

### Assignment 3

Ex 1

$$\text{a) } I_y(x, y) = \frac{\partial}{\partial y} [g(x) \cdot g(y) \cdot I(x, y)] \\ = g(x) \left[ \frac{d}{dy} g(y) \cdot I(x, y) \right]$$

$$I_{yy}(x, y) = \frac{\partial}{\partial y} [g(x) \cdot g(y) \cdot I_y(x, y)] \\ = g(x) \left[ \frac{d}{dy} g(y) \cdot I_y(x, y) \right]$$

$$I_{xy}(x, y) = \frac{\partial}{\partial y} [I_x(x, y)] \\ = \frac{\partial}{\partial y} \left[ \frac{d}{dx} g(x) \cdot g(y) \cdot I(x, y) \right] \\ = \frac{d}{dx} g(x) \cdot \left[ \frac{d}{dy} g(y) \cdot I(x, y) \right]$$

$$\text{b) } P_1(0, 0), P_2(1, 1), P_3(1, 0), P_4(2, 2)$$

$$\cdot P_1 - P_2$$

$$y = x \quad (k = \frac{x-y}{1-0}) \\ p = 0, \theta = \frac{\pi}{4}$$

$$x \cdot \cos(\theta) + y \cdot \sin(\theta) = p$$

$$\cdot P_1 - P_3$$

$$y = 0 \\ p = 0, \theta = \frac{\pi}{2}$$

$$\cdot P_1 - P_4$$

$$y = x \\ p = 0, \theta = \frac{\pi}{4}$$

Observe:

1.  $P_1 \rightarrow P_2 \rightarrow P_4$
2.  $P_1 \rightarrow P_3$
3.  $P_2 \rightarrow P_3$
4.  $P_3 \rightarrow P_4$

} So collinear

$$\cdot P_2 - P_3$$

$$y = 1 \\ p = 1, \theta = 0$$

$$\cdot P_2 - P_4$$

$$y = x \\ p = 0, \theta = \frac{\pi}{4}$$

$$\cdot P_3 - P_4$$

$$y = 2x - 2$$

$$2x - y - 2 = 0 \Rightarrow A = 2, B = -1, C = -2$$

$$\|u\| = \sqrt{A^2 + B^2} = \sqrt{5}$$

$$\cos \theta = \frac{A}{\|u\|} = \frac{2}{\sqrt{5}}, \sin \theta = \frac{B}{\|u\|} = \frac{-1}{\sqrt{5}}$$

$$\theta = \arctan\left(-\frac{1}{2}\right) = -0.46 \text{ rad}$$

$$p = -\frac{C}{\|u\|} = \frac{2}{\sqrt{5}}$$