

Working Title: Reverse Design of Meta-surface Stacks via Neural Network

Tim Turan

January 30, 2020

1 Abstract

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2 Physical Background

2.1 Meta Surfaces

2.2 The S-Matrix Formalism

$$\hat{S} = \begin{pmatrix} \hat{T}^f & \hat{R}^b \\ \hat{R}^f & \hat{T}^b \end{pmatrix} \quad (1)$$

2.3 SASA and the Star Product

2.4 (Convolutional) Neural Networks

Artificial Neural Networks (ANN's or short NN's) are a kind of data structure inspired by the biological Neurons found in Nature. They can be used to find a wide range of input output relations. One classic example is mapping pictures of hand written digits to the actual digits. Rather than explicitly program the relation NN's are trained on a dataset (X, Y) of correct input output pairs.

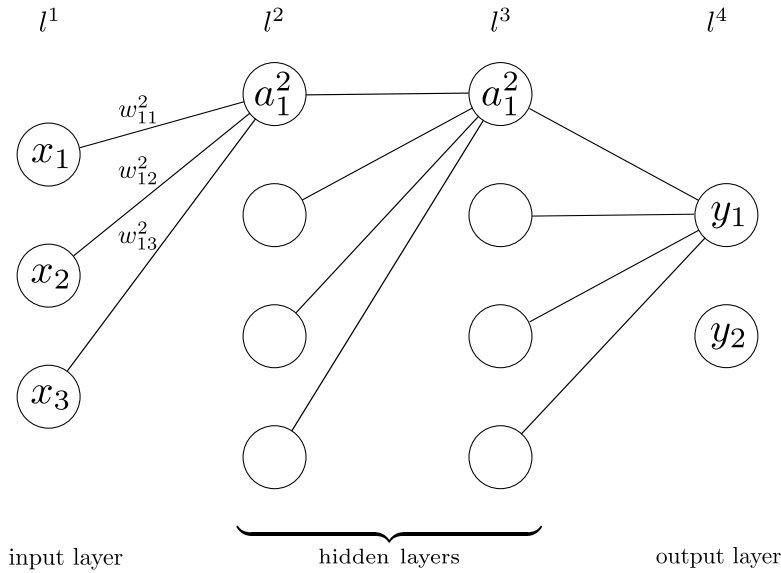


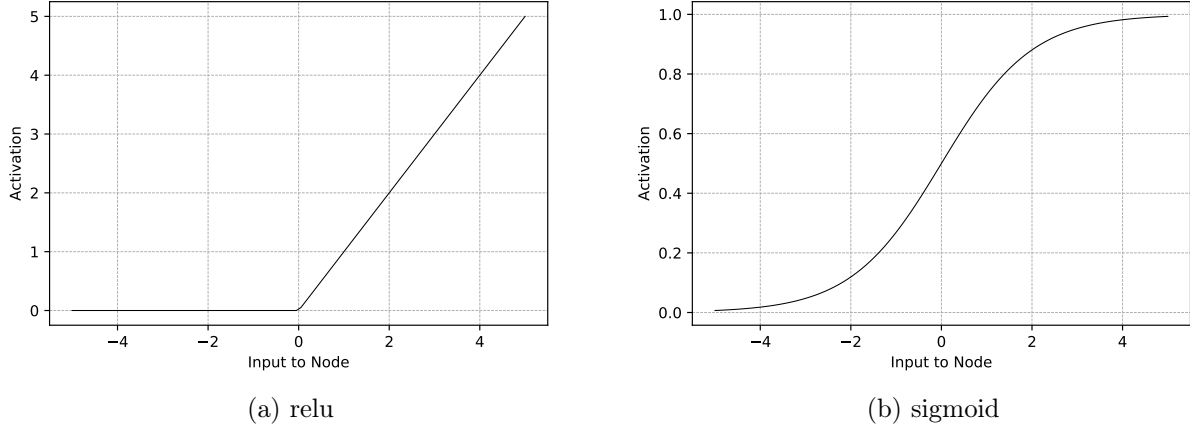
Figure 1: The most simple kind of NN is called densely connected. For clarity only connections to the top most nodes of each layer are shown.

Densely Connected Neural Networks This kind of NN consist of single nodes which are organized into layers. Every node is connected to all the nodes of the previous and next layer thus they are called dense. Each node holds a value called activation a where the activation to the first layer is the input to the network, here: (x_1, x_2, x_3) . To calculate the activation of a node one has to multiply all the previous activations with their respective weights w , add the bias b and finally apply a non-linear activation function σ . For the index notation superscripts specify the layer and subscripts the node. So a_1^2 is the activation of the first node in the second layer. To characterize a weight two subscripts are needed for the end and beginning of the connection. For the example in 1 that means:

$$a_1^2 = \sigma \left(\sum_i w_{1i}^2 x_i + b_1^2 \right) \quad (2)$$

However it is more convenient to stop considering every node individually and to view the involved quantities as vectors and matrices. So that (2) can be written as:

$$\mathbf{a}^l = \sigma \left(\hat{\mathbf{w}}^l \mathbf{a}^{l-1} + \mathbf{b}^l \right) \quad (3)$$

Figure 2: Two examples of activation functions σ .

Training During training the network output $\text{NN}(\mathbf{x}) = \mathbf{y}'$ is calculated through repeated use of (3) and is then compared with the known correct output \mathbf{y} by a cost function $C = C(\mathbf{y}, \mathbf{y}')$. This might simply be the mean squared difference between \mathbf{y} and \mathbf{y}' but there are more sophisticated cost functions for different kind of outputs. Now we can quantify how well the NN is performing but how should the weights and biases be changed to improve this performance? Here a very important Algorithm *Backpropagation* comes into play and allows a efficient calculation of $\nabla C_{\mathbf{b}^l}$ and $\nabla C_{\mathbf{w}^l}$. These are used to gradually minimize the cost function. A very comprehensive explanation of Backpropagation can be found here: [1].

3 The Algorithm

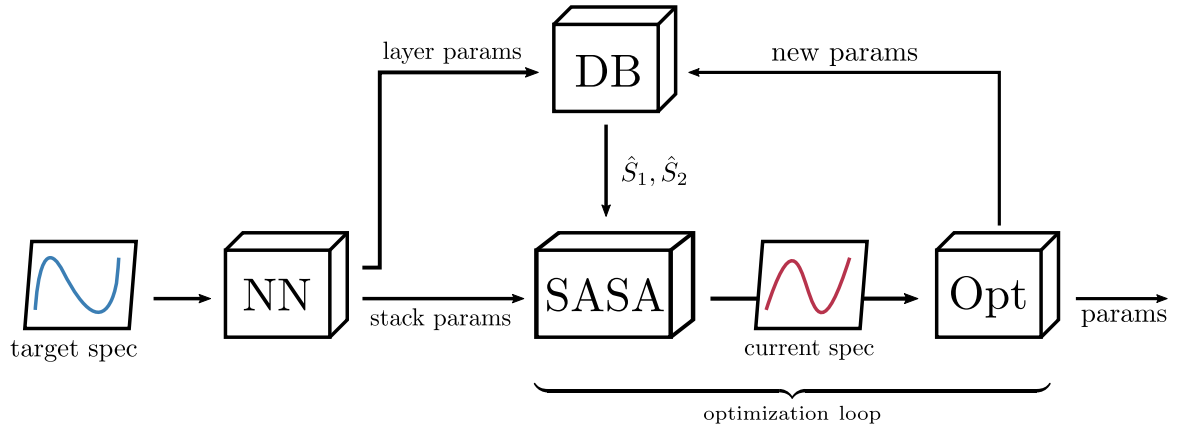


Figure 3: A Flowchart of the Algorithm

NN	convolutional neural ntwork trained to map spectra to stack and layer parameters
DB	database of FMM simulated single layers
SASA	algorithm calculating $\hat{S}_{\text{stack}} = \hat{S}_{\text{stack}}(\hat{S}_1, \hat{S}_2, \dots)$
Opt	optimizer changing parameters to minimize the difference between the current and target spectrum
\hat{S}_1, \hat{S}_2	S-matrices of the top and bottom layer
layer params	these include the geometry of the periodic meta surface cell and the kind of material used
stack params	the rotation angle of the layers to one another and the distance between
new params	the Opt. only changes the continuous parameters, the discrete ones , e.g. material, remain unchanged
optimization loop	this loop is repeated until the target accuracy is reached

4 The Neural Network

5 The Optimizer

6 Results

7 Literaturverzeichnis

References

- [1] Michael Nielsen. <http://neuralnetworksanddeeplearning.com/chap2.html>, December 2019.

8 Anhang