

Problems

1. $x = 4$
2. $f(x,y) = 9x^2 - 2y^2$ & $f'(x,y) = 4 - 4y$

3. A. No

B. Rank = 3

$$[-4, 2, -6]$$

$$[-1, -4, 3]$$

$$[14, 9, 3]$$

$$[-1, \frac{1}{2}, -\frac{3}{2}]$$

$$[-1, -4, 3]$$

$$[14, 9, 3]$$

$$[1, -\frac{1}{2}, \frac{3}{2}]$$

$$[0, -\frac{9}{2}, \frac{9}{2}]$$

$$[14, 9, 3]$$

$$[14, -7, 21]$$

$$[0, -\frac{9}{2}, \frac{9}{2}]$$

$$[14, 9, 3]$$

$$[1, -\frac{1}{2}, \frac{3}{2}]$$

$$[0, -\frac{9}{2}, \frac{9}{2}]$$

$$[0, 16, -18]$$

$$[-4, 2, -6]$$

$$[0, -\frac{9}{2}, \frac{9}{2}]$$

$$[0, 16, -18]$$

$$[-4, 2, -6]$$

$$[0, 1, -1]$$

$$[0, 16, -18]$$

$$[-4, 2, -6]$$

$$[0, 16, -16]$$

$$[0, 16, -18]$$

$$[-4, 2, -6]$$

$$[0, 1, -1]$$

$$[0, 0, -2]$$

$$[-4, 2, -6]$$

$$[0, -\frac{9}{2}, \frac{9}{2}]$$

[0,0,-2]

[-4,2,-6]

[0,-9/2,9/2]

[0,0,-2]

C. (Graduate Students)

4. **Simple Gaussian:** $f(x) = ae^{\frac{(x-b)^2}{2\sigma^2}}$

Multivariate Gaussian: $f(x,y) = A \exp\left(-\left(\frac{(x-x_0)^2}{2\sigma_x^2} + \frac{(y-y_0)^2}{2\sigma_y^2}\right)\right)$

Bernoulli Distribution: $P(n) = p^n (1-p)^{1-n}$

Binomial Distribution: $P_p(n|N) = \binom{N}{n} p^n q^{N-n}$
$$= \frac{N!}{n! (N-n)!} p^n (1-p)^{N-n},$$

Exponential Distribution: $P(x) = D'(x) = \lambda e^{-\lambda x}.$

5. (Graduate Students)

6.