

Question 2: Enzyme Kinetics

8.1

$$V(E) = k_2 [ES] + k_3 [ES] - k_1 [E] [S]$$

$$V(S) = k_2 [ES] - k_1 [E] [S]$$

$$V(P) = k_3 [ES]$$

$$V(ES) = k_1 [E] [S] - k_2 [ES] - k_3 [ES]$$

8.2

```
import numpy as np
```

```
import matplotlib.pyplot as plt
```

```
from scipy.integrate import solve_ivp
```

```
# set the initial paramters
```

```
k1=100
```

```
k2=600
```

```
k3=150
```

```
E0=1
```

```
S0=10
```

```
#V = [E,S,ES,P]^T variable set
```

```
F = lambda t, V: np.array([-k1*V[0]*V[1]+(k2+k3)*V[2],-k1*V[0]*V[1]+k2*V[2],k1*V[0]*V[1]-  
(k2+k3)*V[2],k3*V[2]]) # ODEs
```

```
t_eval = np.arange(0, 0.5, 0.001) # t span
```

```
sol = solve_ivp(F, [0, 0.5], [E0, S0, 0, 0], t_eval=t_eval) # solve the ODE by fourth RK method,  
it is defaulted in solve_ivp func
```

```
# plot the concentration of the four species vs. time
```

```
plt.figure(figsize = (12, 4))
```

```
plt.subplot(221)
```

```
plt.plot(sol.t, sol.y[0])
```

```
plt.xlabel('t/min')
```

```
plt.ylabel('E')
```

```
plt.subplot(222)
```

```
plt.plot(sol.t, sol.y[1])
```

```
plt.xlabel('t/min')
```

```
plt.ylabel('S')
```

```
plt.subplot(223)
```

```
plt.plot(sol.t, sol.y[3])
```

```
plt.xlabel('t/min')
```

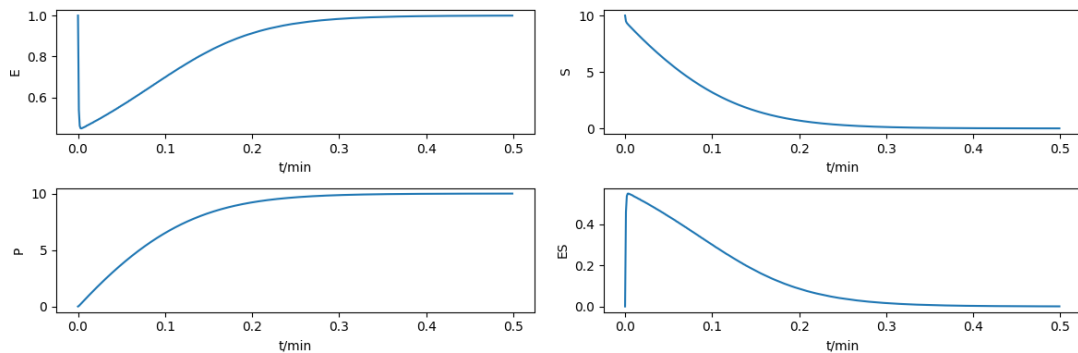
```
plt.ylabel('P')
```

```
plt.subplot(224)
```

```
plt.plot(sol.t, sol.y[2])
```

```
plt.xlabel('t/min')
```

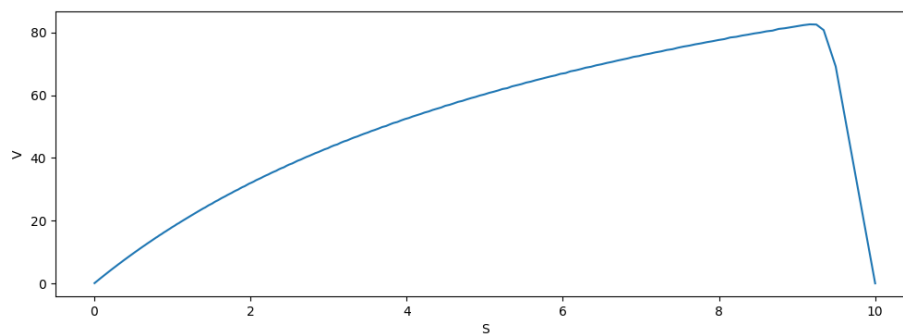
```
plt.ylabel('ES')
plt.tight_layout()
plt.show()
```



8.3

plot the velocity of P vs. the concentration of S

```
plt.figure(figsize = (12, 4))
plt.plot(sol.y[1],k3*sol.y[2])
plt.xlabel('S')
plt.ylabel('V')
plt.show()
```



The V_m is approximately 82 $\mu\text{M}/\text{min}$.