Final Ti Model Results

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1 Objective Function

 $\begin{array}{l} {\rm PARAMETERS\:fdd=}0.1958363809\:qdds=}0.5591275855\:qddp=}0.5690351902\\ {\rm qddd=}0.7745947522\:b0=}58.0906936439\:p0=}1.2185323579\:b1=}.3.2299188646\\ {\rm p1=}0.6862915307\:b2=}593519.1134129359\:m2=}-11.50000000000\:p2=}0.0000000000\\ {\rm ndt=}2.0000000000\:cr1=}-6.0000000000\:cr2=}3.0474400934\:cr3=}-1.2317472193\\ {\rm r1dd=}6.50000000000\:crdd=}10.0000000000\:rmaxhm=}10.1000000000\:npar=}18\\ {\rm VARGS\:-vfdd=}0.1958363809\:-vqdds=}0.5591275855\:-vqddp=}0.5690351902\:-vqddd=}0.7745947522\:-vb0=}58.0906936439\:-vp0=}1.2185323579\:-vb1=}-3.2299188646\\ {\rm -vp1=}0.6862915307\:-vb2=}593519.1134129359\:-vm2=}-11.50000000000\:-vp2=}0.0000000000\\ {\rm -vndt=}2.00000000000\:-vcr1=}-6.00000000000\:-vcr2=}3.0474400934\:-vcr3=}-1.2317472193\\ {\rm -vv1dd=}6.50000000000\:-vcrdd=}10.00000000000\:-vcmaxhm=}10.10000000000\\ \end{array}$

Quantity	From Model	Target
a_{hcp}	5.58523112	5.57678969
$\mathrm{c/a}$	1.58371266	1.58731122
$a_{\rm omega}$	8.93475285	8.73254342
$c_{ m omega}$	5.38726911	5.32343103
a_{4h}	5.57584691	5.56325146
$\mathrm{c_{4h}}$	18.09810672	17.75908031
a_{6h}	5.57365569	5.54639384
c_{6h}	27.18378460	26.77136353
a_{bcc}	6.20079768	6.17948863
a_{fcc}	7.87290654	7.88677000
DE(o,h)	0.58764167	-0.63343333
DE(4h,h)	1.58019500	3.17160000
DE(6h,h)	2.48264833	3.72005000
DE(b,h)	5.35128500	7.63520000
DE(f,h)	3.78088500	4.51880000
c_{11}	171.60928873	176.10000000
c_{33}	198.90063708	190.50000000
c_{44}	47.42549704	50.80000000
c_{12}	94.65941969	86.90000000
c_{13}	61.22624060	68.30000000
$M_{\rm freq0}$	2.59341377	2.85858719
$M_{\rm freq1}$	2.59341378	2.85858719
$M_{\rm freq2}$	2.59341378	2.85858719
$M_{\rm freq3}$	2.59341379	2.85858719
$M_{\rm freq4}$	5.85272461	5.66706047
$M_{\rm freq5}$	5.85272461	5.66706047
$H_{\rm freq0}$	3.82320403	4.80643423
${ m H_{freq1}}$	3.82320403	5.58010025
$H_{\rm freq2}$	6.40288977	5.65316738
H_{freq3}	6.40288977	6.36651842
$H_{\rm freq4}$	7.92857431	6.40050186
$H_{\rm freq5}$	7.92857431	7.64082373
bandw. G	3.69394702	5.87085872
bandw. K	4.65178817	4.97424321
bandw. M	5.19329495	7.78109872
bandw. L	4.21232412	6.34433701
bandw. H	3.54700549	9.70902614
$\mathrm{DOSerr_{h}}$	0.00000000	0.00000000
$\mathrm{DOSerr}_{\mathrm{o}}$	0.00000000	0.00000000
E_{prisf}	98.95340236	220.000000000

- E_{prismatic fault}

98.953tbe:

 $\frac{\mathrm{mJ/m^2}}{\mathrm{mJ/m^2}}$ DFT: 250.000 [Benoit 2012] mJ/m^2 233.000 [Ackland 1999] DFT:

- E_{Basalfault} I2 —

211.658 tbe:

 $\frac{\mathrm{mJ/m^2}}{\mathrm{mJ/m^2}}$ [Benoit 2012] DFT: 260.000

2 **Defect Clusters**

- E_{vacancyformation}

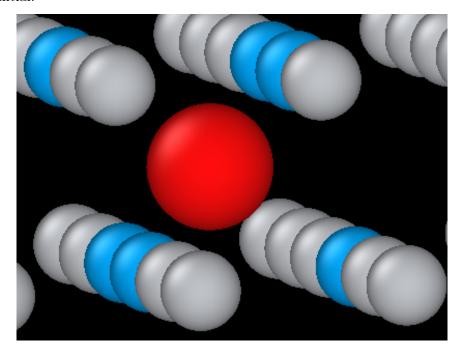
 $2.347~\mathrm{eV}$ tbe:

GGA-PAW: Angsten (2013) DFT: $1.950~\mathrm{eV}$

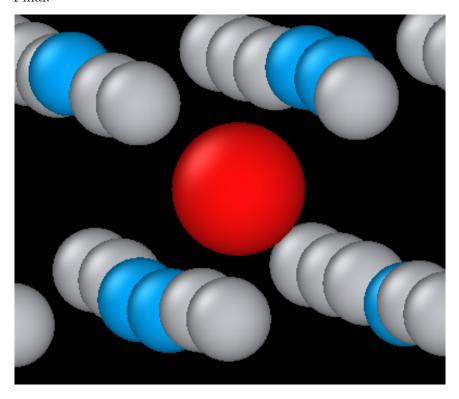
Hashimoto (1984) exp: $1.270~\mathrm{eV}$

Octahedral O interstitial relaxation 2.1

Initial:

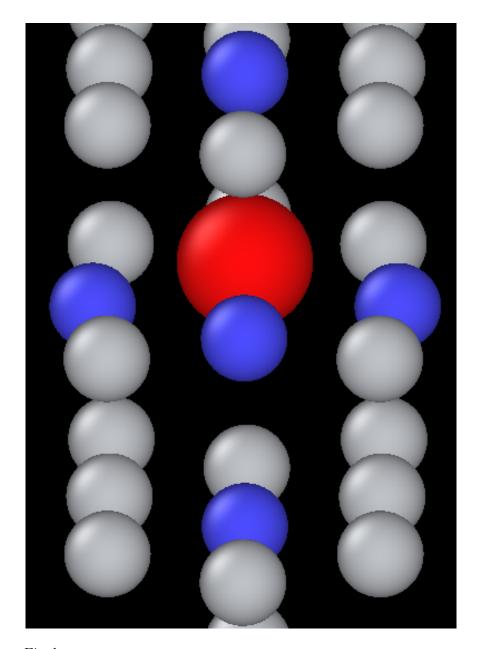


Final:

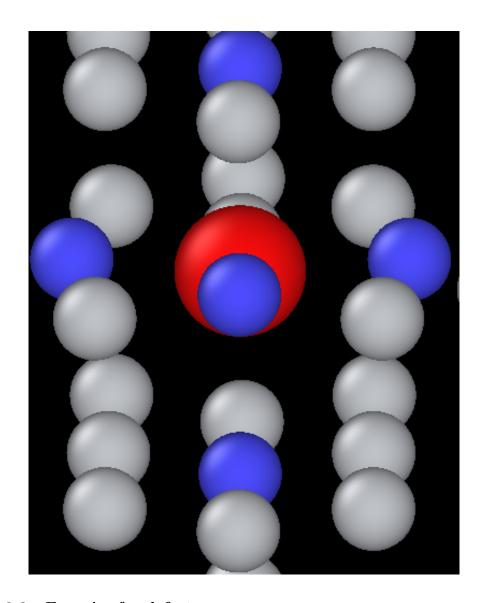


 ${\bf 2.2}\quad {\bf Tetrahedral}\ {\bf O}\ {\bf interstitial}\ {\bf relaxation}$

Initial:



Final:



2.3 Energies for defects

Relative differences are

» ($E_{tetrahedral}$ - $E_{octahedral}$)

tbe: 1.65 eV

GGA-DFT: 1.23 eV Kwasniak (2013)

» ($E_{hexahedral}$ - $E_{octahedral}$)

tbe: 0.90 eV

> Note: Preference for tetrahedral oxygen to go into hexahedral site as seen by images above

All formation energies below use the chemical potential of Akysonov (2013) of value $\mu_{\rm oxygen}=\frac{5.6}{2}eV$.

2.4 All formation energies

Quantity	Energy (eV)
$\mathrm{Ef}_{\mathrm{Vf}}$	2.347
$\mathrm{Ef}_{\mathrm{Tsol}}$	- 21.783
$\mathrm{Ef}_{\mathrm{Osol}}$	- 23.436
$\mathrm{Ef}_{\mathrm{OOsol}}$	- 49.606
$\mathrm{Ef}_{\mathrm{OOosol}}$	- 76.037
$\mathrm{Ef}_{\mathrm{OOOsol}}$	- 102.470
$\mathrm{Ef}_{\mathrm{OOOOsol}}$	- 128.781
$\mathrm{Ef}_{\mathrm{OOOOosol}}$	- 155.148
$\mathrm{Ef}_{\mathrm{Tdilimp}}$	- 28.991
$\mathrm{Ef}_{\mathrm{Odilimp}}$	- 30.645
$\mathrm{Ef}_{\mathrm{OOdilimp}}$	- 56.814
$\mathrm{Ef}_{\mathrm{OOdilimp}}$	- 83.246
Ef _{OOOdilimp}	- 109.679
Ef _{OOOOdilimp}	- 135.989
Efooooodilimp	- 162.357
•	
$\mathrm{Ef}_{\mathrm{Tformation}}$	- 21.783
$\mathrm{Ef}_{\mathrm{Oformation}}$	- 23.436
Ef _{OOformation}	- 46.806
$\mathrm{Ef}_{\mathrm{OOOformation}}$	- 70.437
$\mathrm{Ef}_{\mathrm{OOOformation}}$	- 94.070
$\mathrm{Ef}_{\mathrm{OOOOformation}}$	- 117.581
$\mathrm{Ef}_{\mathrm{OOOOOformation}}$	- 141.148
$\mathrm{Ef}_{\mathrm{TVformation}}$	- 18.905
$\mathrm{Ef}_{\mathrm{OV} \mathrm{formation}}$	- 18.905
$\mathrm{Ef}_{\mathrm{OOV} \mathrm{formation}}$	- 41.910
$\mathrm{Ef}_{\mathrm{OOV}}$ formation	- 66.013
$\mathrm{Ef}_{\mathrm{OOOV}}$ formation	- 88.998
Ef _{OOOOV} formation	- 113.649
$\mathrm{Ef_{OOOOV}_{formation}}$	- 137.110
$\mathrm{Ef}_{\mathrm{Tvac}}$ solbind	- 0.530
$\mathrm{Ef}_{\mathrm{Ovac}_{\mathrm{solbind}}}$	- 2.183
$\mathrm{Ef}_{\mathrm{OOvac}}$ solbind	- 2.547
$\mathrm{Ef}_{\mathrm{OO}\mathrm{vac}\mathrm{sol}\mathrm{bind}}$	- 2.076
Ef _{OOOOvacsolbind}	- 2.724
Ef _{OOOOOvacsolbind} 10	- 1.583
$\mathrm{Ef}_{\mathrm{OOOOOvac}}$	- 1.690

3 Gamma surfaces

Energies are accurate to within 2 mJm⁻², comparing the energies of points in the corners which (the zeros of energy). So surface energies might be ± 2 mJm⁻² off which is reasonable.

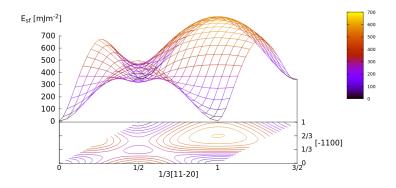
These calculations were done in tight binding with 15 layers for both basal and prismatic. The k-points for the prismatic gamma surfaces were, and for basal they were. DFT comparisons are usind results of Rodney.

The Pyramidal surface was obtained using the same 32 atom cell that Ready used in his paper on the pyramidal gamma surface with DFT pseudopotentials.

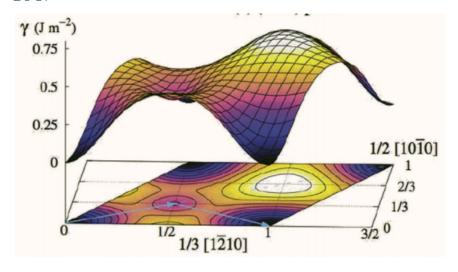
Stacking Fault Energy $[mJm^{-2}]$ Prismatic
Basal I_2 Basal
Pyramidal I

3.1 Basal

TBE:

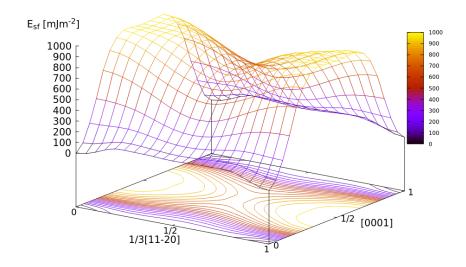


DFT:

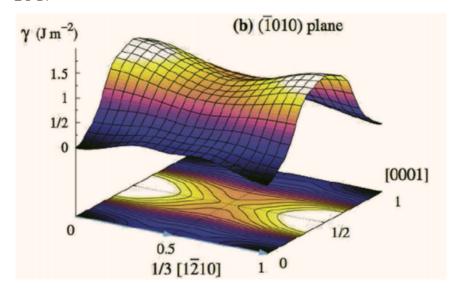


3.2 Prismatic

TBE:

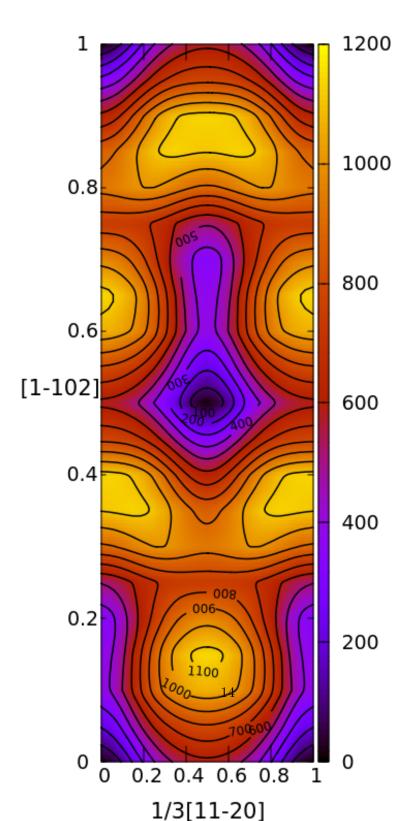


DFT:

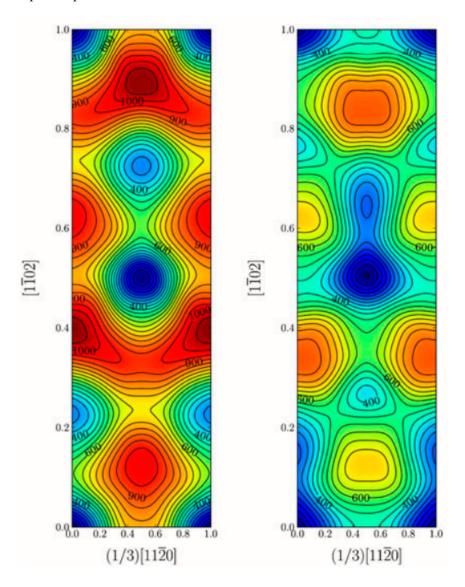


3.3 Pyramidal first order

TBE:



DFT pseudopot:



3.4 Data

 ${\rm basal_{gsdata}\ prismatic_{gsdata}\ pyramidal_{gsdata}}$

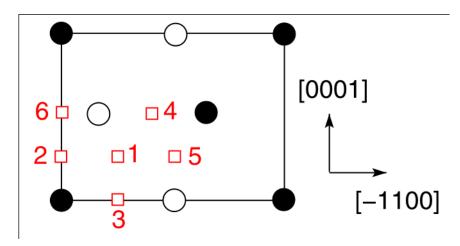
4 Dislocation core structures

4.1 Quadrupolar Array

4.1.1 Methodology

In the following, we see results of dislocation relaxation. The partial differential displacement maps are of dislocations in their initial and final states in different initial positions. The burger's vector seen in these plots is the partial $1/6[11\bar{2}0]$. The original dislocation, of burger's vector $1/3[11\bar{2}0]$, should dissociate into two dislocations on the primatic plane, each with burger's vector $1/6[11\bar{2}0]$. The atoms were relaxed until the root-mean square force acting on each atom was less than 4×10^{-5} Ryd/Bohr.

These relaxations can be distinguished by the different initial positions of the dislocation centre (elastic centre) as following the paper by Tarrat [1]. Cell geometry was 16x16x1, where the unit cell was of four atoms, with x, y and z axes given by [0001], $[\bar{1}100]$ and $1/3[11\bar{2}0]$ respectively.



A quadrupolar array of dislocations was created using the "S" arrangement of Clouet [2]: the cut plane of the dislocation dipole is aligned along the diagonal of the cell; dislocations of the same helicity are found on the same x and y planes. This was found to give more satisfactory results for Peierls barrier calculations (the "O" configuration—where the dipole cut plane is parallel to the x axis—resulted in the peierls barrier increasing with cell size, whereas the opposite was found for the "S" arrangement). Displacements for each of the dislocations were determined by solutions to the anisotropic elasticity equations.

To accommodate for the plastic strain introduced with the addition of a dislocation dipole in the simulation cell, an elastic strain was applied, resulting in the tilting of the principal lattice vectors.

To satisfy periodic boundary conditions, periodic displacements were calculated from the superposition of displacements from a 30x30 array of dislocation dipoles, with the subtraction of the spurious linear term due to the conditional convergence of the sum [3].

4.1.2 Discussion

One can see that all of the dislocations have dissociated on the prismatic plane. But there is a difference between initial positions as to upon which prismatic plane they dissociate on, from the original.

None of these states have dissociated onto the proposed pyramidally spread ground state that is proposed by Clouet [4].

Only initial position 2 actually dissociated on a different prismatic plane to the others.

The positions of the partials are also different once each of the separate initial positions have been relaxed.

IP2 and IP3, although they are on different planes, have a very similar core structure to each other. They are both asymmetric cores.

IP1 has the upper partial dislocation located within an adjacent triangle to the left, compared to IP2 and IP3. The lower partial has been shifted downwards, by one triangle down and to the right, with respect to IP3. The core structure of IP5 is indistinguishable from IP1. These cores can be deemed as metastable, as they have a slightly higher energy than the other cores.

The upper partial of IP4 has been displaced upwards by one Peierls valley with respect to IP3. The lower partial is in the same triangle as IP3. IP4 is a mirrored core.

Each of these cores are asymmetric, using the definition by Tarrat [1]. The energies for each of the dislocation cores, when relaxed to 1×10^{-5} Ryd/Bohr is

Initial position	E_{total} [Ryd]
1	-331.54658899
2	-331.54660063
3	-331.54660053
4	-331.54660061
5	-331.54658717

The dissociation distance is consistent between the different initial positions of the elastic centres. The distance is $\approx 4c = 35.4$ Bohr = 18.7, this is double the distance seen in Ghazisaedi and Trinkle [5] and double the distance that is found in the DFT Zr results by Clouet [2].

TODO Dissociation Distance Analysis

Following [2], one can dislocation elasticity theory to compute the dissociation distance of a dislocation in both the basal and prism planes. The energy variation caused by a dissociation length d is

$$\Delta E_{\text{diss}}(d) = -b_i^{(1)} K_{ij} b_j^{(2)} \ln\left(\frac{d}{r_c}\right) + \gamma d,$$

where $\mathbf{b}^{(i)}$ are the burger's vectors of the dissociated dislocations. γ is the corresponding gamma surface energy and K is the Stroh matrix. Controlling the dislocation core radius and the dislocation elastic energy, one can find the equilibrium dissociation distance as

$$d^{\text{eq}} = \frac{b_i^{(1)} K_{ij} b_j^{(2)}}{\gamma}$$

With the orientation of the simulation cell as, $U_1 = na_{\overline{2}}^{1}[10\overline{1}0], U_2 =$ mc[0001], $U_3 = a\frac{1}{3}[1\bar{2}10]$, one finds the components of the Stroh matrix as:

$$K_{11} = \frac{1}{2\pi} (\bar{C}_{11} + C_{13}) \sqrt{\frac{C_{44} (\bar{C}_{11} - C_{13})}{C_{33} (\bar{C}_{11} + C_{13} + 2C_{44})}}$$
(1)

$$K_{22} = \sqrt{\frac{C_{33}}{C_{11}}} K_{11} \tag{2}$$

$$K_{22} = \sqrt{\frac{C_{33}}{C_{11}}} K_{11}$$

$$K_{33} = \frac{1}{2\pi} \sqrt{\frac{1}{2} C_{44} (C_{11} - C_{12})}$$
(2)

here, $\bar{C}_{11} = \sqrt{C_{11}C_{33}}$.

From the gamma surface, for the basal plane one expects a dissociation of $1/3[1\bar{2}10] = 1/3[1\bar{1}00] + 1/3[0\bar{1}10]$. Then dissociation length in the basal plane is given by

$$d_{\rm b}^{\rm eq} = \frac{(3K_{33} - K_{11})a^2}{12\gamma_{\rm b}}$$

For the prism plane the $1/3[1\bar{2}10]$ dislocation can dissociate into $1/6[1\bar{2}10]\pm \alpha(c/a)[0001]$ where the parameter α controls the position of the stacking fault minimum along the [0001] direction. Only in interatomic potentials like the EAM, do we find that $\alpha = 0.14$.

The dissociation length is

$$d_{\rm p}^{\rm eq} = \frac{(K_{33}a^2 - 4\alpha^2 K_{22}c^2)}{4\gamma_p}$$

1. Analysis with Final Ti model.

$$d_{\rm p}^{\rm eq} = \frac{(K_{33}a^2 - 4\alpha^2 K_{22}c^2)}{4\gamma_n}$$

Using the above equation to calculate the dissociation distance with $K_{33}=6.79853~{\rm GPa}=6.79853/160.21766208~{\rm eV/\mathring{A}^3}=0.042433087~{\rm eV/\mathring{A}^3},~\alpha=0~{\rm and}~\gamma_{\rm p}=98.95340236~{\rm mJm^{-2}}=1.6021766208*10^{-19}*10^{-3}*10^{20}*98.95340236~{\rm eV/\mathring{A}^3}~\$=1.58540827809\$~{\rm eV/\mathring{A}^3},~\alpha=2.955577~{\rm we}$ have the equilibrium dissociation distance in the prismatic plane as $d_{\rm p}^{\rm eq}=0.05845~\mathring{\rm A},$ which seems very small, comparing to the differential displacement maps. . .

Further scrutiny is necessary.

4.1.4 TODO Disregistry Analysis

Look into the theory of dissociation distance in Clouet paper [2]

Disregistry given by the Peierls-Nabarro model. Analytic expression given in Hirth and Lothe [6].

Disregistry D(x) is defined as the displacement difference between the atoms in the plane just above and those just below the dislocation glide plane. The derivative of this function $\rho(x) = \partial D/\partial x$ corresponds to the dislocation density.

$$D_{\text{dislo}} = \frac{b}{2\pi} \left\{ \arctan \left[\frac{x - x_0 - d/2}{\zeta} \right] + \arctan \left[\frac{x - x_0 + d/2}{\zeta} + \frac{\pi}{2} \right] \right\}$$

Given x_0 is the dislocation position, d is dissociation length and ζ is the spreading of each partial dislocation.

$$D_{L} = \sum_{n=-\infty}^{\infty} D_{\text{dislo}}(x - nL)$$

$$= \frac{b}{2\pi} \left\{ \arctan\left[\frac{\tan\left(\frac{\pi}{L}[x - x_{0} - d/2]\right)}{\tanh\left(\frac{\pi\zeta}{L}\right)}\right] + \pi \left\lfloor \frac{x - x_{0} - d/2}{\zeta} + \frac{1}{2} \right\rfloor + \arctan\left[\frac{\tan\left(\frac{\pi}{L}[x - x_{0} + d/2]\right)}{\tanh\left(\frac{\pi\zeta}{L}\right)}\right] + \pi \left\lfloor \frac{x - x_{0} + d/2}{\zeta} + \frac{1}{2} \right\rfloor \right\},$$

where $|\cdot|$ is the floor function.

For an array of dislocations in the S arrangement, $D(x) = D_L(x)$, with L = mc, where m is the number of repeated unit cells in the U_2 direction.

Here, $U_1 = na\frac{1}{2}[10\bar{1}0]$, $U_2 = mc[0001]$, $U_3 = a\frac{1}{3}[1\bar{2}10]$.

Therefore, using this, one can fit the three fitting parameters: the dislocation position x_0 , the dissociation length d, and the spreading ζ . This procedure allows us to determine the location of the dislocation center.

From the Peierls-Nabarro model of an edge dislocation, one finds that the displacement in x $u_x = -\frac{b}{2\pi} \tan^{-1} \frac{x}{\zeta}$, where $\zeta = d/2(1-\nu)$, where the width of the dislocation is 2ζ , where the disregistry is one-half the maximum value at x=0.

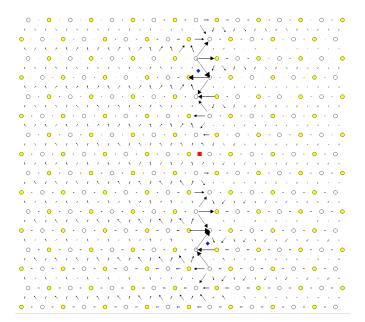
For a screw dislocation, one essentially replaces ζ with $\eta=(1-\nu)\zeta=d/2$ For all interaction models, we find that this center lies in between two (0001) atomic planes. One can see in Fig. 6 of [2] that this position corresponds to a local symmetry axis of the differential displacement map. This is different from the result obtained by Ghazisaeidi and Trinkle [5] in Ti where the center of the screw dislocation was found to lie exactly in one (0001) atomic plane.

4.1.5 IP1

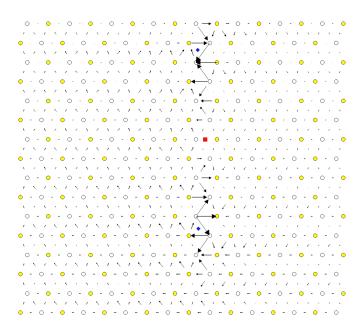
4.1.6 IP2

→○ - ○ - ○ · ○ · ○ · ○ · ○ _0 - 0 - 0 - 0 • - 0 - • - 0 - • - 0 - • - 0 - 0 - 0 - 0 - 0 - 0 - 0

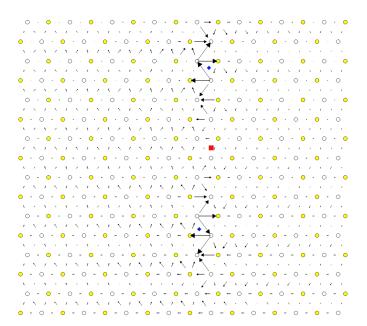
4.1.7 IP3



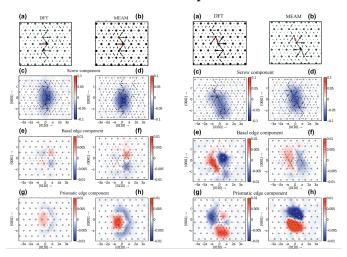
4.1.8 IP4



4.1.9 IP5



4.1.10 Ghazisaeidi Results for comparison



4.1.11 TODO Replot all dislocations and do analysis in Atomman.

This will be very useful as one can see plots of the Nye tensor, so one can truly see where the partials are and their dislocation centres.

4.1.12 Peierls Stress

By straining the cell of a relaxed lattice and incrementally increasing the strain, one can find the minimum stress necessary to move a dislocation from one Peierls valley to the next.

1. Applying strain

Applying strain as in [7].

Here we are incrementing the strain by $0.001C^{\text{rot}}$, where C^{rot} is the transformed elastic constant necessary for transforming a strain into a stress from the relation $\sigma_{ij} = C_{ijkl}\varepsilon_{kl}$.

The original elastic constant matrix in its untransformed state is:

	[171.6093	94.6594	61.2262	0.	0.	0.
	94.6594	171.6093	61.2262	0.	0.	0.
C -	61.2262	61.2262	198.9006	0.	0.	0.
C =	0.	0.	0.	47.4255	0.	0.
	0.	0.	0.	0.	47.4255	0.
	0.	0.	0.	0.	0.	38.4749

Transforming it into the dislocation coordinate system, by the rotation

$$R = \begin{bmatrix} 1 & 0 & 0 \\ 0 & 0 & -1 \\ 0 & 1 & 0 \end{bmatrix}$$

$$C^{\rm rot} = \begin{bmatrix} 171.6093 & 61.2262 & 94.6594 & 0. & 0. & 0. \\ 61.2262 & 198.9006 & 61.2262 & 0. & 0. & 0. \\ 94.6594 & 61.2262 & 171.6093 & 0. & 0. & 0. \\ 0. & 0. & 0. & 47.4255 & 0. & 0. \\ 0. & 0. & 0. & 0. & 38.4749 & 0. \\ 0. & 0. & 0. & 0. & 0. & 0. & 47.4255 \end{bmatrix}$$

For finding the Peierls stress to move partials away from each other on the prismatic plane plane one finds that the stress if given by $\sigma_{xy} = \sigma_{12} = 2C_{66}^{\text{rot}} \varepsilon_{12}$, where $C_{66}^{\text{rot}} = 47.4255$ GPa.

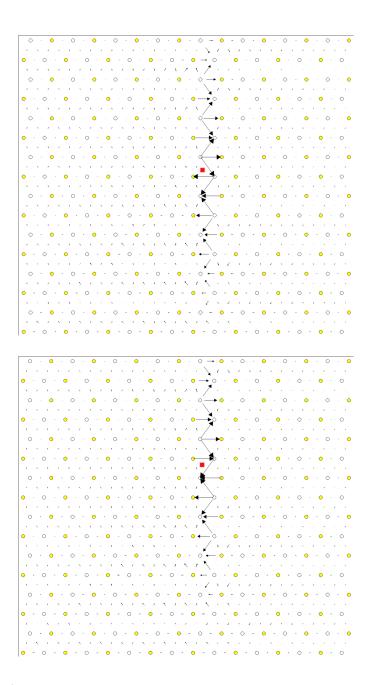
To move the whole dislocation on the prismatic plane, one needs a stress applied which is $\sigma_x z = \sigma_{13} = 2C_{55}^{\rm rot} \varepsilon_{13}$, $C_{55}^{\rm rot} = 38.4749$ GPa.

To move the dislocation onto the basal plane one needs to apply as stress given by $\sigma_y z = \sigma_{23} = 2C_{44}^{\rm rot} \varepsilon_{23}$, $C_{44}^{\rm rot} = 47.4255$ GPa.

2. xz Strain

Applying an xz strain to the lattice causes the dislocation to move along the prismatic plane.

Using an increment in the strain of $1 \times 10^{-4} C^*$, where C^* is the transformed elastic constant, with a value of $C_{44}^* = 38.4749$ GPa, we find that the dislocation moves from one Peierls valley along the prismatic plane at $0.0012 C_{44}^*$, giving a Peierls stress of $\sigma_x z = 2 C_{44} \varepsilon_{xz} = 0.0923$ GPa



3. yz Strain

This is the strain necessary for movement on the basal plane. Following the procedure above, one does not obtain recombination of partials, or any movement of the dislocation onto the basal plane.

Increasing the accumulated strain up to $10\backslash 0.001$ C to see if there is any difference.

Furthermore, one is starting from initial anisotropic elasticity solutions, applying strain and then relaxing, such that one may be able to find a strain where the screw dislocation has spread in the basal plane.

4. xy strain

An xy strain can move the partials of the prismatic plane apart.

One can find the Peierls stress for these single partials to move in opposite directions.

Here the α parameter is 0.03.

This means that the stress necessary to move the partial dislocations apart is

$$\sigma_{12} = C_{1212}\varepsilon_{12}$$

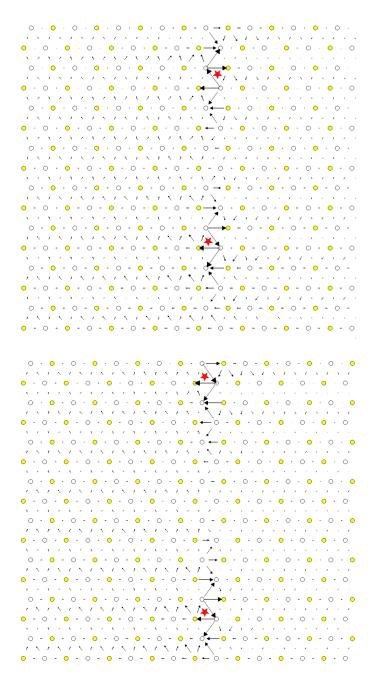
$$= 2C_{66}^{\text{Voigt}} \varepsilon_{6}^{\text{Voigt}}$$

$$= (C_{11} - C_{12})\varepsilon_{6}^{\text{Voigt}}$$

$$= 47.4255 \times 0.03$$

$$= 1.42GPa$$

The strain is applied to the whole cell, as the dislocation cell is periodic, then the stress upon each partial is the same.



5. Pyramidal Strain

For a strain to transform the dislocation into the metastable, pyramidal state, one can apply a strain which applies shear to the dislocation

whereby the maximum resolved shear stress is on the first-order pyramidal plane.

In the coordinate system of the dislocation, one can estimate the strain necessary by the ratio of stresses for the basal and prismatic planes. The proportions strains σ_{xz} and σ_{yz} should be $c/a:\sqrt{3}/2\approx 1.83:1\approx 1:0.54683$.

Unfortunately, this proportion does not work, nor does the ratio σ_{xz} : $\sigma_{yz} \approx 1$: 1/10\$. A much, much lower proportion of the strain is necessary as the dislocation just moves prismatically. Once one finds the Peierls stress for the basal plane, we can estimate a more realistic proportion.

4.1.13 Data

IP1 IP2 IP3 IP4 IP5

4.1.14 Directory of the results

file:///home/tigany/Documents/ti/2019-09-11_final_model/tbe/dislocations/2019-11-08_no_omega_ordering_ec_latpar/file:///home/tigany/Documents/ti/final_model_2019-11

4.2 Cluster Method

4.2.1 Methodology

This secton comprises the results of using the cluster method to simulate single dislocations in the Ti model.

The cluster method simulates dislocations by only imposing periodicity in the direction of the dislocation line (the z-axis, in this case).

As the number of atoms in a cluster increases, the resulting core structure upon relaxation will tend to the bulk core structure, as there is a reduction in the spurious dislocation-surface interaction. Due to the finite size of simulations, the geometry of the cell is important. With sufficient cell size, dislocation core structure should be invariant to the boundary conditions imposed. To ascertain how sensitive the new Ti model is to boundary conditions, two different cell geometries were used: circular and hexagonal. Each of these had two layers of fixed (inert) atoms around a dynamic central region.

All relaxations were carried out using the Fletcher-Powell conjugate gradient algorithm with a force twolerance of 4×10^{-5} Ryd/Bohr $\approx1\times10^{-3}$ eV/, with a k-point mesh of 1x1x30.

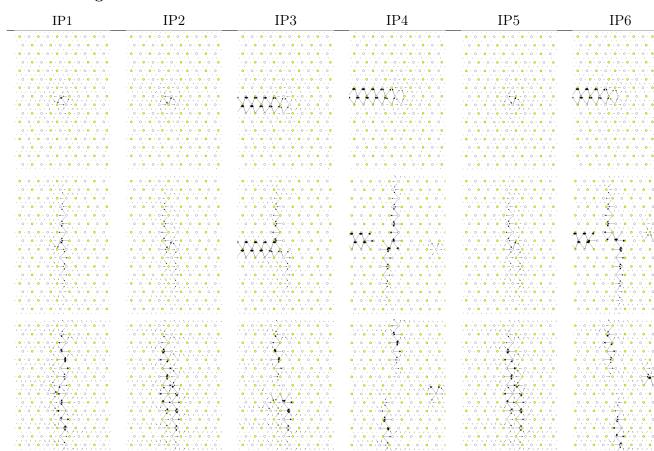
Tarrat [1] deemed that the use of hexagonal cluster cell geometries were more beneficial to determine the core structure of dislocations due to a lower total surface energy, implying a reduction in the magnitude of dislocation-surface interaction.

Upon relaxation of a circular and a hexagonal cell, of 936 and 1082 atoms respectively, the time for the dynamic region of the core of the dislocation to relax was approximately 1.5 times that of using a circular (≈ 43500 seconds to ≈ 28800). The number of steps for the relaxation algorithm to reach tolerance was one less for the hexagonal cell, to the circular cell (195 to 196 steps). Given the cubic scaling of direct-diagonalisation tight-binding, one would expect that the increase in time for these to cells to be $(1082/936)^3 \approx 1.5$, which is exactly what is seen.

4.2.2 Circular Cluster

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4.2.3 Hexagonal Cluster



5 Binding energies to dislocations

A strategy to find the binding energies of different interstitial sites.

- 1. Find cores of the dislocation using my in-house differential displacement map analysis.
- 2. Identify octahedral sites near the cores.
- 3. Translate octahedral sites from the perfect lattice to the lattice with a dislocation by the average displacement of the six surrounding lattice sites. .

- 4. Put the solute into a given interstitial site such that upon application of the transformation of lattice from one dislocation core to another (upon rotation and reflection), the interstitial is in an equivalent position. (If one were to look at each dislocation in with the burgers vector pointing into the page, the site should be equivalent.)
- 5. Relax and find the binding energy by calculating the difference in energy from the relaxed dislocation to the unrelaxed.

5.1 Dissolution Energy Equation

The binding energy of oxygen to a dislocation can be given by the following equation:

$$E_{\text{O-disl.}}^{\text{sol}} = E_{\text{disl}+n\text{O}} - E_{\text{disl}} - \frac{n}{2}E_{\text{O}_2}$$

Here, the energy of molecular oxygen $E_{\rm O_2}/2$ is -5.6eV/atom from Aksyonov 2016 [8].

5.2 Current status of simulation

An S-arrangement of dislocation dipoles what created in a 12x12 supercell of 576 atoms oriented such that the $1/3[11\bar{2}0]$ direction was parallel to the z axis. The dislocation cores were in the initial position 5 (IP5) and relaxed.

The cell was augmented by two extra periodic images in the z-direction, creating a 12x12x3 cell of 1728 atoms.

Oxygen was put into octahedral sites in increasing distance from each of the cores. The distance was up to four octahedral sites from the core along the prismatic plane and four prismatic planes along. This gives 16 sites from which one can extract the dependence of the dislocation binding energy with distance from the dislocation core.

These will provide references for the embedding calculations. It is hoped that embedding will give more accurate answers due to:

- 1. There only being one dislocation in an embedding cell:
 - Dislocation strain fields are long-ranged, therefore one can expect errors due the the additional dislocation-dislocation interaction upon relaxation.

6 BOP

6.1 4 recursion levels

kbT = 0.1

» Lattice parameters:

> hcp

a 2.901660 Å c 4.747485 Å etot -18.342162 eV

> omega

 $\begin{array}{lll} a & 7.917318 \ \mathring{A} \\ c & 2.749892 \ \mathring{A} \\ etot & -17.458700 \ eV \end{array}$

Omega is still not as stable as hcp as expected from model.

» Elastic Constants

Quantity	calc. (10^{11} Pa)	exp. (10^{11} GPa)
C11	1.781	1.761
C12	0.738	0.868
C13	0.611	0.682
C33	1.969	1.905
C44	0.285	0.508
C66	0.522	0.450
K	1.050	1.101
R	0.669	0.618
Н	0.558	0.489

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