

## Problem Set 6, Part I

### Problem 1: Checking for keys above a value

1-1)  $O(n)$  because the anyGreaterInTree method traverse all the keys even if the greater value is found.

1-2)

```
private static boolean anyGreaterInTree(Node root, int v) {  
    if (root == null) {  
        return false;  
    }  
    if (root.key > v) {  
        return true;  
    } else {  
        boolean anyGreaterInLeft = anyGreaterInTree(root.left, v);  
        boolean anyGreaterInRight = anyGreaterInTree(root.right, v);  
        return (anyGreaterInLeft || anyGreaterInRight);  
    }  
}
```

1-3)

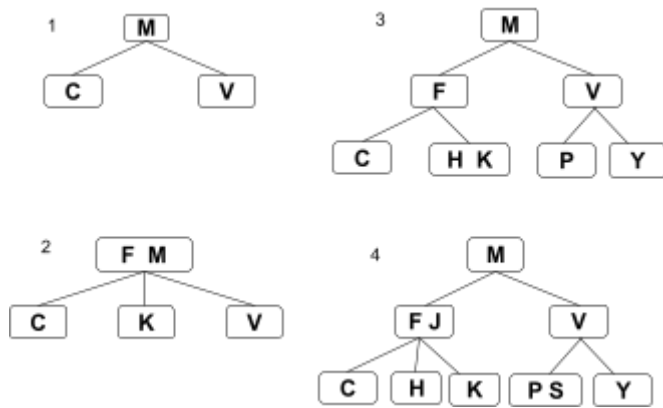
The efficiency is depending on the keys.

The Best case is  $O(1)$  when the root is larger than  $v$ .

The Worst case balanced is  $O(n)$  when the method have to go through all the nodes.

The Worst case unbalanced is  $O(n)$  when the method have to go through all the nodes.

## Problem 2: Balanced search trees



### Problem 3: Hash tables

#### 3-1) linear

0	you
1	a
2	to
3	the
4	my
5	their
6	bring
7	do

#### 3-2) quadratic

0	
1	bring
2	to
3	the
4	do
5	their
6	my
7	

#### 3-3) double hashing

0	bring
1	do
2	to
3	the
4	you
5	their
6	my
7	a

**3-4)** probe sequence: 3, 6, 1, 4, 7

**3-5)** table after the insertion:

0	list
1	try
2	
3	our
4	
5	
6	linked
7	

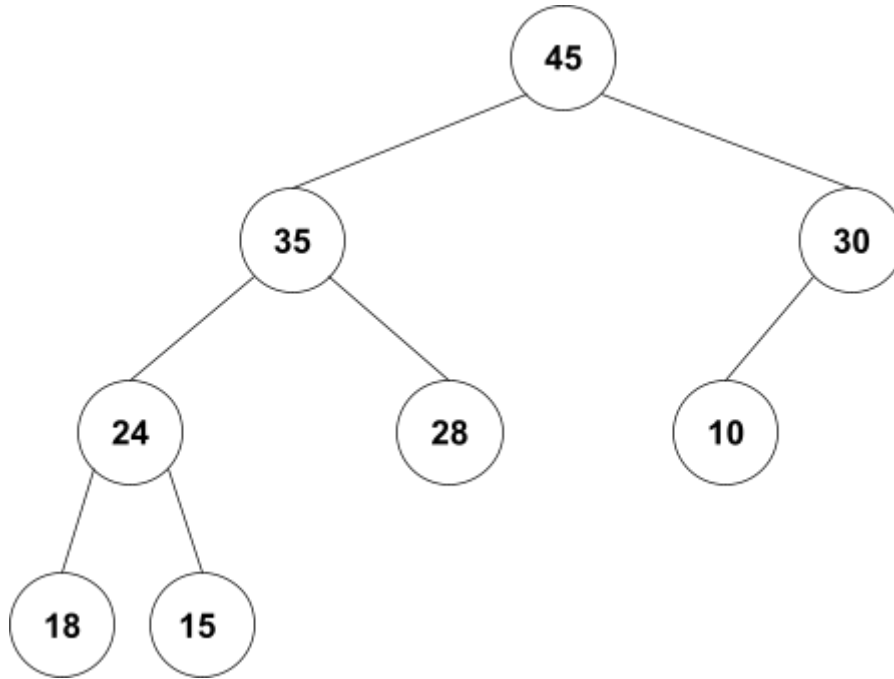
**Problem 4: Complete trees and arrays**

4-1) left child: 81,  $a[2 \cdot 40 + 1]$   
right child: 81,  $a[2 \cdot 40 + 2]$   
Parent: 16,  $a[(40 - 1) / 2]$

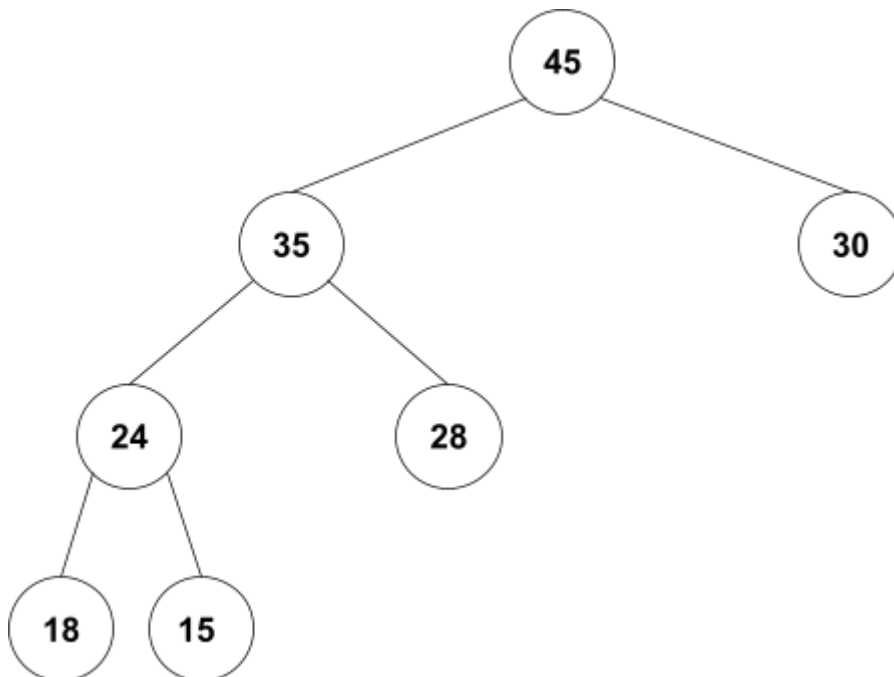
4-2) 6,  $\text{Floor}(\log_2(112))$

4-3) Left child, because node 111 is the bottom node, the parent node is  $a[110 / 2] = 55$ .

**Problem 5: Heaps**  
**5-1)**  
**after one removal**



**After a second removal** (copy your revised diagram from part 1 here, and edit it to show the result of the second removal)



5-2)

