

Binary Search Tree

- Describe efficient recursive algorithms that can be used to compute the size as well as the height of a binary search tree that is given as input. Your algorithms should each use a number of steps that is **at most linear** in the size of the given binary search tree.

Height

```
int findHeight(TreeNode<T> aNode)
{
    if(aNode == 0)
        return -1;

    int lefth = findHeight(aNode.left);
    int righth = findHeight(aNode.right);

    if(lefth > righth)
        return lefth + 1;
    else
        return righth + 1;
}
```

Size

size(tree)

1. If tree is empty then return 0

2. Else

(a) Get the size of left subtree recursively i.e., call
size(tree->left-subtree)

(a) Get the size of right subtree recursively i.e., call
size(tree->right-subtree)

(c) Calculate size of the tree as following:
$$\text{tree_size} = \text{size}(\text{left-subtree}) + \text{size}(\text{right-subtree}) + 1$$

(d) Return tree_size

Proof ?

Write a recurrence

- $\text{Steps}(T) = \text{Steps}(T/2) + c + \text{Steps}(T/2)$