# Multi-scale investigation of dislocation mediated carbon migration in iron

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#### Abstract

We investigate the validity of a dislocation-assisted carbon migration mechanism underpinning the formation of dark etching regions in bearing steels undergoing high-cycle fatigue through use of a multi-scale approach: from quantum mechanics, to stochastic simulations. We start from tight binding simulations of  $1/3\langle111\rangle$  screw dislocations to obtain the 2-d Peierls potential and Fe-C binding energies. These become ingredients for a line-tension model of the  $1/3\langle111\rangle$  screw dislocation to obtain the kink-pair formation energy as a function of stress and carbon concentration. Finally, 3-d kinetic Monte-Carlo simulations of dislocations in an environment of carbon are used to ascertain which temperature and stress regimes dislocation-assisted carbon migration is a valid mechanism.

## 1 Introduction

• What is the DER?

- How is it formed?
- What does carbon binding to dislocations have to do with its formation?
  - What mechanisms are at play?
  - Where is the crux of the argument?
- How does/will atomistic modelling help?
- What simulations do I do to figure this out?

Martensitic steels are frequently used in bearings due to their resilience to service conditions, being subject to high rotational speeds and contact pressures. However, under cyclic loading exceeding a given contact stress, the microstructure of the steel can decay due to the accumulation of plasticity. This signals the onset of rolling cycle fatigue (RCF), which increases the risk of failure from subsurface crack initiation. The microstructural decay corresponds to the observation of Dark Etching Regions (DERs) as seen in optical microscopy, where the darkness of the images is due to the higher reactivity of the phases which compose the DER region to the etchant; exacerbated by the roughness of the DER region.

The degradation of the martensitic microstructure is due to a process of carbon migration driven by plasticity-induced dislocation glide [CITATION]. The martensite is transformed to ferrite (microband and elongated forms) through this process. Residual carbides, untouched at the start of DER formation, gradually dissolve as a result of highly localized plasticity. RCF progression leads to the formation of low and high angle ferrite features, composed from the microband and elongated ferrite. Carbon atoms segregate from the martensitic matrix and (partially) dissolved residual carbides, to form lenticular carbides between these ferrite bands.

However, there is no consensus on where carbon migrates to with the onset of DER formation: where does excess carbon from the martensitic matrix find itself, when the structure decays to low solubility (0.02%) ferrite. It is not known whether carbon atoms inside the martensite are transported towards the transition carbides, a mechanism proposed by Fu et al. [1, 2], or if they segregate to the boundaries of ferrite microbands/elongated ferrite.

Probing the fundamental mechanisms behind DER formation experimentally have proven difficult and inconclusive. A multi-scale modelling approach can shed light on the fundamental mechanisms behind DER formation. Atomistics can provide information of the Peierls energy landscape of dislocations in iron; and how this landscape is modified by the binding of carbon to dislocations. This data can be used in a line tension model, to ascertain the kink-pair nucleation energies of dislocations as a function of carbon content and stress. Finally, one can use a kinetic Monte Carlo model of dislocation kink-pair nucleation in an environment of carbon to determine in what regimes of temperature, stress and carbon concentration, dislocation-assisted carbon migration becomes a feasible mechanism behind DER formation, and what happens to the dislocations how does carbon move in these regimes.

With this work as a foundation, one should be able to compare the affinity of carbon to dislocations/grain boundaries: specifically carbides and grain boundaries, clarifying if carbides grow, as in the theory by Fu, or if they dissolve, as some optical data suggests.

Fu et al. propose that most carbon is initially segregated to dislocations in martensite. Strain generated by pulsating stresses allow dislocations to escape their carbon rich environment. The dislocations, now free, re-attract carbon, allowing the Cottrell atmosphere to reform, subsequently pinning the dislocations. This creates a net carbon flux, which according to their theory, would segregate to carbides, increasing their size. However this is at odds with theory: if carbides were to form in martensite, they should follow the Bagaryatskii/Isaichev orientation relationship. Carbides formed within the DER region have an irregular shape, which must be due to the incomplete dissolution of residual carbides, which is at odds with the theory of carbide growth.

We propose that dislocations are crucial in all aspects of DER formation. Observation of DERs are related to dislocation configurations at a particular number of stress cycles with the added interactions of dissolved carbon. Tempered and residual carbides dissolve upon interaction with dislocations. The carbon atoms that are trapped by the dislocations can cause pinning, affecting their movement and rearrangement. Dislocation models are able to explain the hardening and softening characteristics with application of contact pressure. With further knowledge of the fundamental mechanism behind DER formation, we can surpress dislocation motion in the initial martensitic matrix.

As RCF continues, ferrite microbands decay to nanocrystalline ferrite. At the later stages of RCF, there is a reduction in dislocation density within the grain boundaries of nanocrystalline ferrite, which reduces the solubility of carbon, causing the formation of lenticular carbides around the ferrite bands.

Smelova proposes that the formation of ferrite phases are the result of recrystallisation processes, which also bring doubt upon the work of Fu et al..

- Maybe explain the reasoning behing Fu's conclusion
- Why are other observations more reasonable?
- Where do my simulations fit into this?
  - Segregation energies of carbon do dislocation to cause transport
  - This can lead to a comparison of segregation energies between ferrite boundaries and carbides eventually (relative to carbon trapped in dislocations in bcc iron).

Due to the high dislocation density of martensite, all dissolved carbon is segregated to dislocations—which also pin the dislocations. With applied stress, the dislocations become unpinned and mobile. Dislocations multiply/annihilate; with annihilation, carbon becomes in ordinary solution, which is available to diffuse. This diffusion causes the formation of ferritic microbands. The process of annihilation needs to be understood.

Hedman/Slycke propose that the degradation of the DER can by described by the growth of carbides, where the carbide sized are described by Ostwald ripening, and carbon diffuses both thermally and mechanically by dislocation glide.

Slycke proposes a creep deformation based mechanism which is controlled by vacancies produced by the climb of dislocations.

#### 1.1 Mechanisms

There are many proposed mechanisms for DER formation.

Bush proposes that DER formation is governed by an exchange of material between the carbides and the matrix, which is evidenced by the formation of intrusions/extrusions within the microstructure.

Swahn proposes that the transformation mechanisms which lead to the formation of new features in DER are due to the redistribution of carbon present in the initial microstructure, which in solution in the martensite, and due to the dissolution of carbides.

They further detail that initially, stress induced carbon diffusion leads to the diffusion of carbon from the martensitic lattice to the various defects in the material (mainly dislocations). As plastic deformation accumulates, the movement of dislocations creates carbon rich grain boundary-type interfaces.

It is not certain what role and timescale the dissolution of carbides occurs on.

High operating temperatures are known to accelerate DER formation.

In early stage DER formation, there is a high density of ferrite microbands. Later, regions of homogeneous nanocrystalline ferrite (heavily deformed ferrite) are formed in a cell-like structure.

# 2 Computational Method

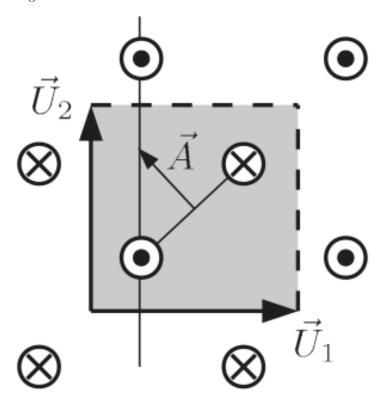
- Use tight-binding model of Paxton and Elsaetter [3].
- Generate dislocations using anisotropic elasticity theory.
- Create clusters of dislocations in both easy and hard core configurations.
- Place carbon in octahedral sites around the core
- Calculate corrections (ZPE etc)

## 3 Results

#### 3.1 Peierls Potential

To determine the Peierls potential, we followed the procedure detailed in Itakura [4]. Quadrupolar arrays of dislocations were constructed by placing dislocations of antiparallel  $1/2\langle111\rangle$  Burgers vectors in an "S" arrangement [5] ??, with initial displacements determined by the anisotropic elasticity solutions. These displacements were modified to be periodic, thereby removing artificial stacking faults which would appear between periodic images after the introduction of the dipole. This was achieved by the subraction of a linear error term from the superposition of displacement fields arising from the dislocations in the simulation cell and its periodic images [6]. To accommodate for the internal stress upon introduction of the dislocation dipole into a simulation cell, an elastic strain was imposed on the cell, resulting in an extra tilt component being added to the cell vectors [5, 6]. Simulation cells were constructed with different initial core positions, which were sampled from the triangular region "EHS" (easy, hard and split) core positions, as detailed in 1. To fix the dislocation positions during

relaxation, the three atoms surrounding the easy core, for each dislocation, were fixed during relaxation.



The interaction energy between the dislocation dipole and periodic images was defined differently to that of Itakura's. We followed the prescription of Bulatov and Cai [6] to find a regularised interaction energy, which is independent of truncation limit, in contrast to the formulas quoted in Itakura's papers [4]. In isotropic elasticity, the elastic energy of a single dislocation dipole in an infinite lattice is given by

$$E_{\rm el}^{\rm inf} = \frac{\mu b^2}{4\pi} ln(\frac{r}{r_c})$$

The contribution from periodic images to the correction is

$$E_{\rm img} = E_{\rm el}(\mathbf{a}, \mathbf{c}_i, r_c) - E_{\rm el}^{\rm inf}(\mathbf{a}, r_c)$$

where

$$E_{\text{img}=\sum_{\mathbf{R}}' E_{\text{dd}}(\mathbf{R}),}$$

where  ${f R}$  is a sum over dislocation dipoles in the periodic images exclusively.

$$E_{\rm dd}(\mathbf{R}) = \frac{\mu b^2}{2\pi} \ln \frac{|\mathbf{R}|^2}{|\mathbf{R} + \mathbf{a}| \cdot |\mathbf{R} - \mathbf{a}|}$$

"Ghost" dipoles are introduced to account for the conditional convergence of the sum at  $\pm \alpha \mathbf{b}$  and  $\pm \beta \mathbf{b}$ , where  $\alpha = \beta = 0.5$ .

The Peierls potential can be calculated by subtraction of the interaction energy of the dislocations in the periodic array, from the energy of the easy core configuration, which is the ground-state dislocation core configuration.

$$\Delta E_{\rm P} = \Delta E^{\rm tbe} - \Delta E_{\rm INT}$$

Comparison of 2d Peierls potentials of the  $1/2\langle 111\rangle$  screw dislocation between DFT can by found in [4]. Data was interpolated using 2d cubic splines. "E", "H" and "S" correspond to easy, hard and split core positions respectively, with the latter also corresponding to atomic positions. The relative energies between the different core positions is smaller in tight-binding compared to DFT; most notably, the energies. This is an artifact in the model, which has been validated in NEB calculations of the  $1/2\langle 111\rangle$  screw dislocation Peierls barrier, as calculated with NEB, is roughly half that when compared to DFT ref Luke's Thesis. The split core as seen in tight-binding is reminiscent of EAM potentials, where the split core energy is lower than that of the hard core, but first, to check that this is so, one must check that the interaction energy between dislocations follows Bulatov and Cai.

This may be attributed to lack of core electron repulsion, resulting from the sd-iron tight-binding model.

Pos	$\Delta E_{ m INT}$	$\Delta E_{\mathrm{tbe}}$	$\Delta E_{\mathrm{P}}$	$\Delta E_{ m P}^{ m DFT}$
1	0	0	0	0
2	-0.7	7.3	7.9	3.2
3	-1.4	16.0	17.4	19.2
4	-2.0	22.2	24.2	31.1
5	-2.5	24.8	27.4	39.3
6	-3.3	3.0	6.3	11.5
7	-6.5	7.1	13.6	39.9
8	-9.6	13.0	22.6	75.2
9	-12.5	5.4	17.9	108.9
10	-4.8	22.1	26.9	34.8
11	-7.2	18.2	25.4	37.9
12	-9.8	14.0	23.8	60.7
13	-3.8	11.5	15.3	17.6
14	-6.9	15.1	22.0	29.9
15	-4.3	18.6	22.9	39.7

#### 3.2 Hard and easy core relaxations

To determine the binding energy of carbon to dislocations, we used the cluster method; where the simulation cells consist of a circular cluster of atoms, split into two regions, with a single dislocation introduced into the centre by using the anisotropic elasticity solutions. Each of the clusters were centred on the easy or hard core positions. The cluster of atoms was split into two regions: a central region of dynamic atoms with radius  $R_1$ , and an annulus of atoms, between  $R_1$  and  $R_2$ , which were fixed to the anisotropic elasticity solutions.

Initially, large cells of with  $R_1 = 6\sqrt{2}a_{\rm bcc}$ , and  $R_2 = 7\sqrt{2}a_{\rm bcc}$  and depth of single burger's vector, were relaxed for both the easy and hard cores, which

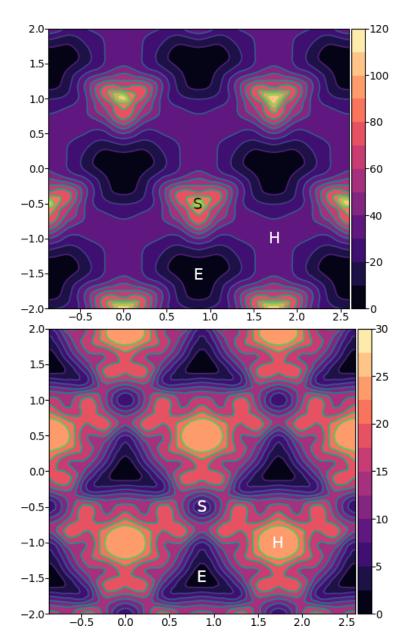


Table 1: Comparison of 2d Peierls potentials of the  $1/2\langle111\rangle$  screw dislocation between DFT cite:Itakura2012 (top) and tight-binding (bottom). Data was interpolated using cubic splines. Energies are in meV, with x and y scales in units of  $\sqrt{2}a_{\rm bcc}=2\sqrt{2/3}b$ . "E", "H" and "S" correspond to easy, hard and split core positions respectively, with the latter also corresponting to atomic positions. The relative energies between the different core positions is smaller in tight-binding compared to DFT. The split core as seen in tight-binding is reminiscent of EAM potentials, where the split core energy is lower than that of the hard core. Some of this discrepancy can be attributed to the difference in simulation method: the cluster method may inhibit the relaxation of the core more than quadrupolar cells, due to finite size effects.

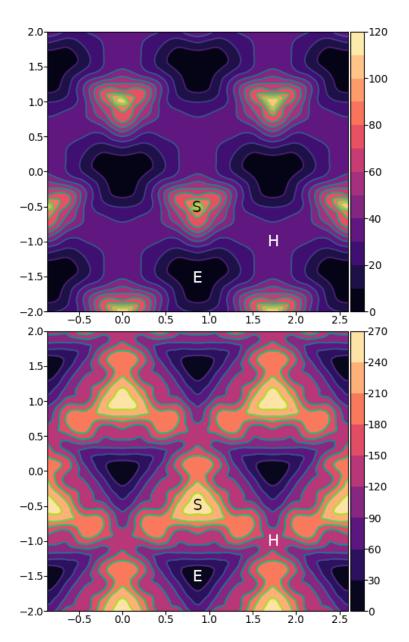


Table 2: Comparison of 2d Peierls potentials of the  $1/2\langle 111\rangle$  screw dislocation between DFT cite:Itakura2012 (top) and tight-binding (bottom). Data was interpolated using cubic splines. Energies are in meV, with x and y scales in units of  $\sqrt{2}a_{\rm bcc}=2\sqrt{2/3}b$ . "E", "H" and "S" correspond to easy, hard and split core positions respectively, with the latter also corresponting to atomic positions. The relative energies between the different core positions is smaller in tight-binding compared to DFT. The split core as seen in tight-binding is reminiscent of EAM potentials, where the split core energy is lower than that of the hard core. Some of this discrepancy can be attributed to the difference in simulation method: the cluster method may inhibit the relaxation of the core more than quadrupolar cells, due to finite size effects.

consisted of 522 and 540 atoms respectively. The three atoms surrounding the core were constrained, to only relax in X-Y plane, to stop the core from moving upon relaxation. The k-point sampling mesh for each of these cells was 1x1x24, with a charge tolerance for self-consistency of 1e-6. Atoms were relaxed until the force on each atom was less than 1e-3 eV/Å.

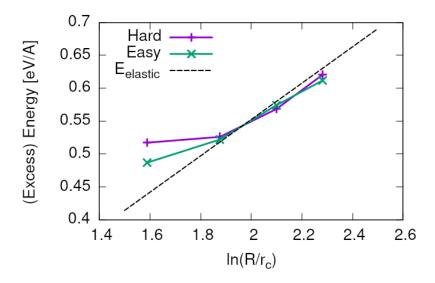
From the relaxed cells, a smaller region of 174 atoms, with  $R_1 = 3\sqrt{2}a_{\rm bcc}$ , and  $R_2 = 4\sqrt{2}a_{\rm bcc}$ , was cut from the dynamic regions. This smaller cell was extended to a thickness of 3b in the Z direction. Carbon interstitials were inserted into octahedral sites near the dislocation core, in the middle layer. Exploiting reflection and rotational symmetry, allows us to use only 10 interstitial sites to obtain the binding energies of carbon  $\sim 2$  b from the core.

The three atoms surrounding the core in the first and third layers were again constrained to relax only in the X and Y directions. No such constraints were imposed on the middle layer.

The core energy difference can be estimated by the difference between the excess energies of the easy and hard cores in the limit that  $\ln \frac{R}{R_0}) \to 0$ . At the smallest value, one finds that the core energy difference  $\Delta E_c^{\rm Easy-Hard} = 76$  meV/b. This is in agreement with the results of Itakura [4], of 82 meV/b.

As found in DFT simulations by Ventelon [7], when a carbon was placed in the vicinity of a relaxed easy dislocation core—in either of the two nearest, distinguishable, octahedral sites—a spontaneous reconstruction of the dislocation core occurred: from easy to hard. Upon reconstruction, the dislocation core moved to a neighbouring triangle, when looking along the  $\langle 111 \rangle$  direction, where the carbon found itself situated in the centre.

Plot of dislocation energy as function of cluster size.



Following the paper by Itakura [8] we calculated the binding energy of carbon each of the screw dislocation cores.

The solution energy is given by

$$E_s = E_{\rm d+C} - E_{\rm d} - E_{\rm C ref.},$$

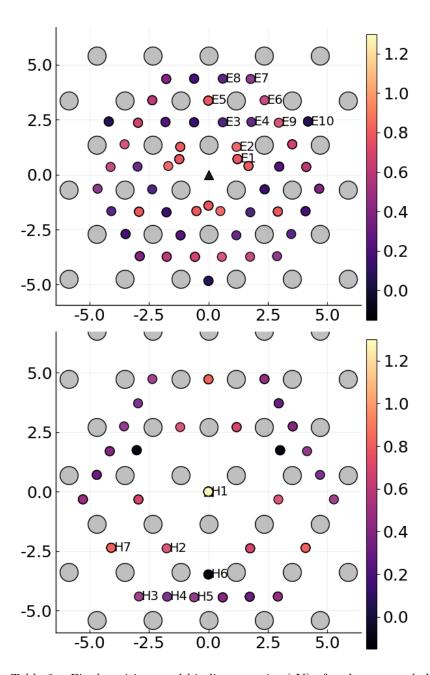


Table 3: Final positions and binding energies (eV) of carbon around the easy core (top) and hard core (bottom). The core was constrained by fixing the top and bottom three atoms surrounding each of the cores. As shown by Ventelon cite:Ventelon2015, the first and second closest octahedral sites to the hard core have their minimum energy inside the hard core.

Site Type	distance from core [b]	$E^z$ [eV]	$\Delta E^z$ [eV]	$E_b$ [eV]	$E_b^z$ [eV]
E1	0.57	0.185	-0.018	0.793	0.775
E2	0.70	0.202	-0.001	0.793	0.793
E3	0.99	0.205	0.002	0.137	0.139
E4	1.21	0.208	0.005	0.229	0.234
E5	1.36	0.210	0.008	0.784	0.791
E6	1.66	0.209	0.007	0.597	0.603
E7	1.89	0.206	0.003	0.385	0.388
E8	1.77	0.203	0.000	0.177	0.178
E9	1.52	0.201	0.000	0.683	0.683
E10	1.95	0.202	0.000	0.067	0.067
H1	0.00	0.196	-0.006	1.298	1.291
H2	1.19	0.210	0.007	0.691	0.698
Н3	2.12	0.209	0.007	0.461	0.467
H4	1.91	0.207	0.005	0.311	0.316
H5	1.80	0.208	0.006	0.403	0.409
H6	1.40	0.207	0.005	-0.119	-0.114
H7	1.35	0.206	0.006	0.825	0.819

Table 4: Table of energies leading to the zero-point energy corrected binding energy.

where  $E_{\rm d+C}$  is the total energy of a relaxed cluster with a carbon interstitial and a dislocation,  $E_{\rm d}$  is the total energy of a relaxed cluster with a dislocation and  $E_{\rm C\ oct.}$  is the total energy of relaxed a cluster with a single carbon in an octahedral site.

The zero-point energy is calculated as in Itakura. After relaxation of the C-dislocation system, a 3x3 Hessian matrix is constructed by taking the numerical derivative of forces observed on the carbon atom after displacement by  $\pm 0.015$  in each of the X, Y and Z directions. The three atoms surrounding the core on the first and third layers were again fixed in Z coordinate. The zero-point energy is given by

$$E_z = \frac{1}{2} \sum_{i=1}^{3} \frac{h}{2\pi} \sqrt{k_i/m_{\rm C}},$$

where  $k_i$  are the eigenvalues of the Hessian and  $m_{\rm C}$  is the mass of carbon. The ZPE corrected solution energy is given by

$$E_s^{\rm Z} = E_s + \Delta E_z,$$

where  $\Delta E_z = E_z - E_{z\text{C ref.}}$  and  $E_{z\text{C ref.}} = 202.5 \text{meV}$  is the zero-point energy of carbon situated in an octahedral site in a perfect cluster of the same size.

These binding energies agree well with experiment and previous calculations. The maximum binding energy found by the Fe-C EAM potential by Becquart [9], was 0.41eV. Kamber *et al.* found a maximum binding energy of 0.5 eV. Cochardt found a value of 0.71 eV, which is within 0.1eV of the largest binding energy for the easy core.

EAM calculations by Clouet [10] found a binding energy of —- by calculating the elastic dipole tensor within Eshelby theory. Hanlumyuang et al. [11]

conducted DFT calculations for the interaction energy 12Å from the core, and their calculations agreed with the continuum limit of Eshelby theory with —.

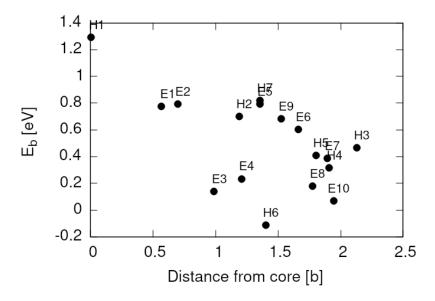
In work by Ventelon [7], the interaction energy of a carbon in a hard core prism configuration was found to be 0.79eV for a thickness in the Z direction of 3b (0.73eV for 6b)—in the convention that a positive binding energy indicates attraction. This is significantly lower than the 1.29eV interaction energy of tight-binding. This discrepancy can be partially explained due to the short cutoff of the carbon interactions in tight-binding—at  $\sim a_{\rm bcc}=2.87$ . In addition, these cells are not fully relaxed, as the three atoms around the core are fixed in Z. As the carbon is separated from its periodic image by 3b=8.61, there is no contribution from the repulsive C-C interaction from periodic images, which is included within DFT.

In the mean-field model of Ventelon, we have

$$E_{\text{int}}(c_d) = E_{\text{int}}^{(0)} + \frac{\Delta E_{\text{Easy-Hard}}}{c_d} + c_d V_{\text{CC}},$$

where  $V_{\rm CC}$  is the C-C interaction energy which can be found by the equation. In tight-binding  $V_{\rm CC}=0$ ,

Distance dependence of binding energies.



## 3.3 Line Tension

One is still doing the work for the line tension model. This model views the dislocation as an elastic string which moves on the Peierls potential  $\Delta E_{\rm P}$ . One is using the julia implementation of the NEB algorithm by Ortner [12]. The equilibrium line shape y(x) of the dislocation is the solution to the 1D Klein-Gordon type equation [13]:

$$-\frac{\mathrm{d}(\Delta E_{\mathrm{P}}[y(x)])}{\mathrm{d}y(x)} + \sigma_{\mathrm{A}}b + T\frac{\partial^{2}y}{\partial x^{2}} = 0,$$

where.

$$T = E_L + \frac{\mathrm{d}^2 E_L}{\mathrm{d}\phi^2},$$

$$E_L = E_{\rm el} + E_{\rm core} = \frac{\mu b^2}{2\pi} \ln\left(\frac{R}{r_c}\right) + E_{\rm core}.$$

I have calculated the coefficients necessary for the line tension model. But there seem to be differences between what Itakura states in his paper and the coefficients that are measured in the Proville paper [13].

One thing I can do to check the coefficients are correct, is to fit to the the kink shape from Luke's thesis to obtain the correct value for the line-tension T.

## 4 Discussion

- How do the results of this work feed into C migration with dislocations?
- How valid is the theory we have vs Fu et al.

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#### 5 Future work

- Validation of line-tension model by reproduction of the dislocation line shape from Itakura 2012 [4].
- Compare the dislocation line shape with Itakura, and find the migration path of the dislocation from the data.
- [Optional] Create Ising model for easy and hard core an compare the binding energies like [14].
- [Optional] Find the elastic dipole tensor to check the binding energy of C within anisotropic elasticity.
- Choose the sites for which one can fit a function (lorentzian) for the interaction energy between C and Fe.
- Find the kink-pair formation enthalpy, with and without carbon, to feed into the kMC code.

## 6 Conclusion

- Outline of the literature review
  - 1. Origin of DER formation through high-cycle fatigue
  - 2. What is the DER region and what phases is it composed of?
  - 3. What are the current mechanisms which explain this?
    - (a) Why are they insufficient?
  - 4. Ouline of the work considering Fe-C dislocation modelling

# 7 Appendix

# 8 Bibliography

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