

1. [C] $\hat{i} \quad \hat{j} \quad \hat{k}$
 $\delta_{ij} \quad \delta_{jk}$

$\rightarrow 0 \quad 0 \quad 0$
 $\rightarrow 0 \quad w_{ij} \quad 0 \quad \delta_{ij}^{(B)}$
 $\rightarrow 0 \quad 0 \quad 0$
 $\rightarrow 0 \quad 0 \quad 0 \quad l=3$

$l \in \{1, 2\}$

$d^{(0)} \quad d^{(1)} \quad d^{(2)} \quad d^{(3)}$
 $l=1 \quad l=2 \quad \delta_{ij} \rightarrow x_j$

$\delta_j^{(2)} = \frac{\partial e_n}{\partial \delta_j^{(1)}} = \sum_{k=1}^{K=6} (\delta_k^{(2)}) (w_{jk}^{(3)}) h'(\delta_j^{(1)})$
 5×6

$\delta_i^{(1)} = \frac{\partial e_n}{\partial \delta_i^{(1)}} = \sum_{j=1}^{J=5} (\delta_j^{(2)}) (w_{ij}^{(2)}) h'(\delta_i^{(1)})$
 5×4

$5 \times 6 + 5 \times 4 = 50$

2. [d]

50
 $0 \quad 0 \quad 0 \quad 0$
 $0 \quad 0 \quad 0 \quad 0 \rightarrow$
 $0 \quad 0 \quad 0 \quad 0 \rightarrow$
 $\vdots \quad \vdots \quad \vdots \quad \vdots \rightarrow$
 $0 \quad 0 \quad 0 \quad 0 \rightarrow$

$d^{(0)} = w$

$a_1 + a_2 + a_3 + a_4 = 50$

find $\max (20 \times a_1) + (a_1 \times a_2) + \dots + (a_{N-1} \times a_N)$
 $= \max [(20 \times a_1) + (a_1 \times a_2)]$

$N-1 \sqrt{(a_1 \times a_2)(a_2 \times a_3) \dots (a_{N-1} \times a_N)} \leq \frac{a_1 \times a_2 + a_2 \times a_3 + \dots + a_{N-1} \times a_N}{N-1}$

$a_1 a_2 = a_2 a_3 = \dots = a_{N-1} a_N \Rightarrow a_1 = a_3 = a_5 = \dots = a_a$

$a_1 a_2 \quad a_3 a_4 \quad a_5 a_6 \quad a_2 = a_4 = a_6 = \dots = a_b$

$\max (20 \times a_a) + (N-1)(a_a a_b) + (a_N \times 3)$

偶 \times 奇 = 偶

偶 \times 偶 = 偶

奇 \times 奇 = 奇

偶 \times \square = 偶

$20 \times N$

3. [d]

$$g = X^{(L)} = \left[\frac{\exp(s_1^{(L)})}{\sum_{k=1}^K \exp(s_k^{(L)})}, \frac{\exp(s_2^{(L)})}{\sum_{k=1}^K \exp(s_k^{(L)})}, \dots, \frac{\exp(s_K^{(L)})}{\sum_{k=1}^K \exp(s_k^{(L)})} \right]$$

$$V = [\mathbb{I}[y=1], \dots, \mathbb{I}[y=K]]$$

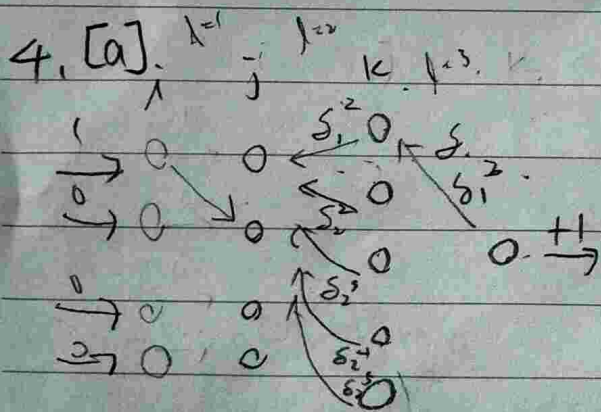
$$\text{err}(x, y) = - \sum_{k=1}^K V_k \ln g_k$$

$$\frac{\partial \text{err}(x, y)}{\partial s_k^{(L)}} = \frac{- \sum_{k=1}^K V_k \ln \frac{\exp(s_k^{(L)})}{\sum_{k=1}^K \exp(s_k^{(L)})}}{\partial s_k^{(L)}} = \frac{- \sum_{k=1}^K V_k \ln \exp(s_k^{(L)})}{\partial s_k^{(L)}} + \frac{\sum_{k=1}^K V_k \ln \sum_{k=1}^K \exp(s_k^{(L)})}{\partial s_k^{(L)}}$$

$$= \frac{- \sum_{k=1}^K V_k s_k^{(L)}}{\partial s_k^{(L)}} + \frac{\sum_{k=1}^K V_k \ln (e^{s_1^{(L)}} + e^{s_2^{(L)}} + \dots)}{\partial s_k^{(L)}} \cdot \frac{\ln e^{s_1^{(L)}} + \dots + e^{s_k^{(L)}}}{e^{s_1^{(L)}} + \dots + e^{s_k^{(L)}}} \cdot \frac{\partial s_1^{(L)}}{\partial s_k^{(L)}} \cdot \dots \cdot 1$$

$$= -V_k + (e^{s_k^{(L)}} \cdot 1 \cdot \frac{1}{\sum_{k=1}^K \exp(s_k^{(L)})})$$

$$= -V_k + g_k$$



$$X_h = (1, 0, 0, 0)$$

$$\frac{\partial \text{err}}{\partial w_{k1}} = \frac{\partial (y_h - \sum_{k=1}^5 w_{k1} \cdot x_k^2)}{\partial w_{k1}}$$

$$w_{k1}^{(3)} = 0 \Rightarrow s_k^{(2)} = 0 \Rightarrow w_k^{(2)} = 0$$

$$\Rightarrow s_1^{(1)} = 0 \Rightarrow w_{01}^{(1)} = 0$$

update rule:

$$w_{ij}^{(l)} \leftarrow w_{ij}^{(l)} - \eta x_i^{(l-1)} \cdot \delta_j^{(l)}$$

$$w_{01}^{(1)} \leftarrow w_{01}^{(1)} - \eta x_0^{(0)} \cdot \delta_1^{(1)}$$

$$\delta_1^{(1)} = \frac{\partial \text{err}}{\partial s_1^{(1)}} = \sum_{k=1}^5 (\delta_k^{(2)} (w_{1k}^{(2)})) \tanh'(s_1^{(1)})$$

$$\tanh' x = \frac{e^x - e^{-x}}{e^x + e^{-x}}$$

$$\tanh'(x) = \frac{4}{(e^x + e^{-x})^2}$$

$$w_{1k}^{(2)} \leftarrow w_{1k}^{(2)} - \eta x_1^{(1)} \cdot \delta_k^{(2)}$$

$$\delta_k^{(2)} = \frac{\partial \text{err}}{\partial s_k^{(2)}} = \delta_1^{(3)} (w_{k1}^{(3)}) (\tanh'(s_k^{(2)}))$$

$$w_{k1}^{(3)} \leftarrow w_{k1}^{(3)} - \eta x_k^{(2)} \cdot \delta_1^{(3)}$$

$$\delta_1^{(3)} = -2(y_h - s_1^{(4)}) = -2(1 - 0) = -2$$

7. [d]

$$G(x) = \text{sign}\left(\sum_{k=1}^3 1 \cdot g_k(x)\right)$$

$$E_{\text{out}}(G) = 0.2$$

$$g_1(x), g_2(x), g_3(x)$$

at least two $g(x)$ raise error. for $E_{\text{out}}(G) = 0.2$

$$\sum_{k=1}^T E_{\text{out}}(g_k(x)) \geq 0.4$$

if G is correct for G . $1 - E_{\text{out}}(G) = 0.8$.

at least two $g(x)$ is correct.

$$\frac{4}{5} \times \frac{1}{5} \times 3 \geq \sum_{k=1}^T E_{\text{out}}(g_k(x))$$

$$1.4 \geq \sum_{k=1}^T E_{\text{out}}(g_k(x)) \geq 0.4$$

P	D	D
0	0	1
1	0	0
0	0	1
0	0	1
0	0	1

8. [c]

$$E_{\text{out}}(g_k) = 0.4 \quad \forall k \in \{1, 2, 3, 4, 5\}$$

$$G(x) = \text{sign}\left(\sum_{k=1}^5 g_k(x)\right)$$

for $X = \{x_1, x_2, \dots, x_n\}$

$$\binom{5}{3} (0.4)^3 (0.6)^2 + \binom{5}{4} (0.4)^4 (0.6) + \binom{5}{5} (0.4)^5$$

$$= 10 \times 0.36 \times 0.064 + 5 \times 0.6 \times 0.0256 + 0.01024$$

$$= 0.31744$$

P	P	P	P	P
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0	0	0	0	0
1	1	1	1	1
1	1	1	1	1

9. [b]

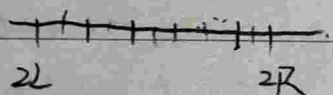
$$X = \{x_1, x_2, \dots, x_N\}$$

$$\# \text{ of } X_S = \frac{N}{2}$$

if x_i is not chosen:

$$\lim_{N \rightarrow \infty} \left(\frac{N-1}{N} \right)^{\frac{N}{2}} = \lim_{N \rightarrow \infty} \left(1 - \frac{1}{N} \right)^{\frac{N}{2}} = \left(\frac{1}{e} \right)^{0.5} \approx 0.60.$$

10.



$$X = \{x_1, x_2, \dots, x_d\} \quad \forall x_i \in \text{even}.$$

$$g_{s, i, \theta}(x) = s \cdot \text{sign}(x_i - \theta) \rightarrow \text{odd}$$

$$\phi_{dS}(x) = \begin{pmatrix} g_{1,1,2L+1}(x), g_{1,1,2L+3}(x), \dots, g_{1,1,2R-1}(x) \\ g_{-1,1,2L+1}(x), g_{-1,1,2L+3}(x), \dots, g_{-1,1,2R-1}(x) \\ \vdots \\ g_{1,d,2L+1}(x), \dots, g_{1,d,2R-1}(x) \\ g_{-1,d,2L+1}(x), \dots, g_{-1,d,2R-1}(x) \end{pmatrix}$$

$$g_{-1,1,2L+1}(x), g_{-1,1,2L+3}(x), \dots, g_{-1,1,2R-1}(x)$$

\vdots

$$g_{1,d,2L+1}(x) \quad \dots \quad g_{1,d,2R-1}(x)$$

$$g_{-1,d,2L+1}(x) \quad \dots \quad g_{-1,d,2R-1}(x)$$

$$|<_{dS}(x, x') =$$

19. [e]

neural networks & deep learning.

because the reason why I step into ML is that I trained a model with CNN to identify the apple. NN really astonished me.

20. [b]

matrix factorization.

I think. this topic is a little abstract to me. maybe the partial reason is that I didn't pay full attention on it.