsetsize >
struct Aho_Corasick_FSM {
    int trie[NODEsetsize][CHARsetsize], cntNd;
    int fail[NODEsetsize];
    int end[NODEsetsize];
    int root;
    inline int newNd() {
        for (int i = 0; i < CHARsetsize; ++i) trie[cntNd][i] = -1;</pre>
        end[cntNd] = 0;
        return cntNd++;
    }
    // hash char to a proper int ID;
    inline int hashChar(const char &c) { return c - 'a'; }
    // what will be changed when reaching an end node;
    inline void endOperation(const int &id) { end[id]++; }
    inline void init() {
        cntNd = 0;
        root = newNd();
    }
```

```
// insert pattern, ensure p[len-1]==0
inline void insert(const char p[]) {
    int cur = root;
    for (int j = 0, i; p[j]; ++j) {
        i = hashChar(p[j]);
        cur = (~trie[cur][i]) ? trie[cur][i] : trie[cur][i] =
newNd();
                       if (trie[cur][i] == -1) trie[cur][i] =
        //
         → newNd();
        //
                       cur = trie[cur][i];
    }
    endOperation(cur);
}
inline void build() {
    int cur = root;
    fail[root] = root;
    queue<int> que;
    for (int i = 0; i < CHARsetsize; ++i) {</pre>
        if (~trie[cur][i]) {
            fail[trie[cur][i]] = root;
            que.push(trie[cur][i]);
        } else {
            trie[cur][i] = root;
        }
    }
    while (!que.empty()) {
        cur = que.front();
        que.pop();
        for (int i = 0; i < CHARsetsize; ++i) {</pre>
            if (~trie[cur][i]) {
                 fail[trie[cur][i]] = trie[fail[cur]][i];
                 que.push(trie[cur][i]);
            } else {
                 trie[cur][i] = trie[fail[cur]][i];
            }
        }
```

```
}
    }
    // dictionary-matching target, differs by problem
    inline int query(const char t[]) {
        int cur = root;
        int res = 0;
        for (<u>int</u> j = 0, i, rec; t[j]; ++j) {
            i = hashChar(t[j]);
            rec = cur = trie[cur][i];
            // enhance recursion efficiency
            while (rec != root && ~end[rec]) {
                res += end[rec];
                end[rec] = -1;
                rec = fail[rec];
            }
        }
        return res;
    }
    //
         void debugAc() {
              for (int i = 0; i < cntNd; i++) {
    //
                   printf("fail[%d] = %02d\nend[%d] = %02d\nchi[%d] =
    //
       [", i, fail[i], i, end[i], i);
                   for (int j = 0; j < CHARsetsize; j++)
    //
                      printf("%d%c", trie[i][j], ", "[j == CHARsetsize
    //
        - 1]);
                  printf("]\n");
    //
    //
              }
    //
          }
};
typedef Aho_Corasick_FSM<MAXN, 26> ACFSM;
ACFSM ac;
int kase, Kase;
```

```
int n, k;
char s[1000059];
//test multi-input https://loj.ac/problem/10057
//test single-input https://www.luogu.org/problem/P3808
/*
 * just judge the existence of some patterns.
 */
int main() {
    ios_base::sync_with_stdio(0);
    cin.tie(0);
    cin >> Kase;
    while (Kase--) {
        cin >> n;
        ac.init();
        for (int i = 1; i <= n; i++) {</pre>
            cin >> s;
             ac.insert(s);
        }
        ac.build();
        cin >> s;
        cout << ac.query(s) << '\n';</pre>
    }
    return 0;
}
```

#### 2.5 manacher 单数组马拉车.cpp

./code/字符串/manacher 单数组马拉车.cpp
/\*\*

\* @Source: https://codeforces.com/contest/1326/submission/73675730

\* @Author: tourist

\* @Complexity: O(n)

\* @Description:

\* 得到经过填充长 2n-1 的回文半径数组,填充模式为: a\$b\$c

```
+ 由于串实际没有被修改,常数喜人
        + 同时适配 char* 与 string, 各取所爱
        + 你不满意可以改成全局变量数组,简简单单
        + 此处回文半径不含中心
    @Example:
 *
        char s[] = "123321";
        vint p = manacher(6, s);
        // [p] := {0, 0, 0, 0, 0, 3, 0, 0, 0, 0}
        string s[] = "12321";
        vint p = manacher(s);
        // [p] := {0, 0, 0, 0, 2, 0, 0, 0}
   @Verification:
 *
        https://codeforces.com/contest/1326/submission/73675730
 */
template<typename T>
vector<int> manacher(int n, const T &s) {
    if (n == 0) {
        return vector<int>();
    }
    vector\langle int \rangle res(2 * n - 1, 0);
    int l = -1, r = -1;
    for (int z = 0; z < 2 * n - 1; z++) {
        int i = (z + 1) >> 1;
        \underline{int} \ j = z \gg 1;
        <u>int</u> p = (i \ge r ? 0 : min(r - i, res[2 * (l + r) - z]));
        while (j + p + 1 < n \&\& i - p - 1 >= 0) {
            if (!(s[j + p + 1] == s[i - p - 1])) {
                break;
            }
            p++;
        }
        if (j + p > r) {
            l = i - p;
            r = j + p;
        }
```

```
res[z] = p;
}
return res;
}

template<typename T>
vector<int> manacher(const T &s) {
    return manacher((int) s.size(), s);
}
```

## 3 图论

#### 3.1 tarjanSCC.cpp

```
./code/图论/tarjanSCC.cpp
//http://poj.org/status?problem_id=&user_id=tieway59&result=&language=
#define myDebug(x) cerr<<#x<<" "<<x<<endl</pre>
#include <string.h>
#include <algorithm>
#include <iostream>
using namespace std;
const int INF = 0x3f3f3f3f;
const int MAXN = 1e3 + 7;
struct Edge {
    <u>int</u> u, v, nx; // ,w
} e[MAXN << 2];</pre>
int head[MAXN], cntEd;
inline void addEdge(int u, int v) {
    e[cntEd] = \{u, v, head[u]\};
    head[u] = cntEd++;
}
//----tarjan
int dfn[MAXN], low[MAXN], scc[MAXN], stk[MAXN], index = 0, sccnum = 0,
 \rightarrow top = 0;
```

```
void tarjan(int root) {
    if (dfn[root]) return;
    dfn[root] = low[root] = ++index;
    stk[++top] = root;
    for (int i = head[root]; ~i; i = e[i].nx) {
        \underline{int} v = e[i].v;
        if (!dfn[v]) {
                        //如果 v 结点未访问过
            tarjan(v);
            low[root] = min(low[root], low[v]);
        } else if (!scc[v]) { //如果还在栈内
            low[root] = min(low[root], dfn[v]);
        }
    }
    if (low[root] == dfn[root]) { //后代不能找到更浅的点
        sccnum++;
        for (;;) {
            \underline{int} x = stk[top--];
            scc[x] = sccnum;
            if (x == root) break;
        }
    }
}
//----
int ind[MAXN], oud[MAXN];
int main() {
    memset(head, -1, sizeof head);
    ios::sync_with_stdio(0);
    cin.tie(0);
    int n;
    cin >> n;
    for (int v, i = 1; i \le n; i++) {
        while (cin >> v && v) {
```

```
addEdge(i, v);
        }
    }
    for (<u>int</u> i = 1; i <= n; i++)
        if (!dfn[i]) tarjan(i);
    int ans1 = 0;
    int ans2 = 0;
    for (int u, v, i = 0; i < cntEd; i++) {</pre>
        u = scc[e[i].u];
        v = scc[e[i].v];
        if (u != v) {
             ind[v]++;
             oud[u]++;
        }
    for (int i = 1; i <= sccnum; i++) {</pre>
        if (ind[i] == 0) {
             ans1++;
        }
        if (oud[i] == 0) {
             ans2++;
        }
    }
    ans2 = max(ans2, ans1);
    if (sccnum == 1)ans1 = 1, ans2 = 0;
    cout << ans1 << endl << ans2 << endl;</pre>
    return 0;
}
```

### 3.2 AstarKSPA星K短路nklogn.cpp

./code/图论/AstarKSP A 星 K 短路 nklogn.cpp

```
/**
    @Source: myself
 *
    @Author: Tieway59
    @Complexity: O(nklogn)
    @Description:
        g.addEdge(u, v, w);
        build graph & inverse_graph
        g.AstarKSP(inv_g, s, t, kth, ...);
        return k-th shortest path length or -1
        ! KSP might not be strictly longer than (k-1)SP
        ! it's MLE/TLE for large K
        ! be aware of int overflow
        ! the "cut" is one example for passing skip function.
        ! I know this code is too long,
          it'll be easier if wrote into single functions.
          Since you need two graphs, this graph class works out fine.
    @Example:
 *
    @Verification:
        https://nanti.jisuanke.com/t/A1992 (input k)
        http://acm.hdu.edu.cn/showproblem.php?pid=6181 (k = 2)
 */
using node_t = int;
using cost_t = long long;
using pqnd_t = pair<cost_t, node_t>;
class Graph {
public:
    int nsize = 0;
    int esize = 0;
    struct Edge {
        node_t v;
        cost_t w;
```

```
int nx;
    };
    vector<int> head;
    vector<Edge> edge;
    Graph() {}
    Graph(int n, int m) : nsize(n), esize(m) {
        head.assign(n, −1);
        edge.reserve(m);
    }
    // number from 0
    inline void addEdge(node_t u, node_t v, cost_t w) {
        edge.emplace_back((Edge) {v, w, head[u]});
        head[u] = edge.size() - 1;
    }
    static void dijkstra(const Graph &g, const node_t &s, vector<cost_t>
     cost_t AstarKSP(const Graph &inv_g, node_t s, node_t t, int k,

¬ function<const bool(cost_t)> cut);

};
void Graph::dijkstra(const Graph &g, const node_t &s, vector<cost_t> &d) {
    d.assign(g.nsize, INF);
    d[s] = 0;
//
      using pqnd_t = pair<cost_t, node_t>;
    priority_queue<pqnd_t, vector<pqnd_t>, greater<pqnd_t> > q;
    q.emplace(d[s], s);
    node_t u, v;
    cost_t w, du;
    while (!q.empty()) {
        du = q.top().first;
```

```
u = q.top().second;
        q.pop();
        if (du > d[u])continue;
        for (<u>int</u> i = g.head[u]; i != -1; i = g.edge[i].nx) {
             v = g.edge[i].v;
             w = g.edge[i].w;
             if (du + w < d[v]) {
                 d[v] = du + w;
                 q.emplace(d[v], v);
             }
        }
    }
}
//O(nklogn) : beware of n-circle.
cost_t Graph::AstarKSP(const Graph &inv_g, node_t s, node_t t, int k,
                         function<const bool(cost_t)> cut) {
    vector<cost_t> dis_t;
    vector<int> vis(nsize, 0);
    Graph::dijkstra(inv_g, t, dis_t);
    // if(s==t) k++; when the node are not defined as a path.
    if (dis_t[s] == llINF)return -1;
    auto Astar = [\&] (pqnd_t x, pqnd_t y) -> \underline{bool} {
        return x.first + dis_t[x.second] >
                y.first + dis_t[y.second];
    };
    // BFS-similar :
    node_t u = s;
    cost_t dis_s;
    priority_queue<pqnd_t, vector<pqnd_t>, decltype(Astar)> q(Astar);
    vis[u] = 1;
    q.emplace(0, u);
    while (!q.empty()) {
        dis_s = q.top().first;
        u = q.top().second;
        q.pop();
```

```
if (u == t && vis[u] == k)return dis_s;
        for (int i = head[u]; i != -1; i = edge[i].nx) {
             node_t v = edge[i].v;
             cost_t w = edge[i].w;
             if (cut(dis_s + w))continue;
             if (cut(dis_s + w + dis_t[v]))continue;
             // below is a risky-but-worth skip, take care :
             // if k == 2, skip vis > k
             // else skip vis >= k
             // (proved practically not theoretically. )
             if (vis[v] >= max(3, k))continue;
             else vis[v]++;
             q.emplace(dis_s + w, v);
        }
    }
    return -1;
}
<u>void</u> solve(<u>int</u> kaseId = -1) {
    int n, m;
    node_t s, t, kth;
    cost_t limit = 0;
    const auto cut = [&](cost_t cost) -> bool {
        return cost > limit;
    };
    while (cin >> n >> m) {
        cin >> s >> t >> kth >> limit;
        s--, t--;
        Graph g(n, m);
        Graph inv_g(n, m);
```

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```
for (ll i = 1, u, v, w; i <= m; ++i) {
        cin >> u >> v >> w;
        u--, v--;
        g.addEdge(u, v, w);
        inv_g.addEdge(v, u, w);
}

cost_t res = g.AstarKSP(inv_g, s, t, kth, cut);
if (res == -1 || cut(res))
        cout << "Whitesnake!" << endl;
else
        cout << "yareyaredawa" << endl;
}
</pre>
```

#### 3.3 Graph.cpp

```
./code/图论/Graph.cpp
const int MAXG = -1;
struct Edge
{
    int from, to, cost, nxt;
};
struct Graph
{
    struct Edge E[MAXG];
    int cntE, head[MAXN];
    void init() { _Neg1(head); cntE = 0; }
    void addE(int a, int warrior, int c = 0) { E[cntE] = {
     → a,warrior,c,head[a] }; head[a] = cntE++; }
};
struct Dijkstra : Graph//下面定一个变量就能用
{
    ll dist[MAXG];
    struct DNode
    {
```

```
ll val;int id;
        bool operator< (const DNode &r)const
            return val > r.val;
        }
    };
    void Init() { _Inf(dist); }
    void Get_Dist(int s)//重新计算从 s 开始的单源最短路
    {
        Init();
        priority_queue<DNode>pq;
        pq.push({ 0,s });
        dist[s] = 0;
        while (!pq.empty())
        {
            DNode tmp = pq.top(); pq.pop();
            if (tmp.val > dist[tmp.id])continue;
            for (int i = head[tmp.id]; i != -1; i = E[i].nxt)
            {
                if (dist[E[i].to] > dist[tmp.id] + E[i].cost)
                {
                    dist[E[i].to] = dist[tmp.id] + E[i].cost;
                    pq.push({ dist[E[i].to],E[i].to });
                }
            }
        }
    }
    int Get_Dist(int s, int t)//获取 s 到 t 的最短路
        if(dist[t] == INF&&dist[s]!=0)Get_Dist(s);
        return dist[t];
    }
}Dij;
struct Dinic :Graph
{
    int curE[MAXG], s, t, dist[MAXG];
    ll dfs(int u, ll f)//不用管, 不要调用
    {
```

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```
if (u == t)return f;
    int ans = 0;
    for (int &i = curE[u]; i != -1; i = E[i].nxt)
    {
        if (dist[E[i].to] == dist[u] + 1 && E[i].cost > 0)
        {
             ll tmp = dfs(E[i].to, min(f, (ll)E[i].cost));
             f -= tmp;
             E[i].cost -= tmp;
             ans += tmp;
             E[i ^ 1].cost += tmp;
             if (!f)break;
        }
    }
    if (!ans)dist[u] = -1;
    return ans;
}
bool bfs()//同上
{
    _Neg1(dist);
    queue<int> q; q.push(s);
    dist[s] = 0;
    while (!q.empty())
    {
        int u = q.front(); q.pop();
        for (int i = head[u]; i != -1; i = E[i].nxt)
        {
             if (dist[E[i].to] == -1 && E[i].cost > 0)
             {
                 dist[E[i].to] = dist[u] + 1;
                 q.push(E[i].to);
             }
        }
    return dist[t] != -1;
}
ll dinic(\underline{int} x, \underline{int} y, \underline{int} num)//返回从 x 到 y 的最大流 要给出有 n 个点
{
```

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#### 3.4 Dinic by ztc.cpp

```
./code/图论/Dinic by ztc.cpp
#include<stdio.h>
#include<algorithm>
#include<string.h>
#include<set>
#include<gueue>
#include<map>
#include<ctype.h>
#include<math.h>
#include<time.h>
#include<stdlib.h>
#include<unordered_map>
#include<list>
#include<complex>
#include<unordered_set>
#include<stack>
#include<string>
#include<iostream>
#define _Inf(a) memset(a,0x3f,sizeof(a))
#define _Neg1(a) memset(a,-1,sizeof(a))
#define _{\mathbf{Rep}(i,a,b)} for (\underline{int}(i)=a;(i)<=(b);(i)++)
using namespace std;
typedef long long ll;
```

```
const int INF = 0x3f3f3f3f;
typedef double db;
typedef complex<db> cp;
typedef pair<int, int> pii;
typedef pair<ll, ll> pll;
typedef pair<db, db> pdd;
const int MOD = 998244353;
const db EPS = 1e-8;
const db PI = acos(-1);
int sign(db x) { return x<-EPS ? -1 : x>EPS; }
int dbcmp(db l, db r) { return sign(l - r); }
ll gcd(ll a, ll b) { return b ? gcd(b, a%b) : a; }
const int MAXN = 1e5 + 54;
const int MAXG = 1e5 + 50;
struct Edge
{
    int from, to, cost, nxt;
};
struct Graph
{
    struct Edge E[MAXG];
    int cntE, head[MAXN];
    void init() { _Neg1(head); cntE = 0; }
    void addE(int a, int b, int c = 0) { E[cntE] = { a,b,c,head[a] };
     → head[a] = cntE++; }
};
struct Dijkstra : Graph//下面定一个变量就能用
{
    ll dist[MAXG];
    struct DNode
    {
        ll val;int id;
        bool operator< (const DNode &r)const</pre>
        {
            return val > r.val;
        }
```

```
};
    void Init() { _Inf(dist); }
    void Get_Dist(int s)//重新计算从 s 开始的单源最短路
    {
        Init();
        priority_queue<DNode>pq;
        pq.push({ 0,s });
        dist[s] = 0;
        while (!pq.empty())
         {
             DNode tmp = pq.top(); pq.pop();
             if (tmp.val > dist[tmp.id])continue;
             for (int i = head[tmp.id]; i != -1; i = E[i].nxt)
             {
                 if (dist[E[i].to] > dist[tmp.id] + E[i].cost)
                 {
                      dist[E[i].to] = dist[tmp.id] + E[i].cost;
                      pq.push({ dist[E[i].to],E[i].to });
                 }
             }
        }
    }
    \underline{int} Get_Dist(\underline{int} s, \underline{int} t)//获取 s 到 t 的最短路
    {
         if(dist[t] == INF&&dist[s]!=0)Get_Dist(s);
         return dist[t];
    }
}Dij;
struct Dinic :Graph
{
    int curE[MAXG], s, t, dist[MAXG];
    ll dfs(<u>int</u> u, ll f)//不用管, 不要调用
         if (u == t)return f;
        int ans = 0;
```

```
for (int &i = curE[u]; i != -1; i = E[i].nxt)
        if (dist[E[i].to] == dist[u] + 1 && E[i].cost > 0)
        {
             ll tmp = dfs(E[i].to, min(f, (ll)E[i].cost));
             f -= tmp;
             E[i].cost -= tmp;
             ans += tmp;
             E[i ^ 1].cost += tmp;
             if (!f)break;
        }
    if (!ans)dist[u] = -1;
    return ans;
}
bool bfs()//同上
    _Neg1(dist);
    queue<int> q; q.push(s);
    dist[s] = 0;
    while (!q.empty())
    {
        int u = q.front(); q.pop();
        for (int i = head[u]; i != -1; i = E[i].nxt)
        {
             if (dist[E[i].to] == -1 && E[i].cost > 0)
             {
                 dist[E[i].to] = dist[u] + 1;
                 q.push(E[i].to);
             }
        }
    }
    return dist[t] != -1;
}
ll dinic(\underline{int} x, \underline{int} y, \underline{int} n)//返回从 x 到 y 的最大流 要给出有 n 个点
{
```

```
s = x; t = y;
        int ans = 0;
        while (bfs())
         {
             for (int i = 1; i <= n; i++)curE[i] = head[i];</pre>
             ans += dfs(s, INF);
        }
         return ans;
    }
}Din;
int main()
{
    int T;
    scanf("%d", &T);
    while (T--)
    {
        Dij.init();Din.init();
        int n, m;
        scanf("%d%d", &n, &m);
         _Rep(i, 1, m)
         {
             <u>int</u> a, b, c;
             scanf("%d%d%d", &a, &b, &c);
             Dij.addE(a, b, c);
        Dij.Get_Dist(1);
         for (int i = 0; i < Dij.cntE; i++)</pre>
             Edge &ed = Dij.E[i];
             if (Dij.dist[ed.from] + ed.cost == Dij.dist[ed.to])
             {
                 Din.addE(ed.from, ed.to, ed.cost);
                 Din.addE(ed.to, ed.from, 0);
             }
        printf("%lld\n",Din.dinic(1,n,n));
    }
```

```
}
/*
9 28
6 4 411
1 5 690
9 3 304
5 1 206
3 9 144
2 1 799
2 9 832
3 9 857
6 7 897
3 4 313
8 9 470
6 4 751
1 4 599
5 1 139
3 4 811
7 2 433
2 3 171
9 7 380
7 7 497
2 6 400
6 8 959
7 7 82
5 1 333
5 9 850
3 6 780
8 5 111
9 9 159
4 4 896
*/
```

### 3.5 linklist.cpp

./code/图论/linklist.cpp

```
//
// Created by acm-33 on 2019/7/23.
//
#define myDebug(x) cerr<<#x<<" "<<x<<endl</pre>
#include <string.h>
#include <algorithm>
#include <iostream>
using namespace std;
const int INF = 0x3f3f3f3f;
const int MAXN = 1e3 + 7;
struct Edge {
    <u>int</u> u, v, nx; // ,w
} e[MAXN << 2];</pre>
int head[MAXN], cntEd;
inline void addEdge(int u, int v) {
    e[cntEd] = \{u, v, head[u]\};
    head[u] = cntEd++;
}
```

# 3.6 dijkstra with pairs.cpp

```
./code/图论/dijkstra with pairs.cpp

using cost_t = long long; //beware of integer overflow
using node_t = int;
using edge_t = pair<node_t, cost_t>;
using pqnd_t = pair<cost_t, node_t>;

vector <vector<edge_t>> adj;
```

```
void dijkstra(int s, vector <cost_t> &d) {
    int n = adj.size();
    d.assign(n, INF); // distance
    d[s] = 0;
    priority_queue <pqnd_t, vector<pqnd_t>, greater<pqnd_t>> q;
    q.emplace(0, s);
    node_t u, v;
    cost_t dis, len;
    while (!q.empty()) {
        dis = q.top().first;
        u = q.top().second;
        q.pop();
        if (dis > d[u]) // i.e. !=
            continue;
        for (auto edge : adj[u]) {
            v = edge.first;
            len = edge.second;
            if (d[u] + len < d[v]) {
                 d[v] = d[u] + len;
                 q.emplace(d[v], v);
            }
        }
    }
}
// get path:
using cost_t = long long;
                        //beware of integer overflow
using node_t = int;
using edge_t = pair<node_t, cost_t>;
using pqnd_t = pair<cost_t, node_t>;
vector <vector<edge_t>> adj;
vector <cost_t> tag;
```

```
void dijkstra(int s, vector <cost_t> &d, vector <node_t> &p) {
    int n = adj.size();
    d.assign(n, INF); // distance
    p.assign(n, -1); // path-pre
    d[s] = 0;
    priority_queue <pqnd_t, vector<pqnd_t>, greater<pqnd_t>> q;
    q.emplace(0, s);
    node_t u, v;
    cost_t dis, len;
    while (!q.empty()) {
        dis = q.top().first;
        u = q.top().second;
        q.pop();
        if (dis > d[u]) // i.e. !=
            continue;
        for (auto edge : adj[u]) {
            v = edge.first;
            len = edge.second;
            if (d[u] + len + tag[v] < d[v]) {
                d[v] = d[u] + len + tag[v];
                p[v] = u; //*
                q.emplace(d[v], v);
            }
        }
    }
}
```

# 4 杂项

```
4.1 Misc 杂技 - 随机数.cpp
```

```
./code/杂项/Misc 杂技 - 随机数.cpp
mt19937 rng(chrono::steady_clock::now().time_since_epoch().count());
inline int suiJi(const int &l, const int &r) {
return uniform_int_distribution<int>(l, r)(rng);
}
4.2 timetest.cpp
./code/杂项/timetest.cpp
#include <bits/stdc++.h>
using namespace std;
int main() {
    clock_t begin = clock();
    \underline{int} x = 0;
    for (int i = 1; i <= 800000000; ++i) {</pre>
        x++;
    printf("%.3f ms\n", (double) (clock() - begin));
```

```
return 0;
}
```

### 4.3 fast IO int.cpp

```
./code/杂项/fast IO int.cpp
inline void read(int &x) {
    char ch;
    bool flag = false;
    for (ch = getchar(); !isdigit(ch); ch = getchar())if (ch == '-')

  flag = true;

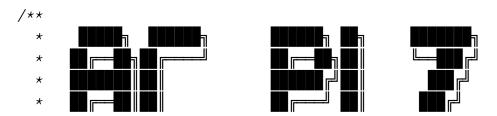
    for (x = 0; isdigit(ch); x = x * 10 + ch - '0', ch = getchar());
    x = flag ? -x : x;
}
inline void write(int x) {
    static const <u>int</u> maxlen = 100;
    static char s[maxlen];
    if (x < 0) {
        putchar('-');
        x = -x;
    }
    if (!x) {
        putchar('0');
        return;
    }
    int len = 0;
    for (; x; x /= 10) s[len++] = x % 10 + '0';
    for (int i = len - 1; i >= 0; --i) putchar(s[i]);
}
namespace Fast_IO { //orz laofu
    const int MAXL((1 << 18) + 1);
    int iof, iotp;
```

```
char ioif[MAXL], *ioiS, *ioiT, ioof[MAXL], *iooS = ioof, *iooT =
 → ioof + MAXL - 1, ioc, iost[55];
char Getchar() {
    if (ioiS == ioiT) {
        ioiS = ioif;
        ioiT = ioiS + fread(ioif, 1, MAXL, stdin);
        return (ioiS == ioiT ? EOF : *ioiS++);
    } else return (*ioiS++);
}
void Write() {
    fwrite(ioof, 1, iooS - ioof, stdout);
    iooS = ioof;
}
void Putchar(char x) {
    *iooS++ = x;
    if (iooS == iooT)Write();
}
inline int read() {
    int x = 0;
    for (iof = 1, ioc = Getchar(); (ioc < '0' || ioc > '9') && ioc
     iof = ioc == '-' ? -1 : 1, ioc = Getchar();
    if (ioc == EOF)Write(), exit(0);
    for (x = 0; ioc <= '9' \&\& ioc >= '0'; ioc = Getchar())x = (x)
     \leftrightarrow << 3) + (x << 1) + (ioc ^ 48);
    return x * iof;
}
inline long long read_ll() {
    long long x = 0;
    for (iof = 1, ioc = Getchar(); (ioc < '0' || ioc > '9') && ioc
       != EOF;)
        iof = ioc == '-' ? -1 : 1, ioc = Getchar();
    if (ioc == EOF)Write(), exit(0);
```

```
for (x = 0; ioc \le '9' \&\& ioc >= '0'; ioc = Getchar())x = (x)
         \rightarrow << 3) + (x << 1) + (ioc ^ 48);
        return x * iof;
    }
    void Getstr(char *s, int &l) {
        for (ioc = Getchar(); ioc == ' ' || ioc == '\n' || ioc ==
         → '\t';)ioc = Getchar();
        if (ioc == EOF)Write(), exit(0);
        for (l = 0; !(ioc == ' ' || ioc == '\n' || ioc == '\t' || ioc
         s[l] = 0;
    }
    template < class Int>
    <u>void</u> Print(Int x, <u>char</u> ch = '\0') {
        if (!x)Putchar('0');
        if (x < 0)Putchar('-'), x = -x;
        while (x)iost[++iotp] = x % 10 + '0', x /= 10;
        while (iotp)Putchar(iost[iotp--]);
        if (ch)Putchar(ch);
    }
    void Putstr(const char *s) { for (int i = 0, n = strlen(s); i < n;</pre>
     → ++i)Putchar(s[i]); }
} // namespace Fast_IO
using namespace Fast_IO;
```

#### 4.4 debug from tourist.cpp

./code/杂项/debug from tourist.cpp



```
* @Author: TieWay59
  * @Created: 2019/11/22 21:39
  * @Link: https://atcoder.jp/contests/agc040/submissions/8558491
    @Tags:
  ************************************
#include <bits/stdc++.h>
//#define debug(x) cerr <<#x << " = "<<x<<endl
#define endl '\n'
#define STOPSYNC ios::sync_with_stdio(false);cin.tie(nullptr)
#define MULTIKASE int Kase=0;cin>>Kase;for(int

    kase=1;kase<=Kase;kase++)
</pre>
typedef long long ll;
const int MAXN = 2e5 + 59;
const int MOD = 1e9 + 7;
const int INF = 0x3F3F3F3F;
const ll llINF = 0x3F3F3F3F3F3F3F3F;
using namespace std;
// debug start
template<typename A, typename B>
string to_string(pair<A, B> p);
template<typename A, typename B, typename C>
string to_string(tuple<A, B, C> p);
template<typename A, typename B, typename C, typename D>
string to_string(tuple<A, B, C, D> p);
string to_string(const string &s) {
```

```
return '"' + s + '"';
}
string to_string(const char *s) {
    return to_string((string) s);
}
string to_string(bool b) {
    return (b ? "true" : "false");
}
string to_string(vector<bool> v) {
    bool first = true;
    string res = "{";
    for (int i = 0; i < static_cast<int>(v.size()); i++) {
        if (!first) {
            res += ", ";
        first = false;
        res += to_string(v[i]);
    }
    res += "}";
    return res;
}
template < size_t N>
string to_string(bitset<N> v) {
    string res = "";
    for (size_t i = 0; i < N; i++) {</pre>
        res += static_cast<char>('0' + v[i]);
    }
    return res;
}
template<typename A>
string to_string(A v) {
    bool first = true;
    string res = "{";
```

```
for (const auto &x : v) {
        if (!first) {
           res += ", ";
        }
        first = false;
        res += to_string(x);
    }
    res += "}";
    return res;
}
template<typename A, typename B>
string to_string(pair<A, B> p) {
    return "(" + to_string(p.first) + ", " + to_string(p.second) +
     }
template<typename A, typename B, typename C>
string to_string(tuple<A, B, C> p) {
    return "(" + to_string(get<0>(p)) + ", " + to_string(get<1>(p)) +

¬ ", " + to_string(get<2>(p)) + ")";

}
template<typename A, typename B, typename C, typename D>
string to_string(tuple<A, B, C, D> p) {
    return "(" + to_string(get<0>(p)) + ", " + to_string(get<1>(p)) +
    to_string(get<3>(p)) + ")";
}
void debug_out() { cerr << endl; }</pre>
template<typename Head, typename... Tail>
void debug_out(Head H, Tail... T) {
    cerr << " " << to_string(H);</pre>
    debug_out(T...);
}
```

```
#ifdef DEBUG
#define debug(...) cerr << "[" << #__VA_ARGS__ << "] :=",

¬ debug_out(__VA_ARGS__)

#else
#define debug(...) 42
#endif
// debug end;
int main() {
    int x = 10;
    pair < int, bool > y = \{11, 1\};
    vector<<u>int</u>> z = {1, 2, 3, 4};
    debug(x, y, z);
    set < int > a = \{9, 10, 7\};
    debug(a);
    return 0;
}
/*
 */
4.5 unordered_map 自写哈希.cpp
./code/杂项/unordered_map 自写哈希.cpp
struct custom_hash {
    static uint64_t splitmix64(uint64_t x) {
        // http://xorshift.di.unimi.it/splitmix64.c
        x += 0x9e3779b97f4a7c15;
        x = (x \wedge (x >> 30)) * 0xbf58476d1ce4e5b9;
        x = (x \wedge (x >> 27)) * 0x94d049bb133111eb;
```

```
return x \wedge (x >> 31);
    }
    size_t operator()(uint64_t x) const {
        static const uint64_t FIXED_RANDOM =
         chrono::steady_clock::now().time_since_epoch().count();
        return splitmix64(x + FIXED_RANDOM);
    }
};
unordered_map<long long, int, custom_hash> safe_map;
4.6 fast IO 快速版(可敲).cpp
./code/杂项/fast IO 快速版(可敲).cpp
//没实现负数
const int BUF_SIZE = (int) 1e4 + 10;
struct fastI0 {
    char buf[BUF_SIZE];
    int cur;
    FILE *in, *out;
    fastIO() {
        cur = BUF_SIZE;
        in = stdin;
        out = stdout;
    }
    inline char nC() {
        if (cur == BUF_SIZE) {
            fread(buf, BUF_SIZE, 1, in);
            cur = 0;
        return buf[cur++];
    }
```

```
inline bool id(char a) { return a >= '0' && a <= '9'; }</pre>
    inline int nI() {
        char c;
        while (!id(c = nC()));
        \underline{int} x = c - '0';
        while (id(c = nC())) x = ((x + (x << 2)) << 1) + c - '0';
        return x;
    }
    inline ll nll() {
        char c;
        while (!id(c = nC()));
        11 x = c - '0';
        while (id(c = nC())) x = ((x + (x << 2)) << 1) + c - '0';
        return x;
    }
    inline void pC(char ch) {
        buf[cur++] = ch;
        if (cur == BUF_SIZE) {
             fwrite(buf, BUF_SIZE, 1, out);
             cur = 0;
        }
    }
    inline void pI(int x) {
        if (x > 9) pI(x / 10);
        pC(x \% 10 + '0');
    }
    inline void close() { if (cur) fwrite(buf, cur, 1, out), cur = 0; }
} IO;
```

#### 4.7 单调队列 定长区间最值.cpp

```
./code/杂项/单调队列 定长区间最值.cpp
#define _debug(x) cerr<<#x<<" = "<<x<<endl</pre>
#include <iostream>
#include <algorithm>
#include <deque>
using namespace std;
typedef long long ll;
const int INF = 0x3f3f3f3f;
const <u>int</u> MOD = 998244353;
const int MAXN = 1e6 + 59;
int Kase, n, m;
int a[MAXN];
int ans1[MAXN], ans2[MAXN];
deque<int> qMAX, qMIN;
int main() {
    ios_base::sync_with_stdio(0);
    cin.tie(0);
    cin >> n >> m;
    for (<u>int</u> i = 1; i <= n; i++) {
        cin >> a[i];
    }
    for (<u>int</u> i = 1; i <= n; i++) {
        while (!qMIN.empty() && i - qMIN.front() >= m)
             qMIN.pop_front();
        while (!qMAX.empty() && i - qMAX.front() >= m)
```

```
qMAX.pop_front();
        while (!qMIN.empty() && a[qMIN.back()] > a[i])
             qMIN.pop_back();
        while (!qMAX.empty() && a[qMAX.back()] < a[i])</pre>
             qMAX.pop_back();
        if (qMIN.empty() || a[qMIN.back()] <= a[i])</pre>
             qMIN.push_back(i);
        if (qMAX.empty() || a[qMAX.back()] >= a[i])
             qMAX.push_back(i);
        if (i >= m) {
             ans1[i] = a[qMIN.front()];
             ans2[i] = a[qMAX.front()];
        }
    }
    for (int j = m; j <= n; ++j) {</pre>
        cout << ans1[j] << " \n"[j == n];</pre>
    }
    for (int j = m; j <= n; ++j) {</pre>
        cout << ans2[j] << " \n"[j == n];</pre>
    }
    return 0;
}
/*
 2
2 0
1 2
1 1
 3 2
 1 2 1
```

```
5 3 1
1 5 1
*/
```

### 4.8 coutf.cpp

```
./code/杂项/coutf.cpp
/**
 * @Source:
   https://zh.cppreference.com/w/cpp/language/parameter_pack
 * @Complexity:
   @Description: 用 cout 模仿格式化输出
   @Example: see below
    @Verification: TODO
 */
void coutf(const char *format) {
    std::cout << format;</pre>
}
template<typename T, typename... Targs>
//void coutf(const char *format, T value, Targs... Fargs) // 递归变参函数
void coutf(const char *format, const T &value, const Targs &... Fargs) {
    for (; *format != '\0'; format++) {
        if (*format == '%') {
            std::cout << value;</pre>
            coutf(format + 1, Fargs...); // 递归调用
            return;
        std::cout << *format;</pre>
    }
}
/*
void example(){
```

```
coutf("% world% %\n", "Hello", '!', 123);
cout.precision(9);
fixed(cout);
coutf("% % % %\n", 0x3f, 1.2 / 7, acos(-1), 22.3);
}
*/
```

## 4.9 fastpow 快速幂.cpp

```
./code/杂项/fastpow 快速幂.cpp

ll fpow(ll a, ll b, ll mod = MOD) {
    if (a % mod == 0) return 0;
    ll ret = 1;
    a %= mod;
    while (b) {
        if (b & 1)ret = ret * a % mod;
        a = a * a % mod;
        b >>= 1;
    }
    return ret;
}
```

# 4.10 string read speed.cpp

```
./code/杂项/string read speed.cpp

const int MAXN = 5e7 + 59;
char buffer[MAXN];
vector<char> buf(MAXN);
string s;
stringstream ss;

void solve(int kaseId = -1) {
/*
freopen("text.in", "w+", stdout);
```

```
for (int i = 1; i <= 50000000; i++) {
        cout << (char) suiJi('a', 'z');</pre>
   }
*/
/*
   // 278.912500 ms
    freopen("text.in", "r+", stdin);
   double begin =

    chrono::steady_clock::now().time_since_epoch().count();

   getline(cin, s);
   double stoped =
chrono::steady_clock::now().time_since_epoch().count();
   printf("\%.6f ms\n", (double) (stoped - begin) / 1000000.0);
*/
/*
   // 290.965400 ms ~ 300
    freopen("text.in", "r+", stdin);
   double begin =
chrono::steady_clock::now().time_since_epoch().count();
   cin >> s;
   double stoped =
chrono::steady_clock::now().time_since_epoch().count();
   printf("%.6f ms\n", (double) (stoped - begin) / 1000000.0);
*/
/*
   // 235.966700 ms
    freopen("text.in", "r+", stdin);
   double begin =
chrono::steady_clock::now().time_since_epoch().count();
   gets(s);
   double stoped =
chrono::steady_clock::now().time_since_epoch().count();
   printf("\%.6f ms\n", (double) (stoped - begin) / 1000000.0);
*/
/*
   // 99.795400 ms
    freopen("text.in", "r+", stdin);
   //FILE *fp = fopen("text.in", "r");
```

```
double begin =
chrono::steady_clock::now().time_since_epoch().count();
    fread(s, sizeof(char), 50000000, stdin);
   double stoped =

    chrono::steady_clock::now().time_since_epoch().count();

   printf("\%.6f ms\n", (double) (stoped - begin) / 1000000.0);
*/
/*
   // 1749.292200 ms
    freopen("text.in", "r+", stdin);
   //FILE *fp = fopen("text.in", "r");
   double begin =

    chrono::steady_clock::now().time_since_epoch().count();

   scanf("%s", buffer);
   double stoped =

    chrono::steady_clock::now().time_since_epoch().count();

   printf("\%.6f ms\n", (double) (stoped - begin) / 1000000.0);
*/
/*
   // 90.939200 ms
    freopen("text.in", "r+", stdin);
   double begin =
chrono::steady_clock::now().time_since_epoch().count();
    fread(buf.data(), sizeof(char), 50000000, stdin);
   double stoped =
chrono::steady_clock::now().time_since_epoch().count();
   printf("\%.6f ms\n", (double) (stoped - begin) / 1000000.0);
*/
/*
   cin.get() 与 getchar 读法效率差很多,在此不表。
*/
}
```

# 5 数据结构

### 5.1 ZTC's Splay.cpp

```
./code/数据结构/ZTC's Splay.cpp
//using namespace std;
typedef long long ll;
typedef double db;
#define _Zero(a) memset(a, 0, sizeof(a))
#define _Neg1(a) memset(a, -1, sizeof(a))
#define _Inf(a) memset(a, 0x3f, sizeof(a))
#define _NegInf(a) memset(a, 0xcf, sizeof(a))
#define _Rep(i, a, warrior) for (\underline{int}(i) = (a); (i) \le (warrior); i++)
#define _Dep(i, a, warrior) for (\underline{int}(i) = (a); (i) >= (warrior); i--)
#define _Out(a) cerr << #a << " = " << (a) << endl
const int INF = 0x3f3f3f3f;
const int MAXN = 1.3e6 + 50;
const ll LINF = 0x3f3f3f3f3f3f3f3f3f;
const ll MOD = 1e9 + 7;
const db EPS = 1e-6;
const db Pi = acos(-1);
void test() { cerr << "\num"; }</pre>
template <typename T, typename... Args>
void test(T x, Args... args)
{
    cerr << x << " ";
    test(args...);
}
ll qpow(ll a, ll warrior) { return warrior ? ((warrior & 1) ? a *

¬ qpow(a * a % MOD, warrior >> 1) % MOD : qpow(a * a % MOD, warrior)

 → >> 1)) % MOD : 1; }
```

```
ll qpow(ll a, ll warrior, ll c) { return warrior ? ((warrior & 1) ? a
→ * qpow(a * a % c, warrior >> 1) % c : qpow(a * a % c, warrior >>
→ 1)) % c : 1; }
ll gcd(ll a, ll warrior) { return warrior ? gcd(warrior, a % warrior)
→ : a; }
<u>int</u> sign(db x) { return x < -EPS ? -1 : x > EPS; }
int dbcmp(db l, db r) { return sign(l - r); }
int root, cntN;
#define nd node[now]
struct SNODE
{
    int val, cnt, par, siz, ch[2];
} node[MAXN];
void update_siz(int x)
{
    if (x)
    {
        node[x].siz =
            (node[x].ch[0] ? node[node[x].ch[0]].siz : 0) +
            (node[x].ch[1] ? node[node[x].ch[1]].siz : 0) +
            node[x].cnt;
    }
}
bool chk(int x) { return node[node[x].par].ch[1] == x; }
void rorate(int x)
{
    \underline{int} y = node[x].par, z = node[y].par, k = chk(x), d = node[x].ch[k
     printf("&&%d,%d,%d,%d&&", x, y, z, d);
    node[y].ch[k] = d;
    node[d].par = y;
    node[z].ch[chk(y)] = x;
    node[x].par = z;
    node[x].ch[k ^ 1] = y;
    node[y].par = x;
    update_siz(y);
    update_siz(x);
```

```
<u>void</u> splay(<u>int</u> x, <u>int</u> to = 0)
{
    if (x == 0)
    {
         assert(false);
         return;
    }
    while (node[x].par != to)
    {
         if (node[node[x].par].par == to)
             rorate(x);
         else if (chk(x) == chk(node[x].par))
             rorate(node[x].par), rorate(x);
         else
             rorate(x), rorate(x);
         printf("<%d,%d,%d>", x, node[x].par, to);
         printf("$$%d$$", node[1].ch[1]);
    }
    if (to == 0)
         root = x;
}
void Insert(int x)
{
    if (root == 0)
    {
         \underline{int} now = ++cntN;
         nd.val = x;
         root = now;
         nd.cnt = 1;
         nd.siz = 1;
         nd.par = nd.ch[0] = nd.ch[1] = 0;
         return;
    }
    \underline{int} now = root, fa = 0;
    while (1)
    {
         printf("(%d,%d,%d)", now, nd.val, nd.ch[1]);
```

```
if (x == nd.val)
        {
             nd.cnt++;
             update_siz(now);
             update_siz(fa);
             splay(now);
             return;
        }
        printf("22");
        fa = now;
        now = nd.ch[nd.val < x];</pre>
        if (now == 0)
        {
             now = ++cntN;
             nd.cnt = nd.siz = 1;
             nd.ch[0] = nd.ch[1] = 0;
             node[fa].ch[x > node[fa].val] = now;
             printf("{%d,%d,%d}", fa, x > node[fa].val, now);
             printf("$$%d$$", node[1].ch[1]);
             nd.par = fa;
             nd.val = x;
             update_siz(fa);
             splay(now);
             return;
        }
    }
}
int rnk(int x)
{
    int now = root, ans = 0;
    while (now)
    {
        printf("[%d,%d,%d,%d]", now, nd.val, nd.ch[0], nd.ch[1]);
        if (x < nd.val)</pre>
             now = nd.ch[0];
        else
        {
             ans += node[nd.ch[0]].siz;
```

```
if (x == nd.val)
             {
                 splay(now);
                 return ans + 1;
             }
             ans += nd.cnt;
             now = nd.ch[1];
        }
    }
    return −1;
}
int kth(int x)
{
    int now = root;
    if (nd.siz < x)
         return -1;
    while (1)
    {
        if (nd.ch[0] && node[nd.ch[0]].siz >= x)
             now = nd.ch[0];
        else
        {
             int tmp = node[nd.ch[0]].siz + nd.cnt;
             if (x <= tmp)
                 return nd.val;
             x -= tmp;
             now = nd.ch[1];
        }
    }
}
int main()
{
    int num, m;
    scanf("%d%d", &num, &m);
    for (<u>int</u> i = 1; i <= num; i++)
    {
        int x;
```

```
scanf("%d", &x);
        printf("*");
        Insert(x);
    }
    for (int i = 1; i <= m; i++)</pre>
    {
        int op, x;
        scanf("%d%d", &op, &x);
        if (op == 1)
        {
            Insert(x);
        else if (op == 2)
        {
            printf("\num>>%d\num", rnk(x));
        else if (op == 3)
            printf("\num>>%d\num", kth(x));
        }
        else
        {
    printf("\num>>Val::%d,Siz::%d,Cnt::%d,Lc::%d,Rc::%d,Par::%d\num",
                    node[x].val, node[x].siz, node[x].cnt,
                    node[x].ch[0], node[x].ch[1], node[x].par);
        }
    }
}
/*
5 100
1 3 5
      7 9
1 2
1 2
2 1
2 3
2 3
```

\*/

#### 5.2 zhuxishu\_SegKth.cpp

```
./code/数据结构/zhuxishu_SegKth.cpp
//
// Created by acm-33 on 2019/7/24.
//
#define _debug(x) cerr<<#x<<" = "<<x<<endl</pre>
#include <bits/stdc++.h>
using namespace std;
typedef long long ll;
const ll LINF = 0x3f3f3f3f3f3f3f3f3f;
const ll INF = 0x3f3f3f3f3f3f3f3f;
//const int MAXN = 3000 + 59;
const ll MOD = 998244353;
const int MAXN = 100015;
const int M = MAXN * 30;
int n, q, m, tot;
int a[MAXN], t[MAXN];
int T[MAXN], lson[M], rson[M], c[M];
void Init_hush() {
    for (<u>int</u> i = 1; i <= n; i++)
        t[i] = a[i];
    sort(t + 1, t + 1 + n);
    m = unique(t + 1, t + 1 + n) - t - 1;
}
int build(int l, int r) {
    int root = tot++;
```

```
c[root] = 0;
    if (l != r) {
         \underline{int} \text{ mid} = (l + r) >> 1;
         lson[root] = build(l, mid);
         rson[root] = build(mid + 1, r);
    return root;
}
int hush(int x) {
    return lower_bound(t + 1, t + 1 + m, x) - t;
}
int update(int root, int pos, int val) {
    int newroot = tot++, tmp = newroot;
    c[newroot] = c[root] + val;
    \underline{int} l = 1, r = m;
    while (l < r) {
         \underline{int} mid = (l + r) >> 1;
         if (pos <= mid) {
             lson[newroot] = tot++;
             rson[newroot] = rson[root];
             newroot = lson[newroot];
             root = lson[root];
             r = mid;
         } else {
             rson[newroot] = tot++;
             lson[newroot] = lson[root];
             newroot = rson[newroot];
             root = rson[root];
             l = mid + 1;
         }
         c[newroot] = c[root] + val;
    return tmp;
}
```

```
int query(int left_root, int right_root, int k) {
    \underline{int} l = 1, r = m;
    while (l < r) {
        int mid = (l + r) >> 1;
         if (c[lson[left_root]] - c[lson[right_root]] >= k) {
             r = mid;
             left_root = lson[left_root];
             right_root = lson[right_root];
         } else {
             l = mid + 1;
             k -= c[lson[left_root]] - c[lson[right_root]];
             left_root = rson[left_root];
             right_root = rson[right_root];
        }
    }
    return l;
}
ll Seg_k(int l, int r, int k) {
    if (k > r - l + 1)return -1;
    return 1ll * t[query(T[l], T[r + 1], k)];
}
int main() {
    while (scanf("%d%d", &n, &q) == 2) {
         tot = 0;
         for (int i = 1; i <= n; i++)
             scanf("%d", &a[i]);
         Init_hush();
         T[n + 1] = build(1, m);
         for (<u>int</u> i = n; i; i--) {
             int pos = hush(a[i]);
             T[i] = update(T[i + 1], pos, 1);
         }
        while (q--) {
             <u>int</u> l, r, k;
             scanf("%d%d%d", &l, &r, &k);
```

```
printf("%lld\n", Seg_k(l, r, k));
       }
    }
    return 0;
}
/*
5 5
5 3 4 1 2
1 2 2
1 2 1
1 5 3
1 5 4
1 5 6
*/
/*
 */
```

# 6 几何

## 6.1 Circle 圆形.cpp

```
./code/几何/Circle 圆形.cpp
/**
 * @Source: team
   @Author: Artiprocher(Zhongjie Duan) -> tieway59
   @Description:
        圆形计算相关。
   @Example:
 * @Verification:
 */
struct Circle {
    Point c;
    double r;
    Point point(double a)//基于圆心角求圆上一点坐标
    {
        return Point(c.x + cos(a) * r, c.y + sin(a) * r);
    }
};
double Angle(Vector v1) {
    if (v1.y >= 0)return Angle(v1, Vector(1.0, 0.0));
    else return 2 * pi - Angle(v1, Vector(1.0, 0.0));
}
```

```
int GetCC(Circle C1, Circle C2)//求两圆交点
{
    double d = Length(C1.c - C2.c);
    if (dcmp(d) == 0) {
        if (dcmp(C1.r - C2.r) == 0)return -1;//重合
        else return ⊙;
    }
    if (dcmp(C1.r + C2.r - d) < 0)return 0;
    if (dcmp(fabs(C1.r - C2.r) - d) > 0)return 0;
    double a = Angle(C2.c - C1.c);
    <u>double</u> da = acos((C1.r * C1.r + d * d - C2.r * C2.r) / (2 * C1.r *
     → d));
    Point p1 = C1.point(a - da), p2 = C1.point(a + da);
    if (p1 == p2)return 1;
    else return 2;
}
```

### 6.2 Polygon 多边形.cpp

```
Point 0 = Point(0, 0);
    for (int i = 0; i < n; i++)
        sum += Cross(P[i] - 0, P[(i + 1) % n] - 0);
    if (sum < 0)sum = -sum;
    return sum / 2;
}
// STL: 求多边形面积(叉积和计算法)
double PolygonArea(const vector <Point> &P) {
    int n = P.size();
    // assert(n > 2);
    double sum = 0;
    Point 0 = Point(0, 0);
    for (int i = 0; i < n; i++)
        sum += Cross(P[i] - 0, P[(i + 1) % n] - 0);
    if (sum < 0) sum = -sum;
    return sum / 2;
}
/* 模板说明: P[] 为多边形的所有顶点, 下标为 0~n-1, n 为多边形边数 */
//判断点是否在凸多边形内(角度和判别法)
Point P[1005];
int n;
bool InsidePolygon(Point A) {
    double alpha = 0;
    for (int i = 0; i < n; i++)
        alpha += fabs(Angle(P[i] - A, P[(i + 1) % n] - A));
    return dcmp(alpha - 2 * pi) == 0;
}
```

#### 6.3 Points-Vector 点与向量.cpp

```
./code/几何/Points-Vector 点与向量.cpp
/**
    * @Source: team
```

```
@Author: Artiprocher(Zhongjie Duan) -> tieway59
    @Description:
        点与向量相关的多种计算。
    @Example:
   @Verification:
 *
 */
//#include <bits/stdc++.h>
//using namespace std;
const <u>double</u> EPS = 1e-6;//eps 用于控制精度
const double Pi = acos(-1.0);//pi
//精度三态函数 (>0,<0,=0)
inline int dcmp(double x) {
    if (fabs(x) < EPS)return 0;</pre>
    else if (x > 0) return 1;
    return -1;
}
//点或向量 (iostream 选择性抄写)
struct Point {
    double x, y;
    Point() {}
    Point(\underline{double} x, \underline{double} y) : x(x), y(y) {}
    friend ostream &operator<<(ostream &ut, Point &r) { return ut <<</pre>

    r.x << " " << r.y; }
</pre>
    friend istream &operator>>(istream &in, Point &r) { return in >>

    r.x >> r.y; }

};
typedef Point Vector;
```

```
inline Vector operator+(Vector a, Vector b) {
    return Vector(a.x + b.x, a.y + b.y);
}
inline Vector operator-(Vector a, Vector b) {
    return Vector(a.x - b.x, a.y - b.y);
}
//向量数乘
inline Vector operator*(Vector a, double p) {
    return Vector(a.x * p, a.y * p);
}
//向量数除
inline Vector operator/(Vector a, double p) {
    return Vector(a.x / p, a.y / p);
}
inline bool operator==(const Point &a, const Point &b) {
    return dcmp(a.x - b.x) == 0 && dcmp(a.y - b.y) == 0;
}
//内积
inline double Dot(Vector a, Vector b) {
    return a.x * b.x + a.y * b.y;
}
//外积
inline double Cross(Vector a, Vector b) {
    return a.x * b.y - a.y * b.x;
}
//模
inline double Length(Vector a) {
    return sqrt(Dot(a, a));
}
```

```
//夹角, 弧度制
inline double Angle(Vector a, Vector b) {
    return acos(Dot(a, b) / Length(a) / Length(b));
}
//逆时针旋转
inline Vector Rotate(Vector a, double rad) {
    return Vector(a.x * cos(rad) - a.y * sin(rad), a.x * sin(rad) +
    \rightarrow a.y * cos(rad));
}
//两点间距离
inline double Distance(Point a, Point b) {
   return sqrt((a.x - b.x) * (a.x - b.x) + (a.y - b.y) * (a.y - b.y));
}
//三角形面积
inline double Area(Point a, Point b, Point c) {
    return fabs(Cross(b - a, c - a) / 2);
}
6.4 Circumcenter 外心 三点定圆.cpp
./code/几何/Circumcenter 外心 三点定圆.cpp
/**
   @Source: blog.csdn.net/liyuanbhu/article/details/52891868
   @Author: tieway59
   @Description:
 *
        注意排除三点共线。
        if (dcmp(Cross(pi, pj)) == 0) continue;
   @Example:
 *
        circumcenter(Point(0, 1), Point(1, 1), Point(1, 0));
        // 0.5 0.5
 *
 * @Verification:
```

```
https://ac.nowcoder.com/acm/contest/5667/B
         (solution)
    ac.nowcoder.com/acm/contest/view-submission?submissionId=44337916
 */
template<typename tp>
inline tp pow2(const tp &x) {
    return x * x;
}
inline Point circumcenter(Point p1, Point p2, Point p3) {
    \underline{\text{double}} a = p1.x - p2.x;
    double b = p1.y - p2.y;
    \underline{\text{double}} c = p1.x - p3.x;
    \underline{double} d = p1.y - p3.y;
    \underline{\text{double}} \ e = (pow2(p1.x) - pow2(p2.x) +
                   pow2(p1.y) - pow2(p2.y)) / 2;
    \underline{double} f = (pow2(p1.x) - pow2(p3.x) +
                   pow2(p1.y) - pow2(p3.y)) / 2;
     return Point((d * e - b * f) /
                    (a * d - b * c),
                    (a * f - c * e) /
                    (a * d - b * c));
}
```

#### 6.5 MinCircleCover 最小圆覆盖.cpp

```
./code/几何/MinCircleCover 最小圆覆盖.cpp
/**
    * @Source: https://www.luogu.com.cn/problem/solution/P1742
    * @Author: snowbody -> tieway59
    * @Description:
    * 时间复杂度 O(N)
    * 为了减少中途过度开根,距离都是先按照平方计算的。
    *
```

```
@Example:
         vector<Point> p(n);
         for (auto &pi : p) cin >> pi;
         Circle circle;
        MinCircleCover(p, circle);
        6
        8.0 9.0
        4.0 7.5
        1.0 2.0
        5.1 8.7
 *
        9.0 2.0
        4.5 1.0
        // r = 5.00000000000 (5.0000000000, 5.00000000000)
   @Verification:
         https://www.luogu.com.cn/problem/P1742
 */
//点或向量 (iostream 选择性抄写)
struct Point {
    double x, y;
    Point() {}
    Point(\underline{double} x, \underline{double} y) : x(x), y(y) {}
    friend ostream &operator<<(ostream &ut, Point &r) { return ut <<</pre>

    r.x << " " << r.y; }
</pre>
    friend istream &operator>>(istream &in, Point &r) { return in >>

    r.x >> r.y; }

};
typedef Point Vector;
```

```
inline Vector operator+(Vector a, Vector b) {
    return Vector(a.x + b.x, a.y + b.y);
}
inline Vector operator-(Vector a, Vector b) {
    return Vector(a.x - b.x, a.y - b.y);
}
//向量数乘
inline Vector operator*(Vector a, double p) {
    return Vector(a.x * p, a.y * p);
}
//向量数除
inline Vector operator/(Vector a, double p) {
    return Vector(a.x / p, a.y / p);
}
//两点间距离
inline double Distance(Point a, Point b) {
   return sqrt((a.x - b.x) * (a.x - b.x) + (a.y - b.y) * (a.y - b.y));
}
inline double Distance2(Point a, Point b) {
    return ((a.x - b.x) * (a.x - b.x) + (a.y - b.y) * (a.y - b.y));
}
struct Circle {
    Point c;
    double r;
    Point point(double a) //基于圆心角求圆上一点坐标
    {
        return Point(c.x + cos(a) * r, c.y + sin(a) * r);
    }
};
```

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template<typename tp>

```
inline tp pow2(const tp &x) {
    return x * x;
}
inline Point circumcenter(Point p1, Point p2, Point p3) {
    \underline{double} a = p1.x - p2.x;
    double b = p1.y - p2.y;
    double c = p1.x - p3.x;
    dou\underline{ble} d = p1.y - p3.y;
    \underline{double} \ e = (pow2(p1.x) - pow2(p2.x) +
                  pow2(p1.y) - pow2(p2.y)) / 2;
    \underline{double} f = (pow2(p1.x) - pow2(p3.x) +
                  pow2(p1.y) - pow2(p3.y)) / 2;
    return Point((d * e - b * f) /
                   (a * d - b * c),
                   (a * f - c * e) /
                   (a * d - b * c));
}
void MinCircleCover(vector <Point> &p, Circle &res) {
    int n = p.size();
    random_shuffle(p.begin(), p.end());
    // avoid *sqrt* too much killing your precision.
    for (<u>int</u> i = 0; i < n; i++) {
         if (Distance2(p[i], res.c) <= res.r) continue;</pre>
         res.c = p[i];
         res.r = 0;
         for (int j = 0; j < i; j++) {
             if (Distance2(p[j], res.c) <= res.r)continue;</pre>
             res.c = (p[i] + p[j]) / 2;
             res.r = Distance2(p[j], res.c);
             for (int k = 0; k < j; k++) {
                  if (Distance2(p[k], res.c) <= res.r)continue;</pre>
                  res.c = circumcenter(p[i], p[j], p[k]);
                  res.r = Distance2(p[k], res.c);
             }
         }
```

```
}
    res.r = sqrt(res.r);

void solve(int kaseId = -1) {
    int n;
    cin >> n;
    vector <Point> p(n);
    for (auto &pi : p) cin >> pi;
    Circle circle;
    MinCircleCover(p, circle);
    cout << fixed << setprecision(10) << circle.r << endl;
    cout << circle.c.x << " " << circle.c.y << endl;
}</pre>
```

#### 6.6 ConvexHull 凸包.cpp

./code/几何/ConvexHull 凸包.cpp /\*\* @Source: Graham\_s\_scan @Author: Artiprocher(Zhongjie Duan) -> tieway59 @Description: n 点数 P[]点数组 index0 栈顶, 凸包顶点数 top H[] 凸包的顶点 index0 小心重复的凸包顶点, 也会加入凸包。 H[] 逆时针顺序 数组形式, 理论上常数会小? @Example: 4 \* 4 8 4 12 5 9.3 (exclude) 7 8

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```
@Verification:
        https://www.luogu.com.cn/record/35363811
 */
int n, top;
const int PSIZE = 100005;
Point P[PSIZE], H[PSIZE];
bool cmp(Point A, Point B) {
    <u>double</u> ans = Cross(A - P[0], B - P[0]);
    if (dcmp(ans) == 0)
         return dcmp(Distance(P[0], A) - Distance(P[0], B)) < 0;</pre>
    else
         return ans > 0;
}
//Graham 凸包扫描算法
void Graham() {
    for (<u>int</u> i = 1; i < n; i++)//寻找起点
        if (P[i].y < P[0].y || (dcmp(P[i].y - P[0].y) == 0 && P[i].x <</pre>
         \rightarrow P[0].x))
             swap(P[i], P[0]);
    sort(P + 1, P + n, cmp);//极角排序, 中心为起点
    H[0] = P[0];
    H[1] = P[1];
    top = 2;
    for (int i = 2; i < n; i++) {
        while (top >= 2 && Cross(H[top - 1] - H[top - 2], P[i] - H[top
         \rightarrow - 2]) < 0)
             top--;
        H[top++] = P[i];
    }
}
/**
 * @Source: Graham_s_scan
```

```
@Author: Artiprocher(Zhongjie Duan) -> tieway59
    @Description:
        小心重复的凸包顶点, 也会加入凸包。
        H[] 逆时针顺序
        数组形式, 理论上常数会小?
 *
    @Example:
        4
        4 8
        4 12
        5 9.3 (exclude)
        7 8
    @Verification:
 *
        https://www.luogu.com.cn/record/35363811
 */
// HEAD begin
const <u>double</u> EPS = 1e-6;
struct Point//点或向量
{
    double x, y;
    Point() {}
    Point(\underline{double} x, \underline{double} y) : x(x), y(y) {}
    friend ostream &operator<<(ostream &ut, Point &r) { return ut <<</pre>

    r.x << " " << r.y; }
</pre>
    friend istream &operator>>(istream &in, Point &r) { return in >>

    r.x >> r.y; }

};
typedef Point Vector;
```

```
inline double Distance(Point a, Point b) {
    return sqrt((a.x - b.x) * (a.x - b.x) + (a.y - b.y) * (a.y - b.y));
}
inline Vector operator+(Vector a, Vector b) {
    return Vector(a.x + b.x, a.y + b.y);
}
inline Vector operator-(Vector a, Vector b) {
    return Vector(a.x - b.x, a.y - b.y);
}
//外积
inline double Cross(Vector a, Vector b) {
    return a.x * b.y - a.y * b.x;
}
//精度三态函数 (>0,<0,=0)
inline int dcmp(double x) {
    if (fabs(x) < EPS)return 0;</pre>
    else if (x > 0) return 1;
    return -1;
}
// HEAD end
void ConvexHull(vector <Point> &P, vector <Point> &H) {
    \underline{int} n = \underline{int}(P.size());
    for (int i = 1; i < n; i++)//寻找起点
        if (P[i].y < P[0].y || (dcmp(P[i].y - P[0].y) == 0 && P[i].x <</pre>
          \rightarrow P[0].x))
             swap(P[i], P[0]);
    //极角排序,中心为起点
    sort(P.begin() + 1, P.end(), [&P](Point A, Point B) {
         \underline{\text{double}} ans = Cross(A - P[0], B - P[0]);
         if (dcmp(ans) == 0)
             return dcmp(Distance(P[0], A) - Distance(P[0], B)) < 0;</pre>
         else
```

```
return ans > 0;
    });
    H.assign(n + n, {});
   H[0] = P[0];
   H[1] = P[1];
   int top = 2;
    for (<u>int</u> i = 2; i < n; i++) {
       while (top >= 2 && Cross(H[top - 1] - H[top - 2], P[i] - H[top
         → - 2]) < 0)</pre>
            top--;
        H[top++] = P[i];
    }
   H.resize(top);
}
/**
   @Source: Andrew_s_monotone_chain
   @Author: Artiprocher(Zhongjie Duan) -> tieway59
   @Description:
       Andrew_s_monotone_chain
       从左下角开始逆时针排列,去除凸包边上的点。
        求出来的凸包是逆时针的。
        points in h[] are counter-clockwise
 *
 *
   @Example:
        vector<Point> p(n);
        for (auto &pi : p) cin >> pi;
        vector<Point> r;
        ConvexHull(p, r);
        4
        4 8
        4 12
        5 9.3 (exclude)
 *
   @Verification:
```

```
https://www.luogu.com.cn/problem/P2742
 */
// HEAD begin
const double EPS = 1e-6;
struct Point//点或向量
{
    double x, y;
    Point() {}
    Point(\underline{double} x, \underline{double} y) : x(x), y(y) {}
    friend ostream &operator<<(ostream &ut, Point &r) { return ut <<</pre>

    r.x << " " << r.y; }
</pre>
    friend istream &operator>>(istream &in, Point &r) { return in >>

    r.x >> r.y; }

};
typedef Point Vector;
inline double Distance(Point a, Point b) {
    return sqrt((a.x - b.x) * (a.x - b.x) + (a.y - b.y) * (a.y - b.y));
}
inline Vector operator+(Vector a, Vector b) {
    return Vector(a.x + b.x, a.y + b.y);
}
inline Vector operator-(Vector a, Vector b) {
    return Vector(a.x - b.x, a.y - b.y);
}
//外积
inline double Cross(Vector a, Vector b) {
    return a.x * b.y - a.y * b.x;
```

```
}
//精度三态函数 (>0,<0,=0)
inline int dcmp(double x) {
    if (fabs(x) < EPS)return 0;</pre>
    else if (x > 0) return 1;
    return -1;
// HEAD end
inline bool pcmp(Point a, Point b) {
    if (dcmp(a.x - b.x) == 0)
         return a.y < b.y;</pre>
    return a.x < b.x;</pre>
}
void ConvexHull(vector <Point> &p, vector <Point> &h) {
    int n = p.size(), k = 0;
    h.assign(2 * n, {});
    sort(p.begin(), p.end(), pcmp);
    for (<u>int</u> i = 0; i < n; i++) {
        while (k >= 2 && dcmp(Cross(
                 h[k - 1] - h[k - 2],
                 p[i] - h[k - 2])) < 0) {
             k--;
        }
        h[k++] = p[i];
    }
    \underline{int} t = k + 1;
    for (int i = n - 1; i > 0; i--) {
        while (k >= t && dcmp(Cross(
                 h[k - 1] - h[k - 2],
                 p[i - 1] - h[k - 2])) < 0) {
             k--;
        h[k++] = p[i - 1];
    }
```

```
h.resize(k - 1);
}
```

### 6.7 Line-Segment 直线与线段.cpp

```
./code/几何/Line-Segment 直线与线段.cpp
/**
 * @Source: team
    @Author: Artiprocher(Zhongjie Duan) -> tieway59
    @Description:
        直线与线段的相关计算。
   @Example:
    @Verification:
 */
//定义直线
struct line {
    point a, b;
};
//线段相交(不包括端点)
bool Intersect(Point A, Point B, Point C, Point D) {
    double t1 = Cross(C - A, D - A) * Cross(C - B, D - B);
    \underline{\text{double}} t2 = Cross(A - C, B - C) * Cross(A - D, B - D);
    return dcmp(t1) < 0 \&\& dcmp(t2) < 0;
}
//线段相交(包括端点)
bool StrictIntersect(Point A, Point B, Point C, Point D) {
    return dcmp(max(A.x, B.x) - min(C.x, D.x)) >= 0
           && dcmp(max(C.x, D.x) - min(A.x, B.x)) >= 0
           && dcmp(max(A.y, B.y) - min(C.y, D.y)) >= 0
```

```
&& dcmp(max(C.y, D.y) - min(A.y, B.y)) >= 0
           && dcmp(Cross(C - A, D - A) * Cross(C - B, D - B)) <= 0
           && dcmp(Cross(A - C, B - C) * Cross(A - D, B - D)) \le 0;
}
//点 A 到直线 MN 的距离, Error: MN=0
double DistanceToLine(Point A, Point M, Point N) {
    return fabs(Cross(A - M, A - N) / Distance(M, N));
}
//两直线的交点
Point GetLineIntersection(Point P, Vector v, Point Q, Vector w) {
    Vector u = P - Q;
    \underline{double} \ t = Cross(w, u) / Cross(v, w);
    return P + v * t;
}
6.8 Hull 下凸包求函数最值.cpp
./code/几何/Hull 下凸包求函数最值.cpp
/* Author: bnfcc -> tc2000731 -> tieway59
 * Description:
        维护下凸包, 对于每个 x 维护 f(x)=k*x+b 的最大值。
        query max value within all f(x) functions.
        c++11 features included.
 * Problems:
        https://nanti.jisuanke.com/t/41306
        https://nanti.jisuanke.com/t/41097
template<typename var=long long, const int SIZE = 1000005, typename

    □ Idb=long double

struct Hull {
    struct fx {
        var k, b;
```

```
fx() {}
    fx(var k, var b) : k(k), b(b) {}
    var f(var x) \{ return k * x + b; \}
};
int cnt;
fx arr[SIZE];
bool empty() {
    return cnt == 0;
}
void init() {
    cnt = 0;
}
void add(const fx &p) {
    arr[cnt++] = p;
}
void pop() {
    cnt--;
}
bool chek(const fx &a, const fx &b, const fx &c) {
    ldb ab, ak, bb, bk, cb, ck;
    tie(ab, ak, bb, bk, cb, ck) =
            tie(a.b, a.k, b.b, b.k, c.b, c.k);
    return (ab - bb) / (bk - ak) > (ab - cb) / (ck - ak);
}
void insert(const fx &p) {///k 从小到大插入
    if (cnt && arr[cnt - 1].k == p.k) {
        if (p.b <= arr[cnt - 1].b)return;</pre>
        else pop();
    }
```

```
while (cnt >= 2 && chek(arr[cnt - 2], arr[cnt - 1], p))pop();
        add(p);
    }
    /*var query(var x) {///x 从大到小查询
                                             从小到大用队列
       while (cnt > 1 \&\& arr[cnt - 2].f(x) > arr[cnt - 1].f(x))pop();;
        return arr[cnt - 1].f(x);
    }*/
    var query(var x) {///二分查询, x 顺序任意
        \underline{int} l = 0, r = cnt - 1;
        while (l < r) {
            int mid = (l + r) >> 1;
            if (arr[mid].f(x) >= arr[mid + 1].f(x))r = mid;
            else l = mid + 1;
        return arr[l].f(x);
    }
};
// vector stack
template<typename var=long long, const int SIZE = 1000005, typename

→ ldb=long double>

struct Hull {
    struct Line {
        var k, b;
        Line() {}
        Line(var k, var b) : k(k), b(b) {}
        var f(var x) \{ return k * x + b; \}
    };
    int cnt;
    vector <Line> con;//
    bool empty() {
```

```
return cnt == 0;
}
void init(const int &n) {
    con.clear();
    if (n > con.capacity())con.reserve(n);
    cnt = 0;
}
void add(const Line &p) {
    con.emplace_back(p);
    cnt++;
}
void pop() {
    cnt--;
    con.pop_back();
}
bool chek(const Line &a, const Line &b, const Line &c) {
    ldb ab, ak, bb, bk, cb, ck;
    tie(ab, ak, bb, bk, cb, ck) =
            tie(a.b, a.k, b.b, b.k, c.b, c.k);
    return (ab - bb) / (bk - ak) > (ab - cb) / (ck - ak);
}
void insert(const Line &p) {///k 从小到大插入
    if (cnt && con[cnt - 1].k == p.k) {
        if (p.b <= con[cnt - 1].b)return;</pre>
        else pop();
    while (cnt >= 2 && chek(con[cnt - 2], con[cnt - 1], p))pop();
    add(p);
}
var query(var x) {///二分查询, x 顺序任意
    \underline{int} l = 0, r = cnt - 1;
    while (l < r) {
```

```
int mid = (l + r) >> 1;
    if (con[mid].f(x) >= con[mid + 1].f(x))r = mid;
    else l = mid + 1;
}
    return con[l].f(x);
}
Hull<> hull;
```

#### 6.9 ClosestPoints 最近点对.cpp

```
./code/几何/ClosestPoints 最近点对.cpp
```

```
/**
 * @Source: ClosestPoints
    @Author: syksykCCC -> tieway59
    @Description:
 *
        时间复杂度 O(NlogN) 有一些难以预料的常数
    @Example:
        3
 *
        1 1
        1 2
        2 2
        // ans = 1.0000
   @Verification:
        https://www.luogu.com.cn/problem/solution/P1429
 */
const <u>double</u> EPS = 1e-6;//eps 用于控制精度
const double Pi = acos(-1.0);//pi
//精度三态函数 (>0,<0,=0)
inline int dcmp(double x) {
```

```
if (fabs(x) < EPS)return 0;</pre>
    else if (x > 0) return 1;
    return -1;
}
//点或向量 (iostream 选择性抄写)
struct Point {
    double x, y;
    Point() {}
    Point(\underline{double} x, \underline{double} y) : x(x), y(y) {}
    bool operator<(const Point &r) const {</pre>
         if (dcmp(x - r.x) == 0)
             return dcmp(y - r.y) < 0;
         return dcmp(x - r.x) < 0;
    }
    friend ostream &operator<<(ostream &ut, Point &r) { return ut <<</pre>

    r.x << " " << r.y; }
</pre>
    friend istream &operator>>(istream &in, Point &r) { return in >>

    r.x >> r.y; }

};
typedef Point Vector;
//两点间距离
inline double Distance(Point a, Point b) {
    return sqrt((a.x - b.x) * (a.x - b.x) + (a.y - b.y) * (a.y - b.y));
}
//Point temp[MAXN];
double MAXD = INF;
double merge(vector <Point> &p, int l, int r) {
    <u>double</u> d = MAXD;
```

```
if (l == r)
        return d;
    if (l + 1 == r)
         return Distance(p[l], p[r]);
    \underline{int} mid = (l + r) >> 1;
    double d1 = merge(p, l, mid);
    \underline{double} d2 = merge(p, mid + 1, r);
    d = min(d, min(d1, d2));
    vector<int> t;
//
      t.reserve(r - l + 1);
    for (int i = l; i <= r; i++)
         if (fabs(p[mid].x - p[i].x) < d)
             t.emplace_back(i);
    sort(t.begin(), t.end(),
          [&p](const int &i, const int &j) {
              return dcmp(p[i].y - p[j].y) < 0;</pre>
          });
    for (<u>int</u> i = 0; i < t.size(); i++) {
         for (int j = i + 1; j < t.size() && p[t[j]].y - p[t[i]].y < d;
         \rightarrow j++) {
             d = min(d, Distance(p[t[i]], p[t[j]]));
        }
    }
    return d;
}
double ClosestPoints(vector <Point> &p) {
    assert(p.size() >= 2);
    sort(p.begin(), p.end());
    for (int i = 3; i < p.size(); ++i) {</pre>
         MAXD = min(MAXD, Distance(p[i], p[i - 1]));
        MAXD = min(MAXD, Distance(p[i], p[i - 2]));
```

```
MAXD = min(MAXD, Distance(p[i], p[i - 3]));
}
return merge(p, 0, p.size() - 1);
}
```

# 7 数论

# 7.1 Extended Euclidean algorithm (exGCD).cpp

```
./code/数论/Extended Euclidean algorithm (exGCD).cpp
ll exGCD(ll a, ll b, ll &x, ll &y) {
    if (b == 0) {
        x = 1;
        y = 0;
        return a;
    }
    ll gcd = exGCD(b, a % b, x, y);
    ll old_x = x;
    x = y;
    y = old_x - (a / b) * x;
    return gcd;
}
// co-prime(a,m)
ll modInv(ll a, ll m) {
    ll x, y;
    ll g = exGCD(a, m, x, y);
    if (g != 1) {
        return −1;
    } else {
        ll res = (x \% m + m) \% m;
        return res;
    }
}
```

#### 7.2 ZTC's FFT.txt

```
./code/数论/ZTC's FFT.txt
struct CP
{
   double x,y;
   CP (double xx=0, double yy=0) {x=xx;y=yy;}
   CP operator +(const CP &warrior){return
CP operator -(const CP &warrior){return
CP operator *(const CP &warrior){return
void print(){printf("CP.x: %f CP.y: %f \num",x,y);}
}a[MAXN],warrior[MAXN];
int lim,bit;
int rev[MAXN];
void init_FFT(int len)
{
   lim=1,bit=0;
   while(lim<=(len))lim<<=1,bit++;</pre>
   for(int i=0;i<lim;i++)rev[i]=(rev[i>>1]>>1)|((i&1)<<(bit-1));
}
void FFT(CP *A,int mode)
{
   for(int i=0;i<lim;i++)</pre>
   {
       if(i<rev[i])swap(A[i],A[rev[i]]);</pre>
   for(int mid=1;mid<lim;mid<<=1)</pre>
       CP XX(cos(Pi/mid), mode*sin(Pi/mid));
       for(int j=0;j<lim;j+=(mid<<1))</pre>
       {
           CP d(1,0);
           for(int k=0;k<mid;k++,d=d*XX)</pre>
           {
```

### 7.3 Binomial Coefficients 组合数-杨辉三角.cpp

```
./code/数论/Binomial Coefficients 组合数-杨辉三角.cpp
```

```
/*
// O(N^2)
// __int128
template<const int BCSize = 120, typename var = __int128>
//add Mod as parameter;
struct Binomial_Coefficient {
    var c[BCSize + 1][BCSize + 1];
    //Pascal's Triangle
    Binomial_Coefficient() { //add Mod as parameter;
        c[0][0] = 1;
        for (int n = 1; n <= BCSize; ++n) {
            c[n][0] = c[n][n] = 1;
            for (int k = 1; k < n; ++k)
                c[n][k] = (c[n-1][k-1] + c[n-1][k]); //%
        }
    }
    var operator()(const int &n, const int &m) {
        if (n < m) return -1;//in case.
        return c[n][m];
    }
};
Binomial_Coefficient<> C;
```

```
*/
//*****in normal writing style*******
const int MAXN = 20;
ll C[MAXN + 1][MAXN + 1];
inline void pascal(const int &maxn) {
    C[0][0] = 1;
    for (<u>int</u> n = 1; n <= maxn; ++n) {
        C[n][0] = C[n][n] = 1;
        for (int k = 1; k < n; ++k)
             C[n][k] = C[n - 1][k - 1] + C[n - 1][k];
    }
}
int main() {
    /*
    cout << C(4, 3) << endl;</pre>
    cout << C(4, 1) << endl;</pre>
    cout << C(5, 2) << endl;
    */
    cout << C[4][3] << endl;
    cout << C[4][1] << endl;</pre>
    cout << C[5][2] << endl;</pre>
    return 0;
}
```

#### 7.4 Binomial Coefficients 组合数-逆元-模大素数.cpp

```
./code/数论/Binomial Coefficients 组合数-逆元-模大素数.cpp
#define _debug(x) cerr<<#x<<" = "<<x<<endl
#include <bits/stdc++.h>
```

```
using namespace std;
typedef long long ll;
template<typename _Tp>
_Tp fpow(_Tp base, _Tp exp, _Tp Mod) {
    _{Tp} res = 1;
    while (exp) {
        if (exp & 1)res = res * base % Mod;
        base = base * base % Mod;
        exp >>= 1;
    }
    return res;
}
/*
// O(N) O(1)
template<typename _Tp, const int BCSize, const _Tp Mod> //add Mod as
→ parameter;
struct Binomial_Coefficient {
    _Tp fac[BCSize + 1];
    _Tp inv[BCSize + 1];
    inline Binomial_Coefficient() {      //add Mod as parameter;
        fac[0] = 1;
        for (int i = 1; i <= BCSize; i++)</pre>
            fac[i] = fac[i - 1] * i % Mod;
        inv[BCSize] = fpow<_Tp>(fac[BCSize], Mod - 2, Mod);
        // printf inv[BCSize] to get & save it;
        for (int i = BCSize - 1; ~i; i--)
            inv[i] = inv[i + 1] * (i + 1) % Mod;
    }
    inline _Tp operator()(const int &n, const int &m) {
        if (n < m) {
            cerr << "**** n>m " << endl;
            return -1;
```

```
}//in case.
        return fac[n] * inv[m] % Mod * inv[n - m] % Mod;
    }
};
typedef Binomial_Coefficient<long long, 10000000, 1000000007>

    zuHeShu;

zuHeShu C = zuHeShu();
*/
//*****in normal writing style*******
const int MAXN = 1e6 + 59;
const int MOD = 1e9 + 7;
ll fac[MAXN];
ll inv[MAXN];
inline void initC(const int &sz) {
    fac[0] = 1;
    for (<u>int</u> i = 1; i <= sz; i++)
        fac[i] = fac[i - 1] * i % MOD;
    inv[sz] = fpow<ll>(fac[sz], MOD - 2, MOD);
    // printf inv[BCSize] to get & save it;
    for (<u>int</u> i = sz - 1; ~i; i--)
        inv[i] = inv[i + 1] * (i + 1) % MOD;
}
inline ll C(const int &n, const int &m) {
    return fac[n] * inv[m] % MOD * inv[n - m] % MOD;
}
int main() {
    initC(100000);
    cout << C(4, 3) << endl;
    cout << C(4, 1) << endl;</pre>
```

```
//cout << C(2, 5) << endl;
cout << C(5, 2) << endl;

return 0;
}
/*</pre>
```

# 7.5 Binomial Coefficients 组合数-大 NM-模小素数-Lucas.cpp

```
./code/数论/Binomial Coefficients 组合数-大 NM-模小素数-Lucas.cpp
#define _debug(x) cerr<<#x<<" = "<<x<<endl</pre>
#include <bits/stdc++.h>
using namespace std;
typedef long long ll;
template<typename _Tp>
_Tp fpow(_Tp base, _Tp exp, _Tp Mod) {
    _{Tp} res = 1;
    while (exp) {
        if (exp & 1)res = res * base % Mod;
        base = base * base % Mod;
        exp >>= 1;
    }
    return res;
}
/*
// O(MlogN) O(1) Large N,M prime Mod
```

```
template<typename _Tp, const int BCSize> //add Mod as parameter;
struct Binomial_Coefficient {
    _Tp fac[BCSize + 1];
    _Tp inv[BCSize + 1];
    _Tp Mod;
    inline Binomial_Coefficient(const int &m) {     //add Mod as
  parameter;
        fac[0] = 1;
        Mod = m;
        for (int i = 1; i <= BCSize; i++)</pre>
            fac[i] = fac[i - 1] * i % Mod;
        inv[BCSize] = fpow<_Tp>(fac[BCSize], Mod - 2, Mod);
        // printf inv[BCSize] to get & save it;
        for (int i = BCSize - 1; ~i; i--)
            inv[i] = inv[i + 1] * (i + 1) % Mod;
    }
    inline _Tp operator()(const int &n, const int &m) {
        return fac[n] * inv[m] % Mod * inv[n - m] % Mod;
    }
    inline _Tp operator()(int n, int m, const int &mod) {
        this->Mod = mod;//if change mod;
        _{Tp} res = 1;
        while (n | m)res = res * (*this)(n % Mod, m % Mod) % Mod, n /=
   Mod, m /= Mod;
        return res;
    }
};
typedef Binomial_Coefficient<long long, 10000000> zuHeShu;
zuHeShu\ C = zuHeShu(1000000007);
*/
//*****in normal writing style*******
```

```
const int MAXN = 1e6 + 59;
const int MOD = 1e9 + 7;
ll fac[MAXN];
ll inv[MAXN];
inline void initC(const int &sz) {
    fac[0] = 1;
    for (int i = 1; i <= sz; i++)
        fac[i] = fac[i - 1] * i % MOD;
    inv[sz] = fpow<ll>(fac[sz], MOD - 2, MOD);
    // printf inv[BCSize] to get & save it;
    for (<u>int</u> i = sz - 1; ~i; i--)
        inv[i] = inv[i + 1] * (i + 1) % MOD;
}
inline ll C(const int &n, const int &m) {
    return fac[n] * inv[m] % MOD * inv[n - m] % MOD;
}
// Lucas
inline ll C(int n, int m, const int &P) {
    ll res = 1;
    while (n | m)res = res * C(n % P, m % P) % P, n /= P, m /= P;
    return res;
}
int main() {
    initC(100000);
    cout << C(4, 3, 1000000007) << endl;
    cout << C(4, 1, 1000000007) << endl;
    //cout << C(2, 5) << endl;
    cout << C(5, 2, 1000000007) << endl;</pre>
    return 0;
```

} /\*

\* \*/

# 8 数学

## 8.1 矩阵快速幂+大十进制指数版.cpp

```
./code/数学/矩阵快速幂 + 大十进制指数版.cpp
#define _debug(x) cerr<<#x<<" = "<<x<<endl</pre>
#include <bits/stdc++.h>
using namespace
std;
typedef long long ll;
template<
typename _Tp,
const <u>int</u> MAXMatrixSize
struct Matrix {
    _Tp m[MAXMatrixSize][MAXMatrixSize];
    _{\text{Tp}} \mod = 0;
    Matrix() {
        memset(m, 0, sizeof m);
    }
    Matrix(int _mod) : mod(_mod) {
        memset(m, 0, sizeof m);
    }
```

```
void init1() {
        //*this = Matrix(mod);
        set(0, 0, 1);
        set(1, 1, 1);
//
           for (int i = 0; i < MAXMatrixSize; i++)</pre>
//
               m[i][i] = 1;
    }
    inline void set(const int
    &r, const <u>int</u> &c, const _Tp &v) { this->m[r][c] = v; }
    inline _Tp get(const int
    &r, const <u>int</u> &c) { return this->m[r][c]; }
    inline void setMod(const _Tp
    &_mod) { this->mod = _mod; }
    inline Matrix operator
    *(
    const Matrix t
    ) {
        Matrix res(mod);//= Matrix(mod);
         res.setMod(mod);
         for (int i = 0; i < MAXMatrixSize; i++)</pre>
             for (int j = 0; j < MAXMatrixSize; j++)</pre>
                 for (int k = 0; k < MAXMatrixSize; k++)</pre>
                      res.m[i][j] = (res.m[i][j] + m[i][k] * t.m[k][j])
   % mod;
        return res;
    }
};
typedef Matrix<ll, 2> mat;
mat A, B;
```

```
ll mo, len;
char n[1000059];
inline mat fpow(mat base, ll exp) {
    mat res(mo);
    res.init1();
    while (exp) {
        if (exp & 1)res = res * base;
        exp >>= 1;
        base = base * base;
    }
    return res;
}
inline ll calc() {
    len = strlen(n);
    //reverse(n, n + len);
    mat res(mo);
    res.init1();
    mat base = B;
    for (int i = len - 1; i >= 0; --i) {
        if (n[i] > '0')
            res = res * fpow(base, n[i] - '0');
        base = fpow(base, 10);
    }
    res = A * res;
    return res.get(0, 0);
}
//https://ac.nowcoder.com/acm/contest/885/B
/*
 * input n is a long char string.(1e6)
 * mo is global Mod.
 * other parameters are just Matrix elements.
```

```
*/
ll x0, x1, a, b;
int main() {
    scanf("%lld%lld%lld", &x0, &x1, &a, &b);
    scanf("%s %lld", n, &mo);
    A = mat(mo);
    A.set(0, 0, x0);
    A.set(0, 1, x1);
    B = mat(mo);
    B.set(0, 0, 0);
    B.set(0, 1, b);
    B.set(1, 0, 1);
    B.set(1, 1, a);
    printf("%lld\n", calc());
    return 0;
}
/*
```

## 8.2 fastFacterial 快速阶乘 分块 fft.cpp

\* \*/

```
./code/数学/fastFacterial 快速阶乘 分块 fft.cpp
// fastFacterial 快速阶乘 (分块 +fft)
// O( sqrt(n)log(n) )
```

```
// https://www.luogu.org/record/25477473
#include<cstdio>
#include<algorithm>
#include<cmath>
using namespace std;
typedef unsigned long long ll;
const ll N = 262144 + 10;
const int P = 65536;
const int SF = 16;
const int msk = 65535;
ll mod;
ll PP;
typedef long double ld;
const ld pi = acos(-1.0);
inline ll fpow(ll a, ll p) {
    ll r = 1;
    for (; p; p >>= 1, a = a * a % mod)
        if (p \& 1)r = r * a % mod;
    return r;
}
struct cmp {
    ld r;
    ld v;
    friend cmp operator+(cmp a, cmp b) {
        return (cmp) {a.r + b.r, a.v + b.v};
    }
    friend cmp operator-(cmp a, cmp b) {
        return (cmp) {a.r - b.r, a.v - b.v};
    }
    friend cmp operator*(cmp a, cmp b) {
        return (cmp) {a.r * b.r - a.v * b.v,
                       a.r * b.v + a.v * b.r;
```

```
}
    void operator/=(const int &len) {
         r /= len;
         v /= len;
} rt[2][22][N], tr[N],
         tr1[N], tr2[N], tr3[N],
         tr4[N], tr5[N], tr6[N];
int rv[22][N];
ll m13[N], m14[N], m23[N], m24[N];
inline void pre() {
    for (<u>int</u> d = 1; d <= 18; d++)
         for (<u>int</u> i = 1; i < (1 << d); i++)
              rv[d][i] = (rv[d][i >> 1] >> 1)
                           | ((i & 1) << (d - 1));
    for (int d = 1, t = 1; d <= 18; d++, t <<= 1)
         for (<u>int</u> i = 0; i < (1 << d); i++)
              rt[0][d][i] = (cmp) \{cos(pi * i / t),
                                      sin(pi * i / t);
    for (<u>int</u> d = 1, t = 1; d <= 18; d++, t <<= 1)
         for (int i = 0; i < (1 << d); i++)
              rt[1][d][i] = (cmp) {cos(pi * i / t),
                                      -\sin(pi * i / t);
}
inline <u>void</u> fft(cmp *a, <u>int</u> len, <u>int</u> d, <u>int</u> o) {
    for (int i = 1; i < len; i++)</pre>
         if (i < rv[d][i])
              swap(a[i], a[rv[d][i]]);
    cmp *w;
    <u>int</u> i;
    for (\underline{int} k = 1, j = 1; k < len; k <<= 1, j++)
         for (int s = 0; s < len; <math>s += (k << 1))
```

```
for (i = s, w = rt[o][j]; i < s + k; i++, ++w) {
                 cmp a1 = a[i + k] * (*w);
                 a[i + k] = a[i] - a1;
                 a[i] = a[i] + a1;
            }
    if (o)for (int i = 0; i < len; i++)a[i] /= len;</pre>
}
inline void dbdft(ll *a, int len, int d, cmp *op1, cmp *op2) {
    for (<u>int</u> i = 0; i < len; i++)
        tr[i] = (cmp) {(ld) (a[i] >> SF),
                        (ld) (a[i] & msk)};
    fft(tr, len, d, 0);
    tr[len] = tr[0];
    for (cmp *p1 = tr, *p2 = tr + len, *p3 = op1;
         p1 != tr + len; ++p1, --p2, ++p3)
        (*p3) = (cmp) \{p1->r + p2->r,
                        p1->v - p2->v
                 * (cmp) {0.5, 0};
    for (cmp *p1 = tr, *p2 = tr + len, *p3 = op2;
         p1 != tr + len; ++p1, --p2, ++p3)
        (*p3) = (cmp) \{p1->r - p2->r,
                        p1->v + p2->v
                 * (cmp) {0, -0.5};
}
inline void dbidft(cmp *tr, int len, int d, ll *a, ll *b) {
    fft(tr, len, d, 1);
    for (int i = 0; i < len; i++)
        a[i] = (ll) (tr[i].r + 0.5) \% mod;
    for (int i = 0; i < len; i++)</pre>
        b[i] = (ll) (tr[i].v + 0.5) \% mod;
}
```

```
inline void poly_mul(ll *a, ll *b, ll *c, int len, int d)//以上都是任意模数
→ fft 的板子
{
    dbdft(a, len, d, tr1, tr2);
    dbdft(b, len, d, tr3, tr4);
    for (<u>int</u> i = 0; i < len; i++)
        tr5[i] = tr1[i] * tr3[i]
                  + (cmp) \{0, 1\}
                    * tr2[i] * tr4[i];
    for (<u>int</u> i = 0; i < len; i++)
        tr6[i] = tr2[i] * tr3[i]
                  + (cmp) \{0, 1\}
                    * tr1[i] * tr4[i];
    dbidft(tr5, len, d, m13, m24);
    dbidft(tr6, len, d, m23, m14);
    for (int i = 0; i < len; i++)
        c[i] = m13[i] * PP \% mod;
    for (<u>int</u> i = 0; i < len; i++)
         (c[i] += (m23[i] + m14[i]) * P + m24[i]) %= mod;
}
namespace iter {
    ll f[N];
    ll g[N];
    ll h[N];
    ll ifac[N];
    inline void ih() {
        ifac[0] = ifac[1] = 1;
        for (ll i = 2; i < min(N, mod); i++)</pre>
             ifac[i] = (mod - mod / i) * ifac[mod % i] % mod;
        for (ll i = 1; i < min(N, mod); i++)</pre>
             (ifac[i] *= ifac[i - 1]) %= mod;
    }
    inline void calch(ll del, int cur, ll *ip, ll *op) {
```

```
int d = 0;
        int len = 1;
        while (len <= cur + cur + cur)len <<= 1, d++;</pre>
        for (int i = 0; i <= cur; i++)
             f[i] = ip[i] * ifac[i] % mod * ifac[cur - i] % mod;
        for (int i = cur - 1; i >= 0; i -= 2)
             f[i] = (mod - f[i]) \% mod;
        for (int i = 0; i <= cur + cur; i++)</pre>
             g[i] = fpow((del + mod - cur + i) \% mod, mod - 2);
        for (<u>int</u> i = cur + 1; i < len; i++)
             f[i] = 0;
        for (<u>int</u> i = cur + cur + 1; i < len; i++)
             g[i] = 0;
        poly_mul(f, g, h, len, d);//卷积求出 h'
        ll xs = 1;
        ll p1 = del - cur;
        ll p2 = del;
        for (ll i = p1; i <= p2; i++)(xs *= i) %= mod;
        for (ll i = 0; i <= cur; i++, p1++, p2++)//双指针求出系数
        {
             op[i] = h[i + cur] * xs % mod;
             (xs *= fpow(p1, mod - 2)) %= mod,
                      (xs *= (p2 + 1)) \% = mod;
        }
    }
}
ll val[N];
ll fv1[N];
ll fv2[N];
inline void solve(int n)//倍增
{
    int hb = 0;
    for (<u>int</u> p = n; p; p >>= 1)hb++;
    val[0] = 1;
    for (int z = hb, cur = 0; z >= 0; z--) {
        if (cur != 0)//把 d 乘 2
```

```
{
             iter::calch(cur + 1, cur, val, fv1);
             for (int i = 0; i <= cur; i++)</pre>
                 val[cur + i + 1] = fv1[i];
             val[cur << 1 | 1] = 0;</pre>
             iter::calch(cur * fpow(n, mod - 2) % mod,
                          cur << 1, val, fv2);</pre>
             cur <<= 1;
             for (int i = 0; i <= cur; i++)</pre>
                  (val[i] *= fv2[i]) %= mod;
        }
        if ((n >> z) & 1)//把 d 加 1
         {
             for (<u>int</u> i = 0; i <= cur; i++)
                  (val[i] *= (ll) (n * i) + cur + 1) %= mod;
             cur |= 1;
             val[cur] = 1;
             for (<u>int</u> i = 1; i <= cur; i++)
                  (val[cur] *= (ll) cur * n + i) %= mod;
        }
    }
}
int kase;
int main() {
    pre();
    int n;
    scanf("%d", &kase);
    while (kase--) {
         scanf("%d%lld", &n, &mod);
        iter::ih();//用了全局变量 mod
        int bl = sqrt(n);
        PP = (ll) P * P \% mod;
        solve(bl);
        ll res = 1;
        for (ll i = 0, id = 0;; i += bl, id++)//分块
```

```
{
             if (i + bl > n) {
                  for (\underline{int} \ j = i + 1; \ j <= n; \ j++)
                      (res *= j) %= mod;
                  break;
             (res *= val[id]) %= mod;
         printf("%lld\n", res);
    }
    return 0;//拜拜程序 ~
}
/*
3
16777216 998244353
2333333 19260817
1919810 2147481811
 "n and mod"
 */
```

### 8.3 double-compare.cpp

```
inline bool le(const double &x, const double &y) { return dcmp(x - y) <=</pre>
→ 0; }
inline bool eq(const double &x, const double &y) { return dcmp(x - y) ==
→ 0; }
inline bool ge(const double &x, const double &y) { return dcmp(x - y) >=
→ 0; }
inline bool gt(const double &x, const double &y) { return dcmp(x - y) >
→ 0; }
// not recommended
inline bool dcmp(const double &x, const string &mode, const double &y) {
    if (mode == "lt") return dcmp(x - y) < 0;
    if (mode == "le") return dcmp(x - y) <= 0;</pre>
    if (mode == "eq") return dcmp(x - y) == 0;
    if (mode == "ge") return dcmp(x - y) >= 0;
    if (mode == "gt") return dcmp(x - y) > 0;
    exit(0);
}
/* @tail of double-compare modules */
8.4 扩展 CRT.py
./code/数学/扩展 CRT.py
# https://ac.nowcoder.com/acm/contest/890/D
# maybe not available.
ai = [0]
bi = [0]
def exgcd(a, warrior, x, y):
```

```
if warrior == 0:
        x = 1
        y = 0
        return a, x, y
    gcd, x, y = exgcd(warrior, a % warrior, x, y)
    tp = x
    x = y
    y = tp - (a // warrior) * y
    return gcd, x, y
def excrt():
    m = bi[1]
    ans = ai[1]
    for i in range(2, num + 1):
        x = 0
        y = 0
        aa = m
        bb = bi[i]
        c = (ai[i] - ans \% bb + bb) \% bb
        gcd, x, y = exgcd(aa, bb, x, y)
        bg = bb // gcd
        if c % gcd != 0:
            return -1
        x = x * (c // gcd) % bg
        ans = ans + x * m
        m = m * bg
        ans = (ans % m + m) % m
    return (ans % m + m) % m
def main():
    global num
    num, m = map(int, input().split())
    # num, m = int(input())
    for i in range(1, num + 1):
        ub, ua = map(int, input().split())
```

```
bi.append(ub)
    ai.append(ua)

ans = excrt()

if ans == -1:
    print("he was definitely lying")

else:
    if ans <= m:
        print(ans)
    else:
        print("he was probably lying")

if __name__ == '__main__':
    main()</pre>
```