

# Written Homework 1

Tim Stolp

06-11-2018

## 1 Introduction

## 2 Regression

- a  $(r - Xw)^T(r - Xw)$   
 $Xw = \hat{r}$   
 $(r - \hat{r})^T(r - \hat{r})$   
 $\hat{r}^i = w^T \hat{x}^i$   
 $(r - w^T \hat{x}^i)^T(r - w^T \hat{x}^i)$   
 $\sum_{i=1}^N (r^i - w^T \hat{x}^i)^2$
- b  $(r - Xw)^T(r - Xw)$   
 $r^T - w^T X^T(r - Xw)$   
 $r^T r - w^T X^T r - r^T Xw + w^T X^T Xw$
- c  $r = N \times 1$   
 $r - Xw$  so  $Xw$  must also be  $N \times 1$   
 $X = N \times (d+1)$   
 $w = (d+1) \times 1$
- d  $r - Xw = N \times 1$   
 $(r - Xw)^T = 1 \times N$   
 $(r - Xw)^T(r - Xw) = 1 \times 1$   
 $E(w|X, r) = 1 \times 1$
- e  $r^T r - w^T X^T r - r^T Xw + w^T X^T Xw$   
 $-X^T r - X^T r + (X^T X + X^T X)w$   
 $wX^T Xw - 2X^T r$
- f  $wX^T Xw - 2X^T r = 0$   
 $X^T Xw = X^T r$   
 $Xw = r$   
 $w = X^{-1}r$

### 3 Bayesian Decision Theory

P = Positive result

I = infected

$$p(I|P) = \frac{p(P|I)p(I)}{p(P|I)p(I)+p(P|I^C)p(I^C)}$$

$$p(I) = 0,0052$$

$$p(I^C) = 1 - 0,0052 = 0,9948$$

$$p(P|I) = 1$$

$$p(P|I^C) = 0,03$$

$$\frac{1 \cdot 0,0052}{1 \cdot 0,0052 + 0,03 \cdot 0,9948} \approx 0,148$$

-

### 4 Association Rules

*Chair*  $\rightarrow$  *Table*

*Support* :  $\frac{1}{3}$

*Confidence* : 1

*Lift* : 2

*Table*  $\rightarrow$  *Chair*

*Support* :  $\frac{1}{3}$

*Confidence* :  $\frac{2}{3}$

*Lift* : 2

*Flowerpot*  $\rightarrow$  *Table*

*Support* :  $\frac{1}{6}$

*Confidence* :  $\frac{1}{2}$

*Lift* : 1

*Table*  $\rightarrow$  *Flowerpot*

*Support* :  $\frac{1}{6}$

*Confidence* :  $\frac{1}{3}$

*Lift* : 1

## 4.1 Discriminant Functions

a  $C_1 = \text{spam}, C_2 = \text{not spam}$

$$g(x, y) = p(C_1|x, y) - p(C_2|x, y)$$

$$\text{choose} \begin{cases} C_1 & \text{if } g(x, y) > 0 \\ C_2 & \text{otherwise} \end{cases}$$

b without normalizing term.

$$g(x, y) = p(x, y|C_1)p(C_1) - p(x, y|C_2)p(C_2)$$

$$p(C_1) = 0,17 \text{ and } p(C_2) = 0,83$$

Take  $x = 4$  and  $y = 5$

$$p(x, y|C_1) = 0,85$$

$$p(x, y|C_2) = 0,06$$

$$g(x, y) = 0,85 \cdot 0,17 - 0,06 \cdot 0,83 = 0,0947 \approx 0,095$$

$0,095 > 0$  so the email is considered spam

c  $g(x, y) = \frac{p(C_1|x, y)}{p(C_2|x, y)}$

$$\text{choose} \begin{cases} C_1 & \text{if } g(x, y) > 1 \\ C_2 & \text{otherwise} \end{cases}$$

Bayes and ignoring the normalization terms:

$$g(x, y) = \frac{p(x, y|C_1)}{p(x, y|C_2)} \cdot \frac{p(C_1)}{p(C_2)}$$

d  $g(x, y) = \log \frac{p(C_1|x, y)}{p(C_2|x, y)}$

$$\text{choose} \begin{cases} C_1 & \text{if } g(x, y) > 0 \\ C_2 & \text{otherwise} \end{cases}$$

Bayes and ignoring the normalization terms:

$$g(x, y) = \log \frac{p(x, y|C_1)}{p(x, y|C_2)} + \log \frac{p(C_1)}{p(C_2)}$$