

CFG constructions

1. Describe context-free grammars that generate each of the following languages.

a) All strings in $\{0,1\}^*$ whose length is divisible by 5.

b) $\{0^n 1^{2n} \mid n \geq 0\}$.

c) $\{0^n 1^m \mid n \neq m - 1\}$.

d) $\{0^i 1^j 2^k \mid i, j \geq 0\}$.

e) $\{0^n 1^m \mid 2n \leq m \leq 3n\}$.

f) $\{0^i 1^j 2^{i+j} \mid i, j \geq 0\}$.

g) $\{0^n w w^R 0^n \mid n \geq 0, w \in \{0,1\}^*\}$.

h) $\{0^n 1^m \mid n \leq m + 3\}$.

i) $\{0^n 1^m \mid n \neq m\}$.

j) All the strings over $\{0,1\}$ with more 0's than 1's.

k) $\{x \# y \mid x, y \in \{0,1\}^* \text{ and } |x| = |y|\}$.

l) $\{0^i 1^j 2^k \mid i = j \text{ or } j = k\}$.