

附录：

```
format short e
```

```
a=0;b=pi;c=0;d=1;
```

```
N=input('请输入剖分数：');
```

```
h1 = (b-a)/N;
```

```
h2 = (d-c)/N;
```

```
n = N + 1 ;
```

```
x = linspace(a,b,n);
```

```
y = linspace(c,d,n);
```

```
%~~~~~精确解~~~~~%
```

```
ue = zeros(n-2,n-2);
```

```
for i = 1 : n-2
```

```
    for j = 1 : n-2
```

```
        ue(i,j) = 1/(9+pi^2)*cos(3*x(i+1))*sin(pi*y(j+1));
```

```
    end
```

```
end
```

```
%矩阵变向量
```

```
UE = reshape(ue',[],1);
```

```
%~~~~~数值解~~~~~%
```

```
%右端项
```

```
f = zeros(n-2,n-2);
```

```
for j = 1:n-2
```

```
    for i = 1:n-2
```

```
        f(i,j) = cos(3*x(i+1))*sin(pi*y(j+1));
```

```
    end
```

```
end
```

```
F = reshape(f',[],1); %矩阵变向量
```

```
%创建系数矩阵
```

```
h12 = 1/h1^2;
```

```
h22 = 1/h2^2;
```

```
E = eye(n-2);%单位矩阵
```

```
B = (h12+h22)*E - h12*diag(ones(1,n-3), 1)...  
    - h12*diag(ones(1,n-3),-1);
```

```
C = (h12+h22)*E - h22*diag(ones(1,n-3), 1)...  
    - h22*diag(ones(1,n-3),-1);
```

```
%考虑边界条件
```

```
B(1,1) = 1/2*h12 + h22;
```

```
B(n-2,n-2) = 1/2*h12 + h22;
```

```
%获得系数矩阵
```

```
A = kron(B,E)+kron(E,C);
```

```
%求解
```

```
U = A\F;
```

```
e = abs(UE - U);
```

```
u = reshape(U,n-2,n-2)';
```

```
norm = norm(e);%L2 范数
```

```
max = max(e);%无穷范数
```