

$$2) \quad f(x_1, x_2, x_3) = (x_3 \cdot_1 (x_3 \cdot_2 x_2)) \wedge (\overline{x_3} \cdot_3 x_2) \wedge x_1 \vee (\bar{x}_1 \wedge \bar{x}_2)$$

$$x_1 \vee (\bar{x}_1 \wedge \bar{x}_2) = (x_1 \vee \bar{x}_1) \wedge (x_1 \vee \bar{x}_2)$$

$$= 1 \wedge (x_1 \vee \bar{x}_2)$$

$$= (x_1 \vee \bar{x}_2)$$

$$\rightarrow x_3 = \underbrace{(x_3 \cdot_1 (x_3 \cdot_2 x_2)) \wedge (\overline{x_3} \cdot_3 x_2)}_{x_3}$$

\rightarrow

$$x_3 \cdot_1 (x_3 \cdot_2 x_2) = x_3 \quad \text{wenn} \quad \cdot_1 \neq \cdot_2$$

$$\rightarrow x_3 \wedge (\overline{x_3} \cdot_3 x_2) = x_3 \wedge (x_3 \cdot_3 \bar{x}_2)$$

$$\rightarrow \cdot_3 = 1$$

$$(x_3 \cdot_1 (x_3 \cdot_2 x_2)) \wedge (\overline{x_3} \cdot_3 x_2) = x_3$$

$$(x_3 \cdot_1 (x_3 \cdot_2 x_2)) \wedge (x_3 \cdot_3 \bar{x}_2) = x_3 \quad ; \quad \text{mit} \quad \cdot_3 = \vee$$

$$\Rightarrow (x_3 \cdot_1 (x_3 \cdot_2 x_2)) = (x_3 \vee x_2)$$

$$\rightarrow \cdot_1 = \cdot_2 = \vee$$

Möglichkeiten:

$$\begin{aligned} f_v(x_1, x_2, x_3) &= x_3 \wedge (x_1 \vee \bar{x}_2) \\ f_1(x_1, x_2, x_3) &= (x_3 \wedge (x_3 \vee x_2)) \wedge (\overline{x_3} \wedge x_2) \wedge (x_1 \vee (\bar{x}_1 \wedge \bar{x}_2)) \\ f_2(x_1, x_2, x_3) &= (x_3 \vee (x_3 \wedge x_2)) \wedge (\overline{x_3} \wedge x_2) \wedge (x_1 \vee (\bar{x}_1 \wedge \bar{x}_2)) \\ f_3(x_1, x_2, x_3) &= (x_3 \vee (x_3 \vee x_2)) \wedge (\overline{x_3} \wedge x_2) \wedge (x_1 \vee (\bar{x}_1 \wedge \bar{x}_2)) \end{aligned}$$

| x_1 | x_2 | x_3 | f_v | f_1 | f_2 | f_3 |
|-------|-------|-------|-------|-------|-------|-------|
| 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| 0 | 0 | 1 | 1 | 1 | 1 | 1 |
| 0 | 1 | 0 | 0 | 0 | 0 | 0 |
| 0 | 1 | 1 | 0 | 0 | 0 | 0 |
| 1 | 0 | 0 | 0 | 0 | 0 | 0 |
| 1 | 0 | 1 | 1 | 1 | 1 | 1 |
| 1 | 1 | 0 | 0 | 0 | 0 | 0 |
| 1 | 1 | 1 | 1 | 1 | 1 | 1 |