

# Forever Young

Time limit: 1 second

My birthday is coming up. Alas, I am getting old and would like to feel young again. Fortunately, I have come up with an excellent way of feeling younger: if I write my age as a number in an appropriately chosen base  $b$ , then it appears to be smaller. For instance, suppose my age in base 10 is 32. Written in base 16 it is only 20!

However, I cannot choose an arbitrary base when doing this. If my age written in base  $b$  contains digits other than 0 to 9, then it will be obvious that I am cheating, which defeats the purpose. In addition, if my age written in base  $b$  is too small then it would again be obvious that I am cheating.

Given my age  $y$  and a lower bound  $l$  on how small I want my age to appear, find the largest base  $b$  such that  $y$  written in base  $b$  contains only decimal digits, and is at least  $l$  when interpreted as a number in base 10.

## Input

The input consists of a single line containing two base 10 integers  $y$  ( $10 \leq y \leq 10^{18}$  – yes, I am very old) and  $l$  ( $10 \leq l \leq y$ ).

## Output

Display the largest base  $b$  as described above.

### Sample Input 1

### Sample Output 1

32 20	16
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### Sample Input 2

### Sample Output 2

2016 100	42
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**Submission guidelines:** You need to upload two files in the FeedbackFruits System.

- (1) Write one page document (upload pdf version of the doc) describing your algorithm or pseudocode. You should describe ***why and how*** your algorithm design should be ***efficient*** (the corresponding program should run fast).
- (2) One program file (**you can upload the zip file for it**) – actual C/C++, Java, or Python code file. Make sure your code finishes its execution within 2 seconds for the largest possible input.

**Hints:** The problem is an application of **Binary Search technique**.