Control of Nonprehensile Rolling Manipulation: Balancing a Disk on a Disk

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Abstract—This paper presents feedback stabilization control of a rolling manipulation system called the disk-on-disk. The system consists of two disks in which the upper disk (object) is free to roll on the lower disk (hand) under the influence of gravity. The goal is to stabilize the object at the unstable upright position directly above the hand. We show that it is possible to stabilize the object at the upright position, while the hand or object rotates to a specific orientation or spins at a constant velocity. We use full-state feedback linearization to derive control laws. We present simulation as well as experimental results demonstrating the controllers.

Index Terms—Disk-on-disk, feedback linearization control, non-prehensile manipulation, rolling manipulation.

I. INTRODUCTION

Non PREHENSILE manipulation primitives such as rolling, sliding, pushing, and throwing are commonly used by humans but usually avoided by robots, who seem to prefer grasping. Dynamic nonprehensile manipulation can raise challenges in high-speed sensing and control, as the manipulated object moves relative to the manipulator throughout the process. An advantage, however, is that dynamics can be exploited to allow the robot to create and control object motions that would otherwise be impossible. Examples include throwing an object outside the kinematic workspace of the robot and using rolling to control more object degrees of freedom than the robot has actuators [1]–[4].

Our long-term goal is to develop a unified framework for planning and control of dynamic robotic manipulation. A typical manipulation plan consists of a sequence of manipulation primitives (such as grasping, rolling, pushing, throwing, etc.),

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with each primitive equipped with its own motion planner and feedback controller. The primitive under study in this paper is nonprehensile rolling manipulation, where a single object rolls on the surface of a controlled manipulator. Problems of interest include planning the motion of the manipulator to achieve the desired rolling motion of the object (see, e.g., [2] and [5]) and feedback control to stabilize the desired trajectory.

In this paper, we study feedback stabilization of a canonical rolling problem: balancing a disk-shaped object on top of a disk-shaped manipulator (referred to as the hand) in a vertical plane. The balancing task is further extended to more difficult problems of stabilization at the upright position, while the hand or object 1) rotates to a specific orientation or 2) spins at a constant velocity. We constrain the motion of the circular hand to rotation about its center. We derive control laws that stabilize the object to the balanced position under the kinematic assumption of rolling at all times. The basin of attraction is reduced when the contact is modeled using Coulomb friction, but it is still large with large friction coefficients. The effectiveness of the controllers has been verified in experiments.

This paper represents a first step toward control for general nonprehensile rolling manipulation by providing theoretical and experimental solutions for the canonical problem of a disk rolling on a disk.

A. Related Work

Several examples of control of rolling have been studied in the literature. Among them is the ball and beam system in which a ball rolls with one degree of freedom along a linear beam. The beam rotates in a vertical plane; therefore, the ball rolls under the influence of gravity. To solve the stabilization problem, approximate input—output linearization is used in [6], where the original equations of motion are approximated by a simplified nonlinear model such that the model becomes exact input—output linearizable. In [7], global asymptotic stability is achieved by a saturation control law which uses state-dependent saturation levels. A sliding-mode controller that is robust to parameter uncertainty is also proposed in [8].

Another related problem is a ball rolling on a plate. It is shown in [9] that an admissible path between any two configurations exists, and motion planning algorithms are provided in [9] and [10]. The control inputs are the angular velocities of the ball, and these inputs can be generated by driving mechanisms inside the ball such as a small wheeled car [11] or rotors [12]. Motion of the ball can also be created by sandwiching the ball between the lower plate and an upper plate and controlling the motion of the upper plate, and controllers have been developed for this system using time-state control [13] and iterative feedback control [14].

Another variant of the ball–plate system is presented in [15], in which the ball rolls freely on a plate which rotates about its two planar axes. Balancing control is achieved using a linearized model of the dynamics.

The roles of the shape and motion of the manipulator in determining the motion of the rolling object were studied in the context of the "butterfly" contact juggling trick in [5]. No analysis is provided of feedback stabilization of rolling trajectories or balanced configurations, however. Inspired by this work, two-phase stabilization control for the butterfly system is addressed in [16] with an energy-based "swing-up" controller followed by a linear-quadratic regulator controller based on linear approximation. The rolling ball is modeled as a simple sliding point mass, and no experimental validation of the controller is provided.

This paper extends our previous work [17] in which we solve a feedback control problem of balancing the object at the unstable upright position. Compared with this balancing-only problem, we study in this paper more difficult problems of balancing with the hand or object at a desired angle or angular velocity.

B. Paper Outline

In Section II, the kinematic and dynamic equations of the diskon-disk system are derived. In Section III, stabilizing controllers that achieve our control objectives are designed based on fullstate feedback linearization. Simulation results are provided in Section IV. The experimental setup and experimental results are presented in Sections V and VI, respectively. Concluding remarks with future research directions are given in Section VII.

II. DYNAMICS OF THE DISK-ON-DISK

In this section, we derive the kinematic and dynamic equations of a smooth planar object rolling on a smooth, motion-controlled planar manipulator, referred to as the "hand." We then restrict to the special case of the disk-on-disk in Section II-C.

We define a coordinate frame $u_{\rm h}\text{-}v_{\rm h}$ attached to the hand, and let $p_{\rm h} \in \mathbb{R}^2$ be the position and $\theta_{\rm h}$ be the orientation of the frame in a world reference frame xy (see Fig. 1). The position and orientation of the frame $u_{\rm o}\text{-}v_{\rm o}$, which is attached to the center of mass of the object, are given by $p_{\rm o} \in \mathbb{R}^2$ and $\theta_{\rm o}$, respectively.

The curve of the hand is parameterized by an arclength parameter $s_h \in \mathbb{R}$, and the shape of the hand is given by $c_h(s_h) \in \mathbb{R}^2$ in the u_h - v_h frame. The parameter s_h increases counterclockwise along the hand. The object is parameterized by an arclength parameter s_o , where s_o increases clockwise, and the object shape in the u_o - v_o frame is given by $c_o(s_o) \in \mathbb{R}^2$. With this choice, the pure rolling assumption yields $\dot{s}_h = \dot{s}_o$. By an appropriate choice of the location of $s_o = 0$, we have $s_h = s_o$ at all times during rolling. For this reason, we specify the contact location by s_h only and do not refer to s_o .

Assuming the hand and object maintain rolling contact at all times, the system's configuration is fully specified by $q = [p_h^T, \theta_h, s_h]^T$.

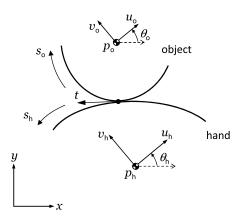


Fig. 1. Schematic of a general planar rolling manipulation system. The $u_{\rm h}$ - $v_{\rm h}$ frame is attached to the hand, and $\theta_{\rm h}$ denotes its orientation with respect to the xy world frame. Similarly, the $u_{\rm o}$ - $v_{\rm o}$ frame is attached to the object, and $\theta_{\rm o}$ denotes the frame's orientation.

A. Kinematic Equations

When we derive the rolling dynamics, it will be necessary to reconstruct the object's position $p_{\rm o}$ and orientation $\theta_{\rm o}$ from the minimal configuration representation $q=[p_{\rm h}^T,\theta_{\rm h},s_{\rm h}]^T$. This section provides the necessary equations.

At a contact point $c_{\rm h}(s_{\rm h}) = [u_{\rm h}(s_{\rm h}), v_{\rm h}(s_{\rm h})]^T$, the tangent vector is expressed as $t = c'_{\rm h} = [u'_{\rm h}, v'_{\rm h}]^T$ at an angle $\phi_{\rm h} = {\rm atan2}(v'_{\rm h}, u'_{\rm h})$ in the $u_{\rm h}$ - $v_{\rm h}$ frame, where the symbol \prime indicates a derivative with respect to the arclength parameter. Using the property $\|\frac{dc_{\rm h}}{ds_{\rm h}}\| = 1$ of arclength parameterizations, the signed curvature of the hand can be written as

$$\kappa_{\rm h}(s_{\rm h}) = \frac{d\phi_{\rm h}}{ds_{\rm h}} = u'_{\rm h}(s_{\rm h})v''_{\rm h}(s_{\rm h}) - u''_{\rm h}(s_{\rm h})v'_{\rm h}(s_{\rm h})$$
(1)

where $\kappa_h > 0$ means that the hand is convex at the contact point. Similarly, the signed curvature of the object is given by

$$\kappa_{\rm o}(s_{\rm h}) = \frac{d\phi_{\rm o}}{ds_{\rm h}} = u_{\rm o}'(s_{\rm h})v_{\rm o}''(s_{\rm h}) - u_{\rm o}''(s_{\rm h})v_{\rm o}'(s_{\rm h})$$
(2)

where $\phi_{\rm o}={\rm atan2}(v_{\rm o}',u_{\rm o}')$. Due to the opposite sense of the parameterization, $\kappa_{\rm o}<0$ indicates convexity. The relative curvature at $s_{\rm h}$ is

$$\kappa_{\rm r}(s_{\rm h}) = \kappa_{\rm h}(s_{\rm h}) - \kappa_{\rm o}(s_{\rm h}) \tag{3}$$

where $\kappa_{\rm r} > 0$ guarantees a single contact point locally.

The angle of the tangent vector measured in the world reference frame is written as

$$\theta_{\rm h} + \phi_{\rm h} = \theta_{\rm o} + \phi_{\rm o}$$

yielding

$$\theta_{0} = \theta_{h} + atan2(v'_{h}, u'_{h}) - atan2(v'_{0}, u'_{0})$$
 (4)

$$\dot{\theta}_{\rm o} = \dot{\theta}_{\rm h} + \dot{s}_{\rm h} \kappa_{\rm r}(s_{\rm h}) \tag{5}$$

$$\ddot{\theta}_{o} = \ddot{\theta}_{h} + \ddot{s}_{h}\kappa_{r}(s_{h}) + \dot{s}_{h}^{2}\kappa_{r}'(s_{h}). \tag{6}$$

To determine the dependence of p_0 and its derivatives on q and its derivatives, we start with the condition that the contact points on the hand and object are coincident

$$p_{\rm h} + R(\theta_{\rm h})c_{\rm h}(s_{\rm h}) = p_{\rm o} + R(\theta_{\rm o})c_{\rm o}(s_{\rm h})$$
 (7)

where the rotation matrix $R(\theta) \in SO(2)$ is given by

$$R(\theta) = \begin{bmatrix} \cos \theta & -\sin \theta \\ \sin \theta & \cos \theta \end{bmatrix}.$$

Noticing that $\frac{d}{dt}R(\theta) = \dot{\theta}R(\theta + \frac{\pi}{2})$ and plugging in (5), we obtain

$$p_{o} = p_{h} + R(\theta_{h})c_{h} - R(\theta_{o})c_{o}$$

$$\dot{p}_{o} = \dot{p}_{h} + \left(R\left(\theta_{h} + \frac{\pi}{2}\right)c_{h} - R\left(\theta_{o} + \frac{\pi}{2}\right)c_{o}\right)\dot{\theta}_{h}$$

$$+ \left(R(\theta_{h})c'_{h} - \kappa_{r}R\left(\theta_{o} + \frac{\pi}{2}\right)c_{o} - R(\theta_{o})c'_{o}\right)\dot{s}_{h}.$$
 (9)

The expression for \ddot{p}_{o} is obtained by differentiating (9) with respect to time and is omitted due to page limitations.

B. Dynamic Equations

The dynamic equations are derived from Lagrange's equations

$$\frac{d}{dt}\frac{\partial L}{\partial \dot{q}} - \frac{\partial L}{\partial q} = \tau \tag{10}$$

with Lagrangian L=K-U and the vector of generalized forces τ , where the kinetic energy K and potential energy U are given by

$$K = \frac{1}{2} \left(m_{\rm h} \dot{p}_{\rm h}^T \dot{p}_{\rm h} + I_{\rm h} \dot{\theta}_{\rm h}^2 + m_{\rm o} \dot{p}_{\rm o}^T \dot{p}_{\rm o} + I_{\rm o} \dot{\theta}_{\rm o}^2 \right)$$
(11)

$$U = g \left(m_{\rm h} p_{\rm h}^T + m_{\rm o} p_{\rm o}^T \right) \begin{bmatrix} 0 \\ 1 \end{bmatrix}$$
 (12)

where $m_{\rm h}, I_{\rm h}$ and $m_{\rm o}, I_{\rm o}$ are the mass and moment of inertia of the hand and object, respectively, and g is the gravitational acceleration. Inserting expressions (4), (5), (8), and (9) into Lagrange's equations (10) yields the dynamic equations.

C. Disk-on-Disk System

We now derive the dynamics for the disk-on-disk shown in Fig. 2. The radii of the hand and object disks are $r_{\rm h}$ and $r_{\rm o}$, respectively, and the hand is constrained to rotation only, i.e., $p_{\rm h}=0$.

Given a contact point expressed in the $u_{\rm h}$ - $v_{\rm h}$ and the $u_{\rm o}$ - $v_{\rm o}$ frames, respectively, as

$$c_{\rm h}(s_{\rm h}) = \begin{bmatrix} -r_{\rm h}\sin(s_{\rm h}/r_{\rm h}) \\ r_{\rm h}\cos(s_{\rm h}/r_{\rm h}) \end{bmatrix}$$
(13)

$$c_{\rm o}(s_{\rm h}) = \begin{bmatrix} -r_{\rm o}\sin(s_{\rm h}/r_{\rm o})\\ -r_{\rm o}\cos(s_{\rm h}/r_{\rm o}) \end{bmatrix}$$
(14)

from (1)–(3), we obtain the constant signed and relative curvatures

$$\kappa_{\rm h} = \frac{1}{r_{\rm h}}, \quad \kappa_{\rm o} = -\frac{1}{r_{\rm o}}, \quad \kappa_{\rm r} = \frac{r_{\rm h} + r_{\rm o}}{r_{\rm h} r_{\rm o}}.$$
(15)

Consequently, using (4)–(6), we obtain

$$\theta_0 = \theta_h + \kappa_r s_h \tag{16}$$

$$\dot{\theta}_{0} = \dot{\theta}_{h} + \kappa_{r} \dot{s}_{h} \tag{17}$$

$$\ddot{\theta}_{0} = \ddot{\theta}_{h} + \kappa_{r} \ddot{s}_{h}. \tag{18}$$

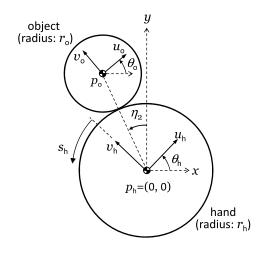


Fig. 2. Schematic of the disk-on-disk system. Both the hand and object are circular disks, and the hand is constrained to rotate about its center at the origin of the xy world frame. The angle η_2 is measured counterclockwise from the y-axis of the world frame to the center of the object.

Substituting (13) and (14) into (8) and (9) and rearranging, we have

$$p_{o} = \begin{bmatrix} -(r_{h} + r_{o})\sin(\theta_{h} + s_{h}/r_{h}) \\ (r_{h} + r_{o})\cos(\theta_{h} + s_{h}/r_{h}) \end{bmatrix}$$
(19)

(11)
$$\dot{p}_{o} = \begin{bmatrix} -(r_{h} + r_{o})\cos(\theta_{h} + s_{h}/r_{h})(\dot{\theta}_{h} + \dot{s}_{h}/r_{h}) \\ -(r_{h} + r_{o})\sin(\theta_{h} + s_{h}/r_{h})(\dot{\theta}_{h} + \dot{s}_{h}/r_{h}) \end{bmatrix}$$
(20)

$$\ddot{p}_{o} = \begin{bmatrix} -(r_{h} + r_{o})\cos(\theta_{h} + s_{h}/r_{h})(\ddot{\theta}_{h} + \ddot{s}_{h}/r_{h}) \\ +(r_{h} + r_{o})\sin(\theta_{h} + s_{h}/r_{h})(\dot{\theta}_{h} + \dot{s}_{h}/r_{h})^{2} \\ -(r_{h} + r_{o})\sin(\theta_{h} + s_{h}/r_{h})(\ddot{\theta}_{h} + \ddot{s}_{h}/r_{h}) \\ -(r_{h} + r_{o})\cos(\theta_{h} + s_{h}/r_{h})(\dot{\theta}_{h} + \dot{s}_{h}/r_{h})^{2} \end{bmatrix}. (21)$$

Inserting these expressions into Lagrange's equations, we solve for the dynamics

$$m_{11}\ddot{\theta}_{\rm h} + m_{12}\ddot{s}_{\rm h} + h_1(q) = \tau_{\rm h}$$
 (22a)

$$m_{21}\ddot{\theta}_{\rm h} + m_{22}\ddot{s}_{\rm h} + h_2(q) = 0$$
 (22b)

where

$$m_{11} = I_{\rm h} + I_{\rm o} + m_{\rm o} (r_{\rm h} + r_{\rm o})^2$$
 (23)

$$m_{12} = m_{21} = m_{\rm o}(r_{\rm h} + r_{\rm o})^2 / r_{\rm h} + I_{\rm o} \kappa_{\rm r}$$
 (24)

$$m_{22} = \kappa_{\rm r}^2 (m_{\rm o} r_{\rm o}^2 + I_{\rm o}) \tag{25}$$

$$h_1(q) = -m_0 g(r_h + r_0) \sin(\theta_h + s_h/r_h)$$
 (26)

$$h_2(q) = -m_0 g r_0 \kappa_r \sin(\theta_h + s_h/r_h). \tag{27}$$

In our experimental implementation, we use a highly geared harmonic drive DC motor to drive the hand. For this reason, it is more convenient to consider the hand's angular acceleration (created by a low-level acceleration controller) as the system input rather than the torque $\tau_{\rm h}$ in (22a). Defining this new acceleration control as $v=\ddot{\theta}_{\rm h}$ and substituting into (22b), we rewrite the dynamics as

$$\ddot{\theta}_{\rm h} = v \tag{28a}$$

$$\ddot{s}_{\rm h} = -\frac{1}{m_{22}} (m_{12}v + h_2(q)). \tag{28b}$$

By plugging (28) into (22a), the relationship between the hand torque τ_h and the new input v is found to be

$$\tau_{\rm h} = \left(m_{11} - \frac{m_{12}^2}{m_{22}}\right)v - \frac{m_{12}}{m_{22}}h_2 + h_1. \tag{29}$$

D. Friction Constraints

The previous derivations are predicated on the assumption that $s_{\rm h}=s_{\rm o}$ at all times, i.e., rolling is guaranteed. For some states and controls, however, this assumption of rolling may require the hand to "pull" on the object, i.e., it requires negative normal force $f_{\rm n}$, which is not physically possible. In others, the magnitude of the required friction force $f_{\rm f}$ may be greater than $\mu f_{\rm n}$ (μ is the Coulomb friction coefficient), which is also not possible and implies slip would occur. The conditions the contact forces must satisfy can be expressed abstractly as constraints on the state (q,\dot{q}) and control v:

$$F_{\mathbf{n}}(q, \dot{q}, v) \ge 0 \tag{30}$$

$$F_{\rm f}(q, \dot{q}, v) \le \mu \tag{31}$$

where the first condition represents the normal force constraint and the second the friction force constraint. The larger the friction coefficient μ , the larger the volume of the state-control space that satisfies the friction conditions for rolling. Outside of this volume, the object slips or falls from the hand. These constraints are not explicitly incorporated into the design of the control laws, but their effects are considered in the simulation studies.

III. STABILIZATION CONTROL

In this section, we propose a controller that performs the following control tasks: 1) balancing of the object at the upright position at a desired orientation and 2) balancing of the object at the upright position while spinning at a constant velocity.

The controller is based on full-state feedback linearization, and it is able to complete both tasks using the same framework with a slight difference in the choice of the change of coordinates.

A. Balancing With the Hand or Object at a Desired Angle

In this section, we propose a controller that rotates the hand or object disk to a specific angular position while balancing the object at the upright position. We present this controller to control the hand angular position, but object angular position control is also possible under the same framework and will be explained later in this section.

The system described by (28) can be expressed in state-space form with the state variable $z = [\theta_h, \dot{\theta}_h, s_h, \dot{s}_h]^T$ as

$$\dot{z}_1 = z_2 \tag{32a}$$

$$\dot{z}_2 = v \tag{32b}$$

$$\dot{z}_3 = z_4 \tag{32c}$$

$$\dot{z}_4 = -\frac{h_2(z)}{m_{22}} - \frac{m_{12}}{m_{22}}v. \tag{32d}$$

The task in this section will be completed by driving both velocities z_2 and z_4 to zero and z_1 to a specific angular position with the center of mass of the object directly above the center of the hand (the balanced position). Because the states z_1 and z_3 couple to determine the location of the center of mass of the object, we introduce the following change of coordinates:

$$\eta_1 = m_{22}\dot{s}_{\rm h} + m_{12}\dot{\theta}_{\rm h} \tag{33a}$$

$$\eta_2 = \theta_{\rm h} + s_{\rm h}/r_{\rm h} \tag{33b}$$

$$\delta = \theta_{\rm h} - \theta_{\rm h}^* \tag{33c}$$

$$\xi = \dot{\theta}_{\rm h} \tag{33d}$$

where θ_h^* represents a target angular position of the hand. The new state η_2 represents the angle to the center of the object measured counterclockwise with respect to the y-axis of the world frame (see Fig. 2). Hence, $\eta_2=0$ implies that the object is at the upright balanced position. The states η_1 and ξ span the original velocity space z_2 - z_4 . The job of the controller is now to stabilize all the states to zero.

The dynamic model is now written as

$$\dot{\eta}_1 = \sigma_1 \sin \eta_2 \tag{34a}$$

$$\dot{\eta}_2 = \sigma_2 \eta_1 + \sigma_3 \xi \tag{34b}$$

$$\dot{\delta} = \xi \tag{34c}$$

$$\dot{\xi} = v \tag{34d}$$

where $\sigma_1 \equiv m_{\rm o} g(r_{\rm h} + r_{\rm o})/r_{\rm h}, \sigma_2 \equiv 1/(r_{\rm h} m_{22})$, and $\sigma_3 \equiv 1 - m_{12}/(r_{\rm h} m_{22})$.

This system is full-state feedback linearizable [18, Ch. 4] if there exists a linearizing output h satisfying

$$\nabla h \operatorname{ad}_{f}^{i} q = 0, i = \{0, 1, 2\}$$
 (35a)

$$\nabla h \operatorname{ad}_{f}^{2} g \neq 0 \tag{35b}$$

where $\operatorname{ad}_f g$ denotes the Lie bracket defined by $\operatorname{ad}_f g = \nabla g f - \nabla f g, f = [\sigma_1 \sin \eta_2, \sigma_2 \eta_1 + \sigma_3 \xi, \xi, 0]^T$, and $g = [0, 0, 0, 1]^T$. The full-state feedback linearization allows us to transform the nonlinear system (34) to a linear one, and the derivatives of the output h correspond to the states of the transformed linear system. We solve (35) for the output h as $h = \eta_2 - \sigma_3 \delta$.

Taking derivatives of h until the input v appears yields

$$\dot{h} = \dot{\eta}_2 - \sigma_3 \dot{\delta}$$

$$=\sigma_2\eta_1\tag{36}$$

$$\ddot{h} = \sigma_2 \sigma_1 \sin \eta_2 \tag{37}$$

$$\ddot{h} = \sigma_2 \sigma_1 \cos \eta_2 (\sigma_2 \eta_1 + \sigma_3 \xi) \tag{38}$$

$$h^{(4)} = \beta(x) + \gamma(x)v \tag{39}$$

where, with $x = [\eta_1, \eta_2, \delta, \xi]^T$

$$\beta(x) = \sigma_1 \sigma_2 \sin \eta_2 \left(\sigma_1 \sigma_2 \cos \eta_2 - (\sigma_2 \eta_1 + \sigma_3 \xi)^2 \right) \tag{40}$$

$$\gamma(x) = \sigma_1 \sigma_2 \sigma_3 \cos \eta_2. \tag{41}$$

By introducing the input transformation

$$v = \frac{1}{\gamma(x)}(u - \beta(x)) \tag{42}$$

the nonlinear system (34) results in a linear system (quadruple integrator) given by

$$\dot{y}_1 = y_2$$

$$\dot{y}_2 = y_3$$

$$\dot{y}_3 = y_4$$

$$\dot{y}_4 = u \tag{43}$$

where $y = [y_1, y_2, y_3, y_4]^T = [h, \dot{h}, \ddot{h}, \ddot{h}]^T$. If we differentiate the output r times until the input appears, the number r is called the relative degree of the system. In order for a system to be full-state feedback linearizable, the relative degree must be equal to the order of the system itself. As shown in (39), the relative degree of the system is 4 ensuring full-state feedback linearization with no internal dynamics.

The new control input u can be easily designed as

$$u = -k_1 y_4 - k_2 y_3 - k_3 y_2 - k_4 y_1 \tag{44}$$

where k_i are positive control gains. This feedback control law gives a characteristic equation of

$$s^4 + k_1 s^3 + k_2 s^2 + k_3 s + k_4 = 0 (45)$$

where k_i are determined so that the roots of the characteristic equation lie in the left half plane. This choice of k_i stabilizes the origin y=0 and, consequently, the origin of the original space $x=[\eta_1,\eta_2,\delta,\xi]^T=0$.

The coordinate transformation (diffeomorphism) described by y=T(x) is valid in the region $\Omega=\{|\eta_2|<\frac{\pi}{2}\}$ since the input transformation (42) is not defined when $\gamma(x)=0$, i.e., $\cos\eta_2=0$. Note that the basin of attraction is practically global since, with no bound on other states, the region Ω determined by η_2 covers all physically possible configurations (outside of this region, the object must fall from the hand).

Remark 3.1: Control of the object's angular position θ_o is also possible by selecting the output $h=\eta_2-\sigma_3'\delta$ with the state $\delta=\theta_o-\theta_o^*$, where $\sigma_3'=\sigma_3/(1-\frac{\kappa_r m_{12}}{m_{22}})$. Then, we obtain the first derivative of δ , using (17), (33a), and (33d)

$$\dot{\delta} = \dot{\theta}_{o} = \dot{\theta}_{h} + \kappa_{r} \dot{s}_{h}
= \frac{\kappa_{r}}{m_{22}} \eta_{1} + \left(1 - \frac{\kappa_{r} m_{12}}{m_{22}}\right) \xi.$$
(46)

As a result, the derivative of h is given by

$$\dot{h} = \dot{\eta}_2 - \sigma_3' \dot{\delta}$$

$$= \sigma_2' \eta_1 \tag{47}$$

where $\sigma_2' = \sigma_2 - \sigma_3' \kappa_r / m_{22}$. The output h and its derivatives then have the same form as the hand position control. Therefore, the same control law (42) can be applied to object angle control with the constants δ_2' and δ_3' replacing δ_2 and δ_3 , respectively.

B. Balancing With Angular Velocity Control

In this section, the control objective of spinning of the hand or object at a constant velocity while balancing the object at the upright position is achieved by the same framework of the feedback linearization controller in the previous subsection. To this end, we modify the state δ as $\delta=\theta_{\rm h}-\dot{\theta}_{\rm h}^*t$, where t denotes time and $\dot{\theta}_{\rm h}^*$ the target hand velocity, yielding the following dynamic model:

$$\dot{\eta}_1 = \sigma_1 \sin \eta_2 \tag{48a}$$

$$\dot{\eta}_2 = \sigma_2 \eta_1 + \sigma_3 \xi \tag{48b}$$

$$\dot{\delta} = \xi - \dot{\theta}_{\rm h}^* \tag{48c}$$

$$\dot{\xi} = v. \tag{48d}$$

This choice of δ could be interpreted as hand position control with changing target position at a constant rate of $\dot{\theta}_h^*$.

The relative degree of the new system is still 4; therefore, the same form of the control law given in (42) and (44) can be used with $y_2 = \dot{h} = \sigma_2 \eta_1 + \sigma_3 \dot{\theta}_h^*$. However, the convergence of the feedback linearized system (43) to the origin now corresponds to that of the original system (48) to $(\eta_1, \eta_2, \delta, \xi) = (-\frac{\sigma_3}{\sigma_3} \dot{\theta}_h^*, 0, 0, \dot{\theta}_h^*)$.

The object velocity in steady state relates to the hand (target) velocity $\theta_{\rm h}^*$ such that

$$\dot{\theta}_{\mathrm{o}}^{*} = -\frac{r_{\mathrm{h}}}{r_{\mathrm{o}}} \dot{\theta}_{\mathrm{h}}^{*} \tag{49}$$

from using the time derivative of (33b) with $\dot{\eta}_2 = 0$ (in steady state) and (17). The control of the object velocity can be achieved using this relationship.

IV. SIMULATION RESULTS

Simulation results for the two control tasks are shown in this section. The values of parameters used in the simulation are the actual values of the disk-on-disk system constructed for experiment in Section V-A: $m_{\rm o}=0.142~{\rm kg}, r_{\rm o}=0.08~{\rm m}, I_{\rm o}=0.4544\times 10^{-3}{\rm kg\cdot m^2}, r_{\rm h}=0.15~{\rm m},$ and $g=9.62~{\rm m/s^2}$ (98.2 % of full gravity). All angles are measured in radians, and all units are SI, unless otherwise noted.

A. Balancing With the Hand or Object at a Desired Angle

For the simulation, we choose the control gains (k_1,k_2,k_3,k_4) such that the all roots of the characteristic equation (45) lie at -6 (in the left half plane), which yields $(k_1,k_2,k_3,k_4)=(24,216,864,1296)$. Given the initial conditions $\eta_2(0)=0.15$ and $\theta_h(0)=0$, the corresponding initial conditions of θ_o and s_h are calculated as $\theta_o(0)=0.431$ and $s_h(0)=0.023$ from (16) and (33b). The disks are initially at rest at the initial configuration, giving $\eta_1(0)=0$ and $\xi(0)=0$. The target hand position is $\theta_h^*=-\frac{\pi}{2}$, yielding $\delta(0)=\frac{\pi}{2}$.

As shown in Fig. 3, all the state variables η_1,η_2,δ , and ξ converge to zero, which physically means that the object stabilizes to the position directly above the hand with its angular velocity converging to zero, while the angular position of the hand converges to the target position of $-\frac{\pi}{2}$. The icons above Fig. 3 show the configurations of the two disks every 0.25 s, and they also show the positions of the hand at $-\frac{\pi}{2}$ in the steady state. Fig. 4 shows the input angular acceleration v (42) to the hand.

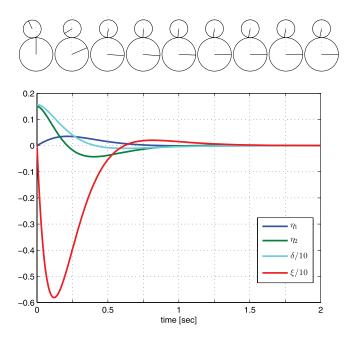


Fig. 3. Simulation results showing η_1,η_2,δ , and ξ converging to zero for balancing with angular position control. The quantities $\frac{1}{10}\delta$ and $\frac{1}{10}\xi$ are plotted instead of δ and ξ so that they can be shown on the same scale as η_1 and η_2 . The icons at the top show the configurations of the disks every 0.25 s.

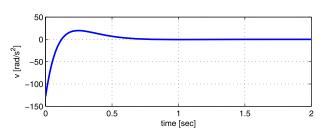


Fig. 4. Simulation result of the acceleration input v.

The necessary friction coefficient $\boldsymbol{\mu}$ to ensure rolling is calculated as

$$\mu \ge \frac{|f_{\mathrm{f}}|}{f_{\mathrm{n}}}$$

where $f_{\rm f}$ represents the friction force and $f_{\rm n}$ the normal force at a contact point. These contact forces acting on the object can be determined from the object's acceleration added with the force to counteract gravity such that

$$f_{\rm n} = m_{\rm o}(\ddot{y}_{\rm o} + g)\cos\eta_2 - m_{\rm o}\ddot{x}_{\rm o}\sin\eta_2 \tag{50}$$

$$f_{\rm f} = m_{\rm o}(\ddot{y}_{\rm o} + g)\sin\eta_2 + m_{\rm o}\ddot{x}_{\rm o}\cos\eta_2.$$
 (51)

In turn, inserting (21) with $\eta_2 = \theta_h + s_h/r_h$, we have

$$f_{\rm n} = -m_{\rm o}(r_{\rm h} + r_{\rm o})(\sigma_2 \eta_1 + \sigma_3 \xi)^2 + m_{\rm o} g \cos \eta_2 \tag{52}$$

$$f_{\rm f} = -m_{\rm o}(r_{\rm h} + r_{\rm o})(\sigma_2 \sigma_1 \sin \eta_2 + \sigma_3 v) + m_{\rm o} g \sin \eta_2.$$
 (53)

As noted earlier, the contact forces f_n and f_f are a function of the state (η_1, η_2, ξ) and control v. Substituting the simulation results into these contact force expressions, Fig. 5 plots the minimum friction coefficient μ needed to ensure rolling as a function of time. At the beginning of the run, when the object is left of

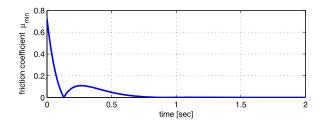


Fig. 5. Plot of the minimum friction coefficient required to prevent slipping at the contact during balancing. The friction force changes sign at approximately $t=0.13~\mathrm{s}$.

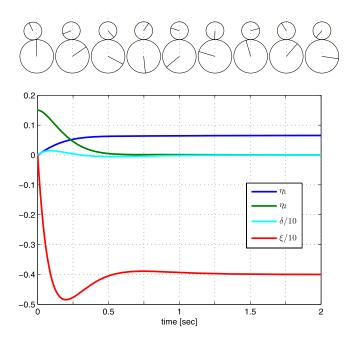


Fig. 6. Simulation results showing η_1 , η_2 , δ , and ξ for balancing with angular velocity control.

center, the large control acceleration v requires a large friction coefficient to prevent slipping. As the object becomes balanced above the hand, the friction coefficient required for rolling drops to zero.

B. Balancing With Angular Velocity Control

For this simulation, we again choose the control gains $(k_1, k_2, k_3, k_4) = (24, 216, 864, 1296)$. The target hand velocity is set at -4 rad/s. The object also starts from rest at the initial condition $\eta_2(0) = 0.15$.

As shown in Fig. 6, the state δ converges to zero, i.e., the angular velocity of the hand converges to the target velocity of -4 rad/s. The convergence of the hand velocity to -4 rad/s is more directly observed with the state ξ . The state η_2 also converges to zero indicating that the center of the object converges to directly above the hand. In fact, $\eta_1 = -\frac{\sigma_3}{\sigma_2}\xi$ in the steady state, which is obtained from (38) by substituting h = 0. The icons above the figure show that the hand and object keep rotating.

Remark 4.1: We might ask whether it is possible to balance the object at a position not directly above the center of the hand. This

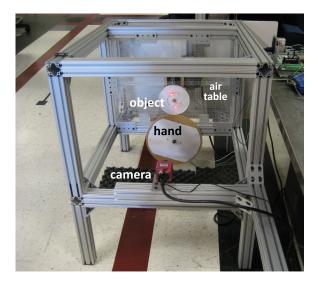


Fig. 7. Disk-on-disk experimental setup. The upper disk (object) rolls on the lower disk (hand). The hand is actuated by a harmonic drive DC motor. A high-speed camera and vision system are used for visual feedback of the object. This snapshot was taken when the system was under control action.

is not practically possible, as the vertical contact force needed to cancel gravity necessarily creates a moment about the object's center of mass. This means that the object (and the hand) must rotate at a constant angular acceleration, resulting in unbounded velocities. This can be seen in the governing equations (34) by plugging a constant value into η_2 and setting $\dot{\eta}_2 = 0$.

V. EXPERIMENTAL SETUP

A. Hardware

Fig. 7 shows our disk-on-disk experimental setup. The hand is the lower disk, actuated by a harmonic drive DC motor (Harmonic Drive RH-8D 6006) equipped with a 50:1 harmonic drive gearhead and a 500 ppr quadrature encoder giving 100 000 counts per revolution at the output shaft. The object disk is free to roll on the hand. The commanded current input to the motor is provided through a motor amplifier (Copley Controls Junus 800-1468). The disk-on-disk system is mounted on an air table that provides frictionless support in a plane tilted 79.0° with respect to horizontal (98.2% of full gravity). Both hand and object are made of 1/4-in-thick acrylic and the object is encircled by a rubber band to increase friction.

The hand control algorithm runs on a PC104 stack with a QNX real-time operating system (RTOS). In addition to the angular position data from the encoder of the hand, the controller utilizes the state of the object disk, which is determined using a high-speed vision system. The vision system, consisting of a PhotonFocus TrackCam camera, a Microenable III frame grabber, and a Windows PC, tracks two markers on the disk at 800 Hz, allowing estimation of the position and orientation of the disk at 800 Hz. The vision program, which is written in C++, sends the orientation of the disk to the controller PC104 stack via TCP/IP (see Fig. 8). The tracking markers may be high-contrast passive markers (e.g., black on white) or active markers (LEDs in the current implementation).

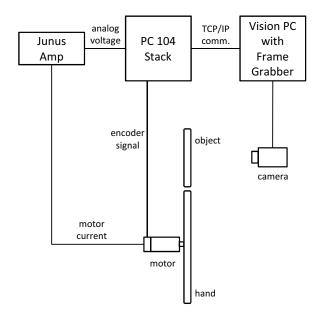


Fig. 8. Schematic of the experimental setup showing signal paths with a side view of the hand and object. The actual disk-on-disk system is tilted 79.0° with respect to the horizontal plane.

B. Controller Implementation

The control algorithm is written in C++ and runs on the PC104 stack. Using the QNX RTOS, the control loop runs at 800 Hz in sync with the vision system. As the control law requires the angular velocity of each disk, we apply differencing plus low-pass filters to the encoder and vision data to estimate velocity.

Since our control law (42) generates acceleration commands v, we implement an additional acceleration control loop converting these controls to the motor current requested from the motor amplifier. This inner controller is written as

$$i_{\text{com}} = i_{\text{ff}}(\dot{\theta_{\text{h}}}, v) + k_{\text{p}}(\theta_{\text{ref}} - \theta_{\text{h}}) + k_{\text{d}}(\dot{\theta}_{\text{ref}} - \dot{\theta}_{\text{h}})$$
 (54)

where $i_{\rm com}$ is the commanded motor current, $i_{\rm ff}$ is a feedforward motor current based on the hand's angular velocity and requested acceleration, $\theta_{\rm ref}$ and $\dot{\theta}_{\rm ref}$ are the desired hand position and velocity obtained by integrating the acceleration command v(t), and $k_{\rm p}$ and $k_{\rm d}$ are PD gains. The feedforward motor current is based on the simple model

$$(I_{\rm h} + I_{\rm m})\ddot{\theta}_{\rm h} = k_{\rm m}i - \mu_{\rm d}\dot{\theta}_{\rm h} - f_{\rm s}{\rm sgn}(\dot{\theta}_{\rm h}) \tag{55}$$

where $I_{\rm h}$ and $I_{\rm m}$ denote the inertia of the hand and the motor rotor, respectively, $k_{\rm m}$ is the motor constant, i is the motor current, $\mu_{\rm d}$ is a viscous friction coefficient, $f_{\rm s}$ is the torque required to overcome friction from rest, and the function ${\rm sgn}(\cdot)$ returns the sign of its argument. The inertia of the motor $I_{\rm m}$ is the reflected inertia due to the gearhead. We estimated the values of $k_{\rm m}$, $\mu_{\rm d}$, and $f_{\rm s}$ in motor modeling experiments, and the feedforward current $i_{\rm ff}$ is calculated by substituting the commanded acceleration v and current hand velocity $\dot{\theta}_{\rm h}$ into (55). After estimating the parameters of the feedforward model, the PD gains were tuned experimentally to reject modeling errors, yielding $(k_{\rm p},k_{\rm d})=(150,0.9)$. Fig. 9 shows that the inner loop

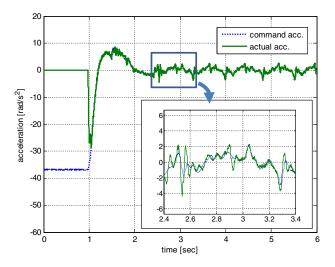


Fig. 9. Experimental result showing the command and actual accelerations of the hand for an experimental run. The actual acceleration follows the command acceleration satisfactorily. The control action starts at $t=1.00~\rm s$.

acceleration controller (54) provides satisfactory tracking of the commanded hand acceleration v.

VI. EXPERIMENTAL RESULTS

The video attachment shows experimental runs of the different controllers performed in a continuous series. (This video can also be seen at https://vimeo.com/54405698.) The initial conditions of each task do not correspond to the controlled initial conditions in the data presented below.

A. Balancing With the Hand or Object at a Desired Angle

The feedback linearization controller in this experiment was commanded to rotate the hand to negative 90° while balancing the object to the upright position. Since feedback linearization-based controllers generally possess high sensitivity to parametric uncertainty or unmodeled dynamics, to enhance its robustness, we added an additional term ρ using integral control [19, Ch. 12.4] to the control input (44) such that

$$u = -k_1 y_4 - k_2 y_3 - k_3 y_2 - k_4 y_1 - k_5 \rho$$
(56)

where the variable ρ is integrating the position error, defined as $\dot{\rho}=\theta_{\rm h}^*-\theta_{\rm h}$. With this choice of ρ , stability is guaranteed locally near the equilibrium position, but the basin of attraction appears to be large enough for the given initial conditions. The same control gains of $(k_1,k_2,k_3,k_4)=(24,216,864,1296)$ were used with $k_5=100$.

Fig. 10 shows the state variables $(\eta_1,\eta_2,\delta,\xi)$ for one experimental run. The initial condition of the experiment was set at $(\eta_1,\eta_2,\delta,\xi)=(0,0.099,1.57,0)$, which means that initially, both disks were at rest and the object disk was placed with its center of mass at an angle of 0.099 rad (5.67°) relative to the world y-axis. The object disk was kept at rest at the initial position using a small block until control action starts at t=0.95 s.

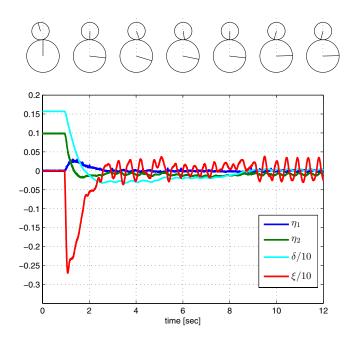


Fig. 10. Experimental result showing the state variables η_1,η_2,δ , and ξ for balancing with angular position control. The target angle of the hand is $-\frac{\pi}{2}$. The control action starts at t=0.95 s. The icons at the top show the configurations of the disks every 2 s.

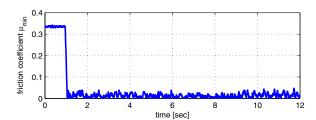


Fig. 11. Plot of the minimum friction coefficient required to prevent slipping at the contact during the experiment. This plot uses the experimental data of the states and control input to calculate the friction coefficient.

After the hand angular position θ_h settles within the range of $\pm 5\%$ of the initial condition at t=8.90 s, the RMS error of θ_h is 0.030 (1.719°) for the target hand position of $-\frac{\pi}{2}$. Similarly, after t=8.90 s, the RMS errors of η_2 , which is the angle to the center of the object with respect to the y-axis, is 0.0092 (0.527°), and the RMS errors of η_1 and ξ , which are related to the angular velocities of the object and hand, are 0.0015 and 0.2018, respectively. Due to the added integral action, the response of θ_h , which can be seen by the hand position error δ , shows a long settling time and overshoot during the transient period in Fig. 10.

We observed the appearance of small-amplitude limit cycles near the balanced configuration. That is because the simulation and experiment differ in a number of ways, including discrete-time implementation, approximate control of the motor acceleration, quantized position sensing, continuous small perturbations from the air table, etc.

Fig. 11 shows that the friction coefficient to prevent slipping is required to be greater than 0.34 for this experiment (at the beginning of the run). This plot uses the experimental data of

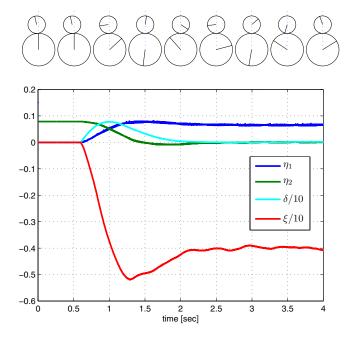


Fig. 12. Experimental result showing the state variables η_1 , η_2 , δ , and ξ for balancing with angular velocity control. The target angular velocity of the hand is -4 rad/s. The control action starts at t=0.60 s. The icons at the top show the configurations of the disks every 0.5 s.

the states and control input to calculate the required minimum friction coefficient using (52) and (53). The actual friction coefficient of approximately 2.0, which is obtained from an empirical measurement, ensures rolling during the experiment.

B. Balancing With Angular Velocity Control

In this experiment, the task of balancing the object is performed, while the hand is simultaneously controlled to spin at an angular velocity of -4 rad/s.

Fig. 12 shows the state variables $(\eta_1,\eta_2,\delta,\xi)$. With the target hand velocity of -4 rad/s, the initial conditions were given as $(\eta_1,\eta_2,\delta,\xi)=(0,0.0787,0,0)$. The control gains were chosen as $(k_1,k_2,k_3,k_4)=(16,96,256,256)$ with the repeated root of the characteristic equation at -4. The control action started at t=0.60. After ξ settles within $\pm 2\%$ of the target velocity, i.e., 0.08 rad/s, at t=2.12 s, the RMS error of the hand velocity is 0.0513 rad/s and the RMS error of η_2 is 0.0016 (0.092°) . The required friction coefficient to prevent slip during this experiment is computed to be greater than 0.08.

VII. CONCLUSION

In this paper, as a first step to understanding the nature of dynamic nonprehensile manipulation, we studied the canonical rolling manipulation problem of a disk rolling on a disk. We derived the kinematic and dynamic equations of the diskon-disk system. Based on these, we derived and demonstrated controllers to balance the object disk at the unstable upright position, while the hand or object rotates to a specific orientation or spins at a constant velocity. The importance of this study is that it is a concrete step toward establishing rolling as a viable

manipulation primitive. The presented approach can possibly be extended in theory to complete the same tasks with nonsymmetric objects, like its center of mass is not on the geometric center, by considering that the control task is to balance the object's center of mass on the vertical line at the contact point. Future work will focus on motion planning and feedback stabilization of a broad class of rolling trajectories for smooth planar objects rolling on smooth planar hands (other than disks) moving with a full three degrees of freedom. The resulting dynamic rolling manipulation primitive will be incorporated into our library of nonprehensile manipulation primitives toward the development of a unified framework for planning and control of dynamic robotic manipulation.

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