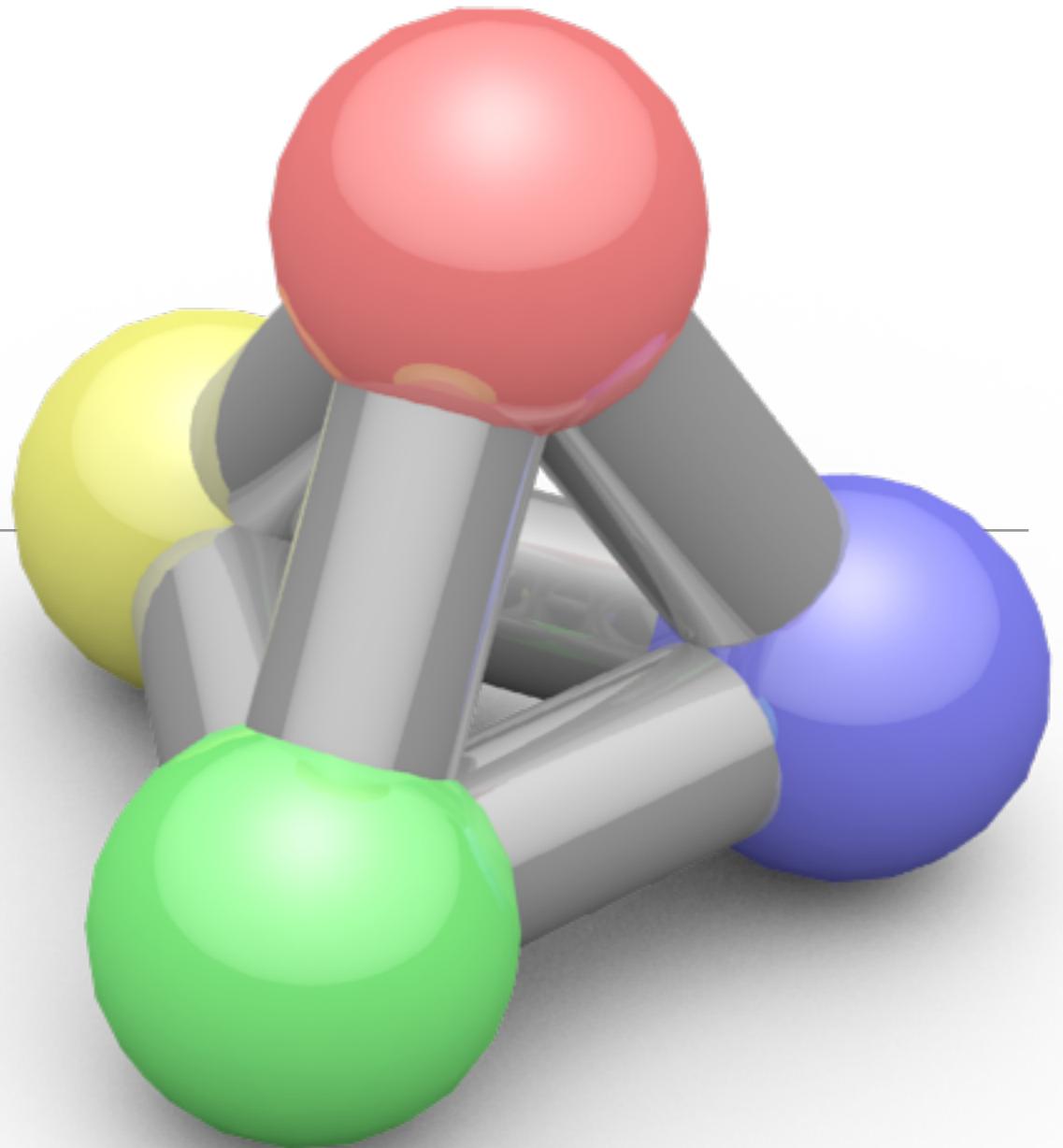


# Global Illumination

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CPSC 453 – Fall 2016

Sonny Chan



# Outline for Today

---

- Motivation
- Radiometry: foundations of physically-based rendering
- Surface reflectance
- The rendering equation
- Solutions to the rendering equation

What is the primary  
goal of rendering?



(photo-realistic)

The goal of photo-realistic rendering is to  
synthesize an image that is  
**indistinguishable from reality.**



Interaction of Light and Matter

Photo by Tobias Ritschel, UCL



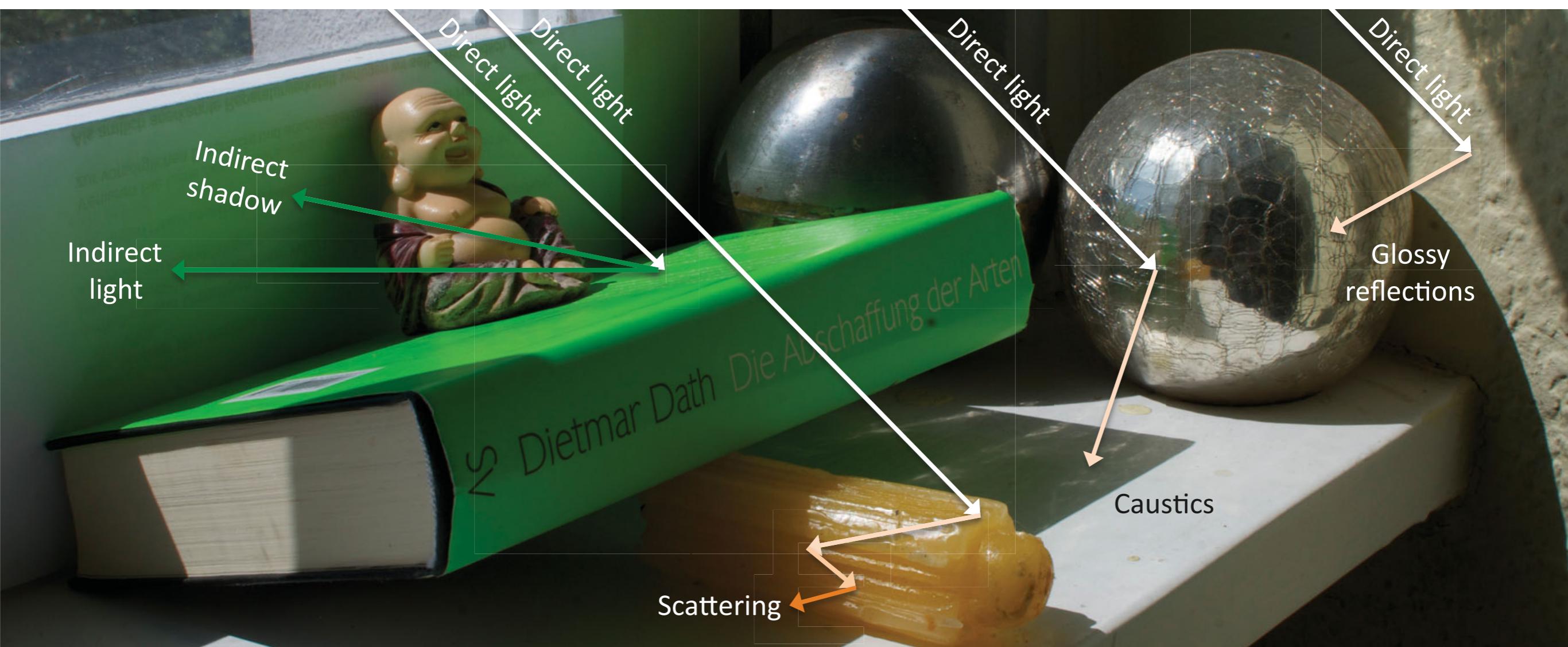
Interaction of Light and Matter

Photo by CPSC 453 student



Interaction of Light and Matter

Photo by Tobias Ritschel, UCL

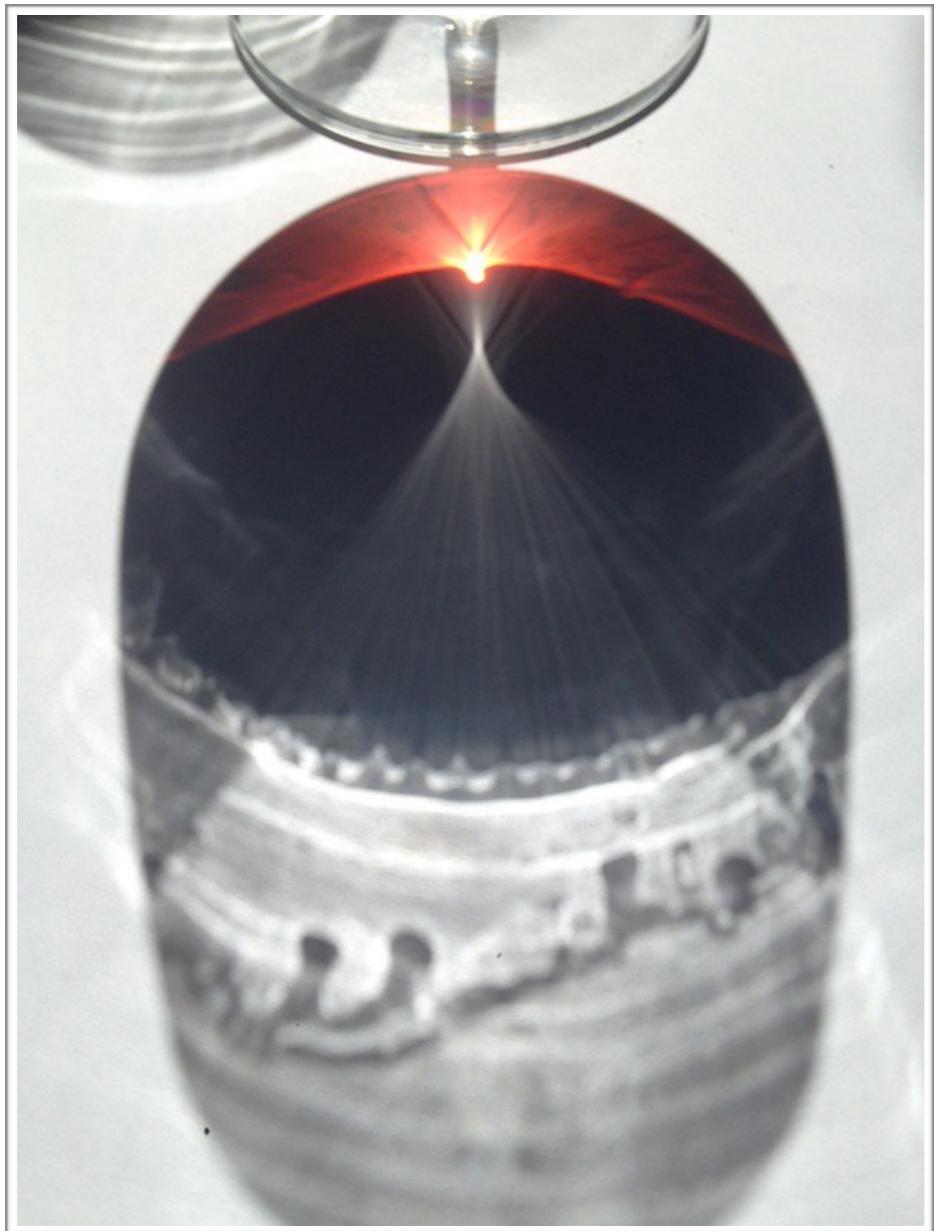


# Interaction of Light and Matter

Photo by Tobias Ritschel, UCL

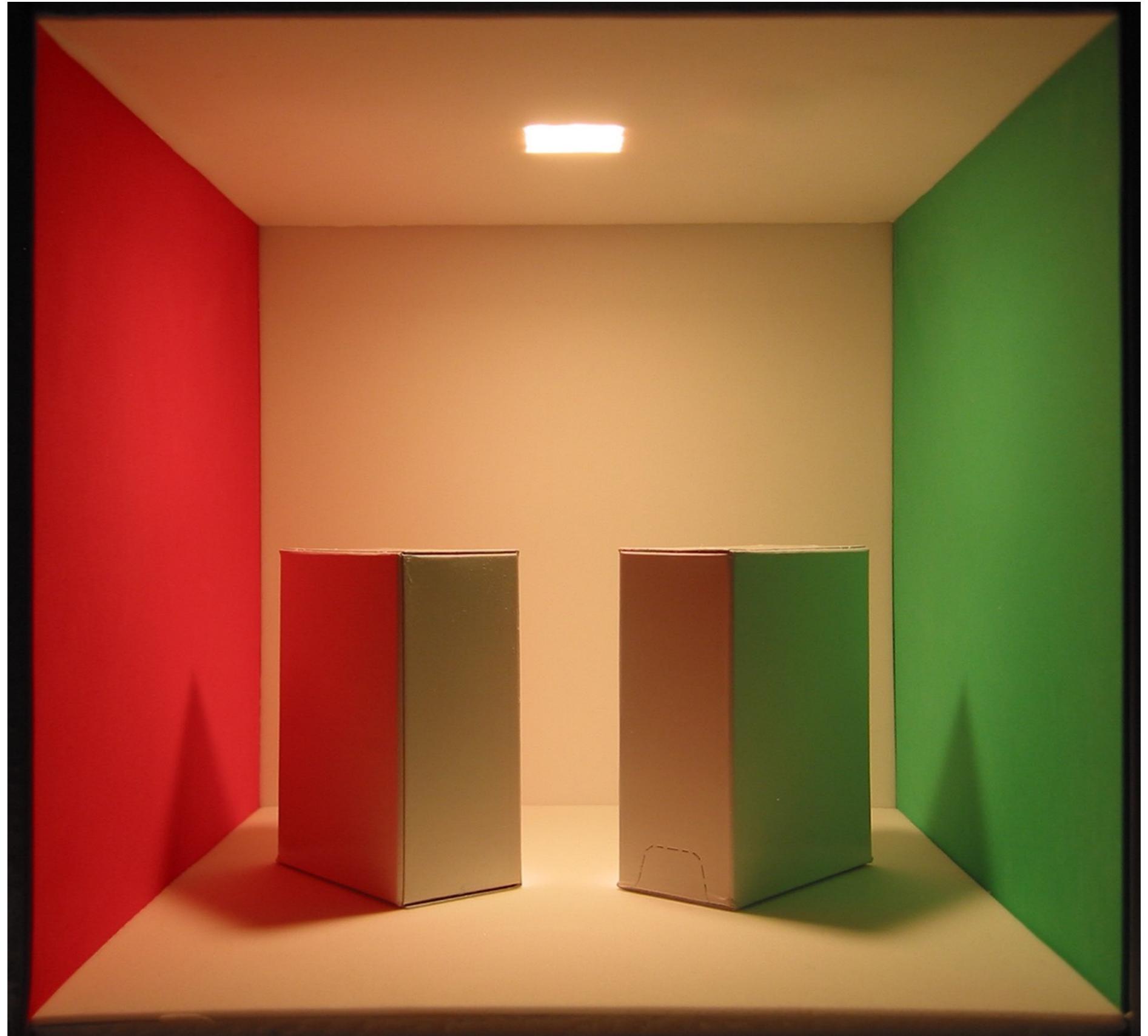
# Caustics

---



9 [from K. Breeden, Stanford University]

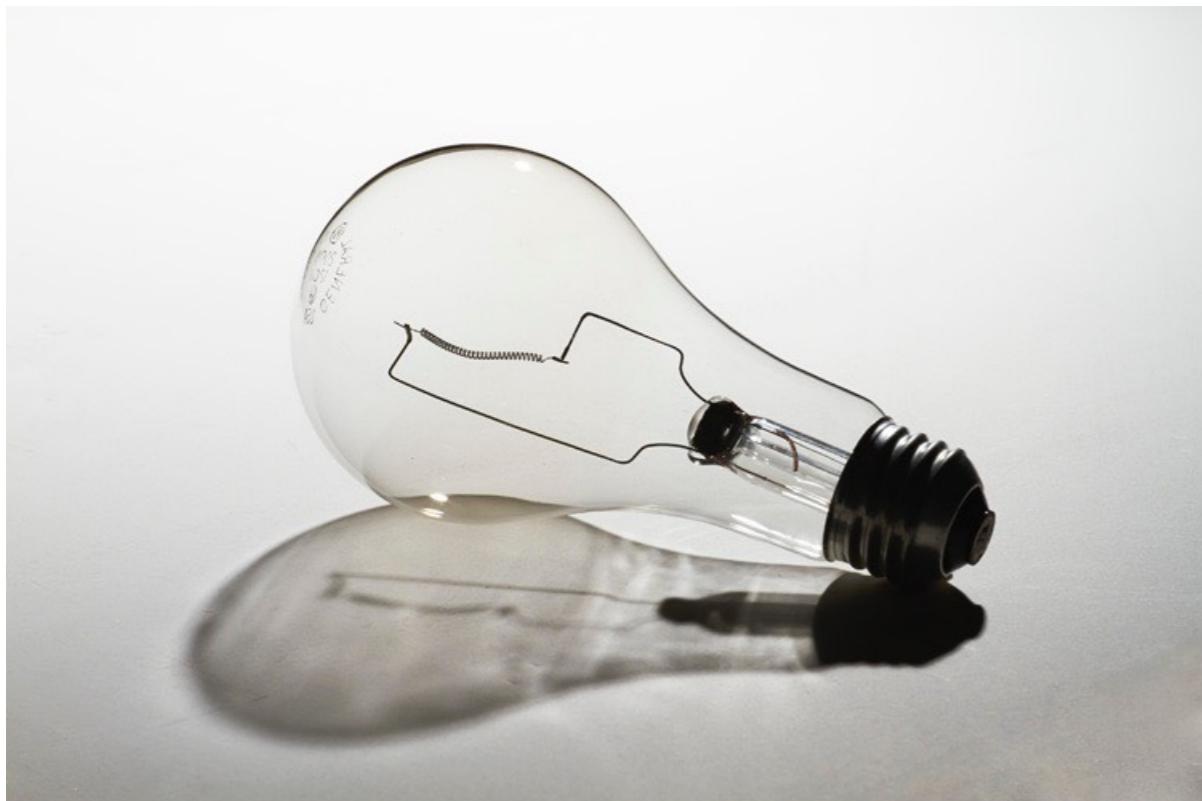
# Radiosity



[construction and photograph by Richard Rosenman] 10

# Shadows

---



[from [learnmyshot.com](http://learnmyshot.com)] 11

**How can we synthesize these  
illumination effects?**

# Radiometry

---

The foundations for physically-based image synthesis



How bright is  
**the sun?**



**What is a  
lumen?**



# Radiometry and Photometry

---

- Measurement of spatial properties of light:
  - radiant power
  - radiant intensity
  - irradiance
  - radiance
  - radiant exitance (radiosity)
- Physically-based rendering performs lighting calculations in a physically correct way

# Radiant Energy and Power

---

- **Power** is energy flux:
  - measured in **watts** (radiometry)
  - or **lumens** (photometry)
- **Energy** is a fundamental physical quantity
  - measured in **joules** (radiometry)
  - or **talbots** (photometry)

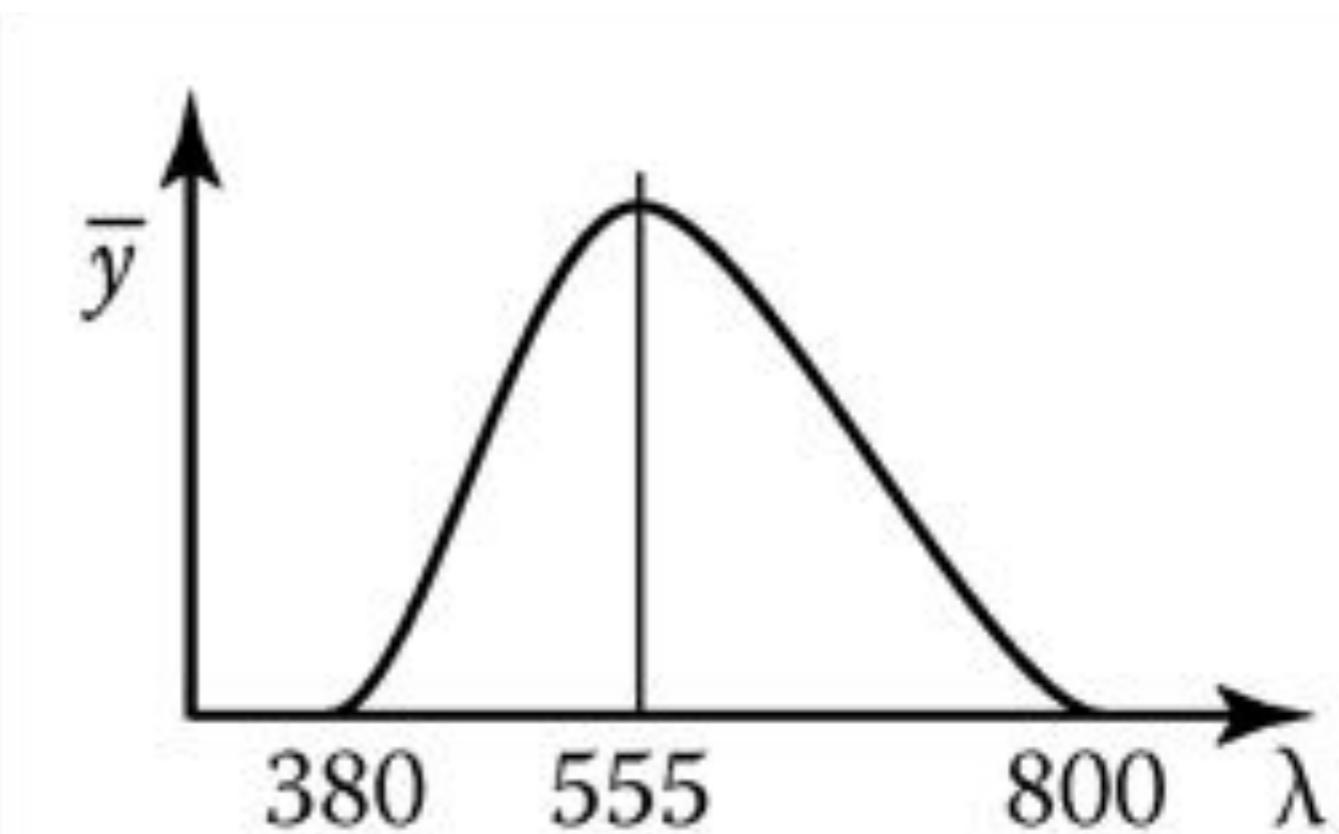
$$\Phi = \frac{dQ}{dt}$$

**What is the difference between  
radiometry and photometry?**

## Luminous Efficiency

---

Photometry is concerned only with measurements in the human-visible light spectrum.



# Radiant Intensity

---

- The radiant (or luminous) intensity is the power per unit solid angle emanating from a light source
  - measured in **watts / steradian** (radiometry)
  - or lumens / steradian = **candelas** (photometry)
- What the heck is a steradian?
- What does this quantity allow us to describe?

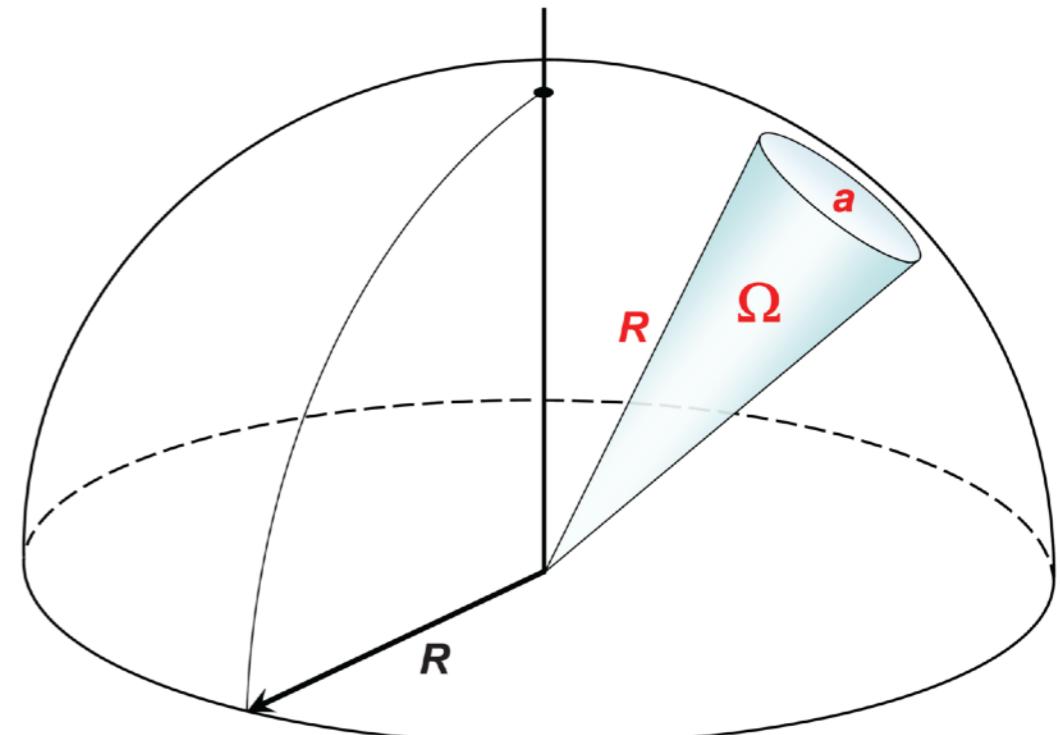
$$I(\omega) = \frac{d\Phi}{d\omega}$$

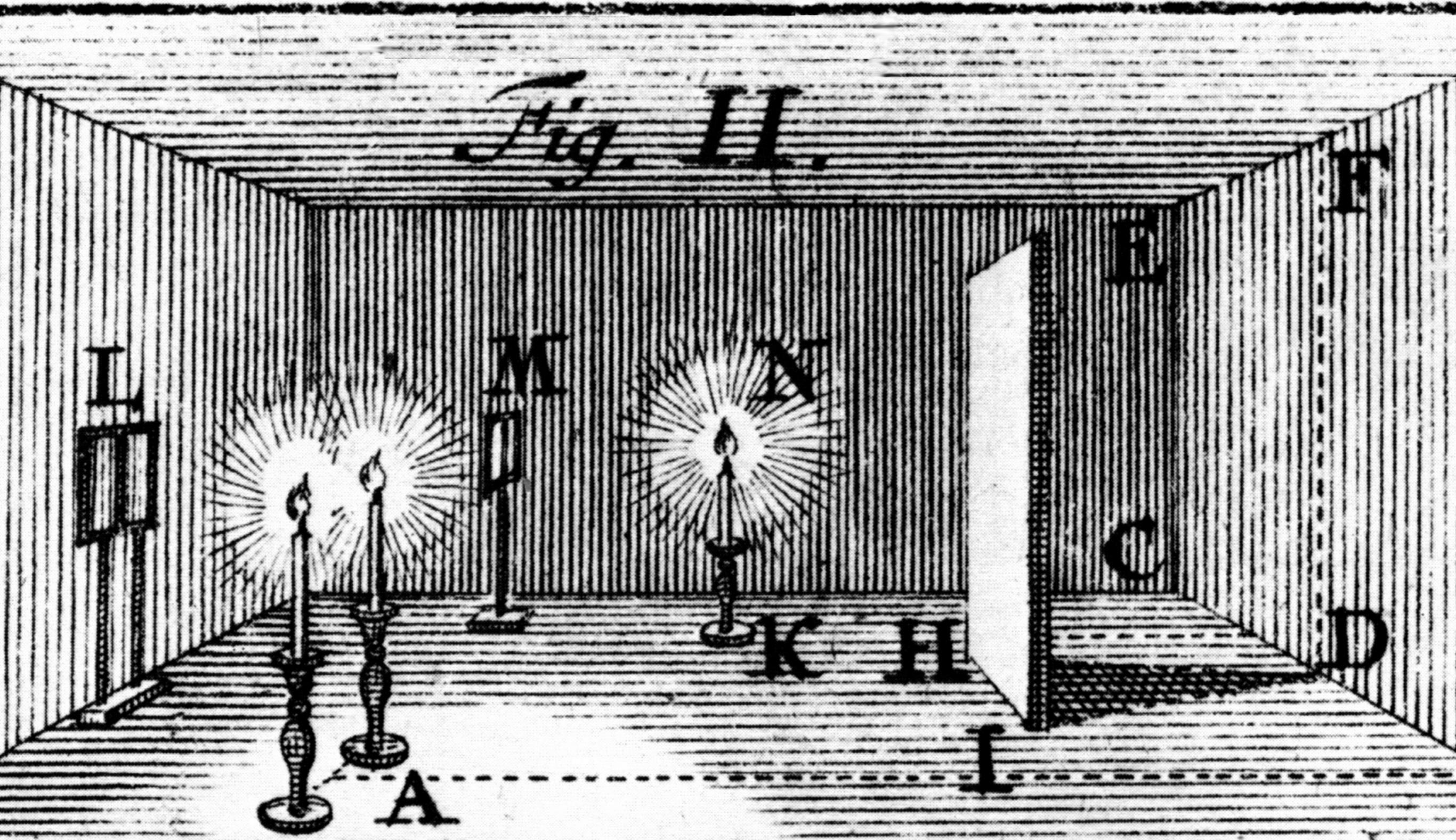
# Solid Angles

---

- Angle is ratio of arc length to radius:  $\theta = \frac{l}{r}$ 
  - a circle has  $2\pi$  radians
- Solid angle is ratio of area to squared radius:  $\Omega = \frac{A}{r^2}$ 
  - measured in steradians (sr)
- How many steradians does a sphere have?

**4π**





What is a candela?

Pierre Bouguer, ca. 1725

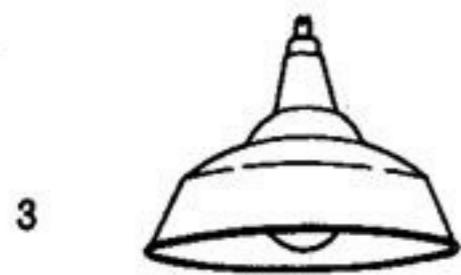
# Luminous Intensity

---

- The candela is one of seven SI base units!
- Originally defined as the amount of light from one standard candle
- Now a monochromatic light source of 555 nm with intensity  $1/683 \text{ W/sr}$

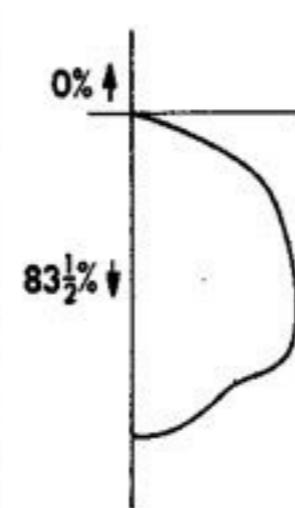


# Light Source Goniometric Diagrams

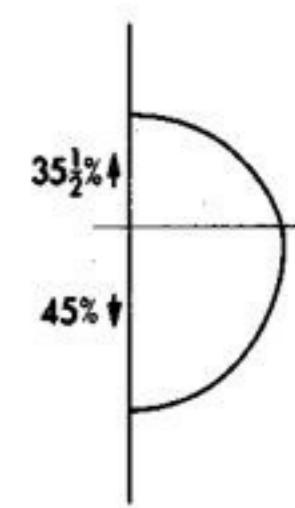


3

Porcelain-enamedel ventilated standard dome with incandescent lamp

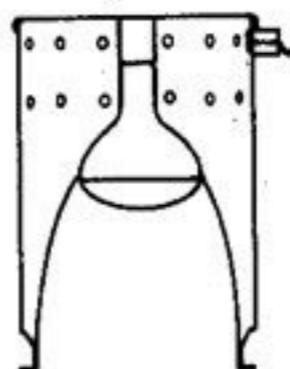
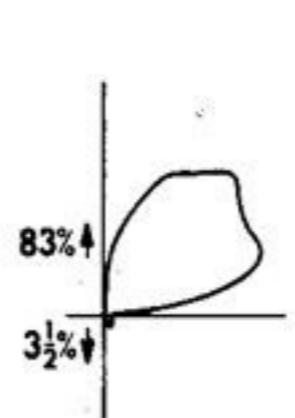


Pendant diffusing sphere with incandescent lamp

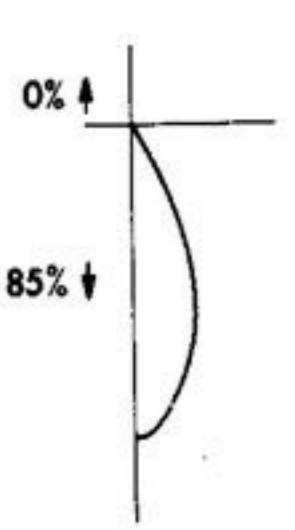


2

Concentric ring unit with incandescent silvered-bowl lamp



R-40 flood with specular anodized reflector skirt; 45° cutoff



# Irradiance

---

- The irradiance (illuminance) is the power for unit area incident on a surface.

$$E(x) = \frac{d\Phi_i}{dA}$$

- measured in **watts / square metre** (radiometry)
- or lumens / square metre = **lux** (photometry)
- What does this quantity allow us to describe?
- Radiant exitance (luminosity) is defined the same way

# Radiance

---

- The surface radiance (luminance) is the intensity per unit area leaving a surface
  - measured in **watts / steradian m<sup>2</sup>** (radiometry)
  - or lumens / steradian m<sup>2</sup> = **nit** (photometry)

$$L(x, \omega) = \frac{d^2\Phi}{d\omega dA}$$

- What can we describe with this quantity?

# Light Beams!

---



Radiance is perhaps the most important measure for physically based rendering.



How bright is  
**the sun?**



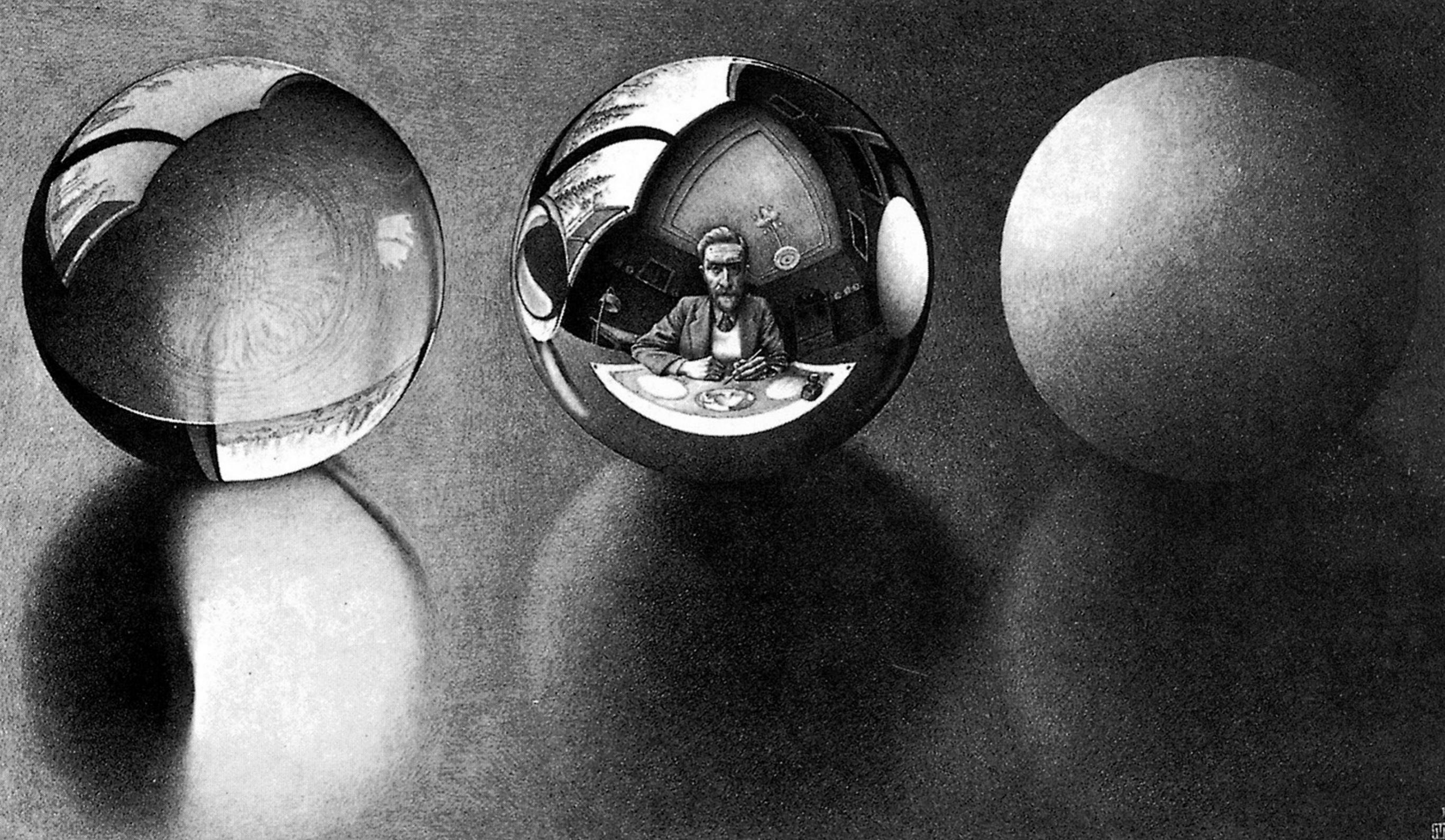
# Typical Values of Luminance

	nit (candela/m <sup>2</sup> )
Surface of the sun	2000000000
Sunlight clouds	30000
Clear sky	3000
Overcast sky	300
Moon	0.03

# Typical Values of Illuminance

	lux (lumens/m <sup>2</sup> )
Direct sunlight plus skylight	100000
Sunlight plus skylight (overcast)	10000
Interior near window (daylight)	1000
Artificial light (minimum)	100
Moonlight (full)	0.01
Starlight	0.0003

[courtesy of P. Hanrahan, Stanford University] 30



Surface Reflectance

M.C. Escher, 1946

# Reflection Models

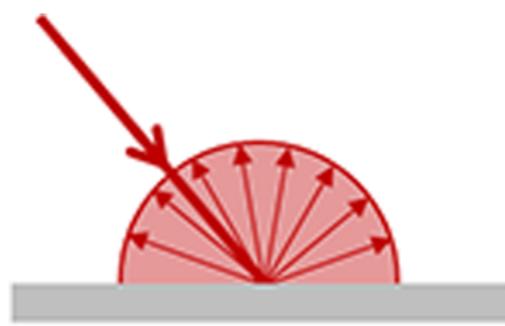
---

- Reflection is the process by which light incident on a surface interacts with the surface such that it leaves on the incident side without change in frequency
- Characterizes many material properties:
  - spectra and colour
  - directional distribution
  - polarization

# Types of Surface Reflectance

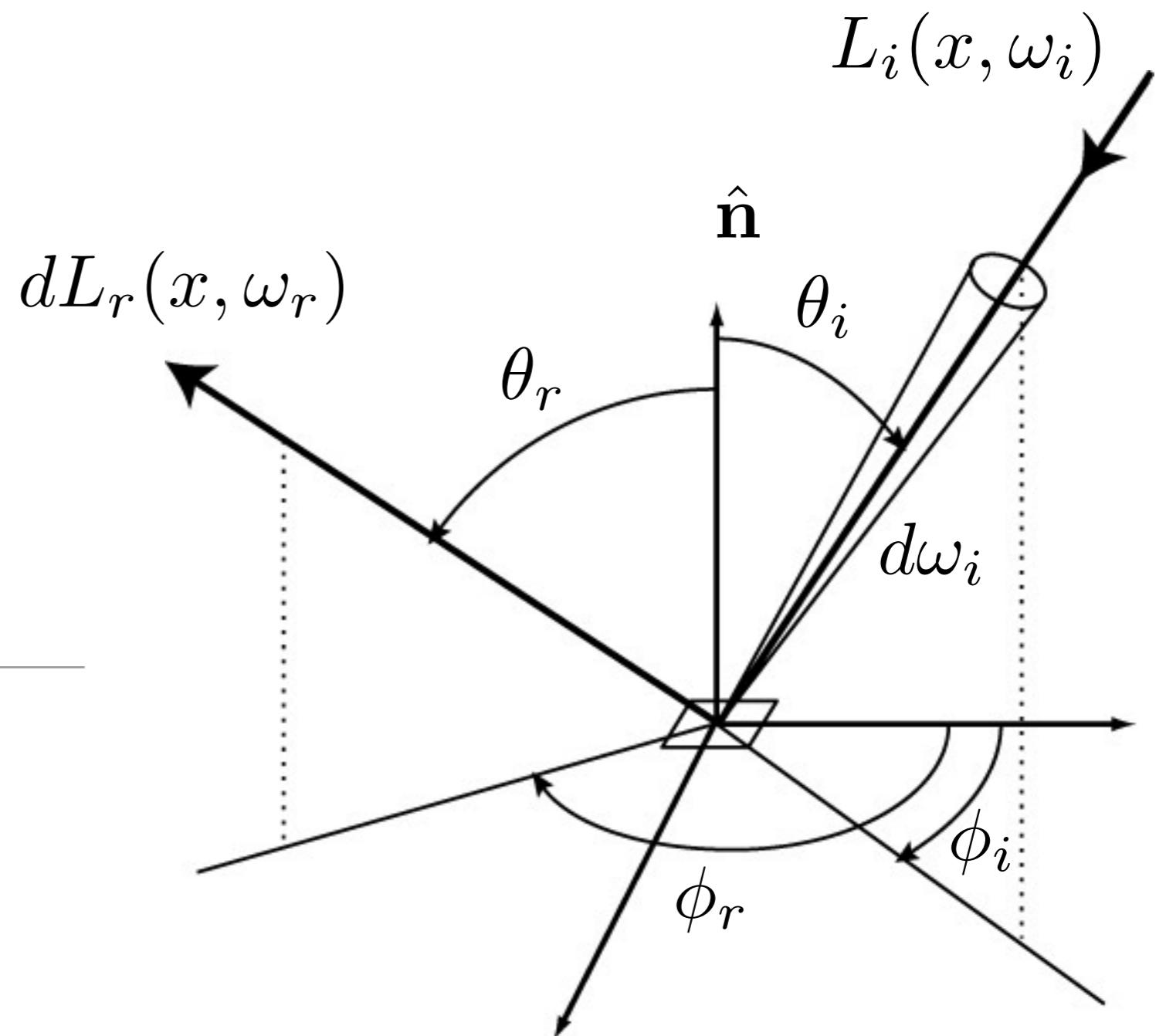
---

- Ideal specular (mirror)
  - reflection law
- Ideal diffuse (matte)
  - Lambert's law
- Specular (glossy)
  - directional diffuse
- Can we make a function to characterize these and more?



## The BRDF

Bidirectional Reflectance  
Distribution Function

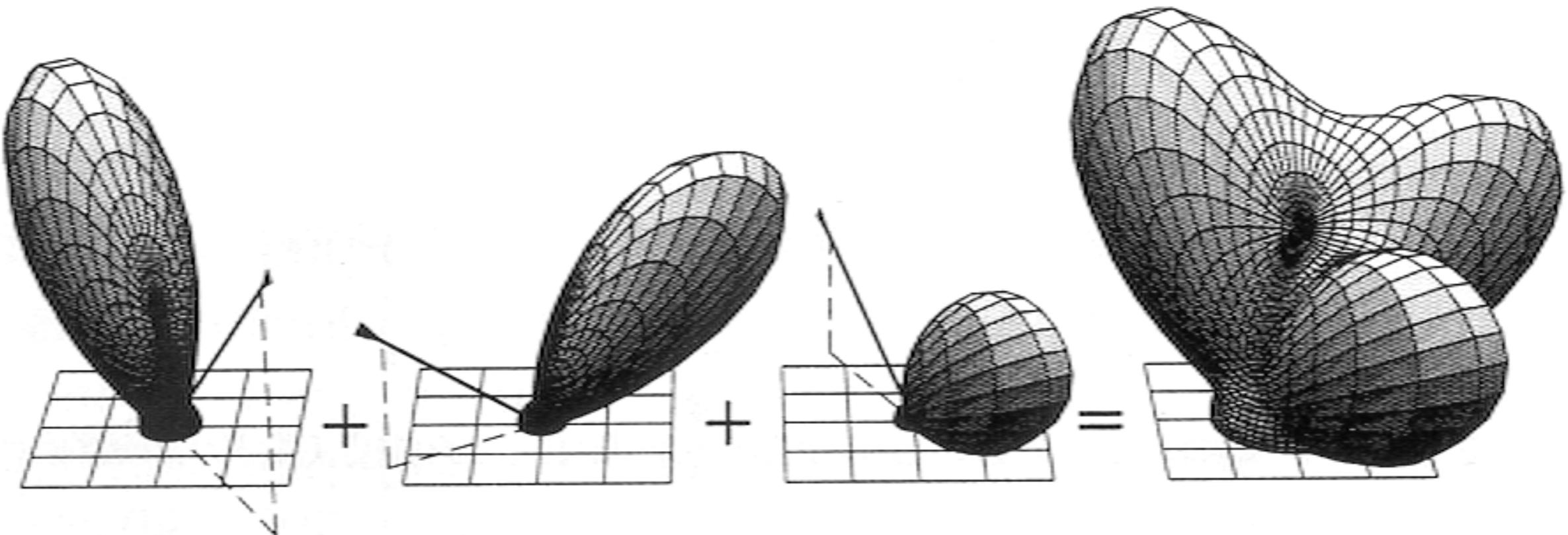


$$f_r(\omega_i \rightarrow \omega_r) = \frac{dL_r(\omega_i \rightarrow \omega_r)}{dE_i}$$

# Properties of the BRDF

---

- **Linearity:** directional distributions can be additively combined

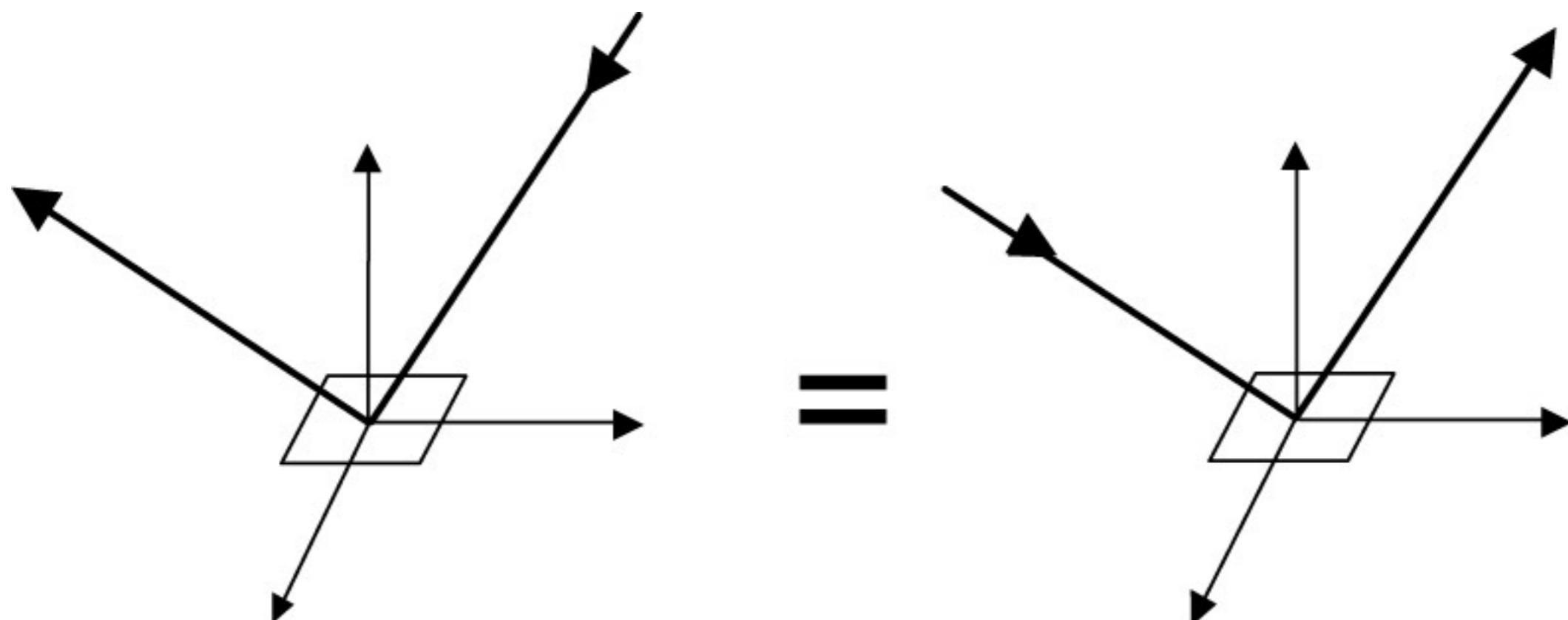


[from F. Sillion *et al.*, Proc. ACM SIGGRAPH, 1991] 35

# Properties of the BRDF

---

- **Reciprocity:** reflectance is unchanged if the incoming and reflected directions are reversed



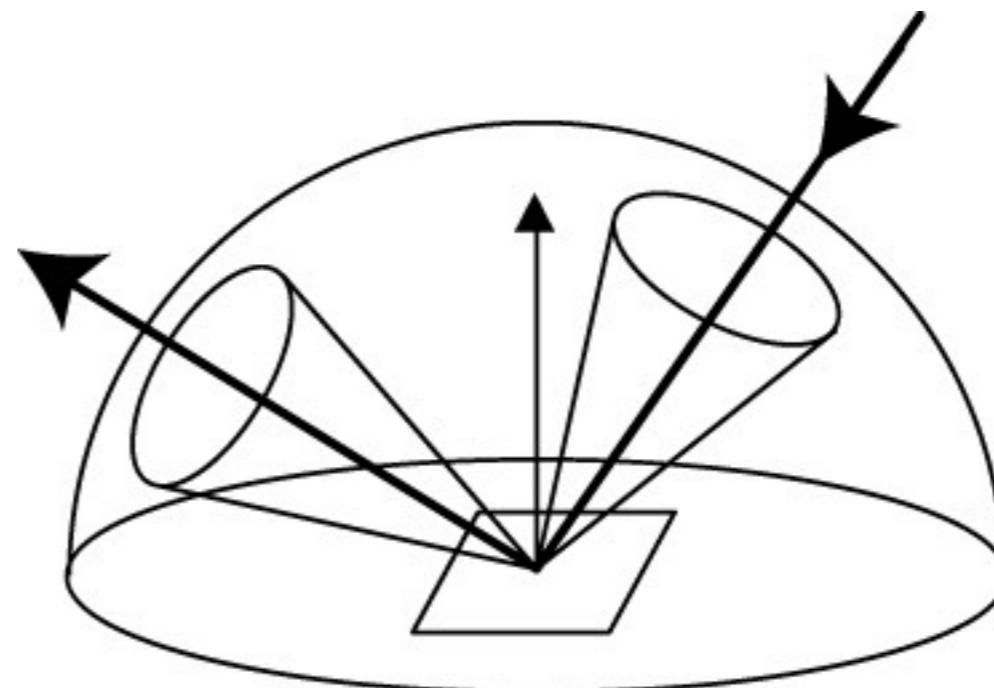
$$f_r(\omega_i \rightarrow \omega_r) = f_r(\omega_r \rightarrow \omega_i)$$

# Properties of the BRDF

---

- **Energy conservation:** total reflected radiant flux must not exceed total incoming radiant flux

$$\frac{d\Phi_r}{d\Phi_i} \leq 1$$



# Recall our heuristic shading equation...

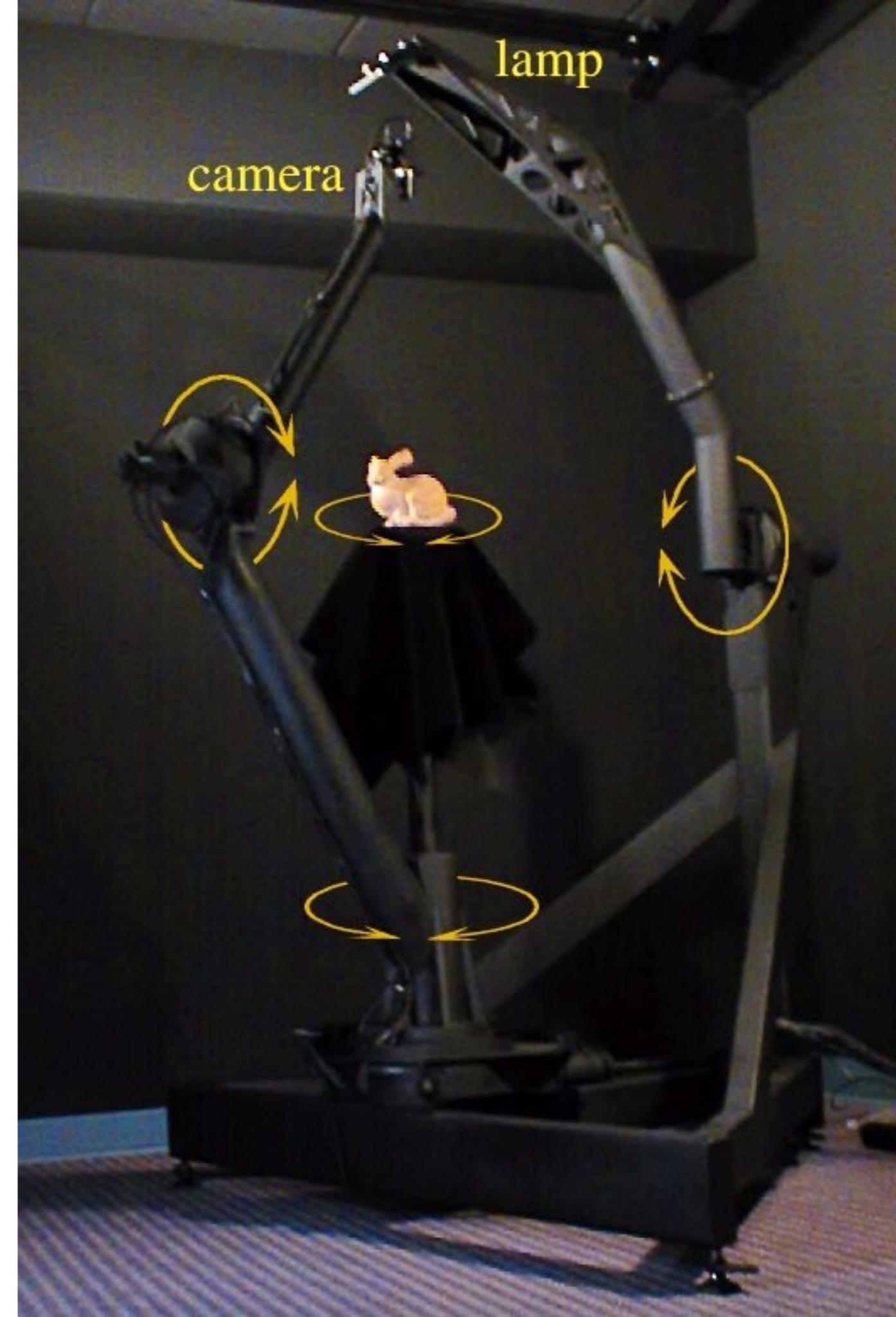
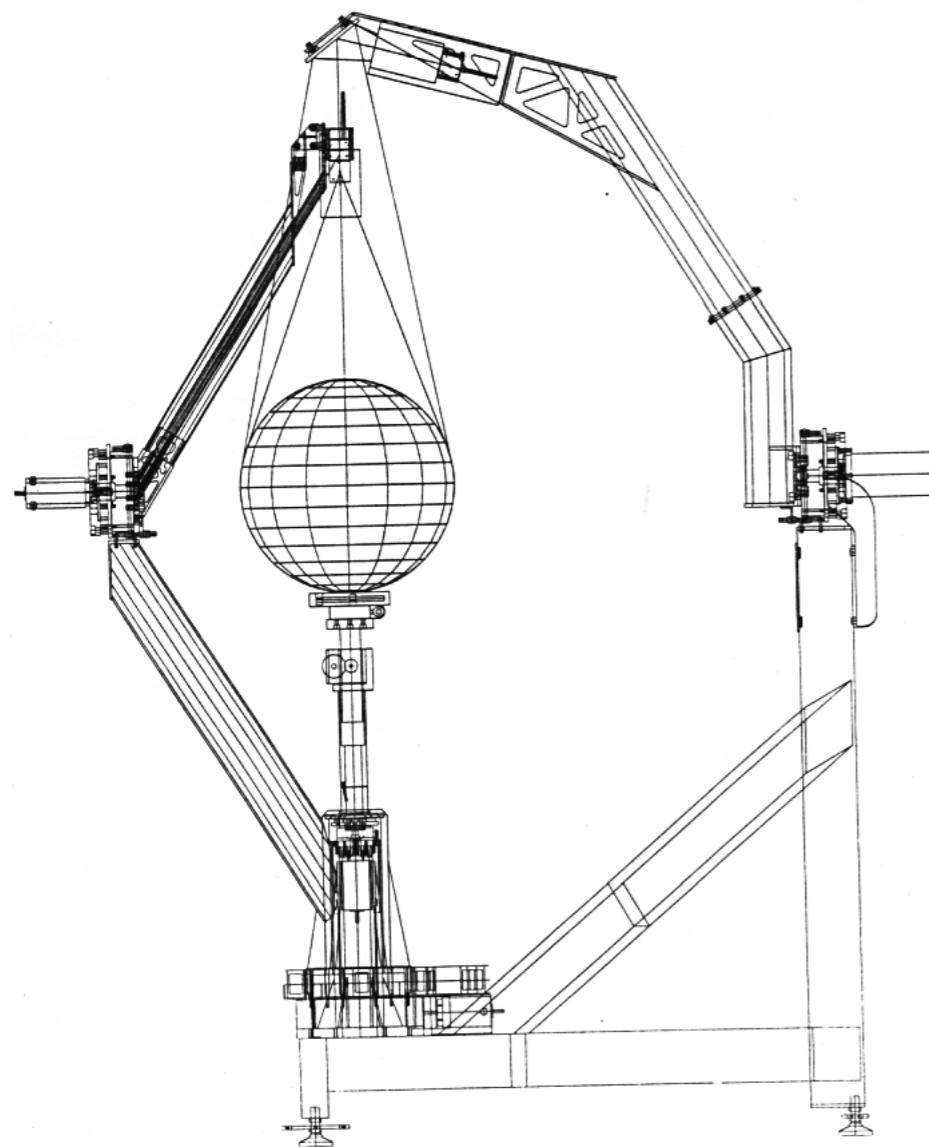
---

- with ambient, diffuse, and specular terms:

$$c = c_r \left( c_a + c_l \max(0, \hat{\mathbf{n}} \cdot \hat{\mathbf{l}}) \right) + c_l c_p \left( \hat{\mathbf{h}} \cdot \hat{\mathbf{n}} \right)^p$$

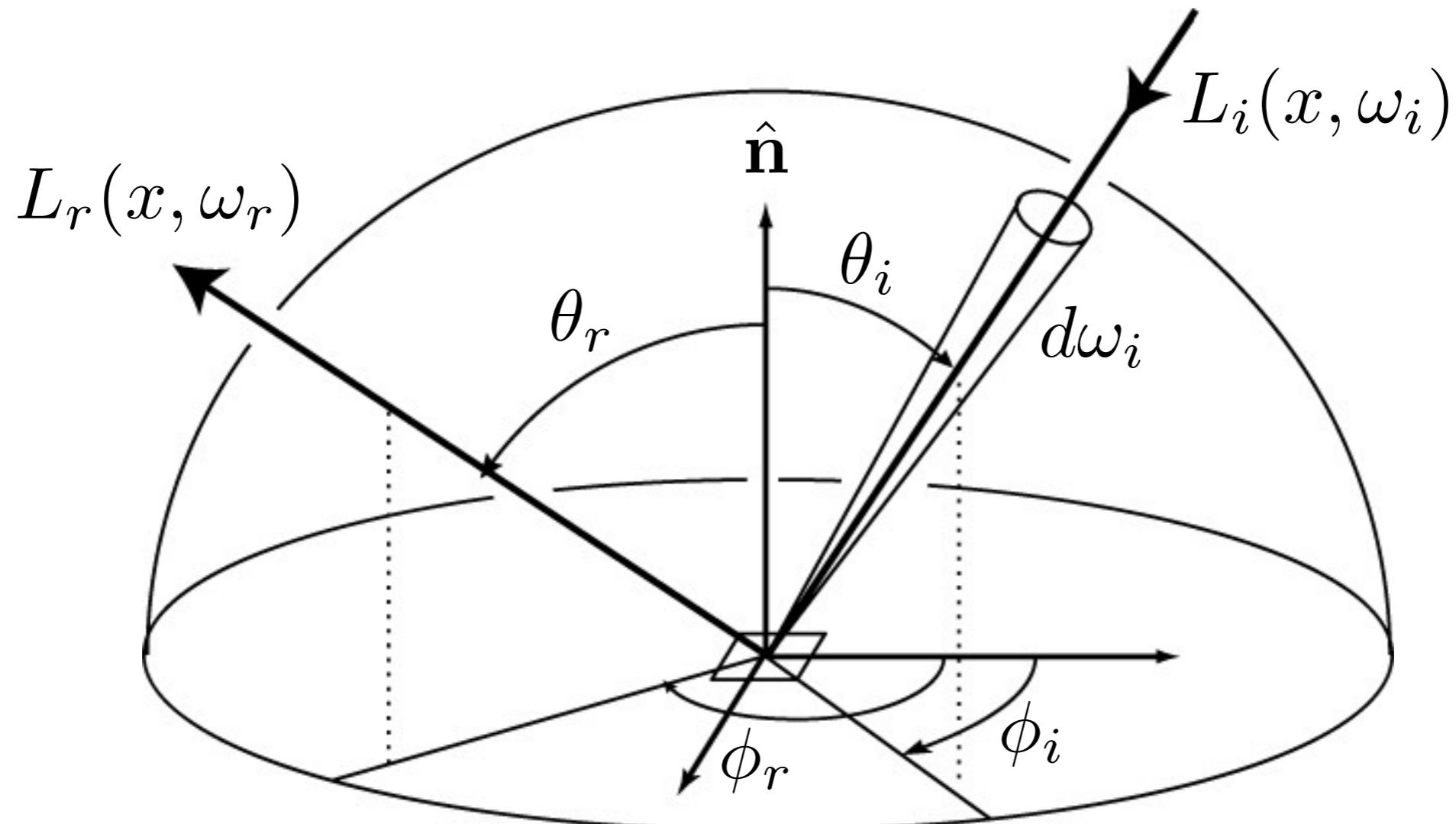
- Is this a valid BRDF?
- (not quite, but it's possible to turn it into one)
- Where else might we be able to obtain BRDFs?

# Gonioreflectometer



# The Reflection Equation

---



$$L_r(x, \omega_r) = \int_{\mathcal{H}^2} f_r(x, \omega_i \rightarrow \omega_r) L_i(x, \omega_i) \cos \theta_i \, d\omega_i$$

[courtesy of P. Hanrahan, Stanford University] 40

# The Rendering Equation

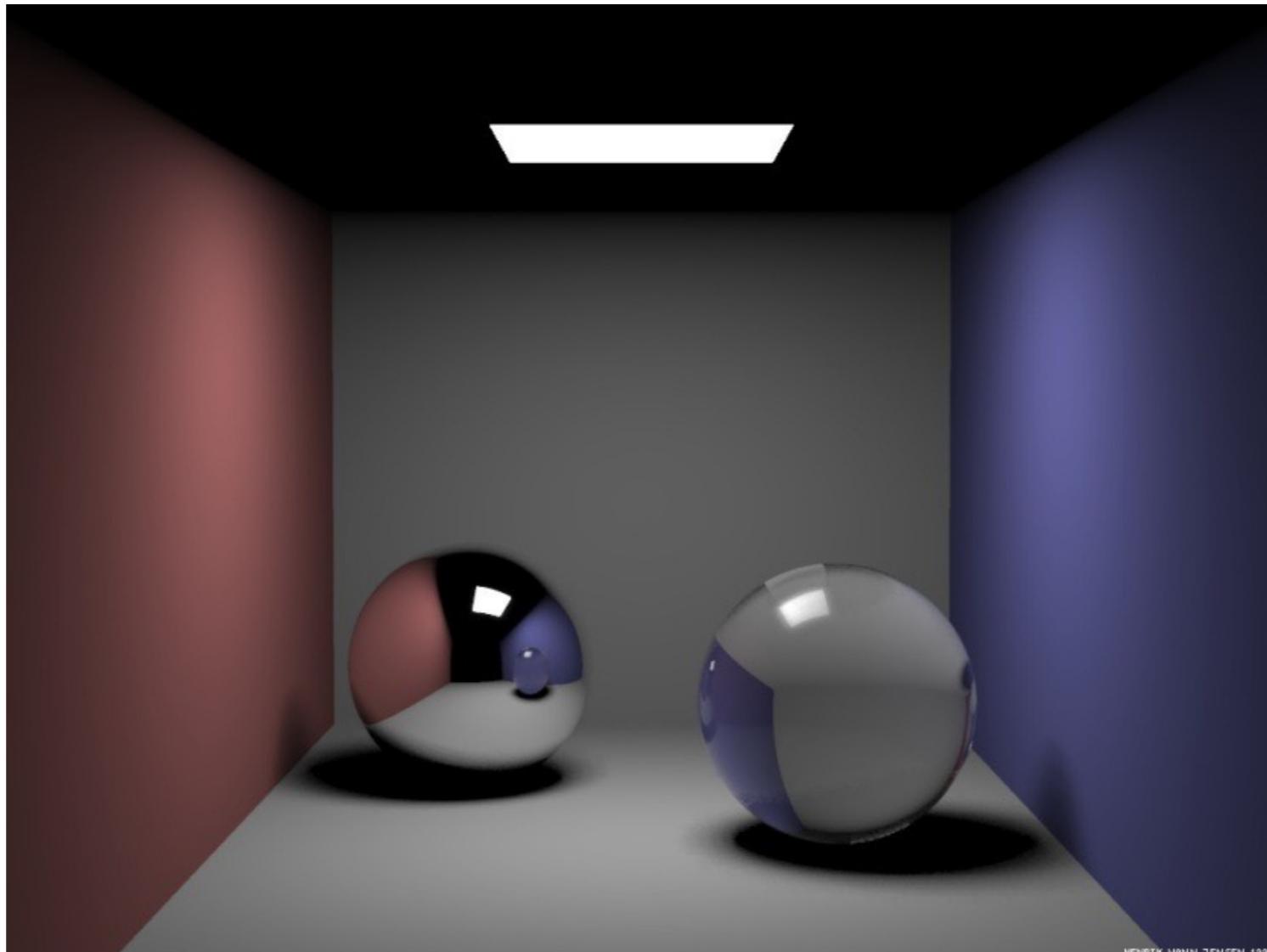
# The Rendering Equation

---

- Goal is to compute direct and indirect illumination
- **Direct (local)** illumination:
  - incoming radiance from light sources only; no shadows
- **Indirect (global)** illumination:
  - hard and soft shadows
  - diffuse inter-reflections (radiosity)
  - glossy inter-reflections (caustics)

# Global Illumination Effects

---

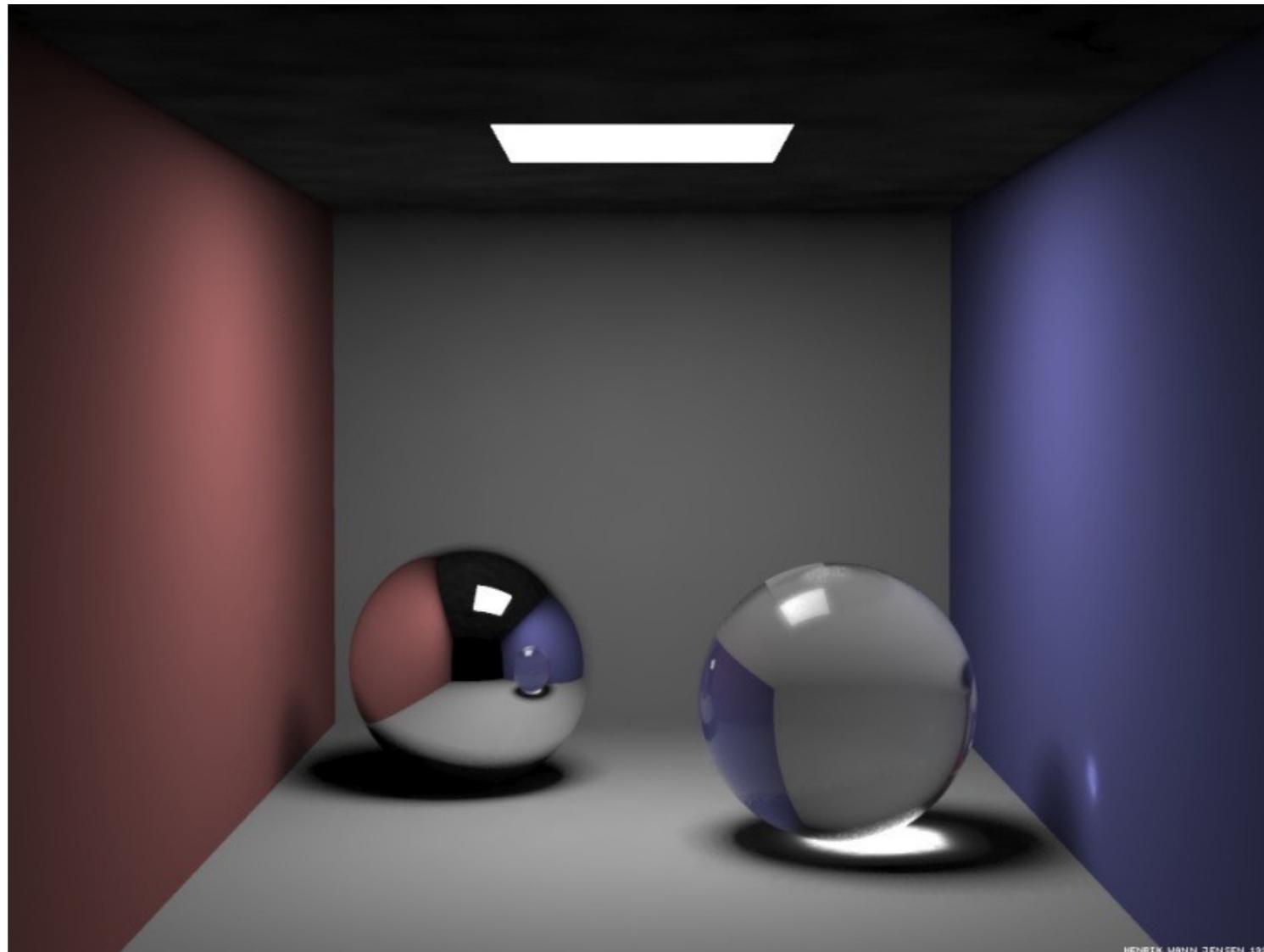


hard and soft shadows

[image by Henrik Wann Jensen, UCSD] 43

# Global Illumination Effects

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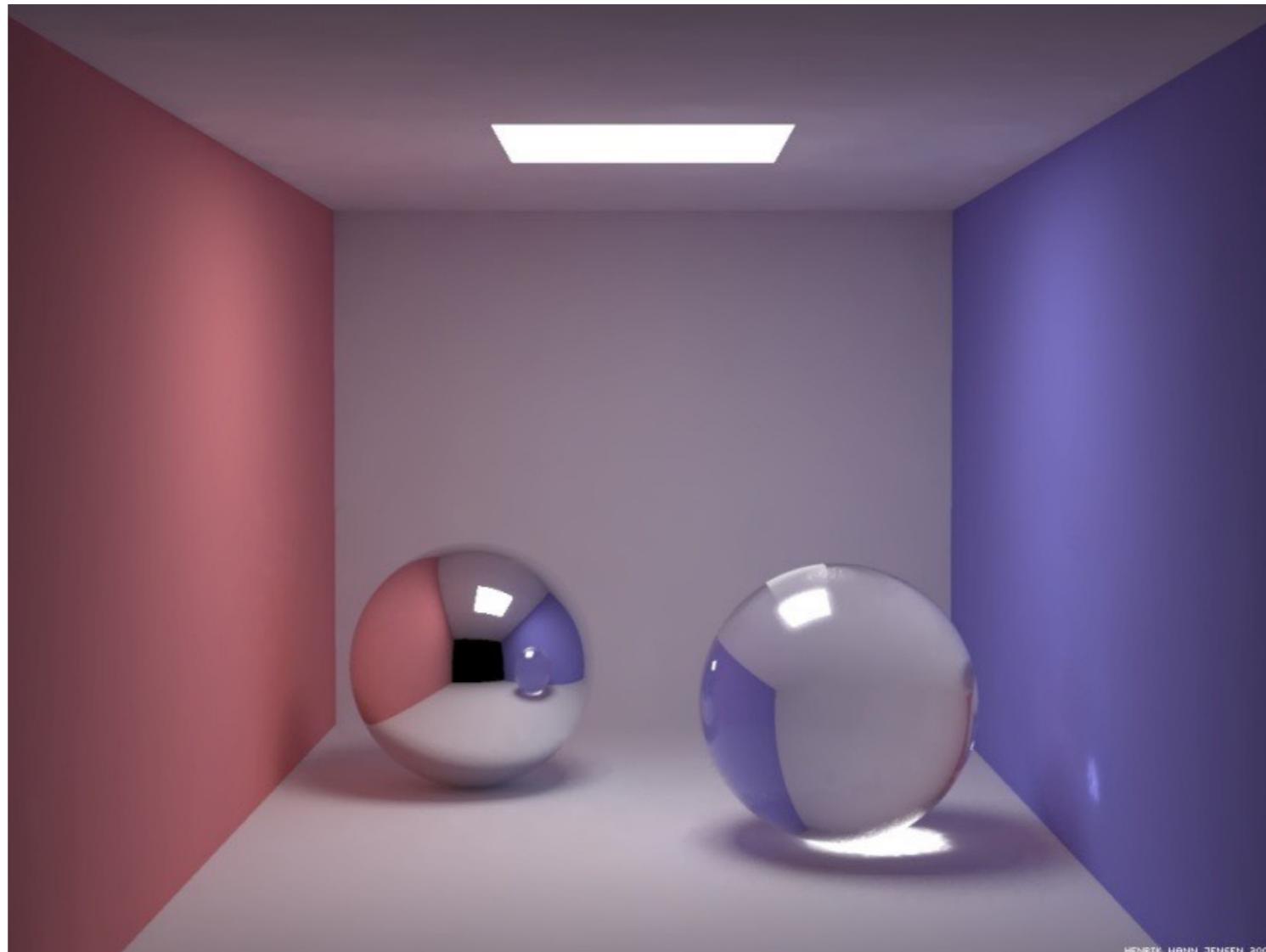


shadows + caustics

[image by Henrik Wann Jensen, UCSD] 44

# Global Illumination Effects

---



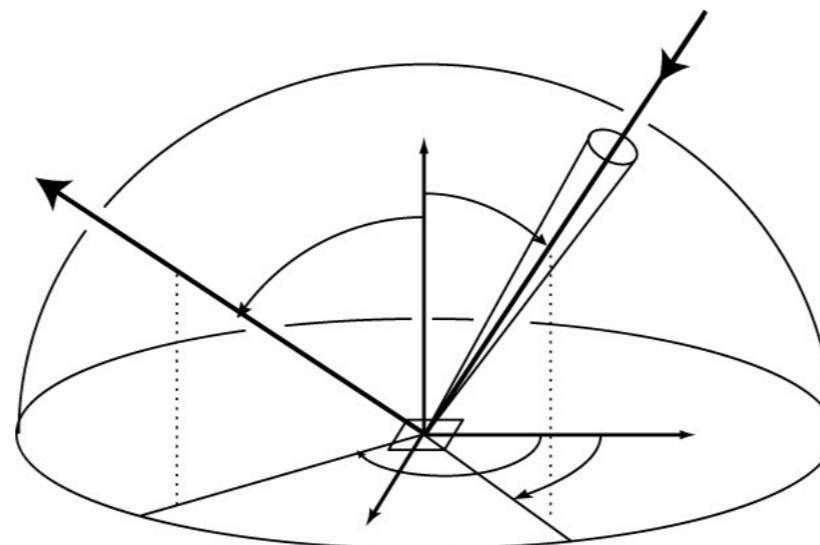
shadows + caustics + radiosity

[image by Henrik Wann Jensen, UCSD] 45

# The Main Challenge

---

- To evaluate the **reflection equation**,
  - the **incoming radiance** must be known



- To evaluate the **incoming radiance**,
  - the **reflected radiance** must be known

# Light Energy Balance

---

- What are the conditions for equilibrium flow of light in an environment?
- **Globally:** The total light energy put into the system must equal the energy leaving the system
  - correct solution must account for all possible light paths!
- **Locally:** The energy flowing into a small region of phase space equal the energy flowing out
  - outgoing – incoming irradiance = emitted – absorbed

# The Surface Rendering Equation

---

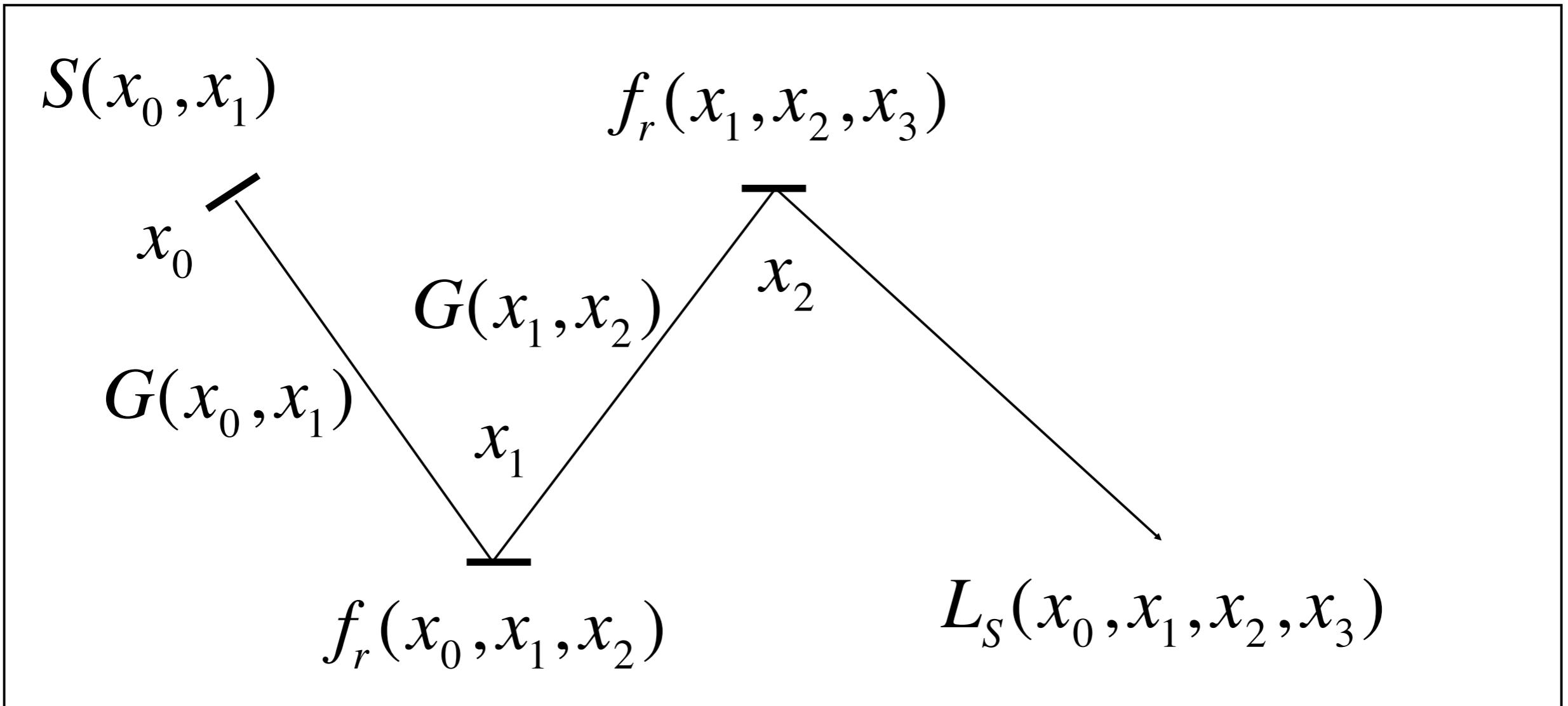
- Outgoing radiance in a given direction is equal to the sum of the emitted and reflected radiance in that direction:

$$\begin{aligned} L_o(x, \omega_o) &= L_e(x, \omega_o) + L_r(x, \omega_o) \\ &= L_e(x, \omega_o) + \int_{\mathcal{H}^2} f(x, \omega_i \rightarrow \omega_o) L_i(x, \omega_i) \cos \theta_i \, d\omega_i \end{aligned}$$

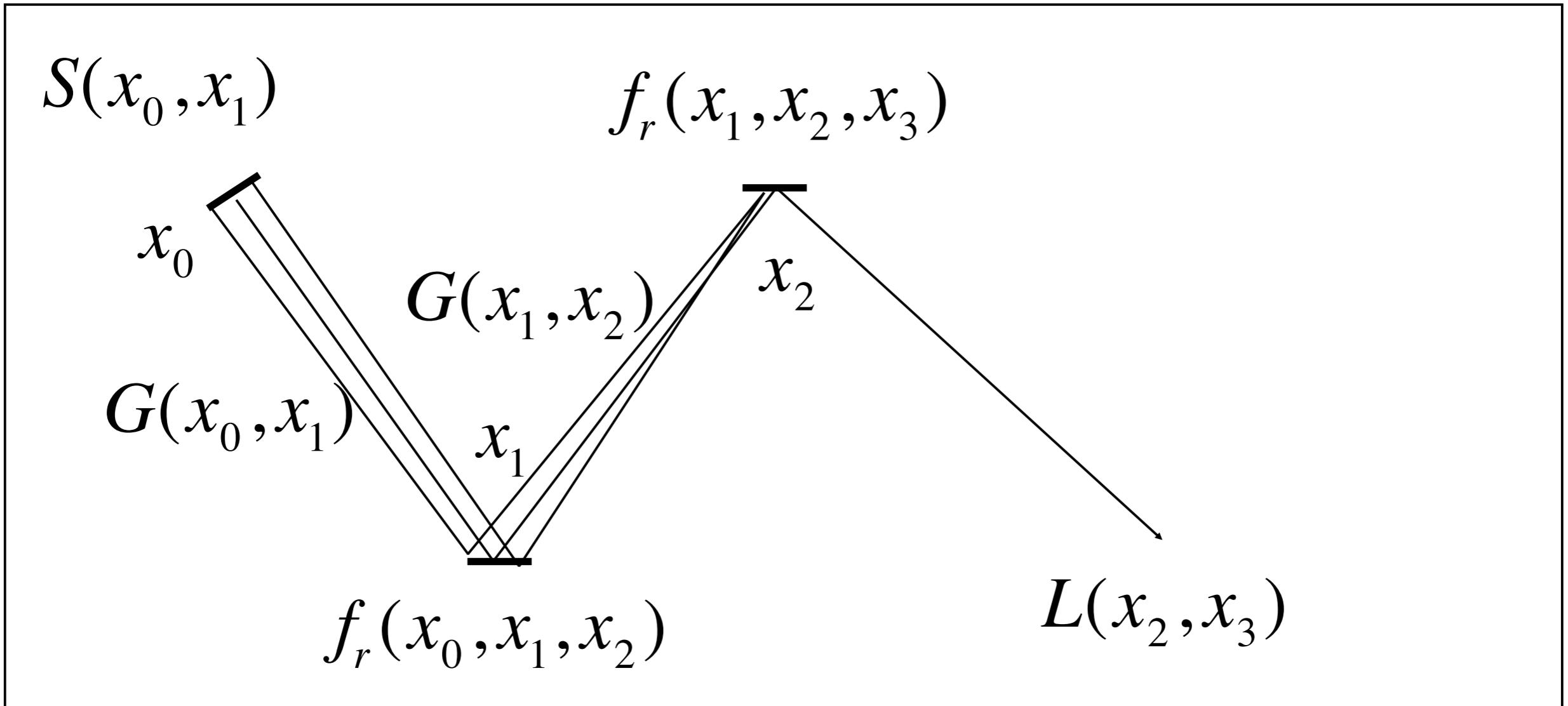
- How the heck do we solve this thing???

# A Light Path

---

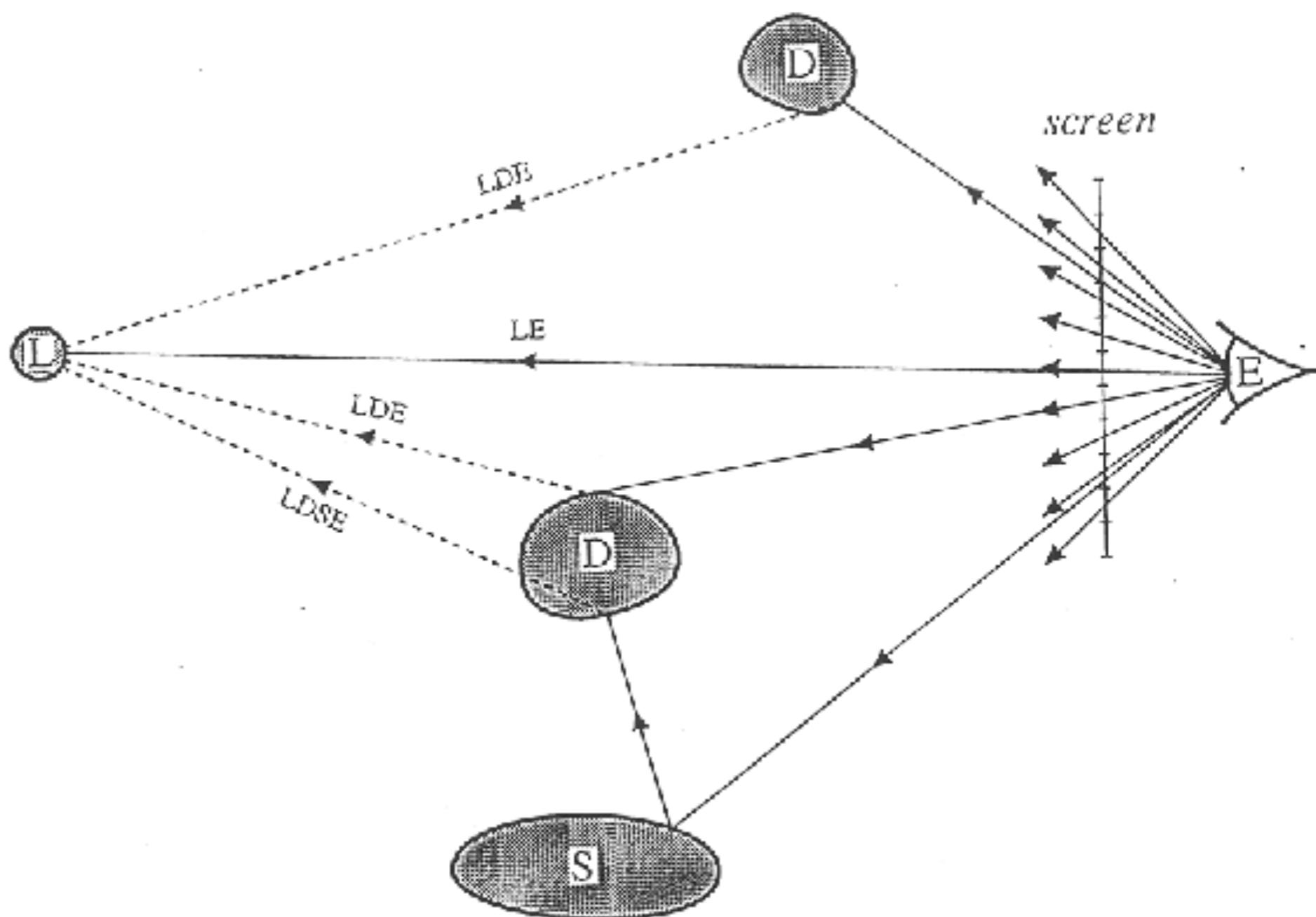


# Light Paths



How many light paths contribute to the ray  $L$ ?

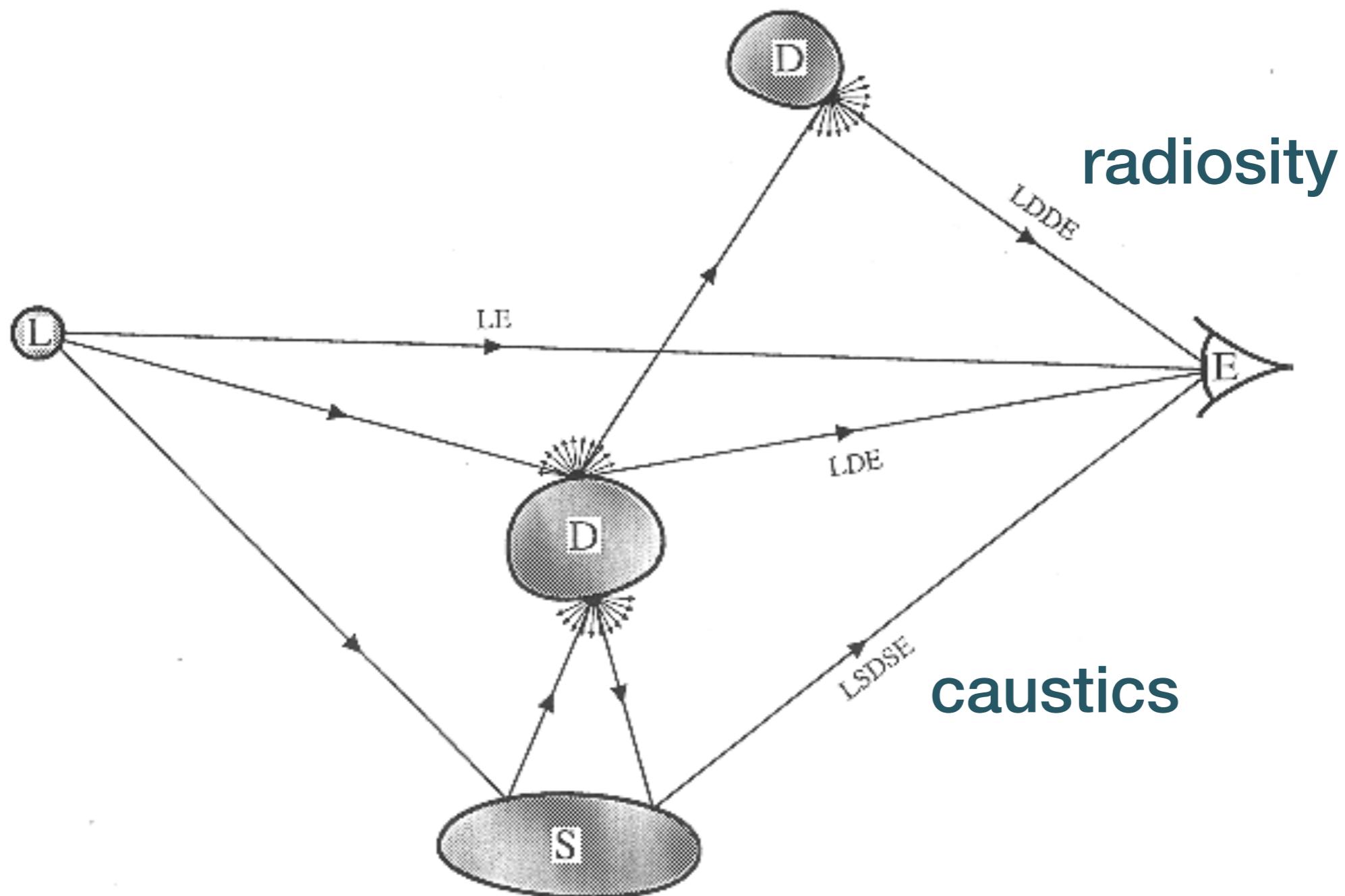
# Light paths you traced in Assignment #4...



[diagram by Paul Heckbert]

# Photon Paths

---



[diagram by Paul Heckbert] 52

# Simulation of Light Transport

---

- Integrate over **all paths of all lengths**

$$\begin{aligned} L(x_{k-1}, x_k) \\ = \sum_{k=1}^{\infty} \int_{M^2} \cdots \int_{M^2} L_s(x_0, \dots, x_{k-2}, x_{k-1}, x_k) dA(x_0) \cdots dA(x_{k-2}) \end{aligned}$$

- Key challenges of physically-based rendering:
  - How do we generate all the possible light paths?
  - How do we sample the space of paths efficiently?

# Monte Carlo Integration

# Monte Carlo Integration

---

- Define a random variable on the integration domain
- Sample the variable and evaluate the integrand
- Integral estimate is the average of samples:

$$\int f(x)dx \quad \Rightarrow \quad F_N = \frac{1}{N} \sum_{i=1}^N f(X_i)$$

# Monte Carlo Integration

---

- **Advantages:**
  - easy to implement
  - robust with complex integrands
  - efficient for high dimensional integrals
- **Disadvantages:**
  - noisy results
  - slow (many samples needed for convergence)

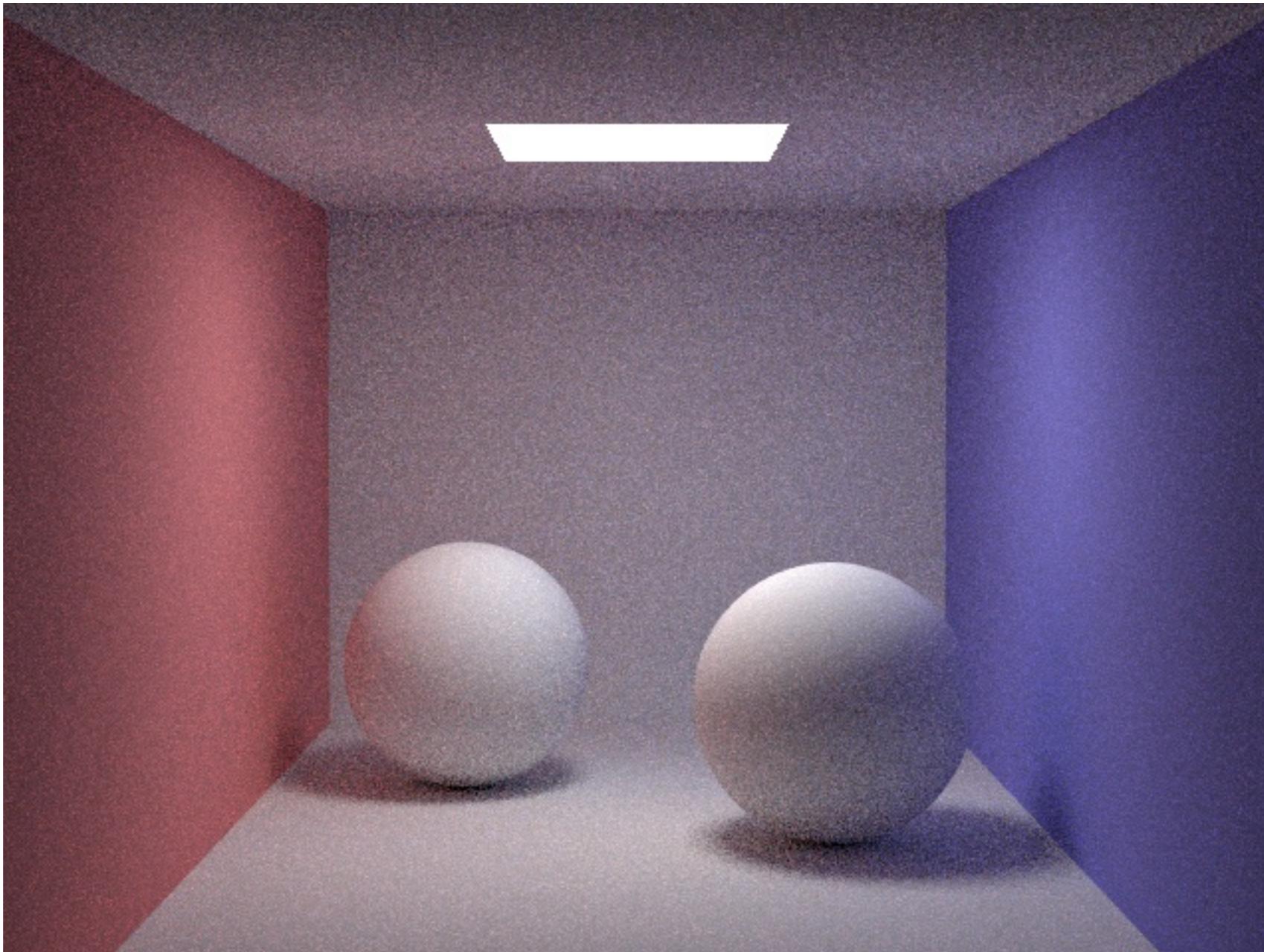
# Monte Carlo Path Tracing

---

- Choose a source ray  $(x, \omega)$
- Find ray-surface intersection  $x = x^*(x, \omega)$ 
  - if light source, return  $L_e(x, \omega)$
  - check ray termination condition
  - choose a new ray direction  $\omega$  drawn from BRDF
  - repeat with new ray  $(x, \omega)$

# Monte Carlo Path Tracing

---

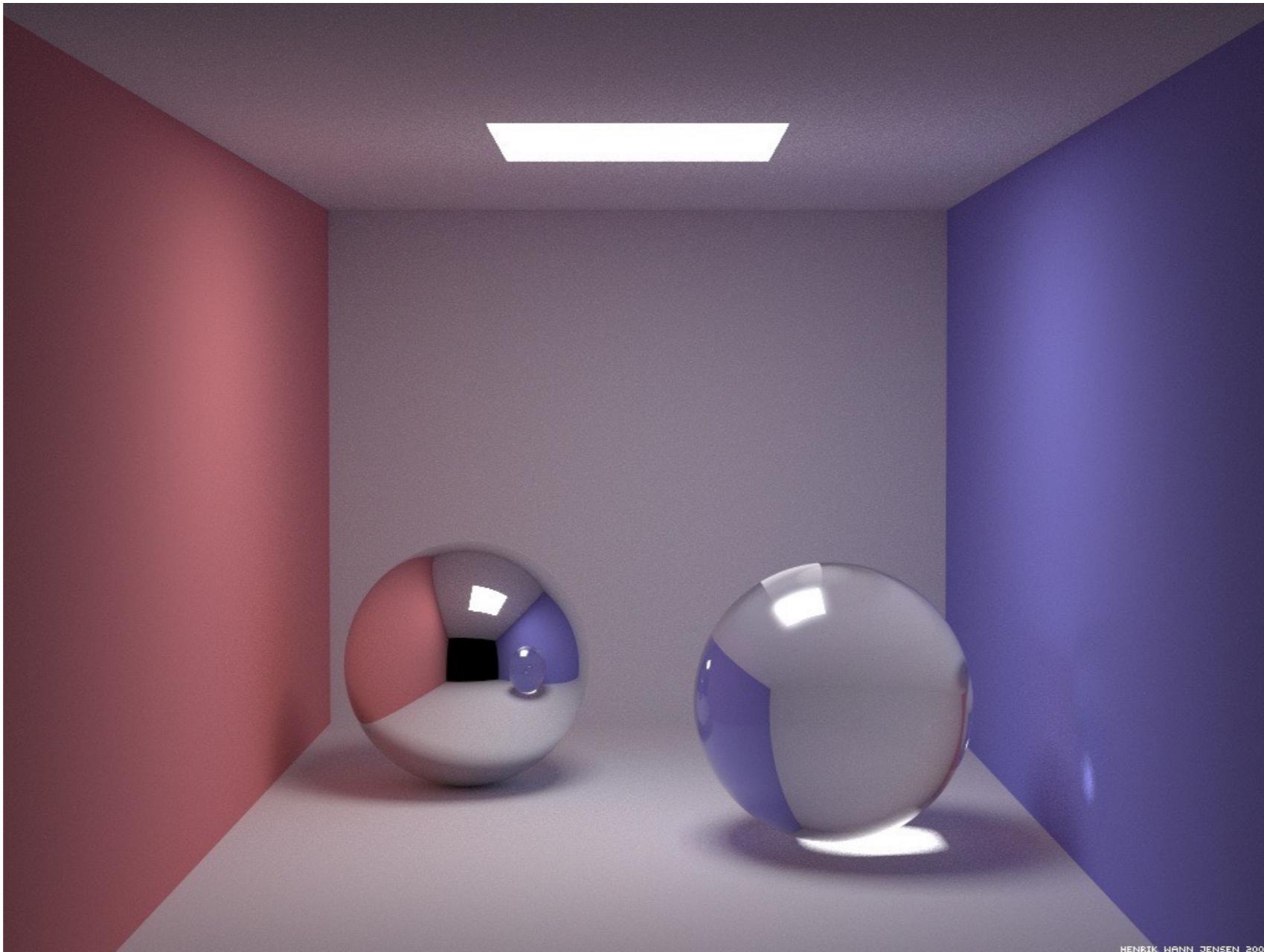


10 paths / pixel

[image by Henrik Wann Jensen, UCSD] 58

# Monte Carlo Path Tracing

---



1000 paths / pixel

[image by Henrik Wann Jensen, UCSD] 59

What scenes can path tracing  
**render well?**

# Large, Hemispherical Light

---



**ARNOLD**

- GLOBAL ILLUMINATION RENDERER -



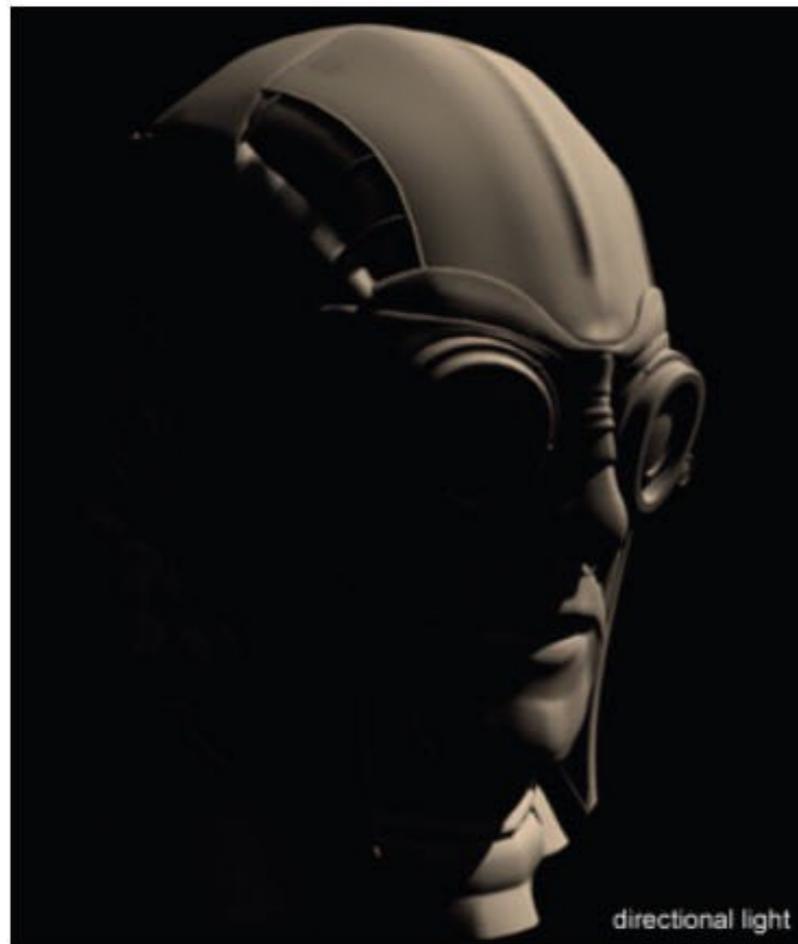
Marcos Fajardo, 1997

Model by *KiKe Oliva*

[KikeOliva@hotmail.com](mailto:KikeOliva@hotmail.com)

# Ambient Occlusion: Pre-Baked Global Illumination

---



Diffuse Only



Ambient Occlusion



Combined

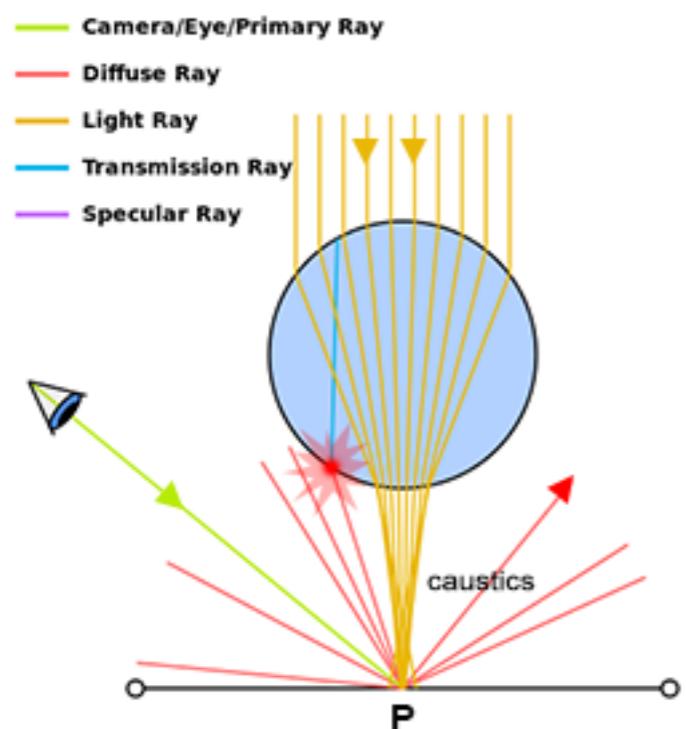


## ARNOLD render:

16 paths/pixel, 2 bounces, 250000 faces, 18 min / dual 800 Mhz

**What scenes does path tracing  
render poorly?**

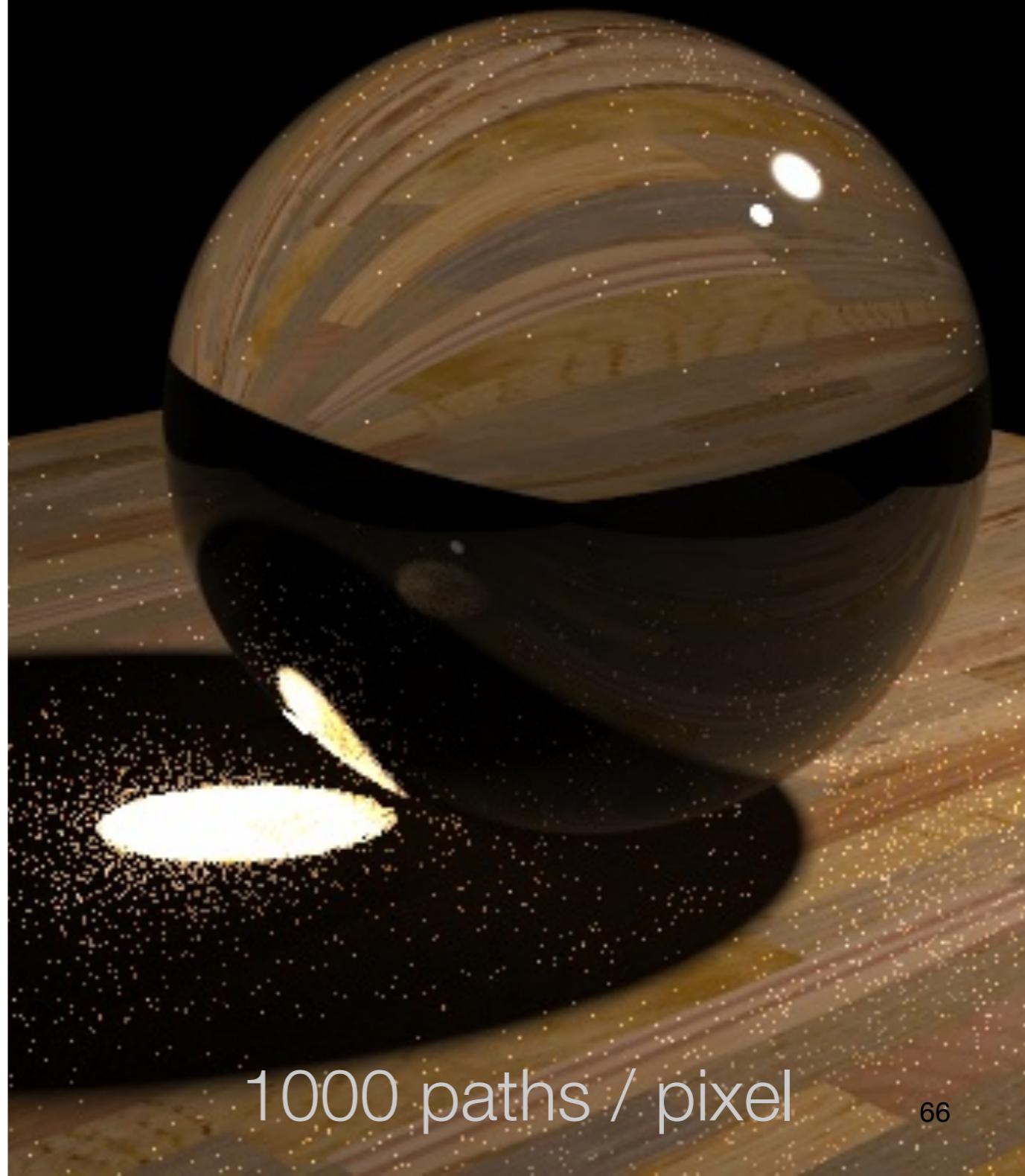
# Caustics!



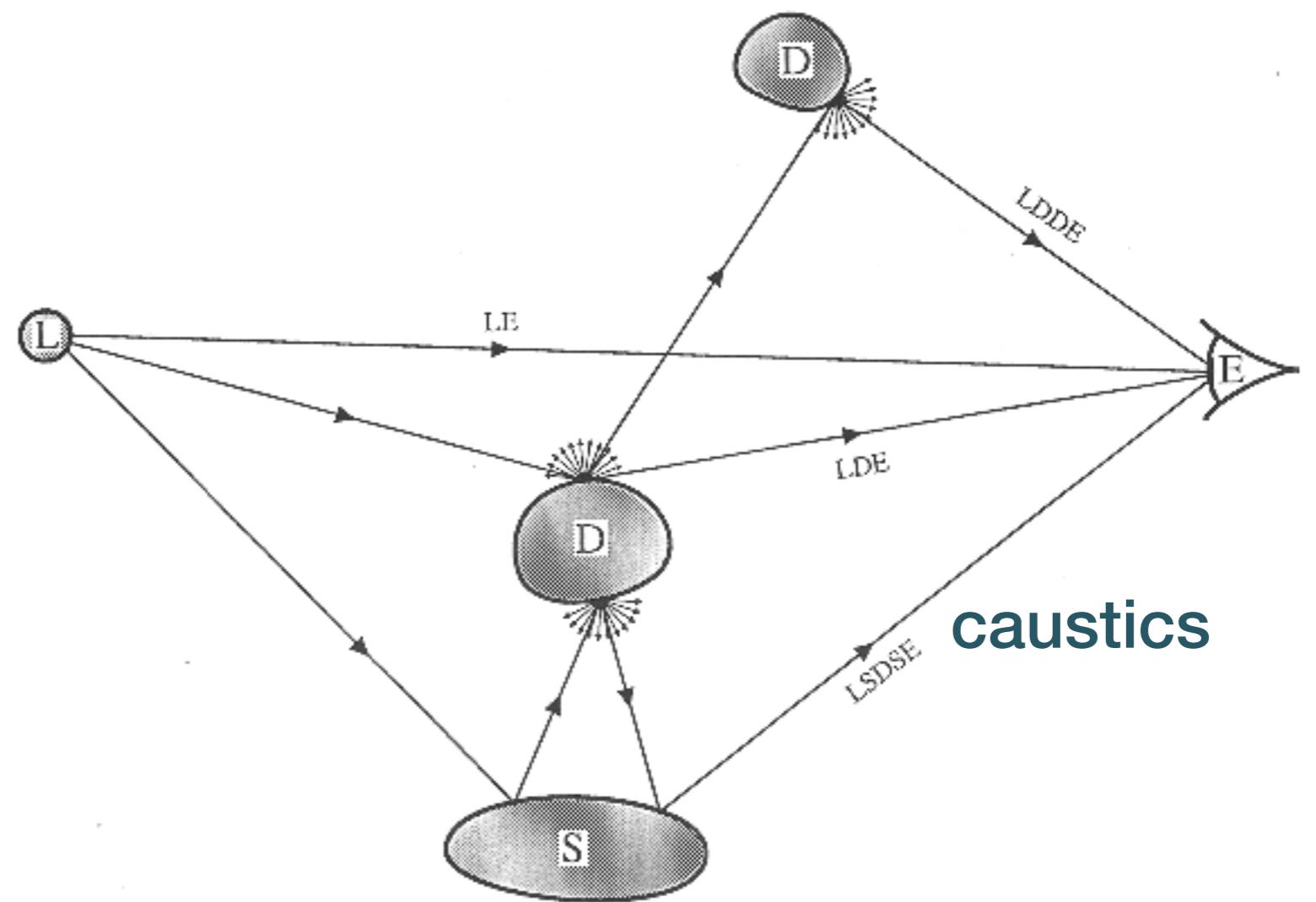
Powered by RayGraph

[www.scratchapixel.com](http://www.scratchapixel.com)

[from [scratchapixel.com](http://scratchapixel.com)]



How might we  
improve this?



# Photon Mapping

Henrik Wann Jensen

Henrik Wann Jensen

## Realistic Image Synthesis Using Photon Mapping

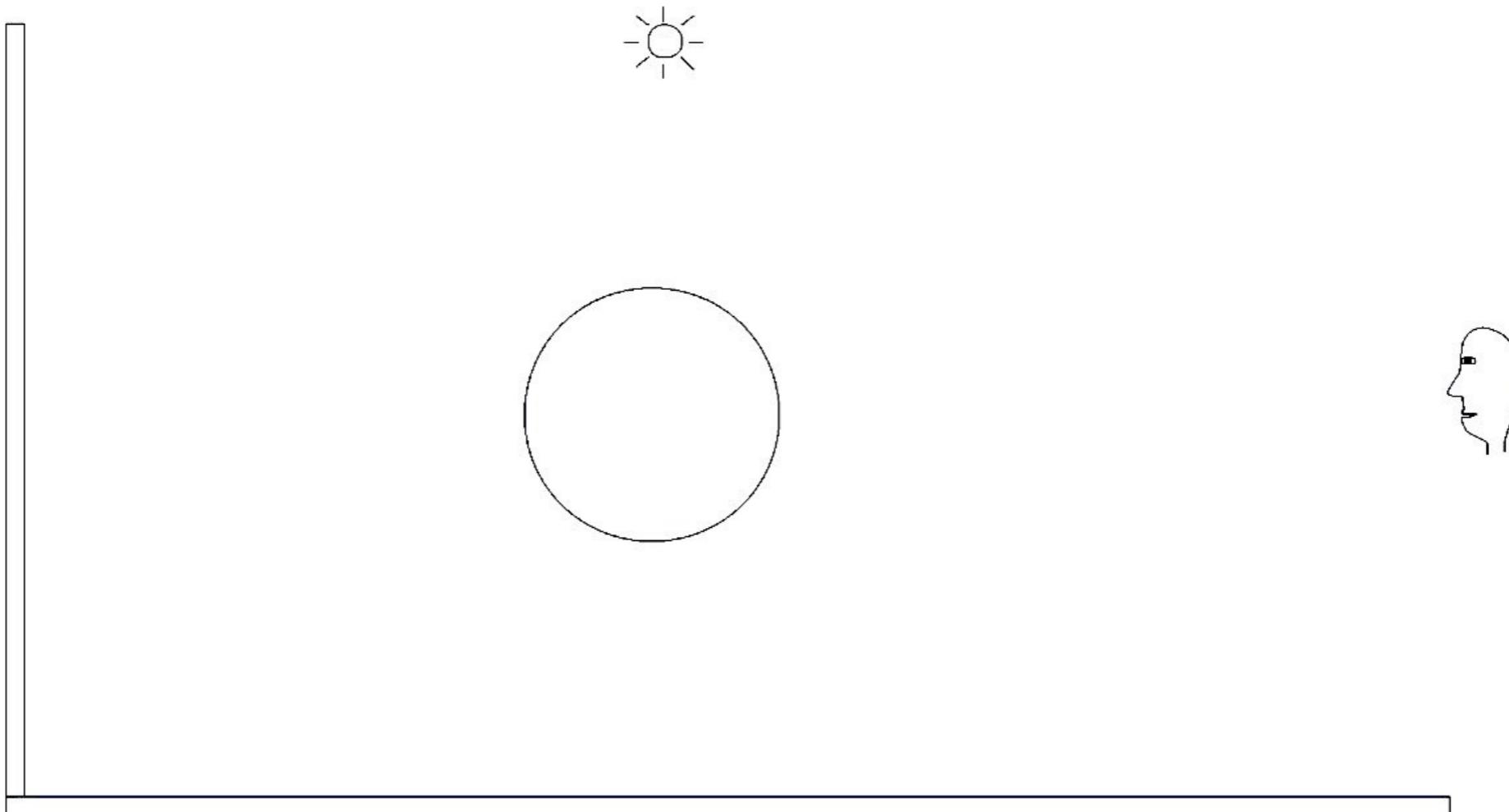


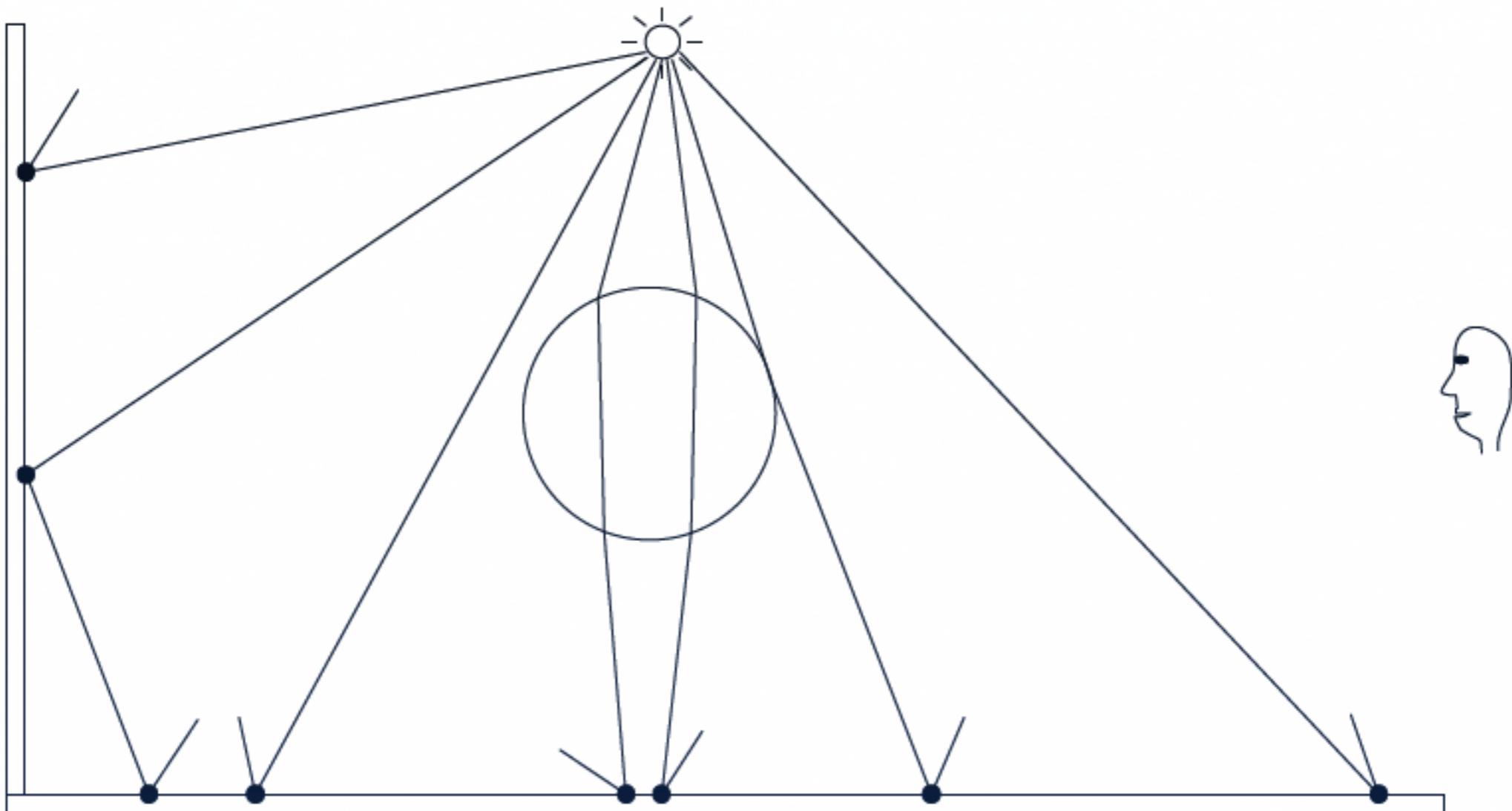
Foreword by Pat Hanrahan

# Photon Mapping

---

- Trace rays emanating from the light sources: “**photons**”

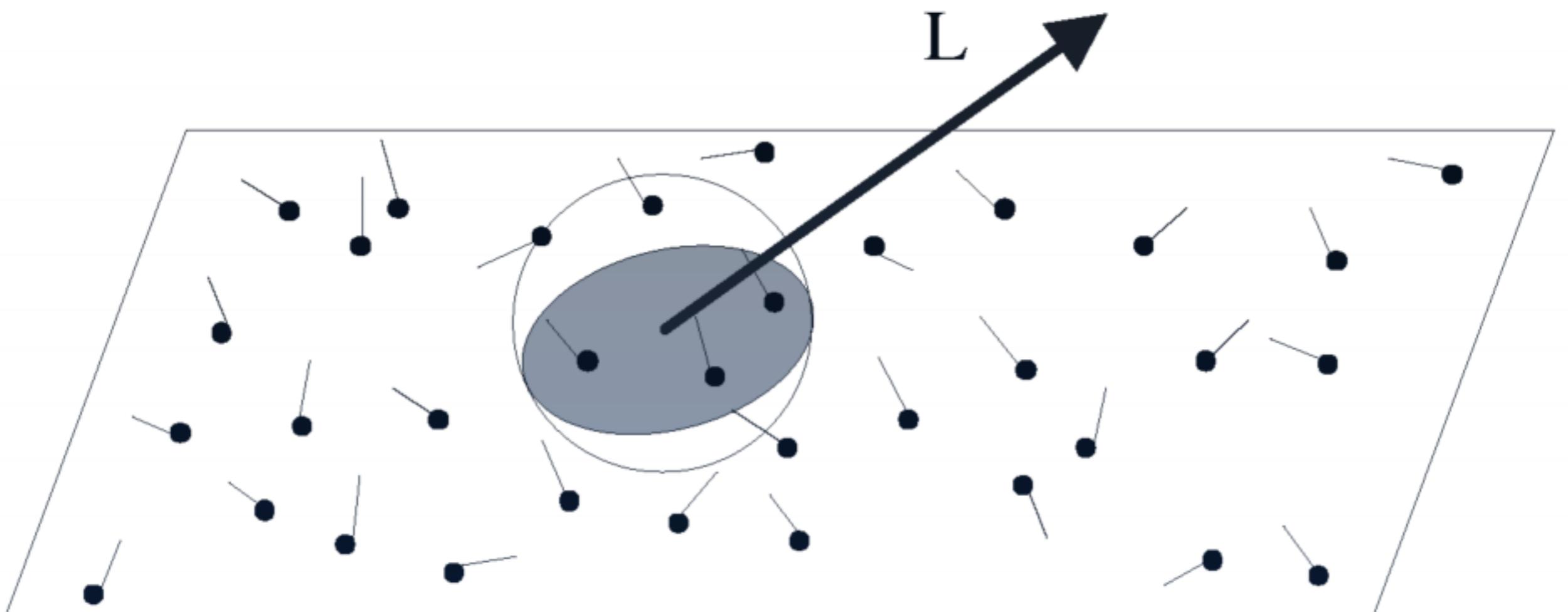




Photons will stick or “bounce” with some probability proportional to surface reflectance

# Irradiance Gather

---

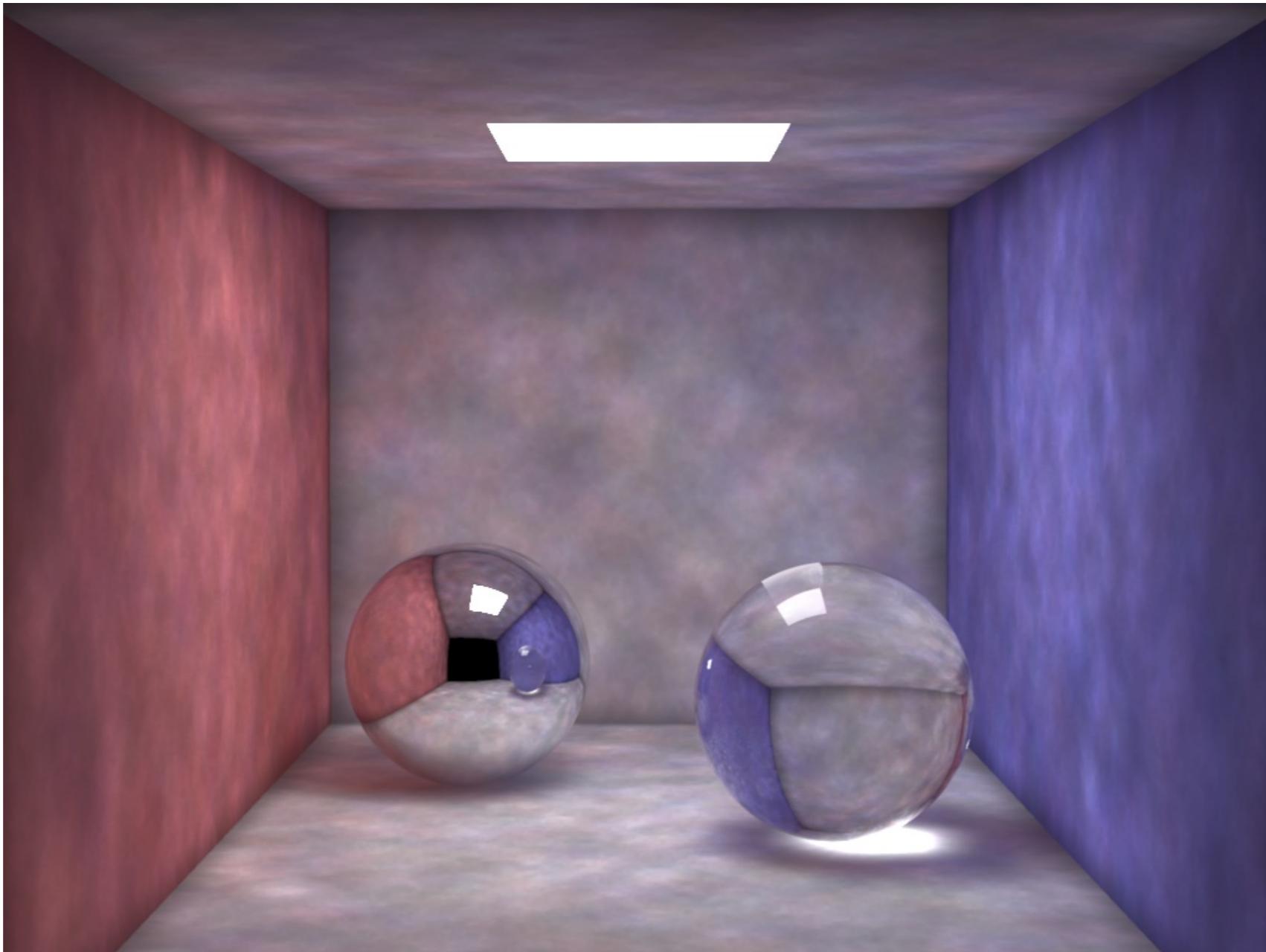


$$L_r(x, \omega_r) = \int_{\mathcal{H}^2} f_r(x, \omega_i \rightarrow \omega_r) L_i(x, \omega_i) \cos \theta_i \, d\omega_i$$

[courtesy of P. Hanrahan, Stanford University] 71

# Photon Mapping

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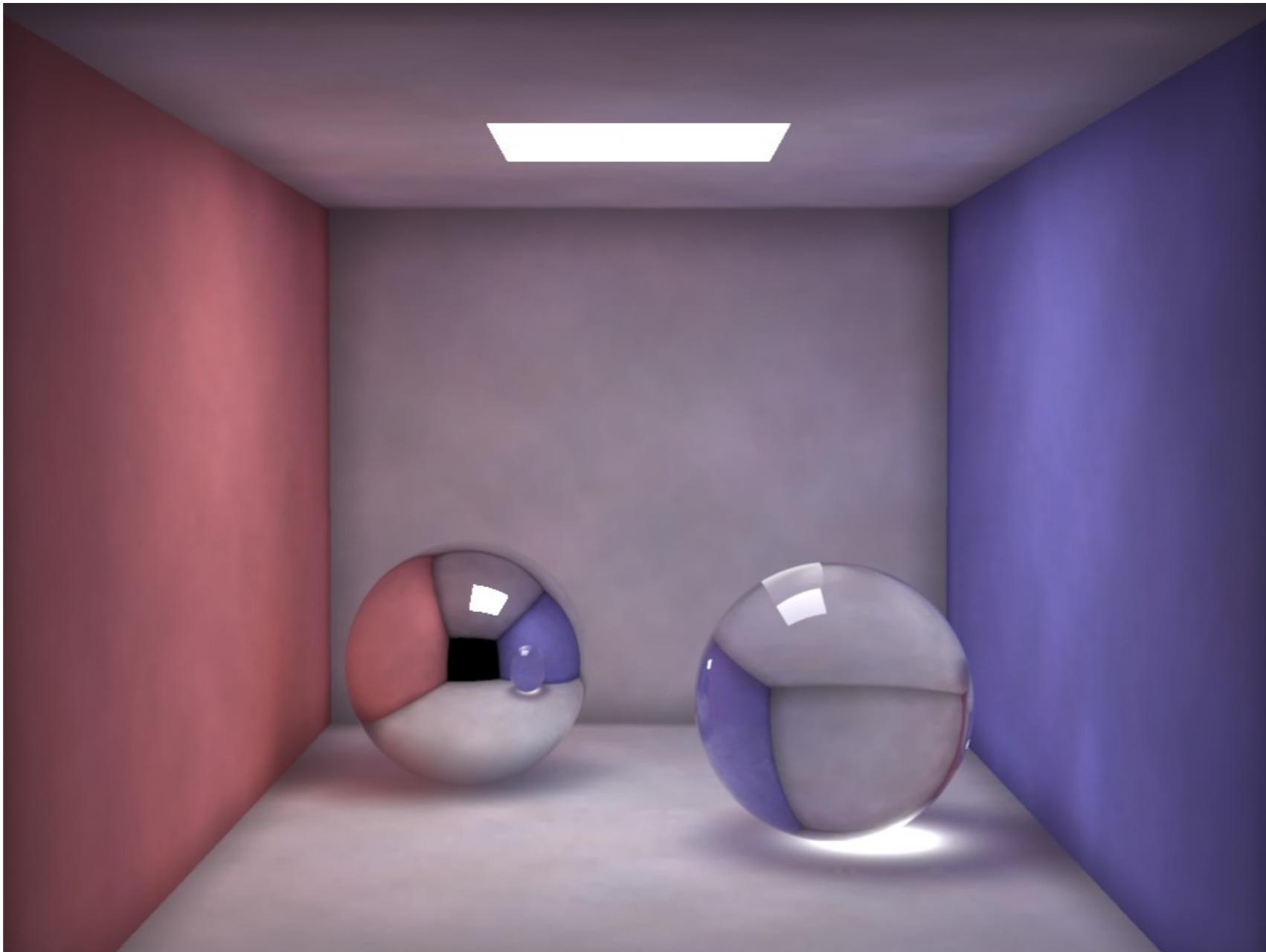


100 000 photons, gather 50 for radiance estimate

[image by Henrik Wann Jensen, UCSD] 72

# Photon Mapping

---

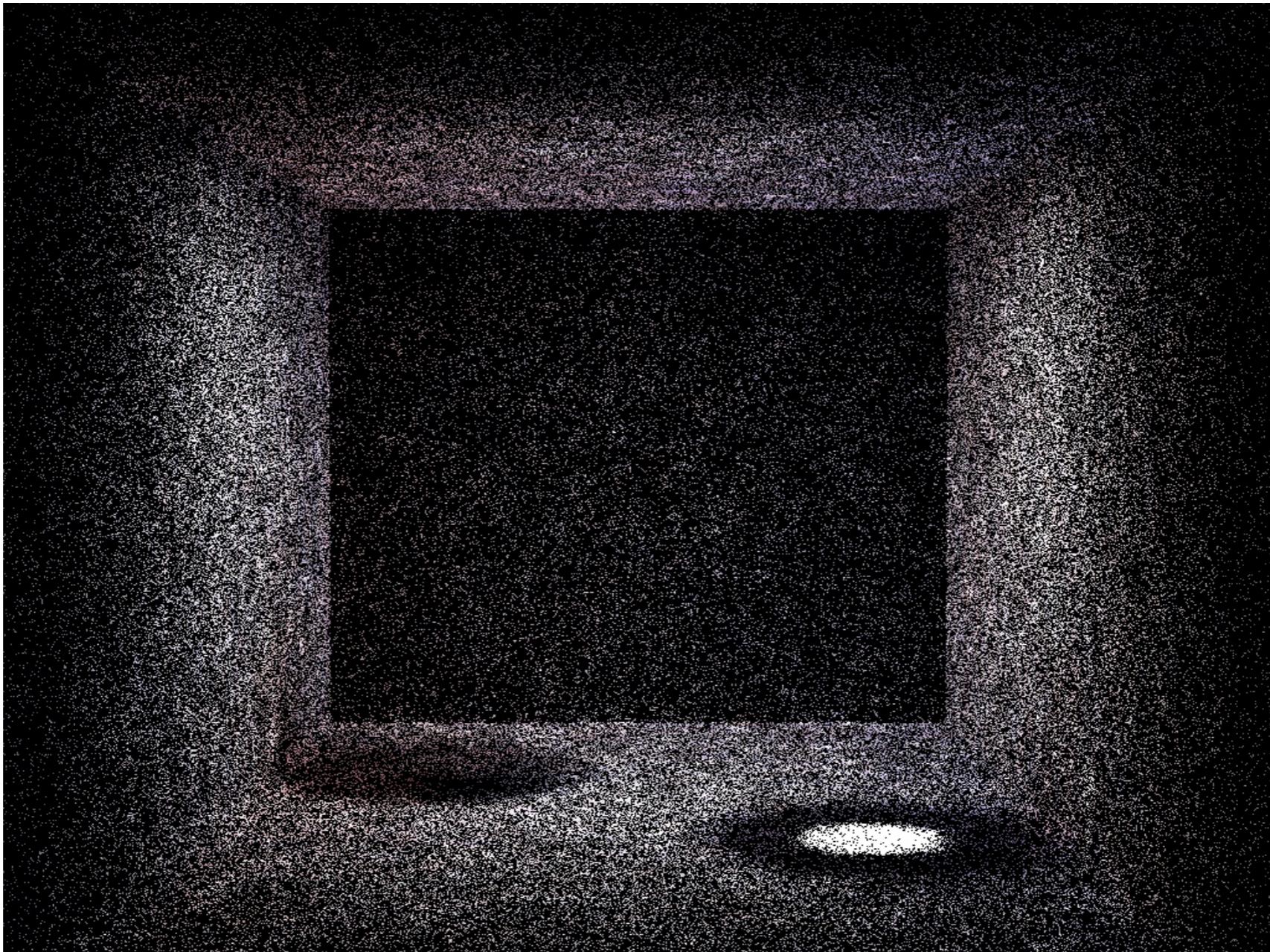


500 000 photons, gather 500 for radiance estimate

[image by Henrik Wann Jensen, UCSD] 73

# Photon Mapping

---

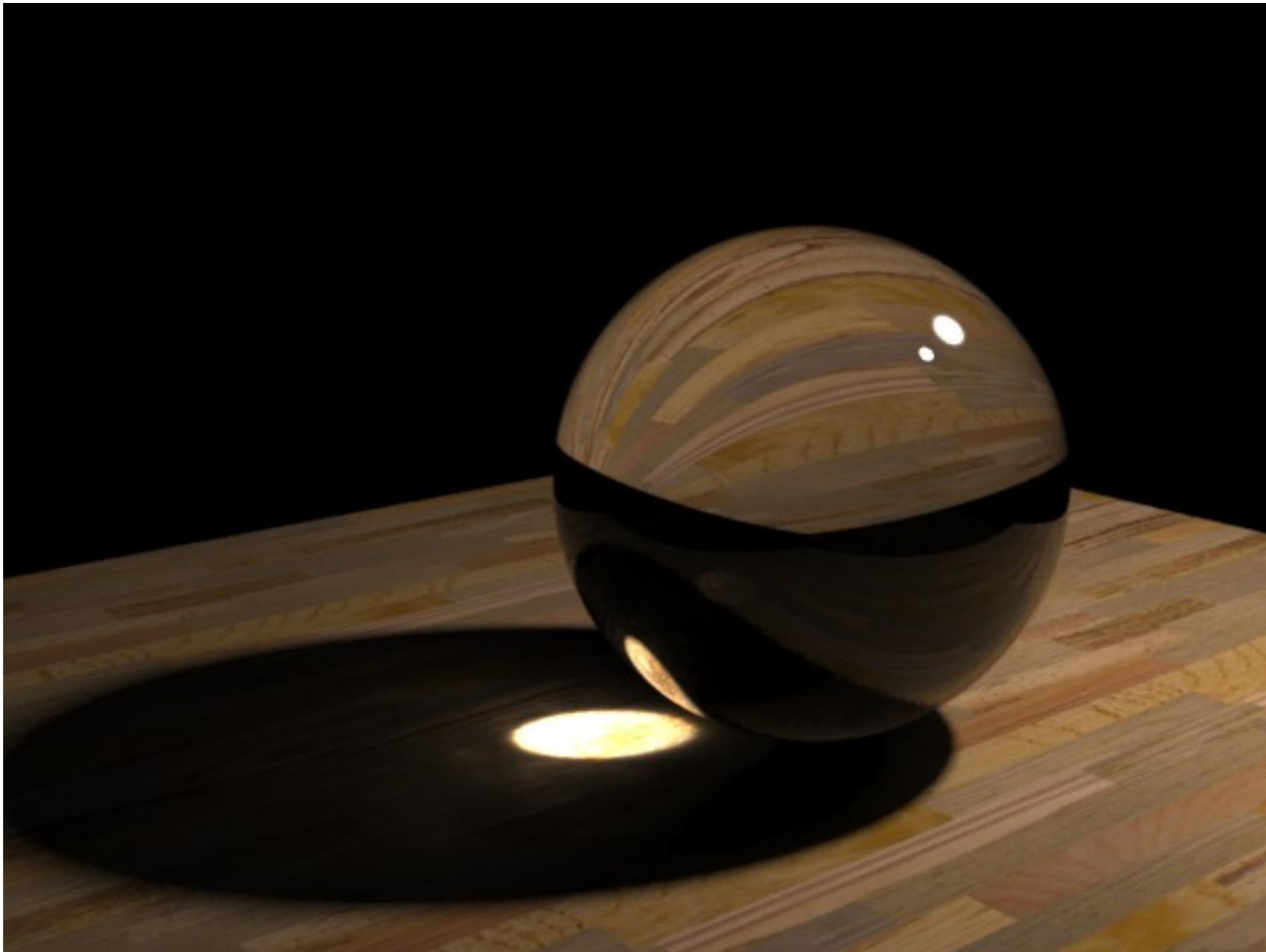


positions of 200 000 photons

[image by Henrik Wann Jensen, UCSD] 74

# Photon Mapping: Caustics

---

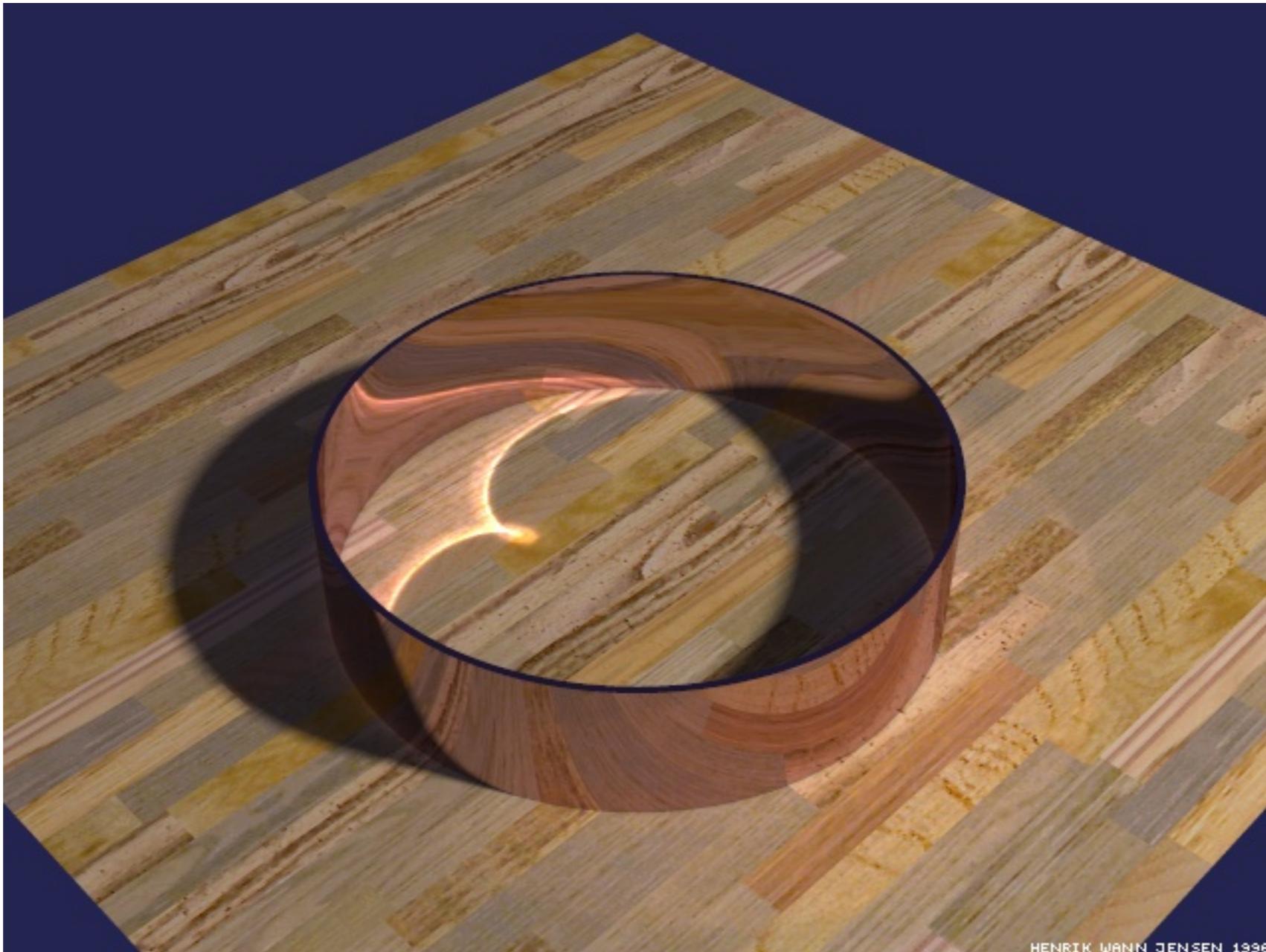


10 000 photons, gather 50 for radiance estimate

[image by Henrik Wann Jensen, UCSD] 75

# Photon Mapping: Caustics

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HENRIK WANN JENSEN 1996

50 000 photons, gather 50 for radiance estimate

[image by Henrik Wann Jensen, UCSD] 76

# Photon Mapping: Caustics

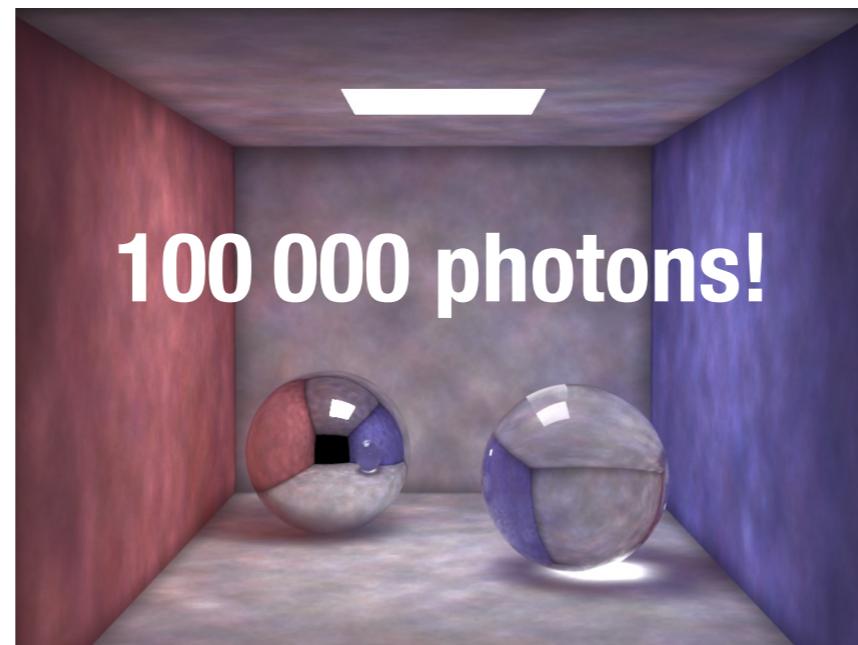
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Henrik likes cognac

[image by Henrik Wann Jensen, UCSD] 77

# What are the main challenges or limitations?



# Real or Synthetic?

---



RENDERED USING DALI - HENRIK WANN JENSEN 2000

[image by Henrik Wann Jensen, UCSD] 79

# Real or Synthetic?

---



# Real or Synthetic?

---



[from [wsj.com](http://wsj.com)] 81

# Real or Synthetic?

---





I still haven't talked about how to do this...



[from [blendernation.com](http://blendernation.com)]

Matt Pharr, Wenzel Jakob, Greg Humphreys

# PHYSICALLY BASED RENDERING

From Theory to Implementation

**Third** Edition

The Reference

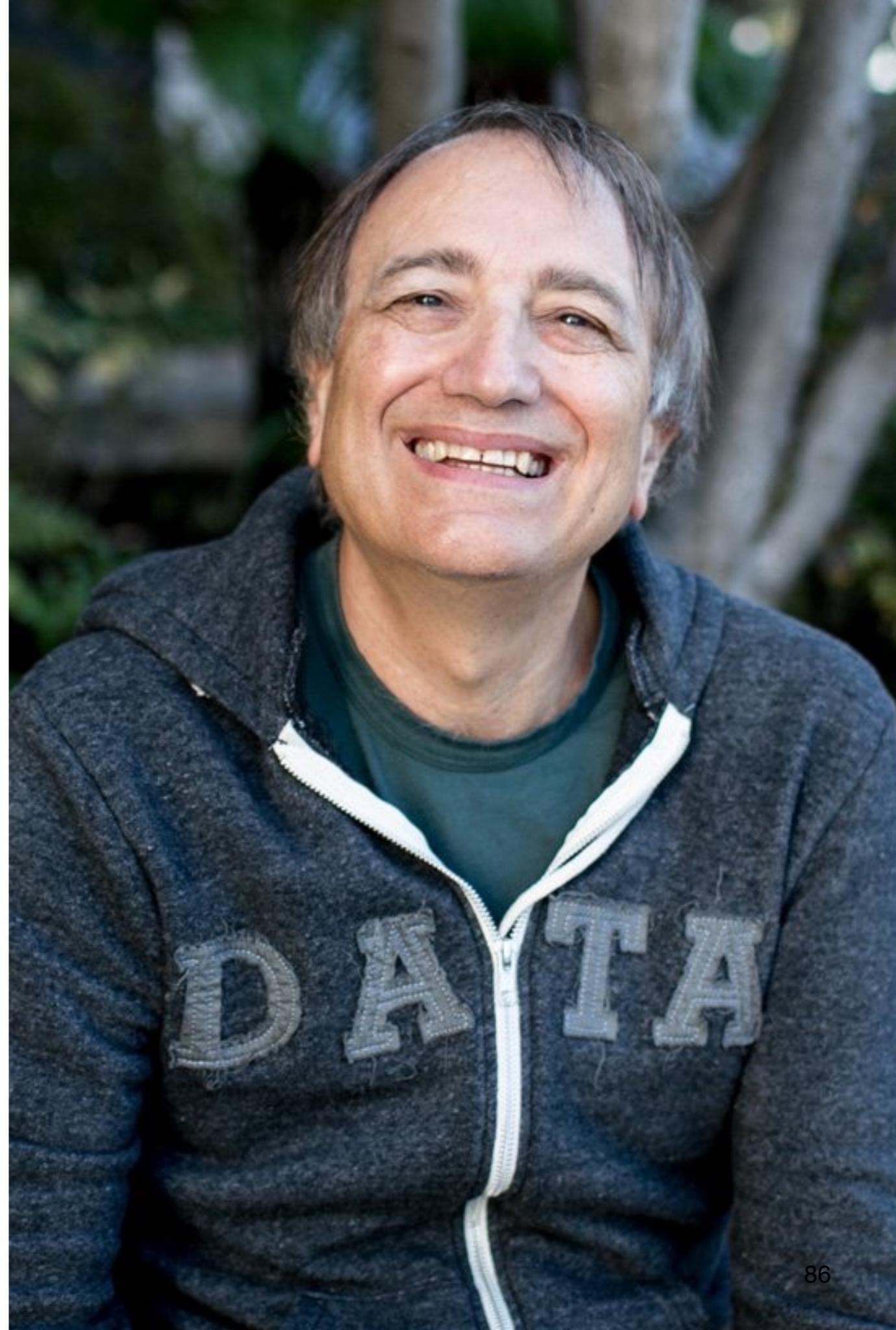


# Who is Pat Hanrahan?

---

[accolades too numerous to list]

Most of today's lecture content  
was adapted, borrowed, or  
downright pilfered from the works  
of Dr. Hanrahan. Thanks Pat!



# Things to Remember

---

- Heuristic lighting techniques we learned in this course cannot reproduce global illumination effects
  - caustics, radiosity, and shadows are neglected
- Physically-based rendering equations allow for accurate simulation of light transport
  - but we get integral equations that are wicked hard to solve!
- Various Monte Carlo integration techniques can be used to synthesize realistic images in reasonable time