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# Effects of O in a binary-phase TiAl–Ti<sub>3</sub>Al alloy: from site occupancy to interfacial energetics

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## Abstract

We have investigated site occupancy and interfacial energetics of a TiAl–Ti<sub>3</sub>Al binary-phase system with O using a first-principles method. Oxygen is shown to energetically occupy the Ti-rich octahedral interstitial site, because O prefers to bond with Ti rather than Al. The occupancy tendency of O in TiAl alloy from high to low is  $\alpha_2$ -Ti<sub>3</sub>Al to the  $\gamma$ - $\alpha_2$  interface and  $\gamma$ -TiAl. We demonstrate that O can largely affect the mechanical properties of the TiAl–Ti<sub>3</sub>Al system. Oxygen at the TiAl–Ti<sub>3</sub>Al interface reduces both the cleavage energy and the interface energy, and thus weakens the interface strength but strongly stabilizes the TiAl/Ti<sub>3</sub>Al interface with the O<sub>2</sub> molecule as a reference. Consequently, the mechanical property variation of TiAl alloy due to the presence of O not only depends on the number of TiAl/Ti<sub>3</sub>Al interfaces but also is related to the O concentration in the alloy.

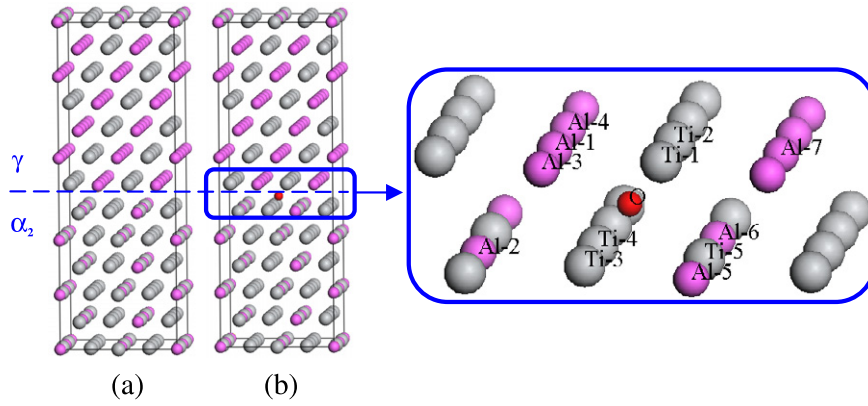
(Some figures in this article are in colour only in the electronic version)

## 1. Introduction

TiAl alloys are considered to be excellent candidates for aerospace applications due to their high melting temperature, low density, high Young's modulus, and good oxidation and creep resistance. However, they suffer from a rather low ductility and toughness at room temperature, which limits their applications [1]. The current emphasis of research is on improving ductility and toughness at room temperature of TiAl alloys while maintaining its attractive high temperature characteristics. Extensive studies of  $\gamma$ -TiAl have been made since the 1980s, particularly on the intrinsic electronic structure, interatomic bonding, grain boundary, impurity, and alloying elements, as well as their effects on mechanical properties [2–14]. As a second phase of the  $\gamma$ -TiAl based alloys, the addition of  $\alpha_2$ -Ti<sub>3</sub>Al is capable of improving the ductility of TiAl [15]. The interest in Ti–Al based alloys (i.e. in the binary-phase  $\gamma/\alpha_2$  alloys) is further encouraged because of their superior specific strength and oxidation resistance [16, 17].

It is generally accepted that a trace amount (parts per million, ppm) of impurity would result in an obvious variation of mechanical properties of materials [18–22]. For the TiAl based alloys, O impurity has been paid special attention as it significantly reduces the ductility of TiAl [23]. Oxygen can be absorbed easily from the air during heat-treatments and melting. Liu *et al* [24] studied the competition in occupation between O and H, and revealed that O has a crucial effect on the environmental embrittlement. The O abatement will increase the ductility and change the deformation mechanism [23, 25]. Interstitial O concentration can be lowered by an addition of Er to form an oxide [26]. Oxygen embrittlement has been determined at an electronic level for the defect and bulk TiAl [27, 4]. Dang *et al* investigated the effect of O on the electronic structure, and found that the localized effect of O is not beneficial to the ductility of  $\gamma$ -TiAl [28].

Despite these studies, little work focuses on the effects of impurities on the TiAl/Ti<sub>3</sub>Al interface, which is extremely important for the mechanical properties of the binary-phase TiAl–Ti<sub>3</sub>Al alloy. In this paper, we investigate the site



**Figure 1.** The supercell of the  $\text{TiAl}[\bar{1}\bar{1}0](111) \parallel \text{Ti}_3\text{Al}[\bar{1}\bar{1}\bar{2}0](0001)$  interface. (a) The clean system; (b) the system with O at the most stable interstitial site in the interface. Oxygen and its first and second nearest neighbor Al and Ti are labeled. The larger (gray), middle-sized (pink), and smaller (red) spheres represent the Ti, Al, and O atoms, respectively.

preference and energetics of the  $\text{TiAl}/\text{Ti}_3\text{Al}$  interface without and with O impurity using a first-principles method. The results are of close relevance to the tailoring of the mechanical properties of  $\text{TiAl}$  alloys with O impurity.

## 2. Computational method

We employ a first-principles method based on density functional theory using the Vienna *ab initio* Simulation Package (VASP) [29, 30]. The ion–electron interaction is described by the ultrasoft pseudopotential [31], and the exchange–correlation function is defined by the generalized gradient approximation according to the parameterization of Perdew and Wang [32]. The plane-wave cutoff energy is 350 eV. The relaxation is continued until the forces on all the atoms have converged to less than  $10^{-3}$  eV  $\text{\AA}^{-1}$ .

It is known that the binary-phase alloys possess improved ductility and toughness over single phase alloys. The  $\gamma$ -TiAl exhibits the  $\text{L1}_0$  crystal structure and the lattice parameters are calculated to be  $a = 3.99$   $\text{\AA}$  and  $c = 4.08$   $\text{\AA}$  while the  $\alpha_2$ - $\text{Ti}_3\text{Al}$  exhibits the  $\text{D0}_{19}$  crystalline structure and the lattice parameters are calculated to be  $a = 5.74$   $\text{\AA}$  and  $c = 4.65$   $\text{\AA}$  [33, 34]. The calculated lattice parameters agree well with the corresponding experimental data (for  $\text{TiAl}$ ,  $a = 4.00$   $\text{\AA}$  and  $c = 4.08$   $\text{\AA}$ ; for  $\text{Ti}_3\text{Al}$ ,  $a = 5.77$   $\text{\AA}$  and  $c = 4.62$   $\text{\AA}$ ) [35]. The crystallographic habit plane relationship at the interface is  $\text{TiAl}[\bar{1}\bar{1}0](111) \parallel \text{Ti}_3\text{Al}[\bar{1}\bar{1}\bar{2}0](0001)$  (i.e. the close-packed directions are aligned). Such a coherent  $\text{TiAl}/\text{Ti}_3\text{Al}$  interface is the only one that has been confirmed by the transmission electron microscopy (TEM) observations experimentally [36–38]. The  $\gamma$ -TiAl has an in-plane lattice spacing of  $a_{(110)\{111\}} = 2.83$   $\text{\AA}$ , which matches well with the  $\alpha_2$ - $\text{Ti}_3\text{Al}$  with an in-plane lattice spacing of  $a_{(1000)\{0001\}} = 2.87$   $\text{\AA}$ . The layer distance along the  $[111]$  direction in  $\text{TiAl}$  and that along the  $[0001]$  direction in  $\text{Ti}_3\text{Al}$  have the same value of  $d_{[111]} = d_{[0001]} = 2.32$   $\text{\AA}$ . These values are derived from the theoretical lattice parameter values. Since the difference of the in-plane lattice spacing between  $\text{TiAl}$  and  $\text{Ti}_3\text{Al}$  is very small (differs by 1%), the in-plane lattice spacing is assumed to be identical to that of  $\text{TiAl}$  and then

**Table 1.** The lattice parameters of the bulk  $\text{TiAl}$ ,  $\text{Ti}_3\text{Al}$  and the  $\text{TiAl}$ – $\text{Ti}_3\text{Al}$  system (in units of  $\text{\AA}$ ). The variations in percentage between the bulk  $\text{TiAl}(\text{Ti}_3\text{Al})$  and the  $\text{TiAl}$ – $\text{Ti}_3\text{Al}$  system are also listed.

Lattice parameter	Bulk			Variation (%)	
	TiAl	Ti <sub>3</sub> Al	TiAl–Ti <sub>3</sub> Al	TiAl	Ti <sub>3</sub> Al
$a$	9.91	9.94	9.89	−0.2	−0.5
$b$	11.27	11.46	11.42	1.3	−0.3
$a_{(110)\{111\}}/a_{(1000)\{0001\}}$	2.83	2.87	2.86	1.1	−0.3

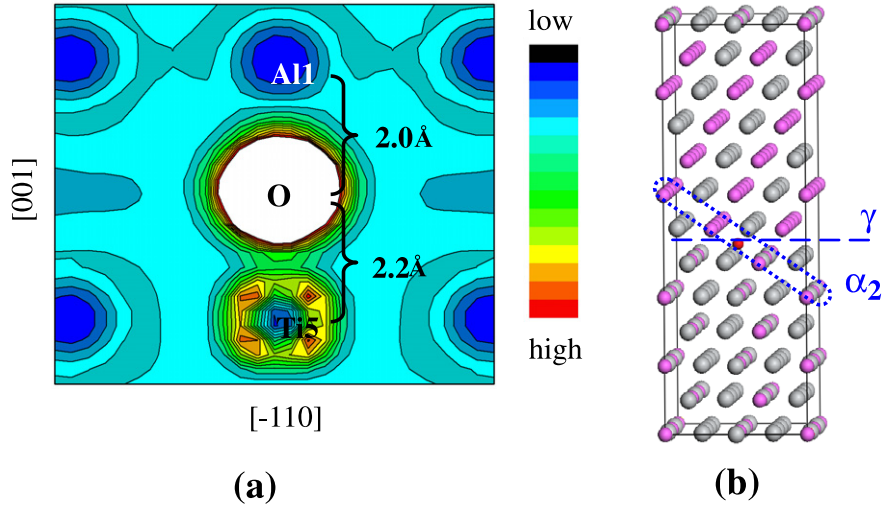
full relaxations are performed. After the relaxation, the lattice parameter of the  $\text{TiAl}$ – $\text{Ti}_3\text{Al}$  supercell is 9.89  $\text{\AA}$  and 11.42  $\text{\AA}$ , respectively, just between that of  $\text{TiAl}$  and  $\text{Ti}_3\text{Al}$ , as shown in table 1. The resulting  $\text{TiAl}$  bulk is tensile while the  $\text{Ti}_3\text{Al}$  bulk is compressed after the interface relaxation. The variation is lower than 2%. This is also the case if we use the lattice parameters of  $a_{(110)\{111\}}$  for the  $\text{TiAl}$  bulk and  $a_{(1000)\{0001\}}$  for the  $\text{Ti}_3\text{Al}$  bulk layers (see table 1). We can thus predict that the bond length variation in the resulting bulk (far from the interface) will also be within 2%.

For the  $\text{TiAl}/\text{Ti}_3\text{Al}$  interface, the supercell of six layers of  $\text{TiAl}$  and six layers of  $\text{Ti}_3\text{Al}$  is used, containing 192 atoms, and a  $3 \times 3 \times 1$   $k$ -point mesh is used, which is illustrated in figure 1(a). In this structure, the atomic rows composed of Ti atoms only (in both  $\text{TiAl}$  and  $\text{Ti}_3\text{Al}$ ) are aligned continuously across the interface, according to the high-resolution electron microscopy observation [36]. There are two  $\text{TiAl}/\text{Ti}_3\text{Al}$  interfaces with the same structure in the supercell. A distance of  $\sim 13.8$   $\text{\AA}$  between these two neighboring interfaces is found to be sufficient to achieve reasonable convergence.

## 3. Results and discussion

### 3.1. The site preference of O in the $\text{TiAl}$ – $\text{Ti}_3\text{Al}$ binary-phase alloy

In order to study the effect of O impurity on the structure and bonding properties of binary-phase  $\text{TiAl}$ – $\text{Ti}_3\text{Al}$  alloy, it is necessary to identify the site preference of O. Only interstitial sites are considered here due to the smaller atomic radius of O



**Figure 2.** (a) Map of the electronic charge density in the (110) plane of the O-doped binary-phase system. (b) The (110) plane goes across the TiAl/Ti<sub>3</sub>Al interface, at which the O atom is included.

in comparison with Ti and Al. We take into account different types of tetrahedral interstitial sites (TIS) and octahedral interstitial sites (OIS).

The formation energy of O ( $E_O^f$ ) occupying an interstitial site can be calculated by

$$E_O^f = E_{\text{TiAl-Ti}_3\text{Al-O}}^T - E_{\text{TiAl-Ti}_3\text{Al}}^T - E_O, \quad (1)$$

where  $E_{\text{TiAl-Ti}_3\text{Al-O}}^T$  and  $E_{\text{TiAl-Ti}_3\text{Al}}^T$  are the total energies of the TiAl-Ti<sub>3</sub>Al supercell with and without O, respectively, and  $E_O$  is the energy of half of the O<sub>2</sub> molecule, which is -4.35 eV according to the present calculation.

The results are shown in table 2. The negative value of O formation energy indicates that the doped system is more stable than the pure one. This conclusion was reached at static conditions (temperature will destabilize the reaction). Oxygen is shown to be energetically favorable to occupy the Ti-rich OIS surrounded by six Ti atoms in the Ti<sub>3</sub>Al phase with the lowest formation energy of -6.23 eV. The occupancy tendency from high to low is  $\alpha_2$ -Ti<sub>3</sub>Al to the  $\gamma$ - $\alpha_2$  interface and  $\gamma$ -TiAl, with the corresponding formation energies -6.23 eV, -5.42 eV, and -4.40 eV, respectively. This is consistent with experimental observations [15]. Our results suggest O is preferable to bond with Ti rather than Al. This should be because the electronegativity difference between O (3.44, Pauling electronegativity) and Ti (1.54) is larger than that between O and Al (1.61). This is further confirmed by the electronic structure of the binary-phase system with an O atom at the most stable interstitial site at the TiAl/Ti<sub>3</sub>Al interface, as shown in figure 2. Noticeable pair-wise covalent and directional bonding is found in the region between O and its first nearest neighbor (FNN) Ti atom, but no such strong bonding appears between O and Al, indicating that the Ti-O bonding is stronger than the Al-O one.

Now we investigate how the temperature affects the O dissolution by estimating the chemical potential of O<sub>2</sub>. The chemical potential of O<sub>2</sub> as a function of temperature ( $T$ ) and

**Table 2.** Formation energies (in eV) of the O atom at different types of TIS and OIS in the binary-phase TiAl-Ti<sub>3</sub>Al supercell.  $\Delta E$  is the energy increment from the most stable system; in brackets is the atom species and the number surrounding O.

Structure		Formation energy (eV)	$\Delta E$ (eV)
Ti <sub>3</sub> Al	Ti-OIS (6Ti)	-6.23	0
	OIS (4Ti-2Al)	-4.75	1.48
	TIS (3Ti-1Al)	-4.20	2.03
	TIS (3Ti-1Al)	-3.83	2.40
TiAl/Ti <sub>3</sub> Al interface	Ti-OIS (5Ti-1Al)	-5.42	0.81
	OIS (3Ti-3Al)	-4.09	2.14
	OIS (4Ti-2Al)	-4.69	1.54
	TIS (3Ti-1Al)	-4.23	2.00
	TIS (2Ti-2Al)	-3.45	2.78
	TIS (2Ti-2Al)	-3.49	2.74
TiAl	OIS (2Ti-4Al)	-3.20	3.03
	Ti-OIS (4Ti-2Al)	-4.40	1.83

partial pressure of O<sub>2</sub> ( $P$ ) can be calculated by

$$\mu_O(T, P) = \frac{1}{2}E_{\text{O}_2} + \mu_O(T, P^0) + \frac{1}{2}k_B T \ln\left(\frac{P}{P^0}\right), \quad (2)$$

where  $E_{\text{O}_2}$  is the total energy of an isolated O<sub>2</sub> molecule, and  $\mu_O(T, P^0)$  is the chemical potential of O<sub>2</sub> at temperature  $T$  and one standard pressure  $P^0$ , which could be obtained from experimental data [39]. For  $P = P^0$ , the temperature dependence of the chemical potential of O<sub>2</sub> is listed in table 3.

As shown in table 2, the O formation energy in the TiAl-Ti<sub>3</sub>Al system at absolute 0 K is in the range between -3.20 and -6.23 eV, with half of the energy of the O<sub>2</sub> molecule as the reference (-4.35 eV). Table 3 shows that the chemical potential of O<sub>2</sub> decreases with increasing temperature. Consequently, the formation energy of O increases and thus the stability of the O-doped binary system decreases with increasing temperature, but the occupancy preference remains unchanged. Further, the formation energy of O remains negative until very high temperatures (as high as

**Table 3.** Chemical potential of O<sub>2</sub> at different temperatures.

$T$ (K)	0	500	1000	2000	2500	3000	4000	4500	5000
$\mu_{\text{O}}$ (eV)	-4.35	-4.89	-5.5	-6.83	-7.54	-8.27	-9.78	-10.55	-11.34

**Table 4.** Cleavage energies ( $\gamma_{\text{cl}}$ ) of the TiAl(111), Ti<sub>3</sub>Al(0001), and TiAl–Ti<sub>3</sub>Al interface for both the clean and O-doped systems.  $\Delta\gamma_{\text{cl}}$  is the energy variation with reference to the respective clean system.

	$\gamma_{\text{cl}}$ (J m <sup>-2</sup> )	$\Delta\gamma_{\text{cl}}$ (%)
TiAl–Ti <sub>3</sub> Al	3.62	0
TiAl–Ti <sub>3</sub> Al–1O	3.47	-4
TiAl–Ti <sub>3</sub> Al–2O	3.33	-8
TiAl(111)	3.45	0
TiAl(111)–O	3.23	-6
TiAl(111)–2O	3.00	-13
Ti <sub>3</sub> Al(0001)	4.03	0
Ti <sub>3</sub> Al(0001)–O	3.99	-1
Ti <sub>3</sub> Al(0001)–2O	3.94	-2

**Table 5.** The bond lengths of the Al–Ti, Ti–Ti, and Al–Al among first and second nearest neighbor atoms of O's interstitial site, crossing the TiAl/Ti<sub>3</sub>Al interface for the clean system and the O-doped system, and the increments of bond lengths caused by O (in units of Å).

	Clean system	O-doped system	Increment
Ti1–Ti3/Ti2–Ti4	2.826	2.985	0.159
Al1–Ti3/Al1–Ti4	2.837	2.955	0.118
Ti1–Ti5/Ti2–Ti5	2.896	2.975	0.079
Al1–Al2	2.851	2.882	0.031
Ti3–Al3/Ti4–Al4	2.843	2.873	0.030
Ti1–Al5/Ti2–Al6	2.844	2.867	0.023
Ti5–Al7	2.946	2.968	0.022

2500 K). Hence, basically O can still stabilize the TiAl–Ti<sub>3</sub>Al system.

### 3.2. Effects of O on the cleavage energy of the TiAl/Ti<sub>3</sub>Al interface

We now turn to investigate the bonding property of the interface in binary-phase TiAl–Ti<sub>3</sub>Al alloy. We calculated the cleavage energy of the TiAl/Ti<sub>3</sub>Al interface with and without an O atom occupying the energetically preferred Ti–OIS (5Ti–1Al) in the TiAl/Ti<sub>3</sub>Al interface. We use the Ti<sub>3</sub>Al–O system as a reference system (i.e. O situated at the surface of Ti<sub>3</sub>Al after the cleavage) because the present results indicate that energetically O tends to stay in Ti<sub>3</sub>Al rather than TiAl (table 2). In order to investigate the effect of O concentration, the two-O-atom case at the interface is also taken into account. Both O atoms are placed in the energetically preferred Ti–OIS (5Ti–1Al) and the distance between them is 5.7 Å. Such a configuration is found to be energetically stable by our calculation.

The cleavage energy  $\gamma_{\text{cl}}$  is defined as the energy required per unit area to separate the solid into two semi-infinite halves by creating two surfaces, neglecting diffusional and plastic degrees of freedom. The cleavage energy can be a direct measure of the interface bond strength, considered as the lower bound to the actual energy cost measured in a cleavage experiment [40]. Here, the cleavage energies ( $\gamma_{\text{cl}}$ ) of the TiAl/Ti<sub>3</sub>Al interface without and with O are then calculated through

$$\gamma_{\text{cl(TiAl–Ti}_3\text{Al)}} = \frac{E_{\text{TiAl}}^{\text{slab}} + E_{\text{Ti}_3\text{Al}}^{\text{slab}} - E_{\text{TiAl–Ti}_3\text{Al}}}{2A} \quad (3)$$

and

$$\gamma_{\text{cl(TiAl–Ti}_3\text{Al–O)}} = \frac{E_{\text{TiAl}}^{\text{slab}} + E_{\text{Ti}_3\text{Al–O}}^{\text{slab}} - E_{\text{TiAl–Ti}_3\text{Al–O}}}{2A}, \quad (4)$$

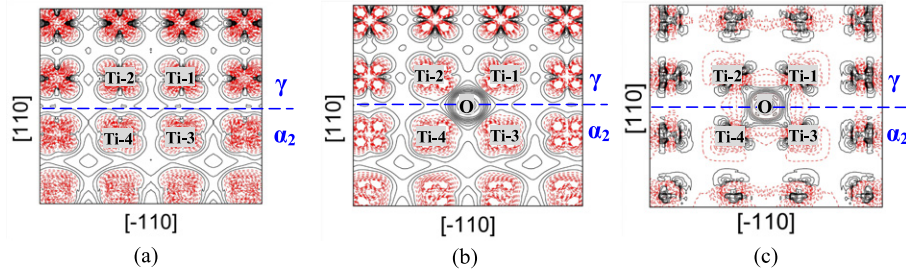
where  $E_{\text{TiAl–Ti}_3\text{Al}}$  and  $E_{\text{TiAl–Ti}_3\text{Al–O}}$  are the total energy of the clean and O-doped binary-phase system,  $A$  is the interface area

of the binary-phase system, and  $E_{\text{TiAl}}^{\text{slab}}$  and  $E_{\text{Ti}_3\text{Al}}^{\text{slab}}$  are the total energies of the six-layer TiAl and Ti<sub>3</sub>Al with the same-size supercells as the binary-phase system, but removing the Ti<sub>3</sub>Al and TiAl layers, respectively.  $E_{\text{Ti}_3\text{Al–O}}^{\text{slab}}$  is the total energy of the six-layer Ti<sub>3</sub>Al with O at the most stable site at both surfaces in the supercell. For the calculation of the energy of the separate TiAl and Ti<sub>3</sub>Al phases, the slabs have been optimized.

In addition, we calculated the cleavage energy of TiAl(111) and Ti<sub>3</sub>Al(0001) with and without O. The order of the bond strength is Ti<sub>3</sub>Al(0001) > TiAl/Ti<sub>3</sub>Al interface > TiAl(111), and the corresponding order of cleavage energy is 4.03 > 3.62 > 3.45 J m<sup>-2</sup>. The cleavage energy decreases with the introduction of O to all the interface systems, and it further decreases when the amount of O increases. The decrements of cleavage energy in percentages are listed in table 4, suggesting that all three kinds of interfaces in TiAl alloy are weakened by the introduction of O. Particularly, the cleavage energy of the clean TiAl/Ti<sub>3</sub>Al interface is 3.62 J m<sup>-2</sup> and decreases to 3.47 J m<sup>-2</sup> and 3.33 J m<sup>-2</sup> after the addition of one O and two O, respectively. Moreover, with the O concentration identical in all the interface systems, the order of bond strength remains the same as that of the clean systems. Despite the lowest cleavage energy of the TiAl(111) in both the clean and O-doped systems, it is difficult to clarify whether fracture occurs in the TiAl, Ti<sub>3</sub>Al lamellae, or along the TiAl/Ti<sub>3</sub>Al interface, because the local O concentration plays an important role as well.

We now investigate the intrinsic mechanism of the weakening effect of O-doping at the TiAl/Ti<sub>3</sub>Al interface. We calculate the bond lengths of the Al–Ti, Ti–Ti, and Al–Al among first and second nearest neighbor atoms of the O interstitial site, crossing the TiAl/Ti<sub>3</sub>Al interface with and without O existing. As listed in table 5, the bond lengths are increased due to O-doping, and the increment of the bond length of the first nearest neighbor atoms is larger than that of the second nearest neighbor atoms, implying a decrease of bond strength at the TiAl/Ti<sub>3</sub>Al interface surrounding O in spite of the newly formed O–Ti/O–Al bonds.





**Figure 3.** The charge density difference contour maps on the (001) Ti layer cross the TiAl/Ti<sub>3</sub>Al interface. (a) and (b) show the first charge density difference contour maps for the clean system and the O-doped system, respectively, while (c) shows the second charge density difference contour map. Black solid and red dotted lines correspond to the gain and the loss of electrons, respectively.

Furthermore, we investigate the spatial redistribution of electron density induced by O impurities. We plotted the first charge density difference contour maps on the (001) Ti layer, crossing the TiAl/Ti<sub>3</sub>Al interface, of the clean and the O-doped systems in figures 3(a) and (b), which are obtained by subtracting the electron density of free atoms from that of the binary-phase system. We also plotted the second charge density difference contour map on the (001) Ti layer in figure 3(c), by subtracting the first electron density difference of the clean system from that of the O-doped binary-phase system. We can clearly see the O-induced charge redistribution from the charge density difference maps. In figures 3(a) and (b), directional charge redistribution is found between Ti atoms in the TiAl phase (the upper part of figure 3), indicating an obvious Ti<sub>d</sub>–Ti<sub>d</sub> directional bonding. In figure 3(b), the charge accumulates in the region between O and its FNN Ti atoms, indicating a strong Ti–O bonding. In figure 3(c), we can clearly see the charge density reduction among the FNN Ti sites and the charge density increment between O and its FNN Ti atoms, implying that the charge transfers from the region between Ti–Ti to O–Ti and the Ti<sub>d</sub>–Ti<sub>d</sub> bonding is weakened. It could be deduced that the forming of O–Ti bonding is not strong enough to compensate for the decrease of the Ti–Ti and Ti–Al bonding, and the overall effect of O-doping is the decrease of the interface bond strength.

### 3.3. Effects of O on the TiAl/Ti<sub>3</sub>Al interface energy

Now we investigate the effects of O on the interface energy of the TiAl/Ti<sub>3</sub>Al system, which can be viewed as the energy required to form the interface from bulk materials. In contrast to the cleavage energy, it is not an absolute measure of the interface bond strength; instead, it compares the interfacial bonds to the bonding in the bulk material [41]. All the interfacial energies are calculated after atomic relaxations, although the lattice relaxations near the interface are small. Here, the interface energies ( $\gamma_{\text{int}}$ ) of the TiAl/Ti<sub>3</sub>Al interface without and with O are then calculated through

$$\gamma_{\text{int(TiAl-Ti}_3\text{Al)}} = \frac{E_{\text{TiAl-Ti}_3\text{Al}} - E_{\text{TiAl}}^{\text{bulk}} - E_{\text{Ti}_3\text{Al}}^{\text{bulk}}}{2A} \quad (5)$$

and

$$\gamma_{\text{int(TiAl-Ti}_3\text{Al-O)}} = \frac{E_{\text{TiAl-Ti}_3\text{Al-O}} - E_{\text{TiAl}}^{\text{bulk}} - E_{\text{Ti}_3\text{Al}}^{\text{bulk}} - E_{\text{O}_2}^{\text{ref}}}{2A}, \quad (6)$$

**Table 6.** The interface energies of the clean TiAl/Ti<sub>3</sub>Al interface ( $\gamma_{\text{int(TiAl/Ti}_3\text{Al)}}$ ) and the O-doped TiAl/Ti<sub>3</sub>Al interface ( $\gamma_{\text{int(TiAl/Ti}_3\text{Al-O)}}$ ). For the calculation of  $\gamma_{\text{int(TiAl/Ti}_3\text{Al-O)}}$ , three different reference systems are taken into account.

	meV Å <sup>-2</sup>	mJ m <sup>-2</sup>
$\gamma_{\text{int(TiAl/Ti}_3\text{Al)}}$	7	120
$\gamma_{\text{int(TiAl/Ti}_3\text{Al-O)}}$ with different references		
O <sub>2</sub> molecule	−39	−631
O in TiAl	−4	−59
O in Ti <sub>3</sub> Al	14	222

where  $E_{\text{TiAl-Ti}_3\text{Al}}$  and  $E_{\text{TiAl-Ti}_3\text{Al-O}}$  are the total energies of the clean and the O-doped binary-phase systems.  $A$  is the interface area,  $E_{\text{TiAl}}^{\text{bulk}}$  and  $E_{\text{Ti}_3\text{Al}}^{\text{bulk}}$  are the total energies of the 96-atom TiAl and Ti<sub>3</sub>Al, respectively, and  $E_{\text{O}_2}^{\text{ref}}$  is the reference energy of the O<sub>2</sub> molecule. During the formation of the interface, O at the interface can be absorbed from the air, or diffused from the TiAl or Ti<sub>3</sub>Al phase. The interface energy of the O-doped system depends on the reference system of O. We consider all the possible cases for the O from different reference systems, i.e. the O<sub>2</sub> molecule, TiAl, and Ti<sub>3</sub>Al. In equation (6),  $E_{\text{O}_2}^{\text{ref}}$  is different depending on the system that O is from.

As listed in table 6, the interface energy is calculated to be 120 mJ m<sup>-2</sup> for the clean TiAl/Ti<sub>3</sub>Al interface. As a comparison, the interface energy of the clean TiAl–Ti<sub>3</sub>Al interface was calculated to be 110 mJ m<sup>-2</sup> by Fu *et al* [42]. While it decreases to −631 mJ m<sup>-2</sup> and −59 mJ m<sup>-2</sup> for the TiAl/Ti<sub>3</sub>Al–O system with reference to the O<sub>2</sub> molecule and O in TiAl, respectively. The results indicate that O can stabilize the TiAl/Ti<sub>3</sub>Al interface in these two cases, and the O<sub>2</sub> molecule case is much more stable. In contrast, the interface energy increases to 222 mJ m<sup>-2</sup> with reference to O in Ti<sub>3</sub>Al, indicating that the stability of the interface is weakened in this case.

The experimental results [43] show that the TiAl–Ti<sub>3</sub>Al alloys containing O less than 1000 ppm (weight) do not exhibit fully lamellar microstructures, as was expected by the choice of the heat treatment. For the alloys containing O more than 1000 ppm, the alloys exhibit the fully lamellar microstructure due to the O stabilization. As a matter of fact, almost all the TiAl/Ti<sub>3</sub>Al interfaces in the alloys exist in the lamellar microstructure, which suggests the TiAl/Ti<sub>3</sub>Al interfaces are

stabilized by the presence of O. Thermodynamically, O is most probably from the O<sub>2</sub> molecule or TiAl rather than Ti<sub>3</sub>Al according to the calculated O formation energy (table 2). This could be the reason why O has been observed to stabilize the TiAl/Ti<sub>3</sub>Al interfaces experimentally.

Such a positive value of the interface energy suggests that the clean TiAl/Ti<sub>3</sub>Al interface is not energetically stable. For the O-doped system, if we choose the O<sub>2</sub> molecule as a reference, the interface energy of the O-doped TiAl/Ti<sub>3</sub>Al interface is much lower than the clean case. The interface energy after the addition of O is decreased by as much as ~6 times, suggesting O will strongly stabilize the TiAl/Ti<sub>3</sub>Al interface and make it easier to form, which is consistent with the experimental results [43]. The decrement of interface energy lies in the formation of the O–Ti bonding after the addition of O at the interface.

Experimentally, it is desirable to prepare the TiAl alloys with a suitable heating treatment, making both grains and lamellae of alloys as fine as possible [44–48]. This suggests that the ductility of the TiAl alloys strongly depends on the TiAl/Ti<sub>3</sub>Al interface area. Larger TiAl/Ti<sub>3</sub>Al interface area should correspond to the higher ductility. According to the present calculation with reference to the O<sub>2</sub> molecule, the presence of O makes the TiAl/Ti<sub>3</sub>Al interface easier to form by largely decreasing the interface energy. On the other hand, the experimental results show that the increased O content is well correlated with reduced ductility [23]. The O-induced brittleness of the TiAl alloy might be due to the weakening of the interfaces as well as the pinning of the dislocations by O [49]. Consequently, the mechanical property variation of TiAl alloy due to the presence of O not only depends on the number of TiAl/Ti<sub>3</sub>Al interfaces but also is related to the O concentration in the alloy.

#### 4. Summary

In summary, we investigated the effect of O on electronic structure, cleavage energy, and interface energy in a TiAl/Ti<sub>3</sub>Al binary-phase system using a first-principles method. Oxygen is shown to energetically occupy the Ti-rich octahedral interstitial site, because O prefers to bond with Ti rather than Al. The occupancy tendency of O in TiAl alloy from high to low is  $\alpha_2$ -Ti<sub>3</sub>Al to the  $\gamma$ - $\alpha_2$  interface and  $\gamma$ -TiAl. The cleavage energy of the TiAl/Ti<sub>3</sub>Al interface decreases to 3.47 J m<sup>-2</sup> due to the presence of O, 4% lower than that of the O-free TiAl/Ti<sub>3</sub>Al interface, indicating that the TiAl/Ti<sub>3</sub>Al interface is weakened with O existing. For the O-doped system, if we choose the O<sub>2</sub> molecule as a reference, O can largely decrease the TiAl/Ti<sub>3</sub>Al interface energy, with an implication that O can strongly stabilize the TiAl/Ti<sub>3</sub>Al interface and make it easier to form. Consequently, the mechanical property variation of TiAl alloy due to the presence of O not only depends on the number of TiAl/Ti<sub>3</sub>Al interfaces but also is related to the O concentration in the alloy.

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