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CS 47

11/15/18

1a.  $F(x,y,z) = x'z + xy = x'y'z + yz + xy$

Boolean Expression	Identity
$x'y'z + yz + xy$	
$x'y'z + (1)yz + xy$	
$x'y'z + (x + x')yz + xy$	$1 = x + x'$
$x'y'z + xyz + x'yz + xy$	Distributive
$x'(y'z + yz) + xy(z + 1)$	Distributive 2x
$x'(z(y + y')) + xy(1)$	Distributive and $z + 1 = 1$
$x'(z(1)) + xy$	Simplify and $y + y' = 1$
$x'z + xy$	Simplify

1b.  $F(a,b,d) = a'b'c'd' + a'b'cd + a'b'cd' + ab'c'd' + ab'cd' + ab'cd = b'(c+d')$

Boolean Expression	Identity
$a'b'c'd' + a'b'cd + a'b'cd' + ab'c'd' + ab'cd' + ab'cd$	
$a'b'c(d + d') + ab'c(d' + d) + a'b'c'd' + ab'c'd'$	Distributive 2x
$a'b'c(1) + ab'c(1) + a'b'c'd' + ab'c'd'$	$d + d' = 1$
$a'b'c + ab'c + a'b'c'd' + ab'c'd'$	Simplify
$b'c(a' + a) + b'c'd'(a' + a)$	Distributive 2x
$b'c(1) + b'c'd'(1)$	$a + a' = 1$
$b'c + b'c'd'$	Simplify
$b'(c + c'd')$	Distributive
$b'((c + c')(c + d'))$	Distributive
$b'(1(c+d'))$	$c + c' = 1$

$b'(c+d')$	Simplify
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1c. LHS

x	y	z	$x'$	$x'z$	xy	$x'z + xy$
0	0	0	1	0	0	0
0	0	1	1	1	0	1
0	1	0	1	0	0	0
0	1	1	1	1	0	1
1	0	0	0	0	0	0
1	0	1	0	0	0	0
1	1	0	0	0	1	1
1	1	1	0	0	1	1

RHS

x	y	z	$x'$	$y'$	$x'y'z$	yz	xy	$x'y'z + yz + xy$
0	0	0	1	1	0	0	0	0
0	0	1	1	1	1	0	0	1
0	1	0	1	0	0	0	0	0
0	1	1	1	0	0	1	0	1
1	0	0	0	1	0	0	0	0
1	0	1	0	1	0	0	0	0
1	1	0	0	0	0	0	1	1
1	1	1	0	0	0	1	1	1

LHS = RHS

$x'z + xy$	$x'y'z + yz + xy$
0	0
1	1
0	0
1	1
0	0
0	0
1	1
1	1

1d.

LHS

a	b	c	d	a'	b'	c'	d'	a'b' c'd'	a'b' cd	a'b' cd'	a b' c'd'	ab'c d'	ab'c d	a'b'c'd' + a'b'cd + a'b'cd' + ab'c'd' + ab'cd' + ab'cd
0	0	0	0	1	1	1	1	1	0	0	0	0	0	1
0	0	0	1	1	1	1	0	0	0	0	0	0	0	0
0	0	1	0	1	1	0	1	0	0	1	0	0	0	1
0	0	1	1	1	1	0	0	0	1	0	0	0	0	1
0	1	0	0	1	0	1	1	0	0	0	0	0	0	0
0	1	0	1	1	0	1	0	0	0	0	0	0	0	0
0	1	1	0	1	0	0	1	0	0	0	0	0	0	0

0	1	1	1	1	0	0	0	0	0	0	0	0	0	0
1	0	0	0	0	1	1	1	0	0	0	1	0	0	1
1	0	0	1	0	1	1	0	0	0	0	0	0	0	0
1	0	1	0	0	1	0	1	0	0	0	0	1	0	1
1	0	1	1	0	1	0	0	0	0	0	0	0	1	1
1	1	0	0	0	0	1	1	0	0	0	0	0	0	0
1	1	0	1	0	0	1	0	0	0	0	0	0	0	0
1	1	1	0	0	0	0	1	0	0	0	0	0	0	0
1	1	1	1	0	0	0	0	0	0	0	0	0	0	0

RHS

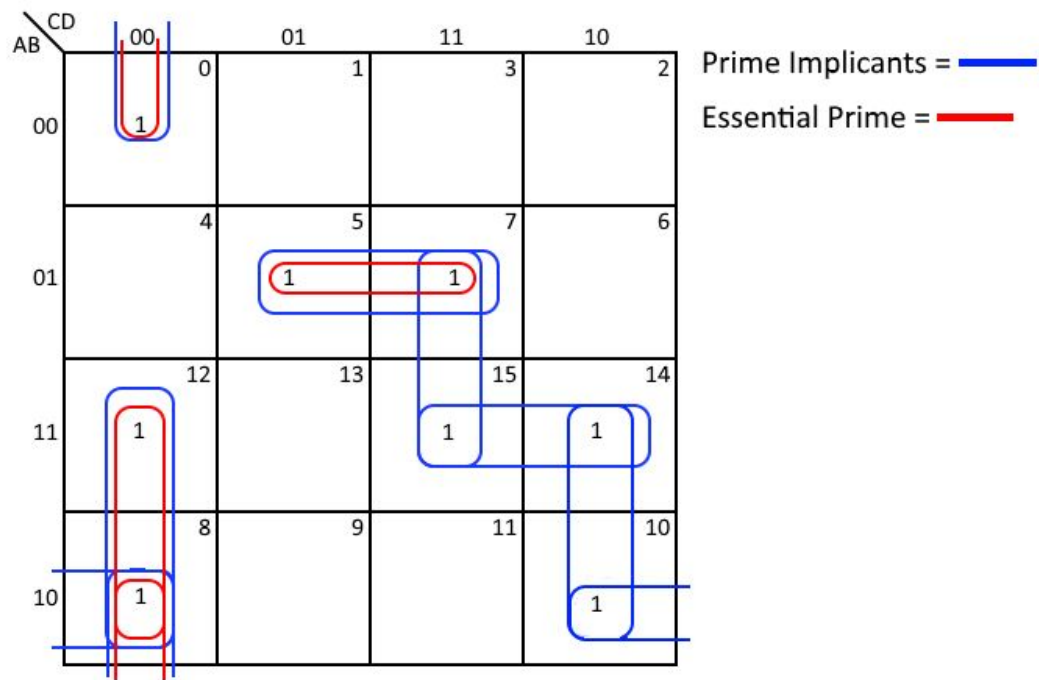
a	b	c	d	b'	d'	c+d'	b'(c+d')
0	0	0	0	1	1	1	1
0	0	0	1	1	0	0	0
0	0	1	0	1	1	1	1
0	0	1	1	1	0	1	1
0	1	0	0	0	1	1	0
0	1	0	1	0	0	0	0
0	1	1	0	0	1	1	0
0	1	1	1	0	0	1	0
1	0	0	0	1	1	1	1
1	0	0	1	1	0	0	0
1	0	1	0	1	1	1	1
1	0	1	1	1	0	1	1
1	1	0	0	0	1	1	0
1	1	0	1	0	0	0	0

1	1	1	0	0	1	1	0
1	1	1	1	0	0	1	0

LHS = RHS

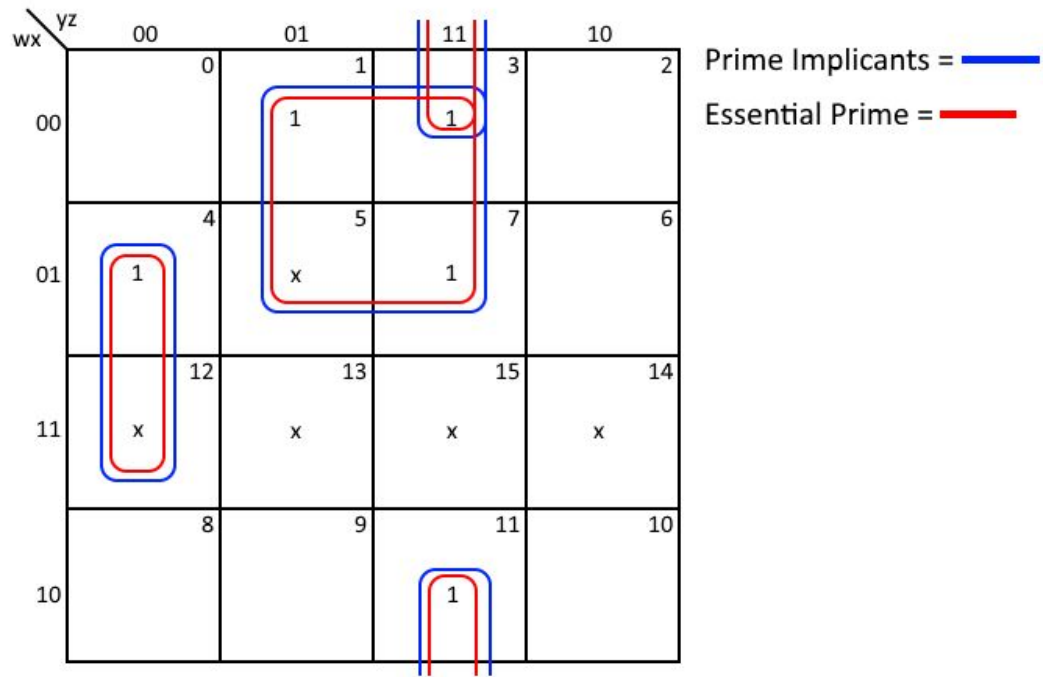
$a'b'c'd' + a'b'cd + a'b'cd' + ab'c'd' + ab'cd' + ab'cd$	$b'(c+d')$
1	1
0	0
1	1
1	1
0	0
0	0
0	0
0	0
1	1
0	0
1	1
1	1
0	0
0	0
0	0
0	0

2a.



$$\begin{aligned}
 F(ABCD) &= A'B'C'D' + AB'C'D' + AB'C'D' + ABC'D' + A'BC'D + A'BCD + \\
 &\quad ABCD + ABCD' + AB'CD' + ABCD' \\
 &= B'C'D'(A' + A) + AC'D'(B' + B) + A'BD(C' + C) + ABC(D + D') + \\
 &\quad ACD'(B' + B) \\
 &= B'C'D' + AC'D' + A'BD + ABC + ACD'
 \end{aligned}$$

2b.



$$\begin{aligned}
 F(wxyz) &= w'xy'z' + wxy'z' + w'x'y'z + w'x'yz + w'xy'z + w'xyz + w'x'yz + wx'yz \\
 &= xy'z'(w' + w) + w'x'z'(y' + y) + w'xz'(y' + y) + x'yz(w' + w) \\
 &= xy'z' + w'z'(x' + x) + x'yz \\
 &= xy'z' + w'z' + x'yz
 \end{aligned}$$

3.

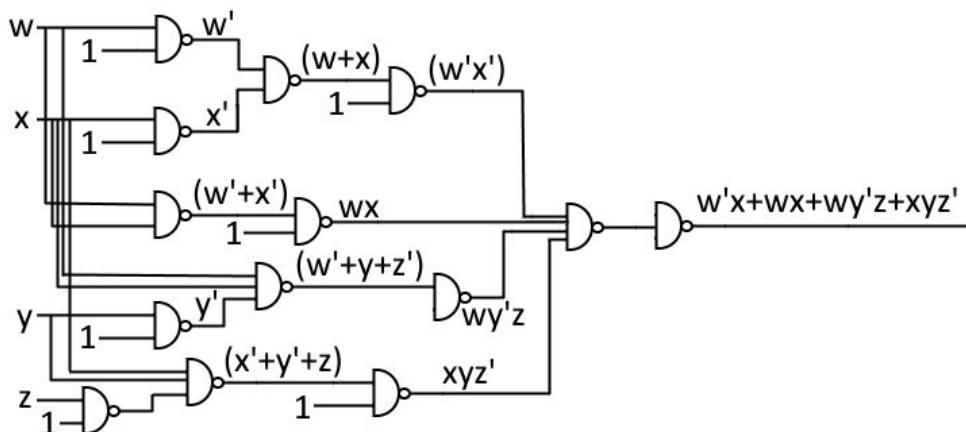
Decimal number	w	x	y	z	$F(w,x,y,z)$
0	0	0	0	0	1
1	0	0	0	1	1
2	0	0	1	0	1
3	0	0	1	1	1
4	0	1	0	0	0
5	0	1	0	1	0
6	0	1	1	0	1
7	0	1	1	1	0
8	1	0	0	0	0
9	1	0	0	1	1
10	1	0	1	0	0
11	1	0	1	1	0
12	1	1	0	0	1
13	1	1	0	1	1
14	1	1	1	0	1
15	1	1	1	1	1



$$\Sigma m(0,1,2,3,6,9,12,13,14,15)$$

xw \ yz	yz			
	00	01	11	10
00	0 1	1 1	3 1	2 1
01	4	5	7	6 1
11	12 1	13 1	15 1	14 1
10	8	9 1	11	10

$$F(w,x,y,z) = w'x' + wx + wy'z + xyz'$$



4.

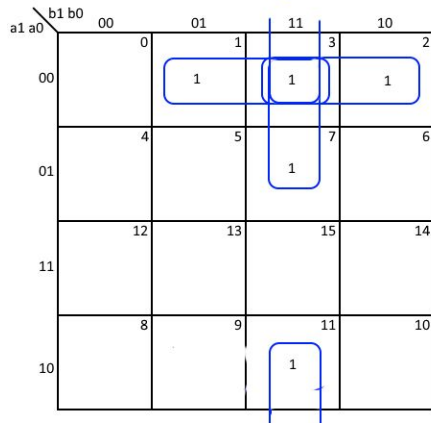
$a_1$	$a_0$	$b_1$	$b_0$	L	E	G
0	0	0	0	0	1	0
0	0	0	1	1	0	0
0	0	1	0	1	0	0
0	0	1	1	1	0	0
0	1	0	0	0	0	1
0	1	0	1	0	1	0
0	1	1	0	0	1	0
0	1	1	1	1	0	0
1	0	0	0	0	0	1
1	0	0	1	0	1	0
1	0	1	0	0	1	0
1	0	1	1	1	0	0
1	1	0	0	0	0	1
1	1	0	1	0	0	1
1	1	1	0	0	0	1
1	1	1	1	0	1	0

L:  $\Sigma_m(1,2,3,7, 11)$

E:  $\Sigma_m(0,5,6,9,10,15)$

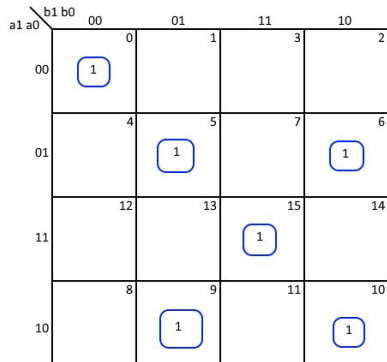
G:  $\Sigma_m(4,8,12,13,14)$

L K-Map



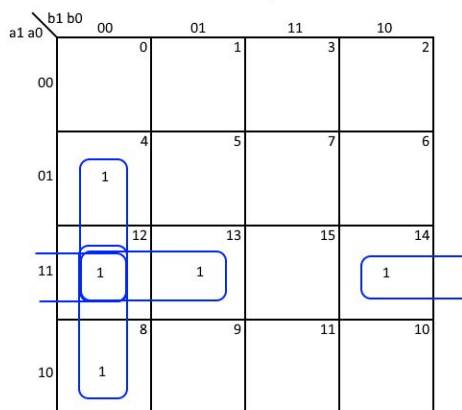
$$L(a_1, a_0, b_1, b_0) = a_1' a_0' b_0 + a_1' a_0' b_1 + b_1 b_0 a_1' + b_1 b_0 a_0'$$

E K-Map



$$E(a_1, a_0, b_1, b_0) = a_1' a_0' b_1' b_0' + a_1' a_0 b_1' b_0 + a_1' a_0 b_1 b_0' + a_1 a_0' b_1' b_0 + a_1 a_0' b_1 b_0' + a_1 a_0 b_1 b_0$$

G K-Map



$$G(a_1, a_0, b_1, b_0) = a_0 b_1' b_0' + a_1 b_1' b_0' + a_1 a_0 b_1' + a_1 a_0 b_0'$$

