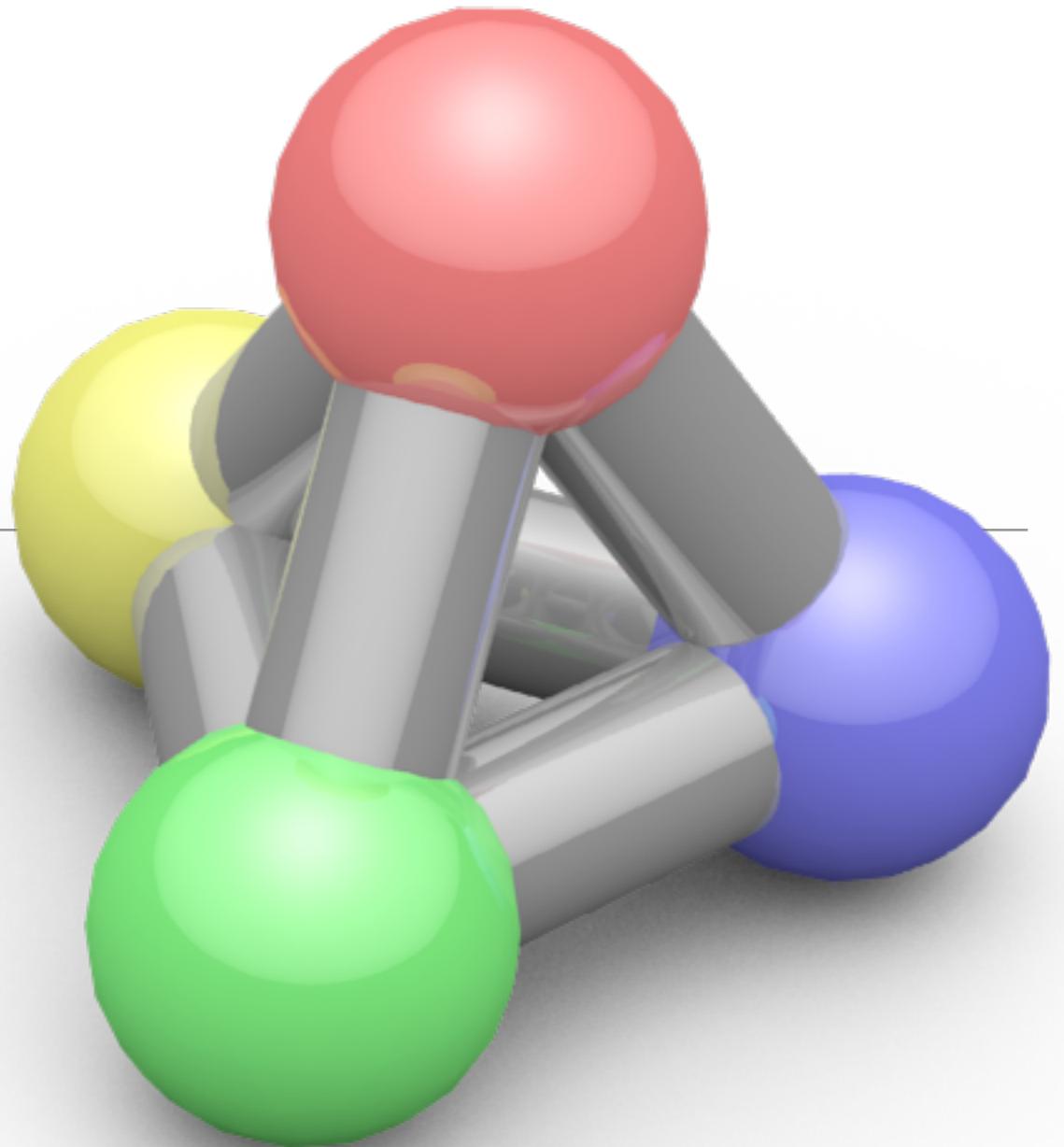


# Materials & Shading

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CPSC 453 – Fall 2016

Sonny Chan





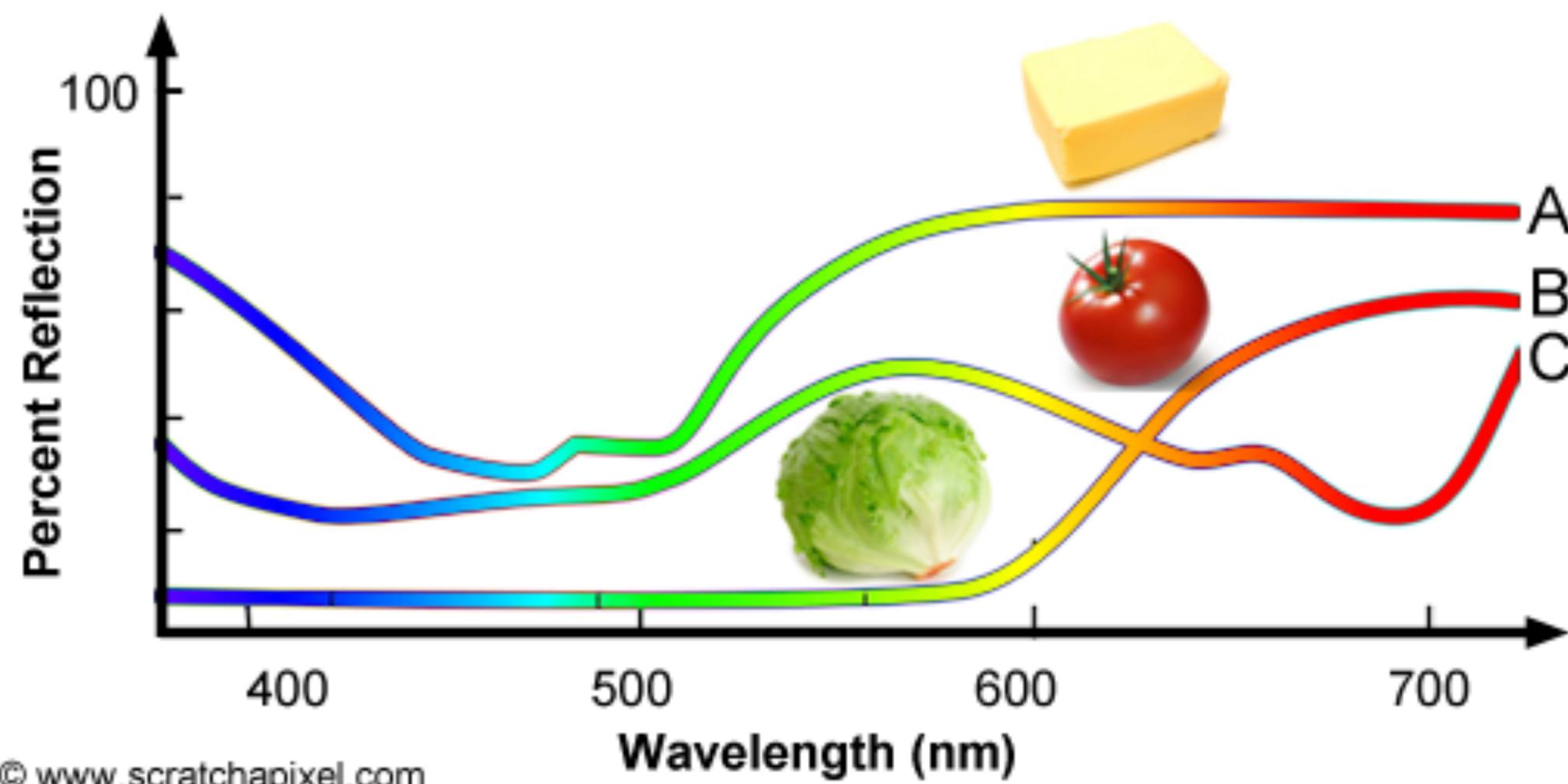
# Materials

Rendered by Unreal Engine

The appearance of a material is determined by the manner in which light is reflected from it, or transmitted through it.

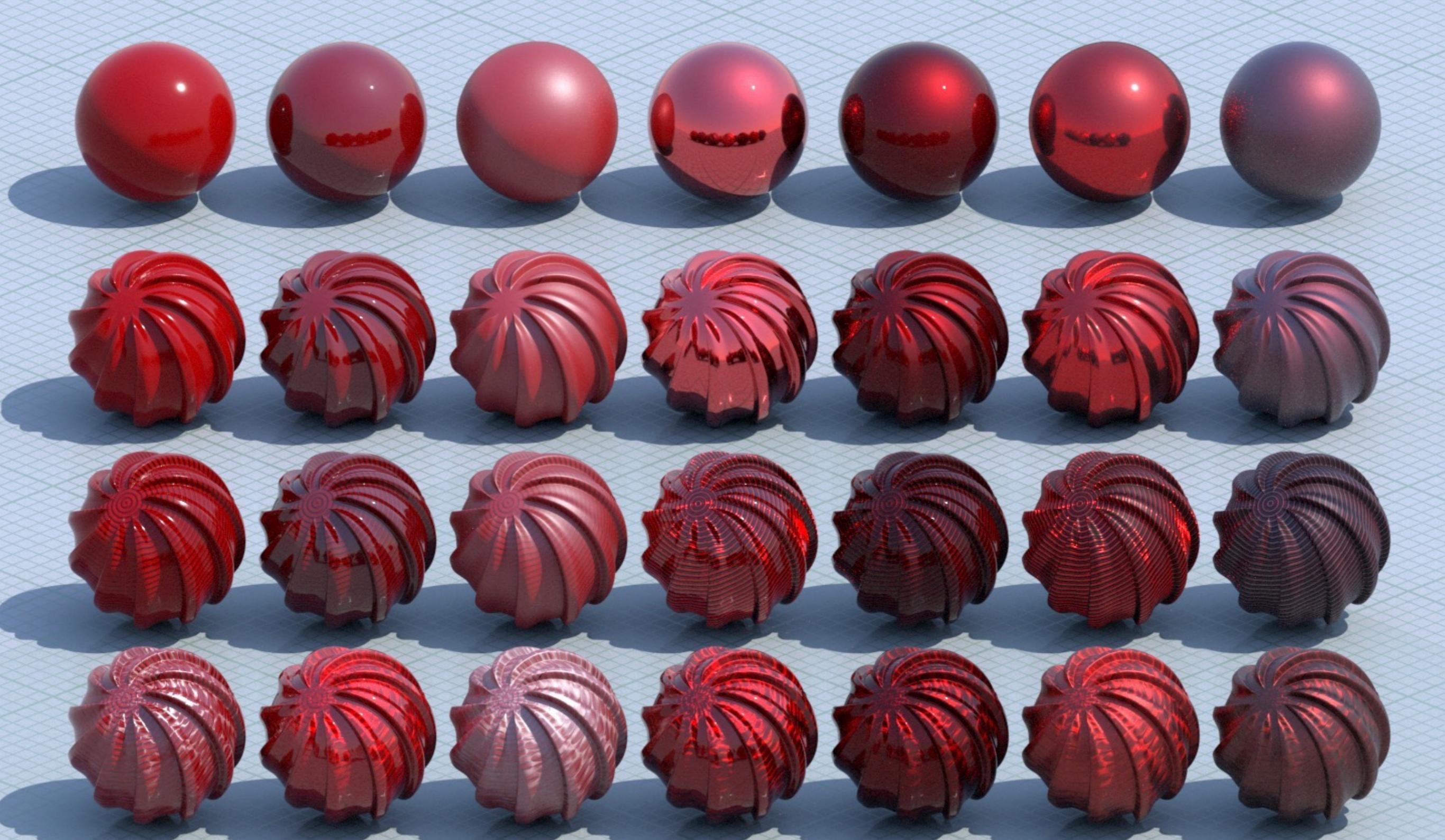
**What is the most basic  
material property?**

# Colour: Spectral Reflectance Curves



© www.scratchapixel.com

[from [scratchapixel.com](http://www.scratchapixel.com)]<sub>5</sub>



But not the only factor!

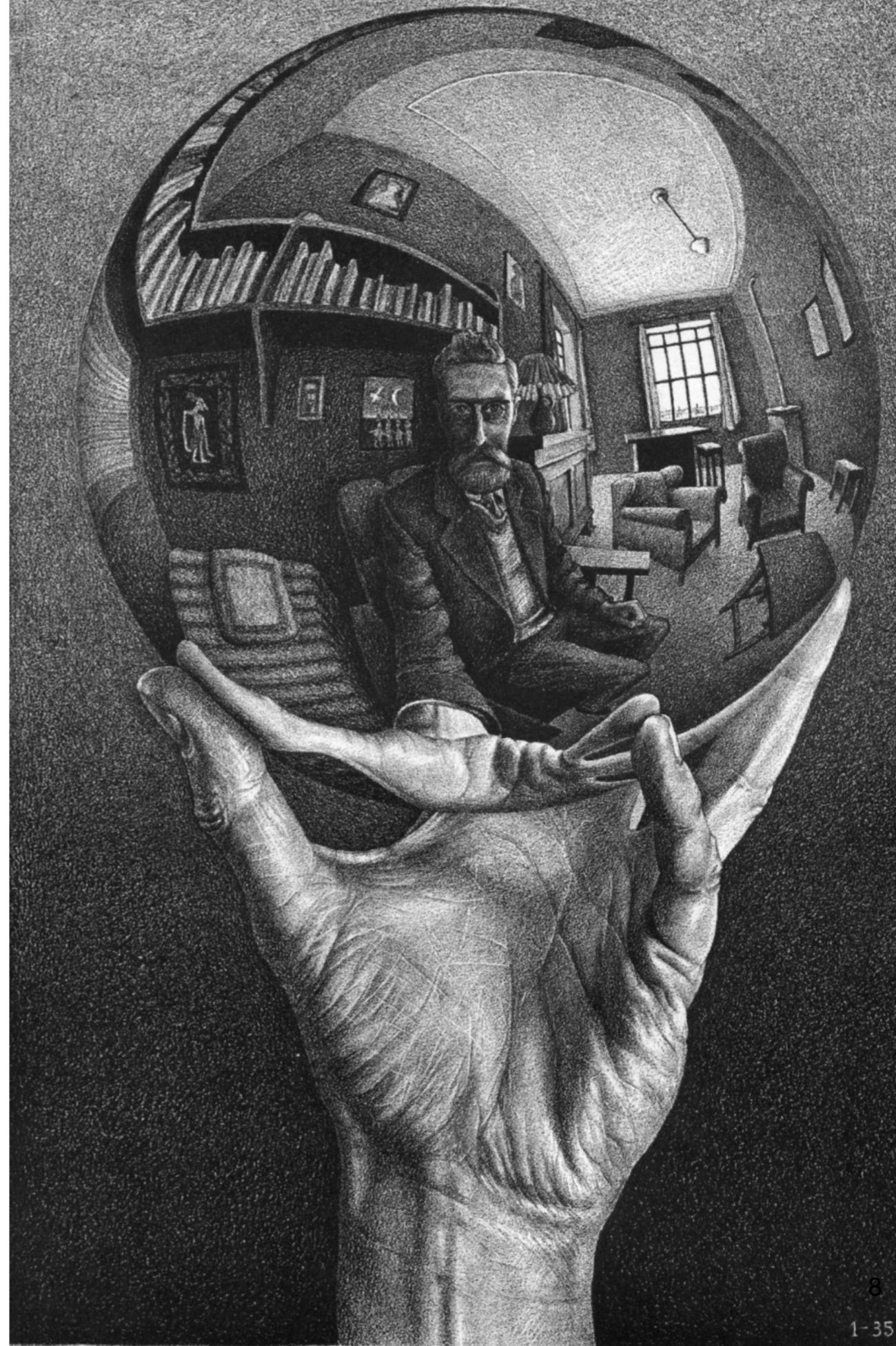
RenderMan PxrLM

Let's take a look at some  
**real world materials**

# Hand with Reflecting Sphere (Self-Portrait)

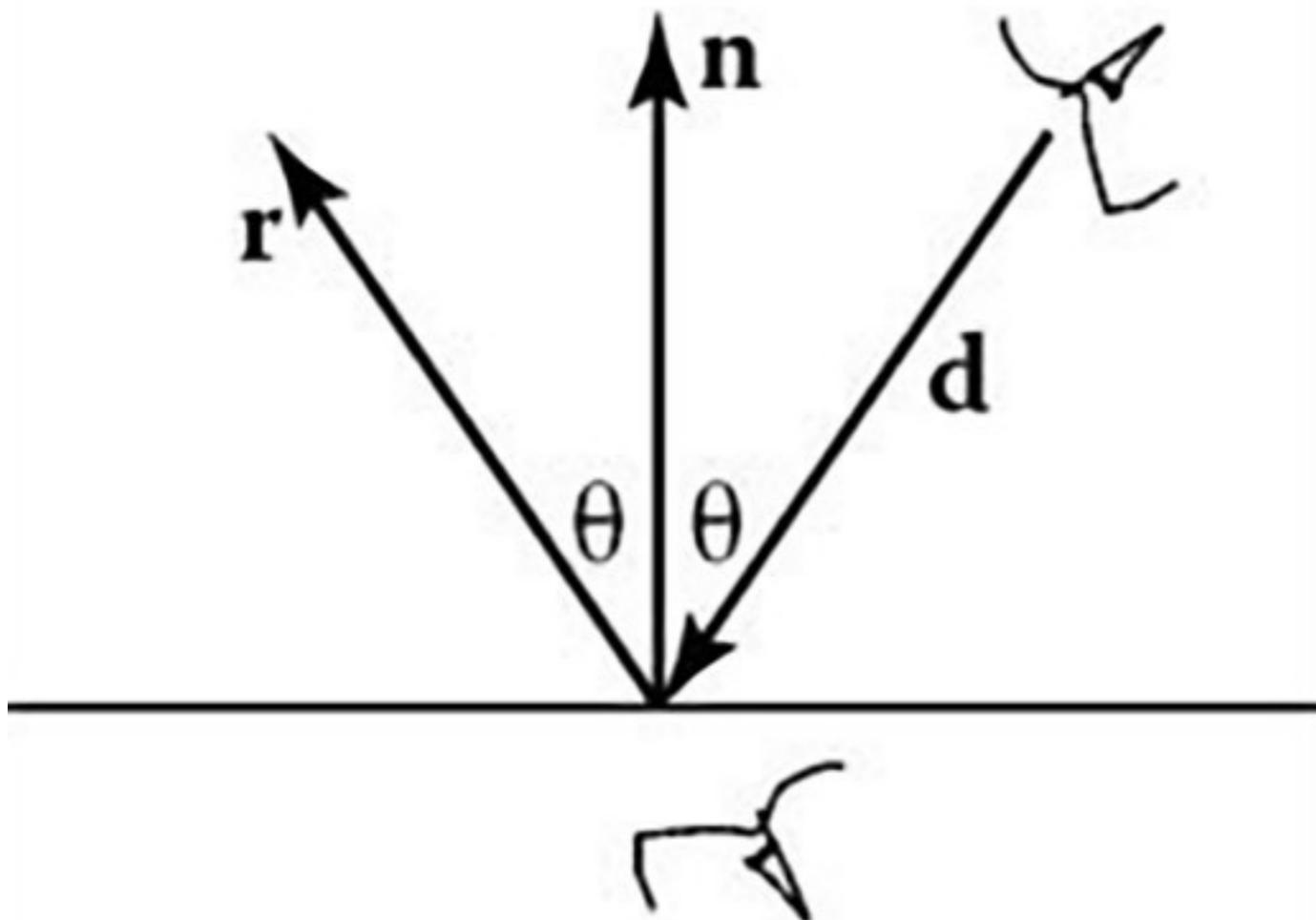
---

M.C. Escher, 1935



# Ideal Specular Reflections

---



$$\mathbf{r} = \mathbf{d} - 2(\mathbf{d} \cdot \hat{\mathbf{n}})\hat{\mathbf{n}}$$

Trace another ray, as if you were looking from underneath.



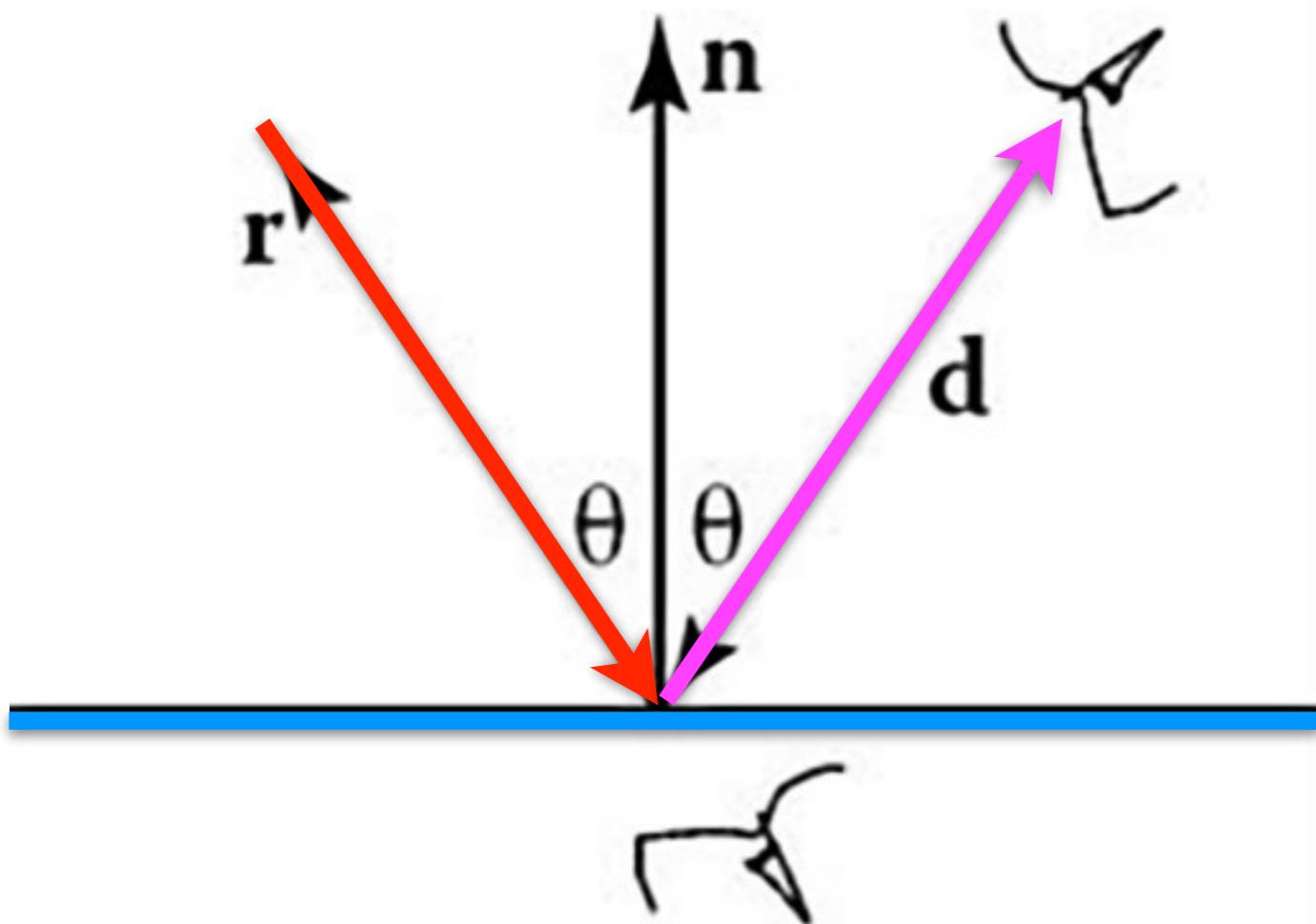
**Real surfaces are not perfectly specular!**



**Real surfaces are not perfectly specular!**

# Mixed Specular Reflections

---



$$\mathbf{r} = \mathbf{d} - 2(\mathbf{d} \cdot \hat{\mathbf{n}})\hat{\mathbf{n}}$$

Combine reflected ray's light with the surface material colour.

# A Glass Marble

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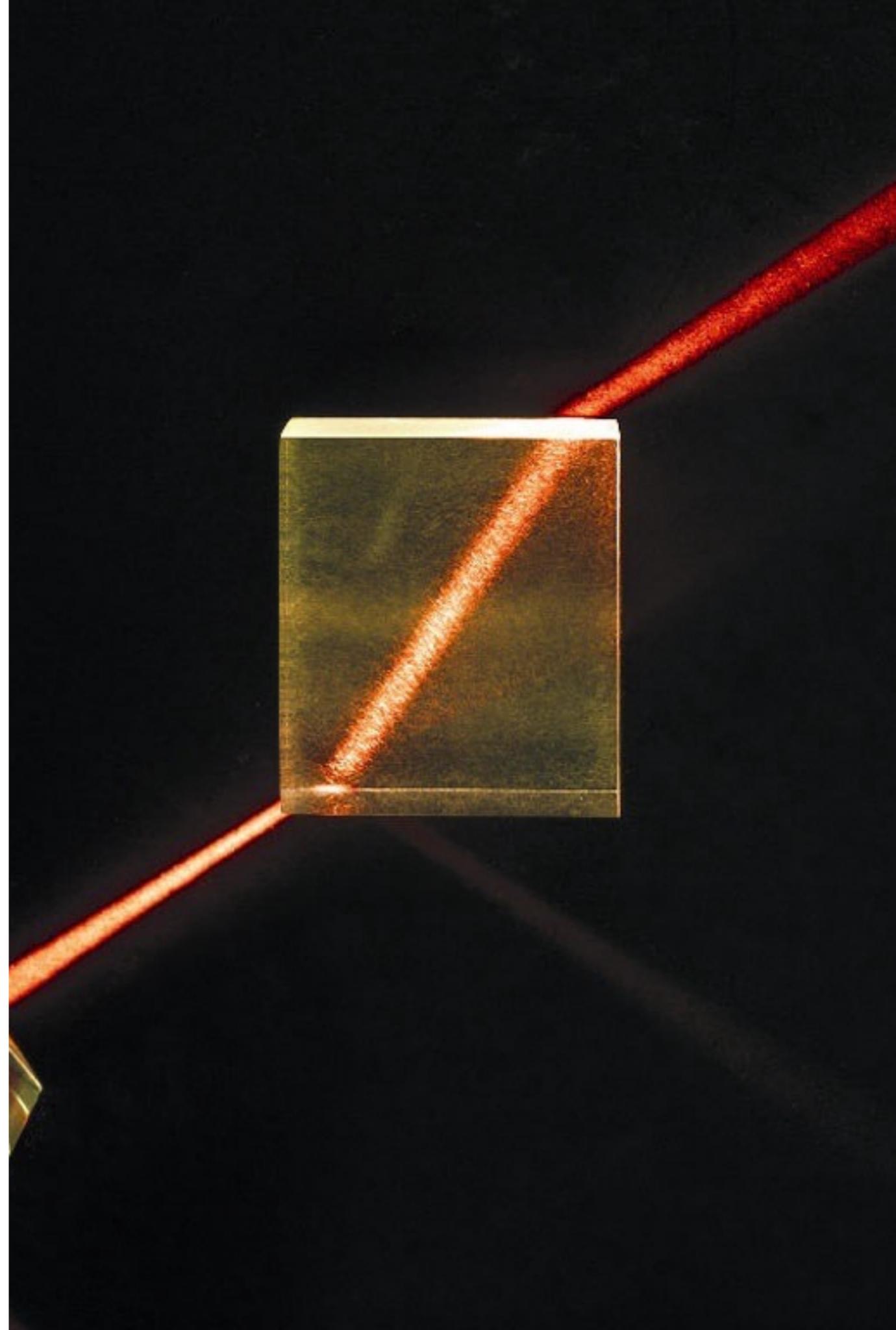
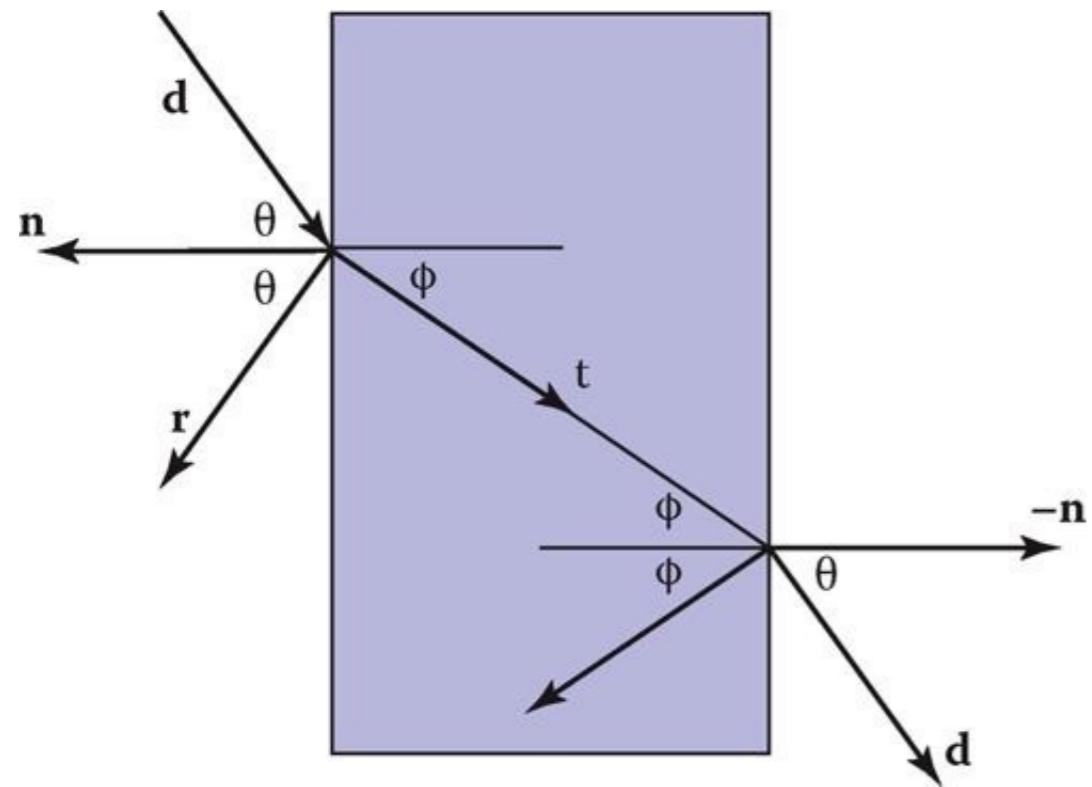
What do we do with this material?



# Snell's Law

- Ratio of sines of angles is equal to ratio of velocities:

$$\frac{\sin \theta}{\sin \phi} = \frac{v}{v_t} = \frac{n_t}{n}$$





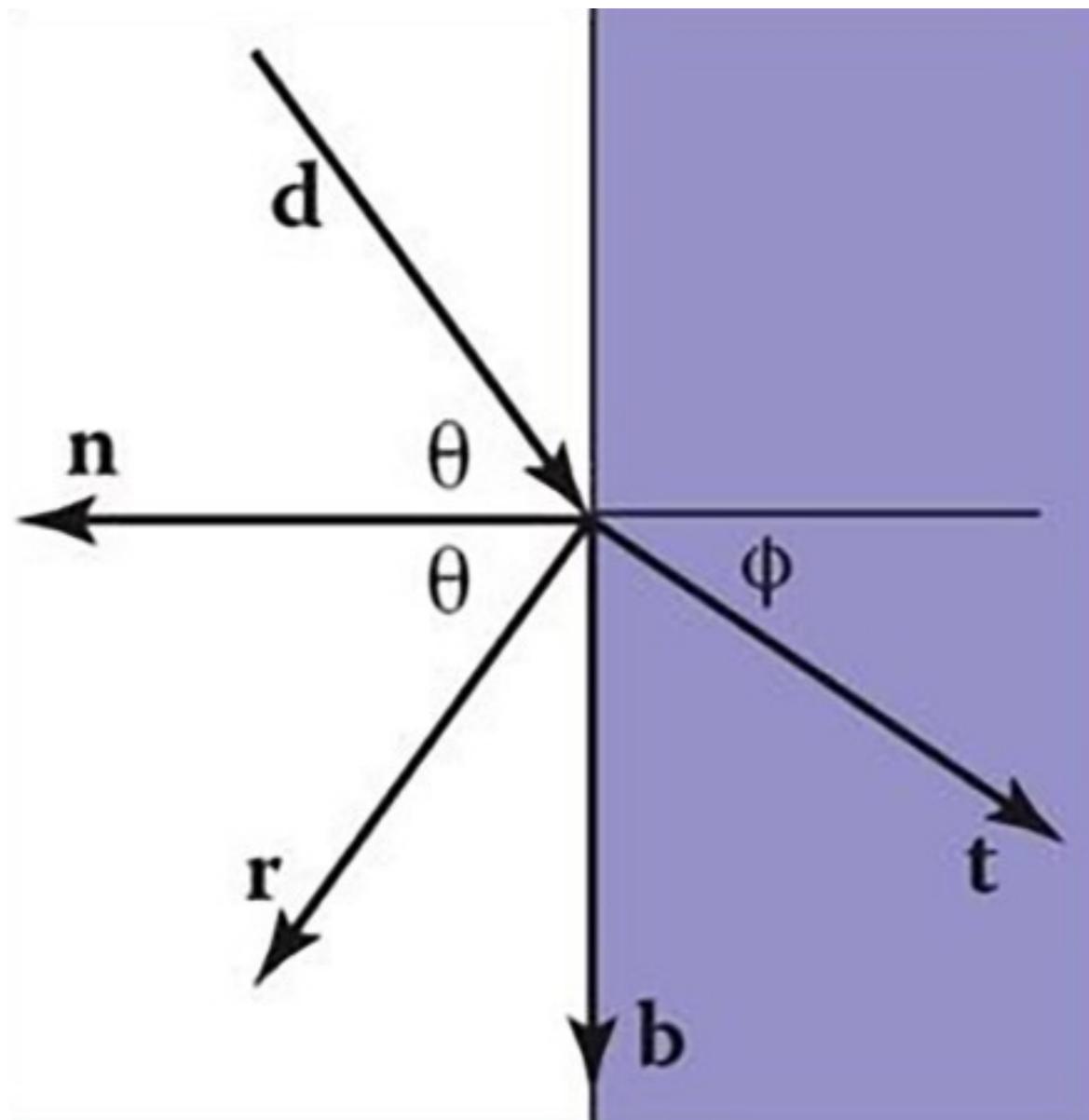
# Index of Refraction

of some common materials

n	Material
1.0001	air
1.333	water
1.47	olive oil
1.52	crown glass
1.62	flint glass
2.15	cubic zirconia
2.42	diamond

# Ray Tracing Refraction

---



$$n \sin \theta = n_t \sin \phi$$

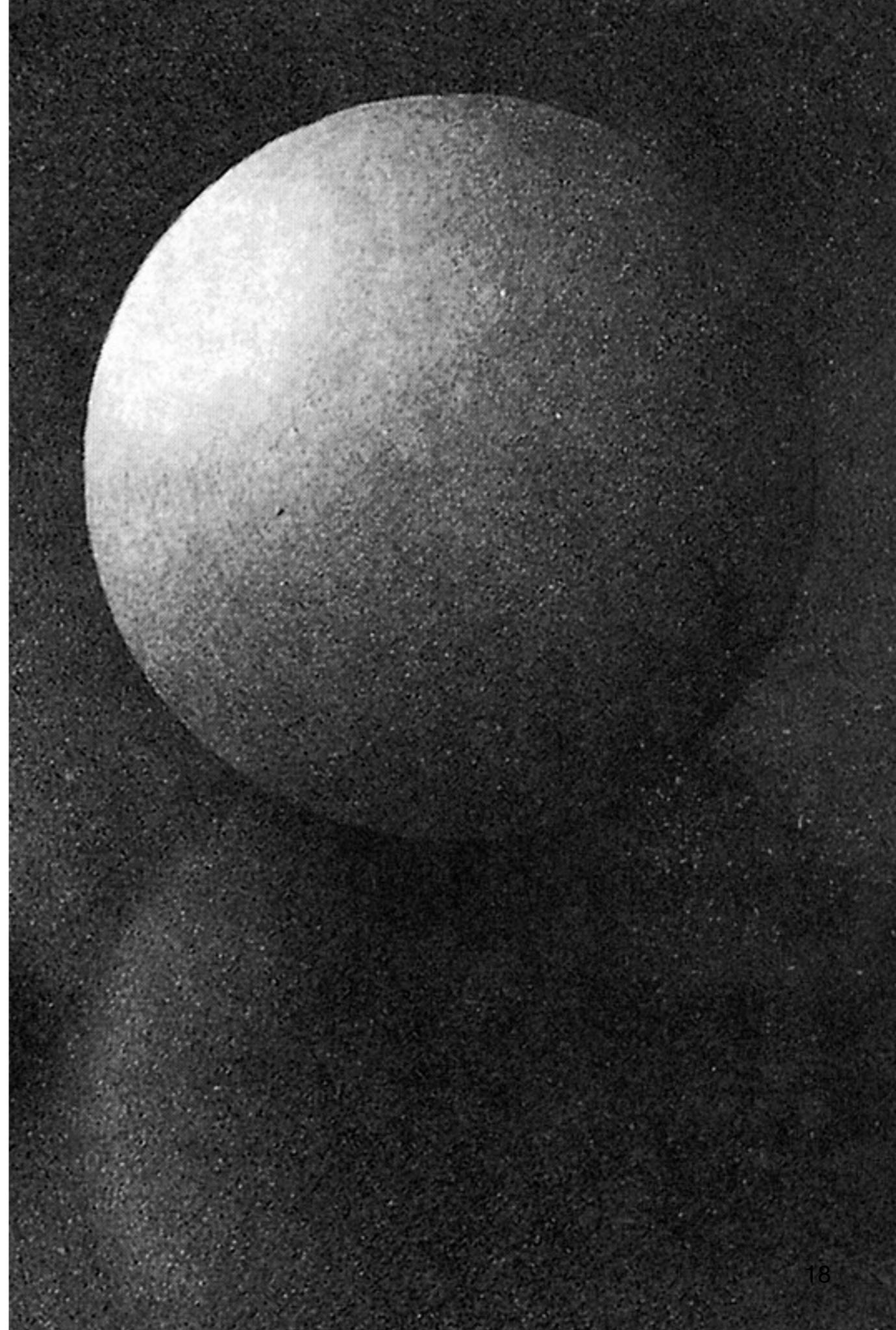
$$\cos^2 \phi = 1 - \frac{n^2(1 - \cos^2 \theta)}{n_t^2}$$

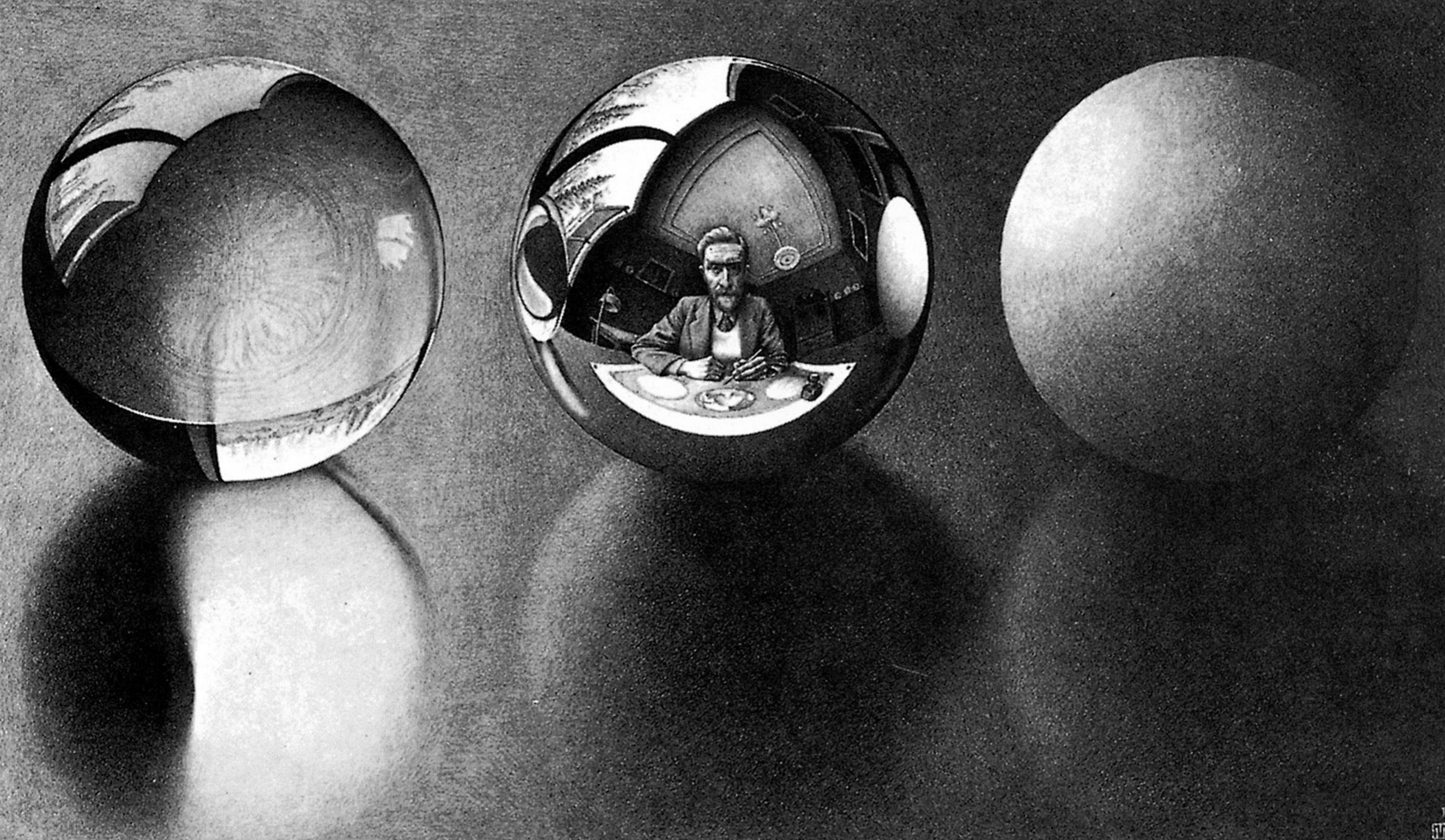
$$\mathbf{t} = \frac{n(\mathbf{d} + \hat{\mathbf{n}} \cos \theta)}{n_t} - \hat{\mathbf{n}} \cos \phi$$

# A Diffuse Reflector

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M.C. Escher, 1946





Three Spheres II

M.C. Escher, 1946

# Properties of Diffuse Reflectors

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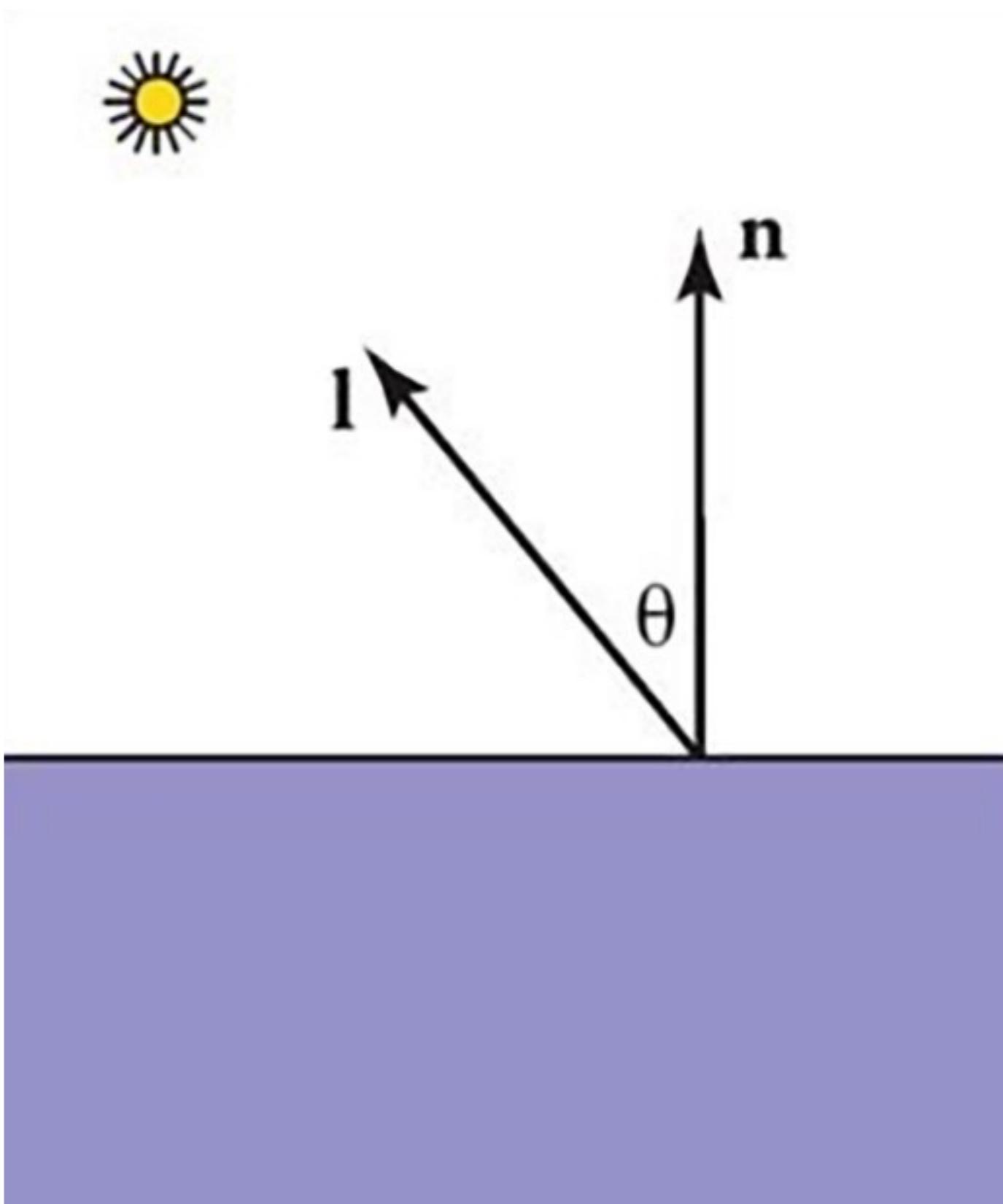


# Diffuse Reflection

- Brightness dependent *only* on the direction of incident light
- View direction has no effect on appearance
- Lambert's cosine law:

$$c \propto \hat{\mathbf{n}} \cdot \hat{\mathbf{l}}$$

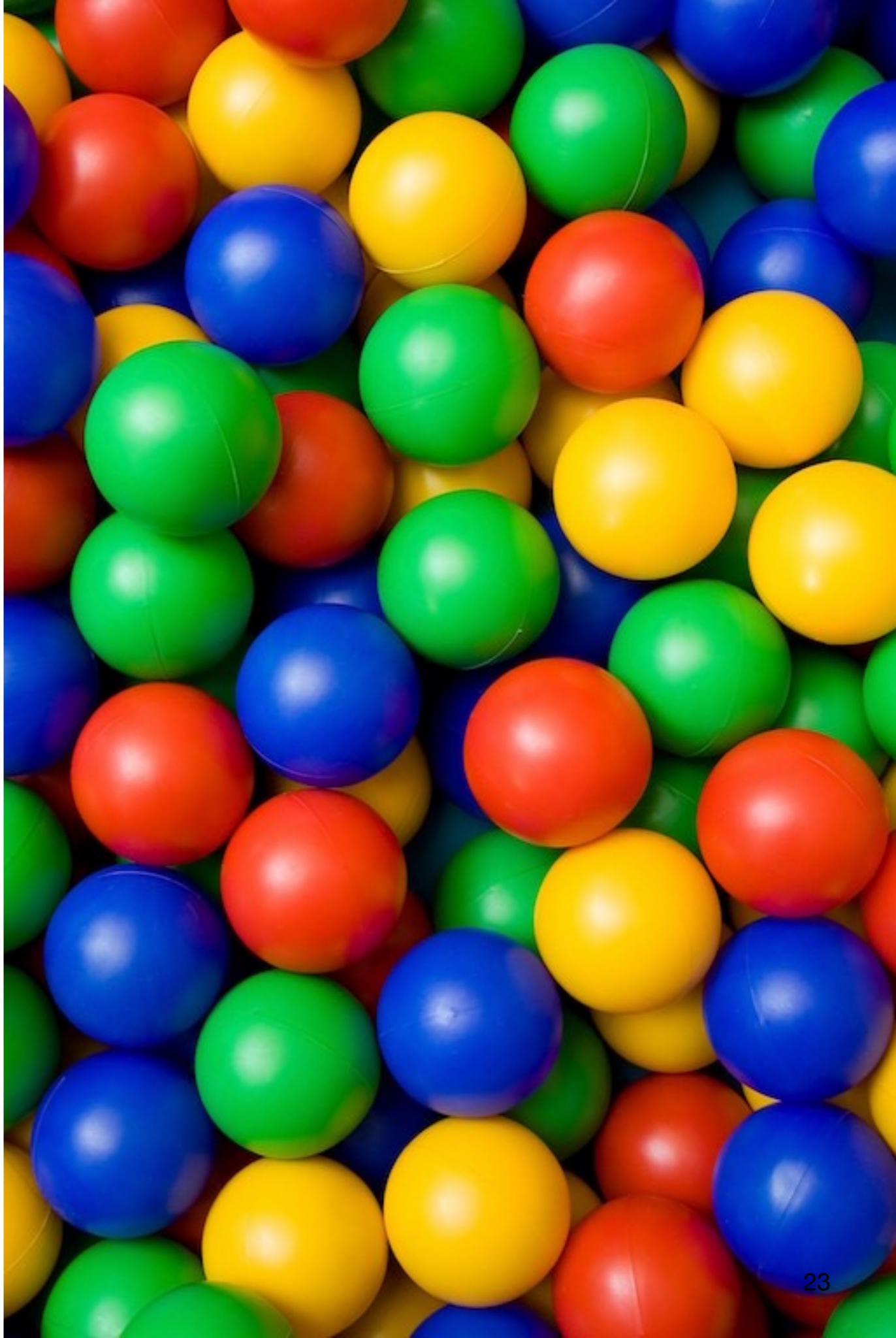
$$c = c_r c_l \max(0, \hat{\mathbf{n}} \cdot \hat{\mathbf{l}})$$



# Specular Highlights

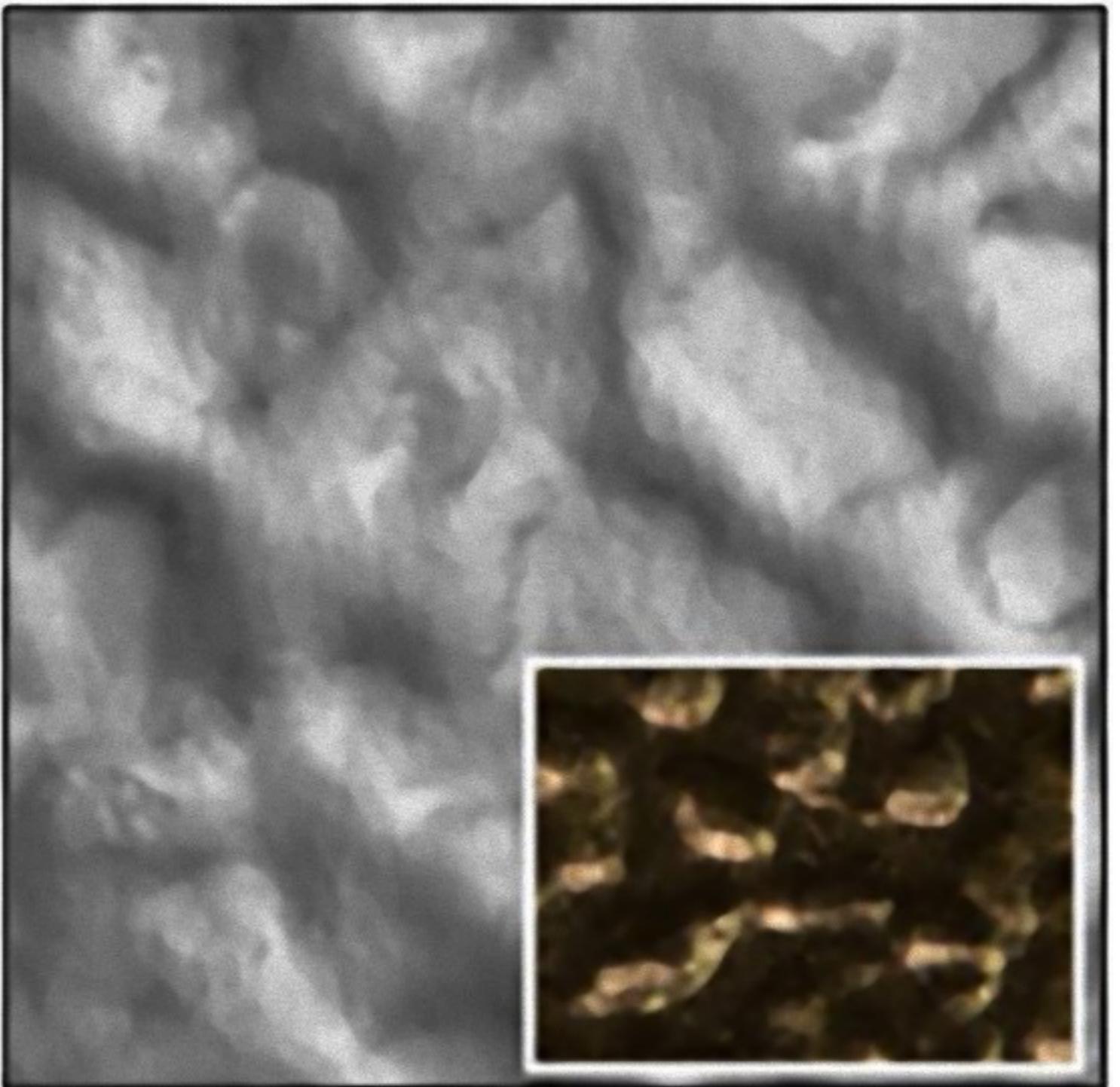
---

A Heuristic Approximation



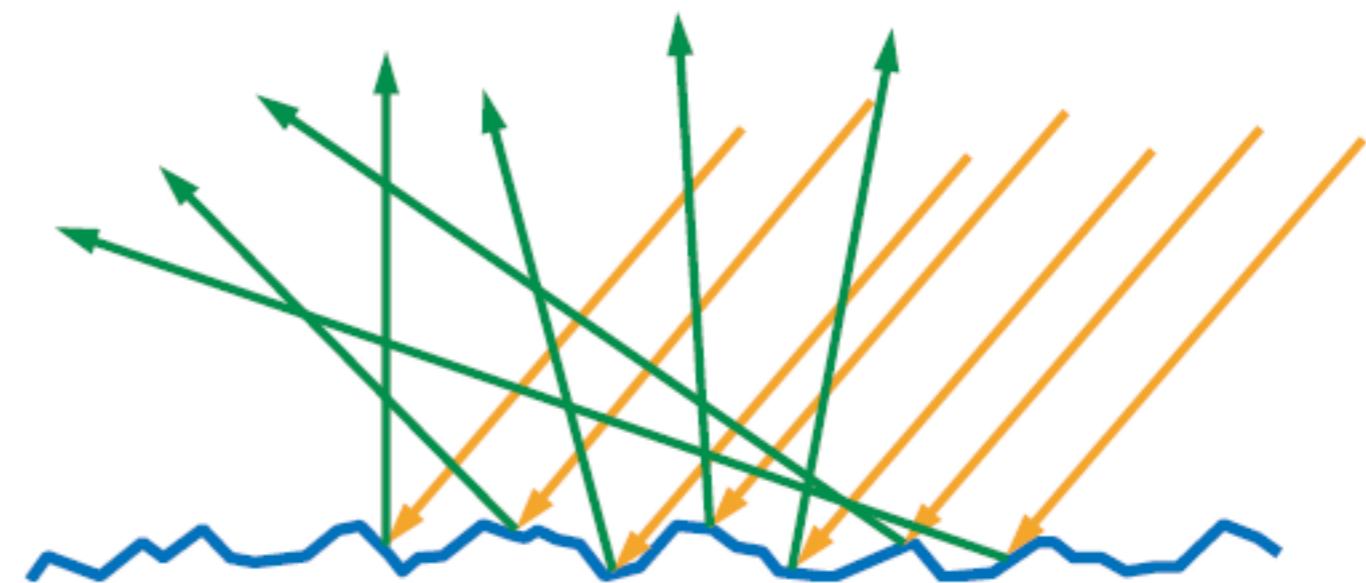
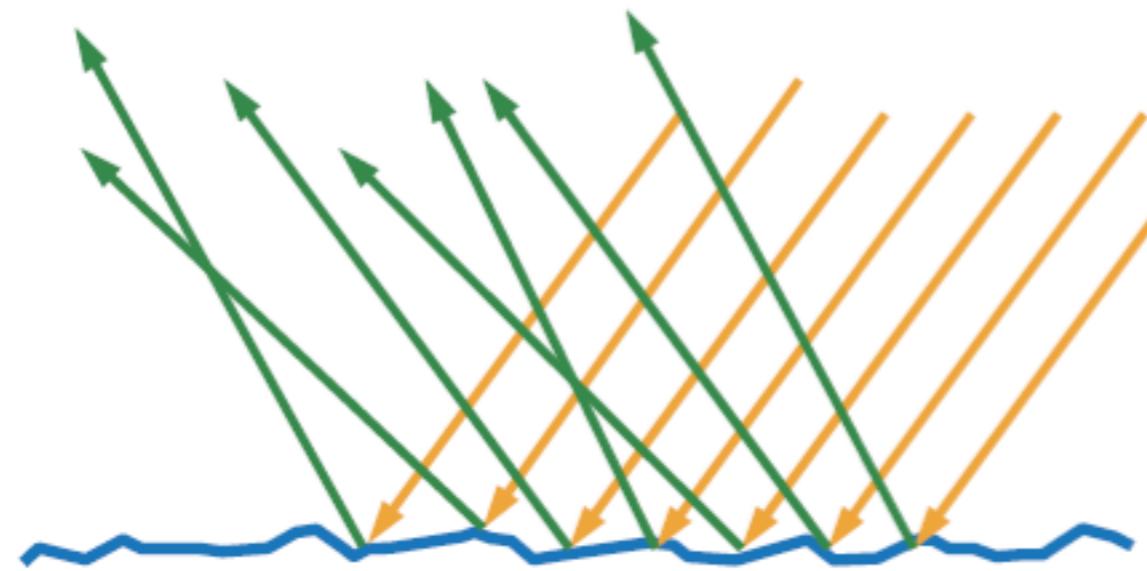


# Plastic, Magnified



[image from [gelsight.com](http://gelsight.com)] <sub>25</sub>

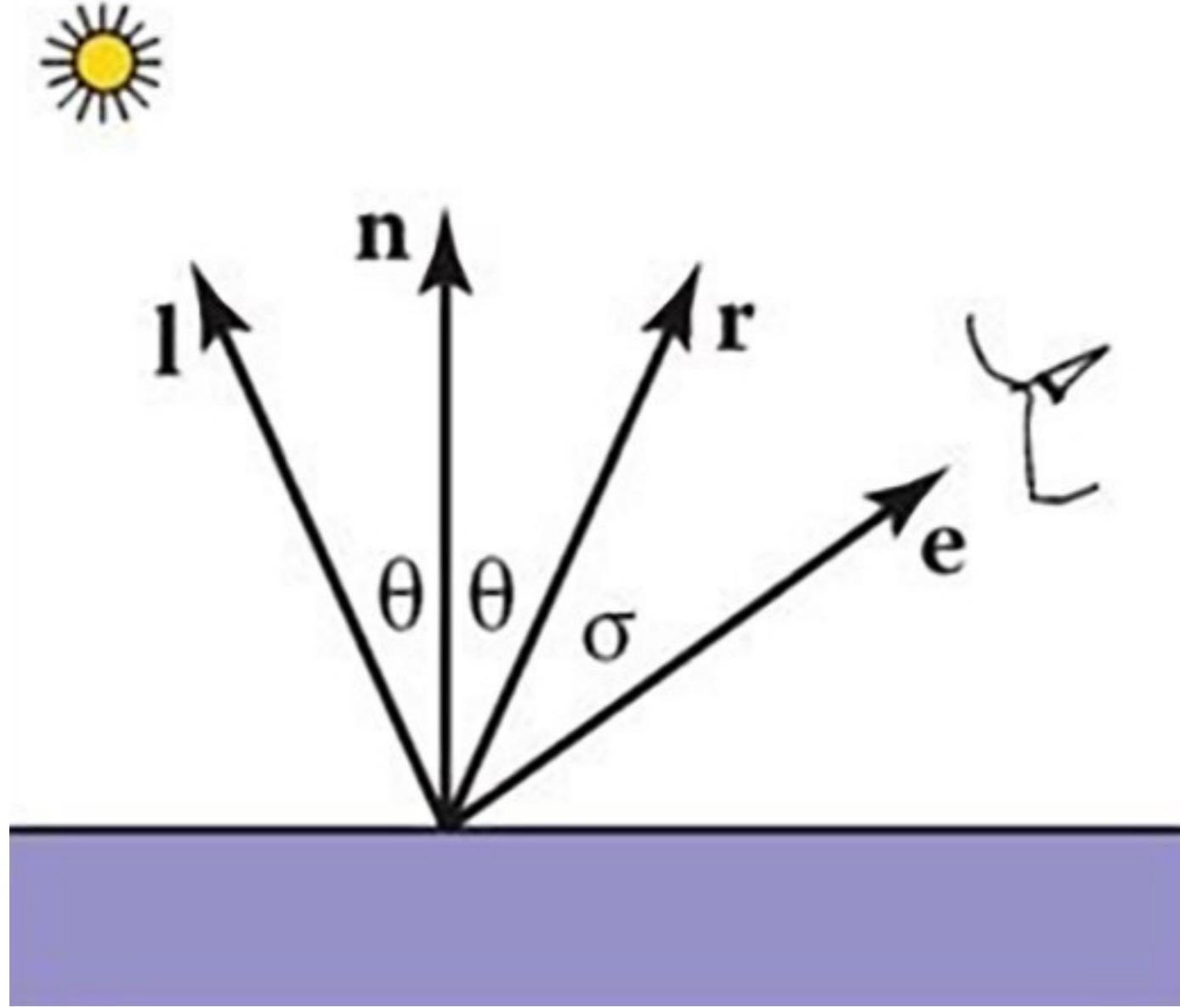
# Microfacet Geometry Model



[images from *Real-Time Rendering*, A K Peters, 2008] 26

# Phong Lighting Model

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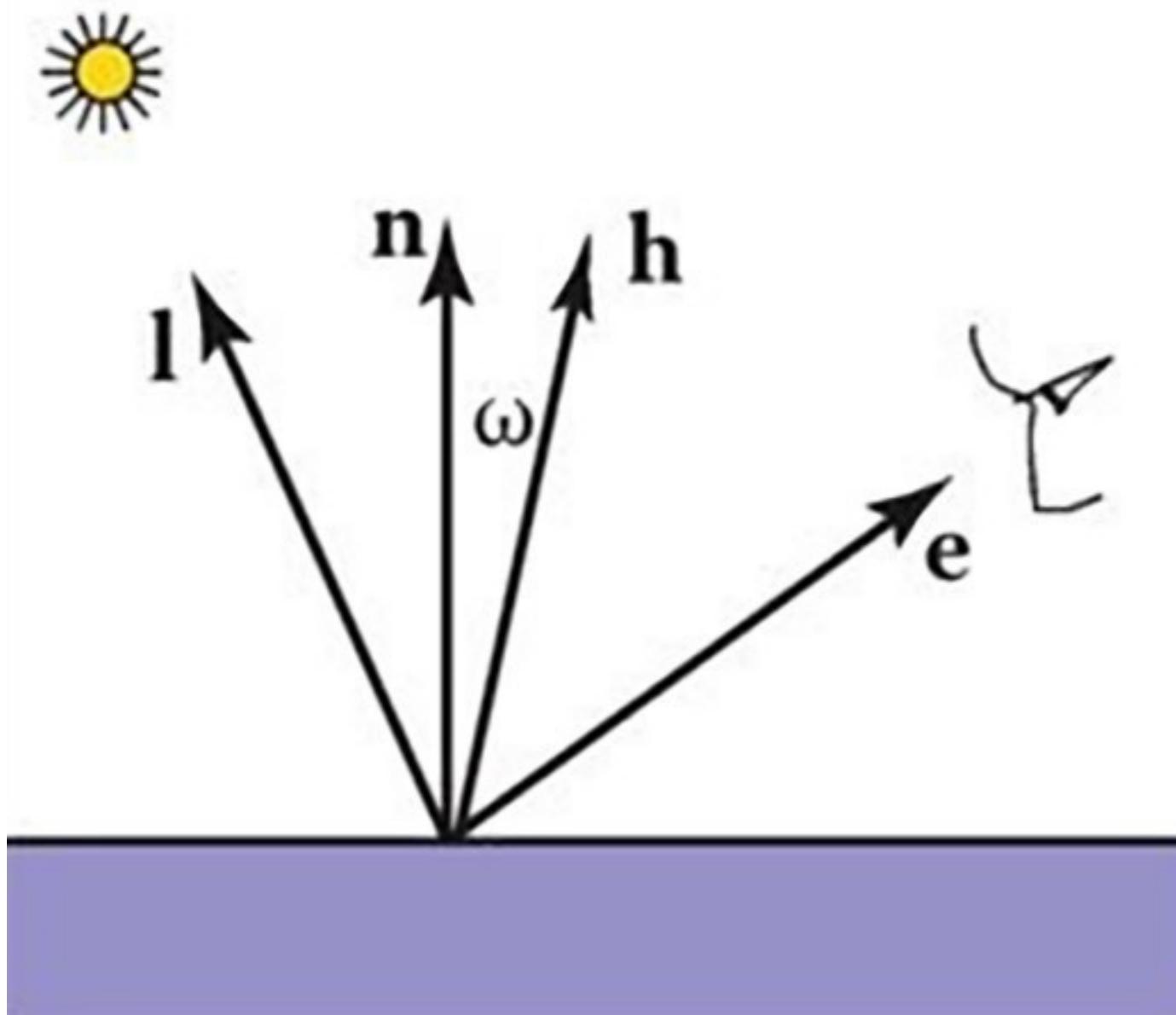


$$\mathbf{r} = -\mathbf{l} + 2(\mathbf{l} \cdot \hat{\mathbf{n}})\hat{\mathbf{n}}$$

$$c = c_l \max(0, \hat{\mathbf{e}} \cdot \hat{\mathbf{r}})^p$$

# Blinn-Phong Lighting Model

---



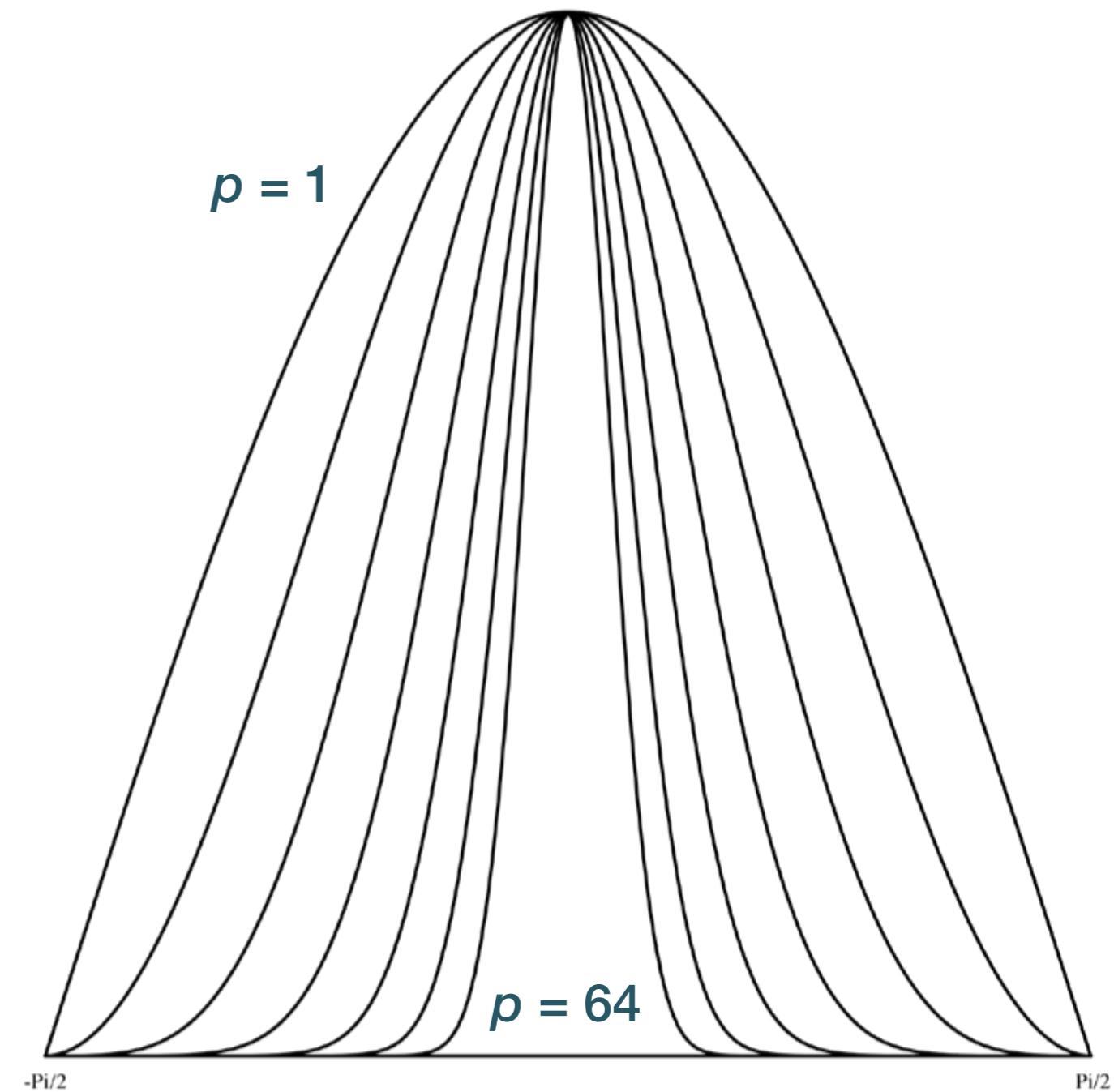
$$\hat{\mathbf{h}} = \frac{\mathbf{e} + \mathbf{l}}{||\mathbf{e} + \mathbf{l}||}$$

$$c = c_l \max(0, \hat{\mathbf{h}} \cdot \hat{\mathbf{n}})^p$$

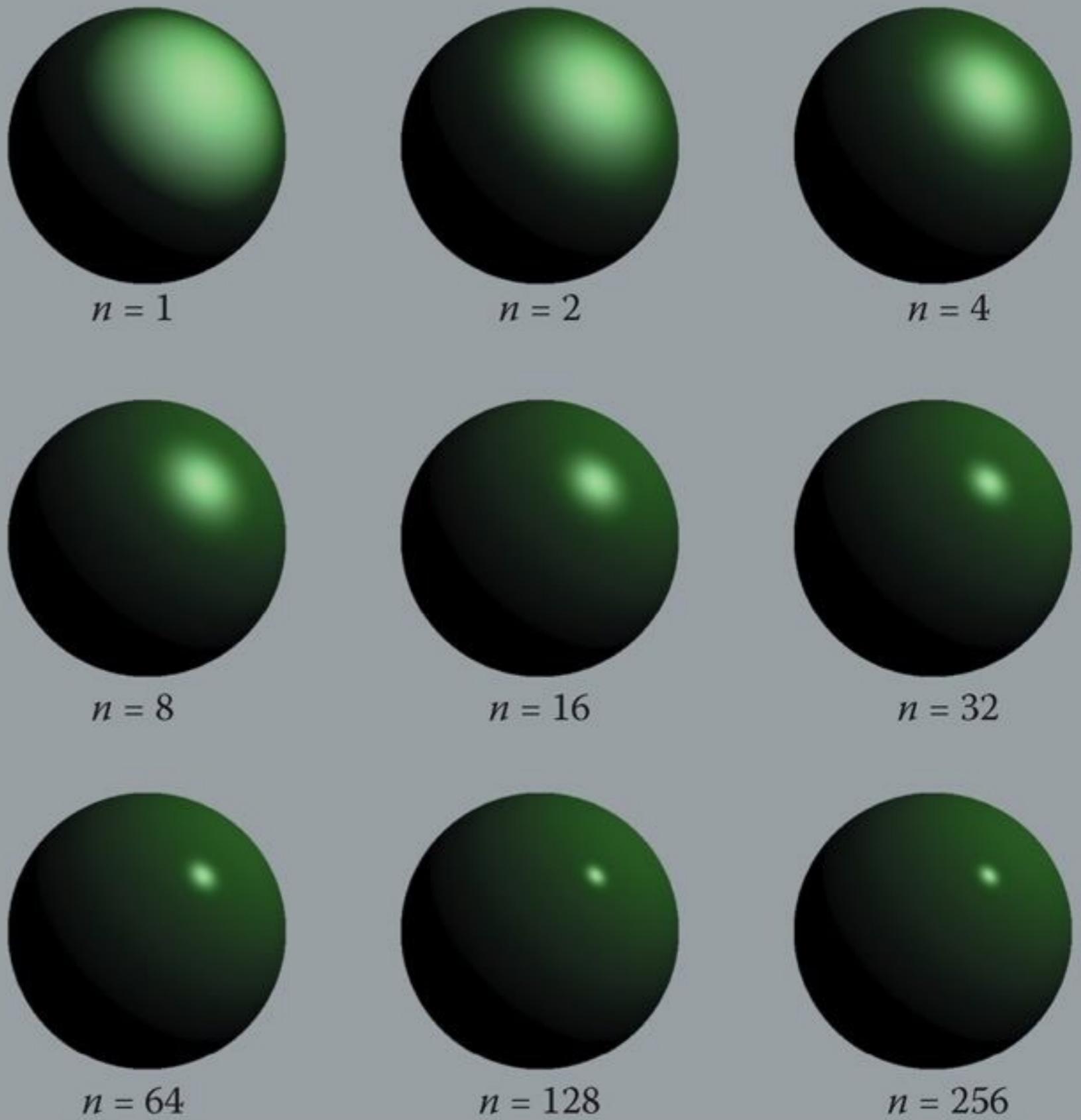
# The Phong Exponent

---

$$y = \cos^p \theta$$



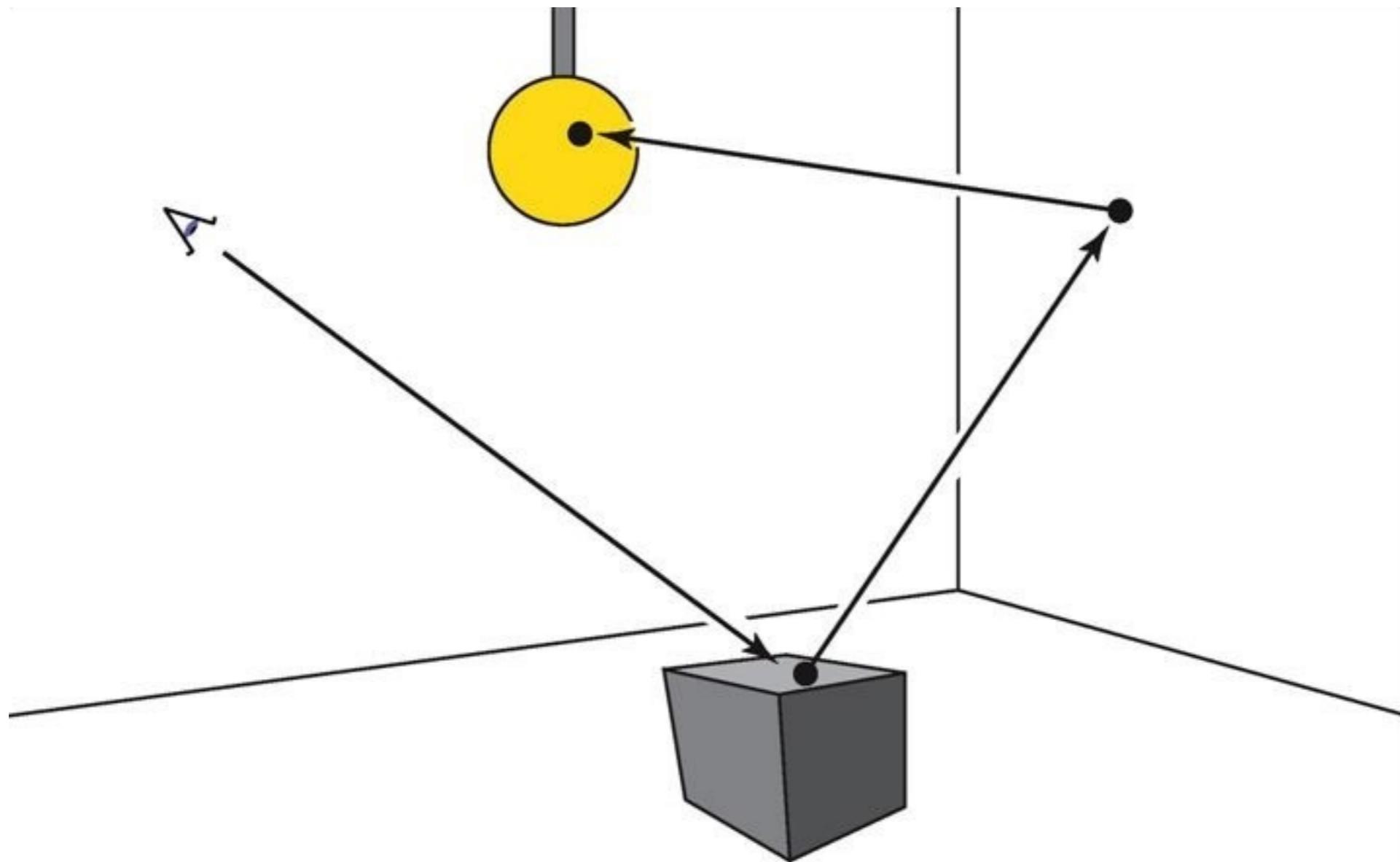
# Phong Highlights



What about  
ambient light?

# Indirect Lighting

---



Material reflection works both ways!

# Global Illumination

---



indirect

direct

combined

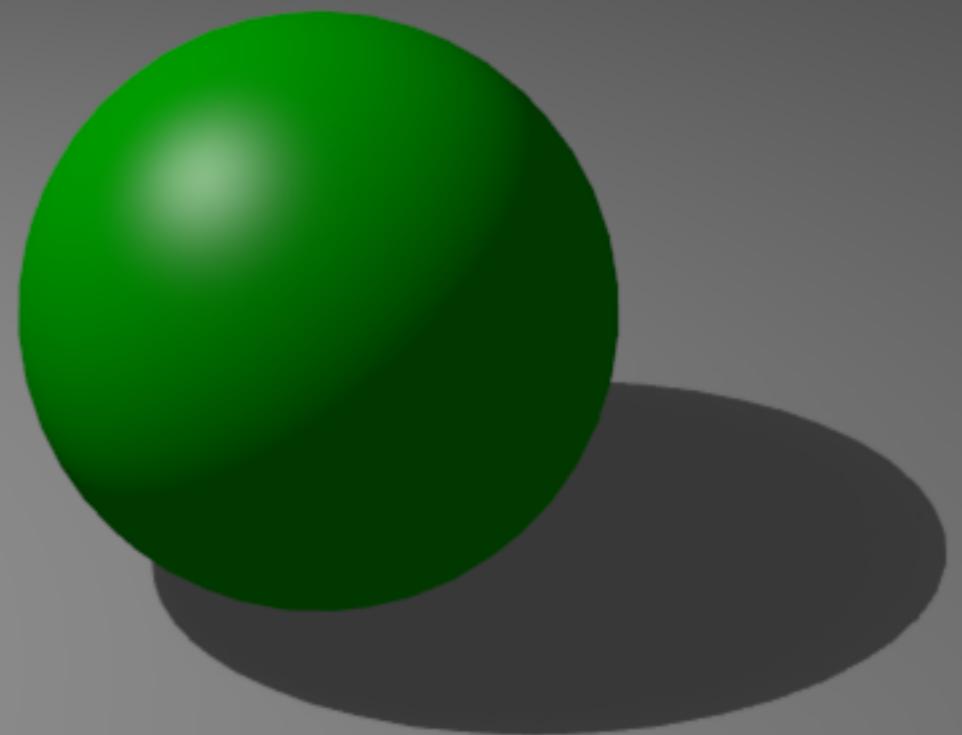
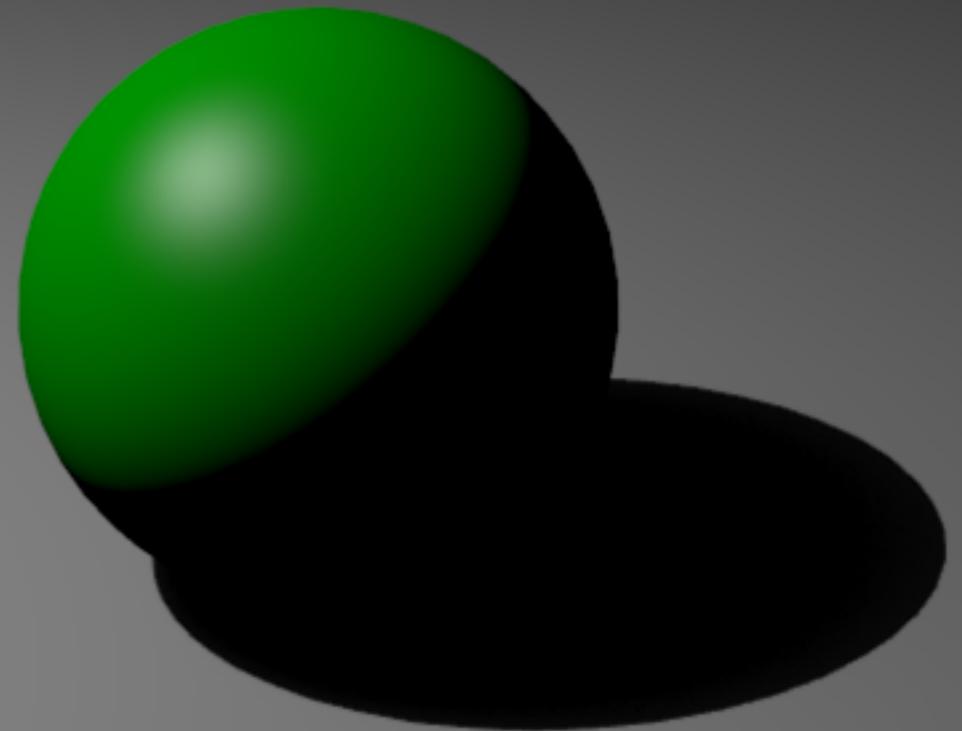
**Global illumination is really hard and expensive to compute!**

# Ambient Light

---

Approximated by a constant light source that represents the average indirect light energy in the scene.

$$c = c_r c_a$$



# Our final heuristic shading equation...

---

- with ambient, diffuse, and specular terms:

$$c = c_r \left( c_a + c_l \max(0, \hat{\mathbf{n}} \cdot \hat{\mathbf{l}}) \right) + c_l c_p \left( \hat{\mathbf{h}} \cdot \hat{\mathbf{n}} \right)^p$$

- $c_r$  is reflectance (diffuse) colour of material
- $c_p$  is specular colour of material
- $p$  is Phong exponent, or shininess of material
- $c_l$  is light source intensity (colour)
- $c_a$  is ambient light intensity (colour)

**What kinds of materials  
can't we model?**

# A Glass of Milk

---

Would you drink it?

[image courtesy of P. Hanrahan]



# Subsurface Scattering

---



skim milk



whole milk



diffuse “milk”?

[images courtesy of P. Hanrahan, Stanford University] 38

# Subsurface Scattering

---



surface only



translucent skin

[images courtesy of P. Hanrahan, Stanford University] 39

# Other biological materials?

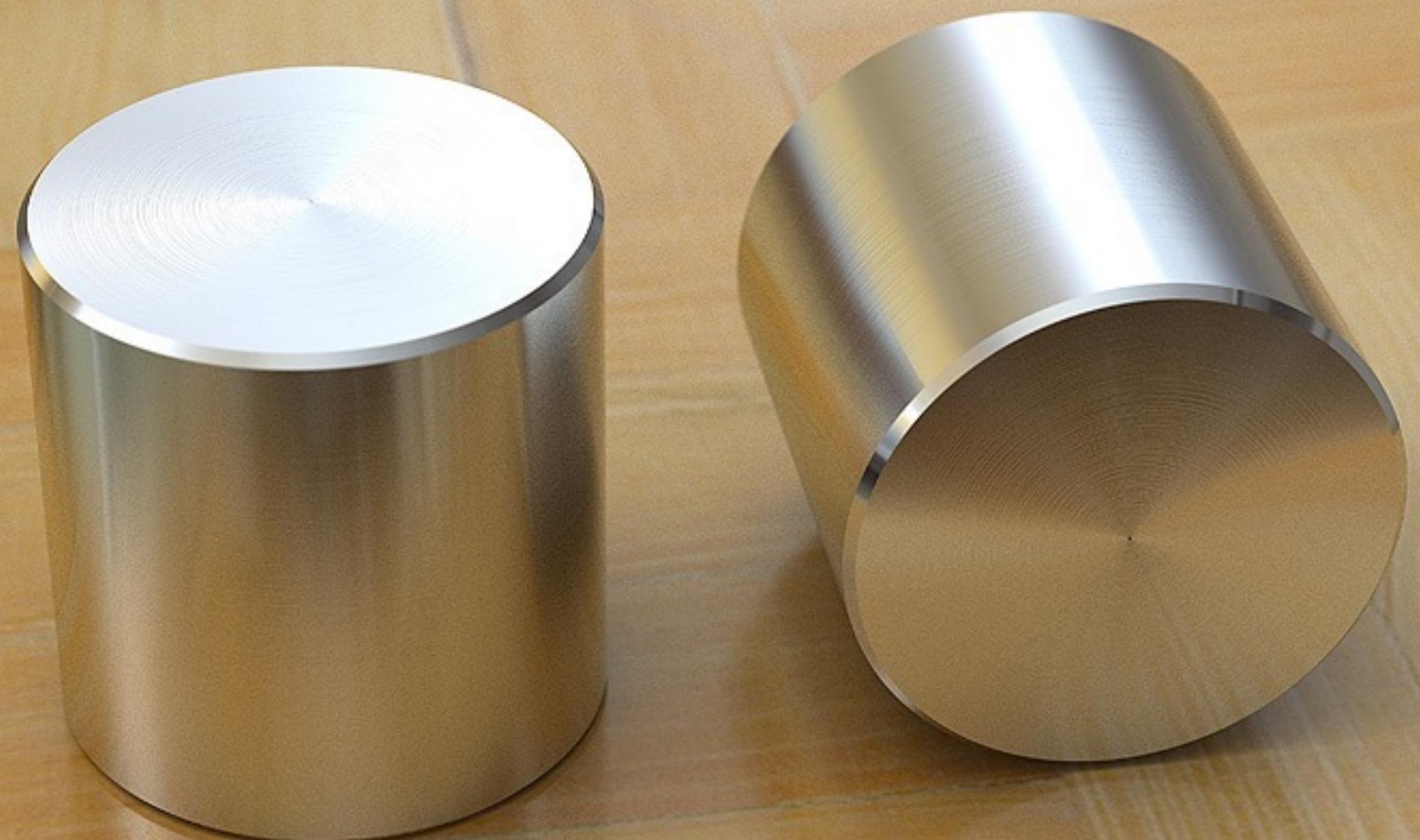
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real hair



shaded “hair”?





[from [blendernation.com](http://blendernation.com)]



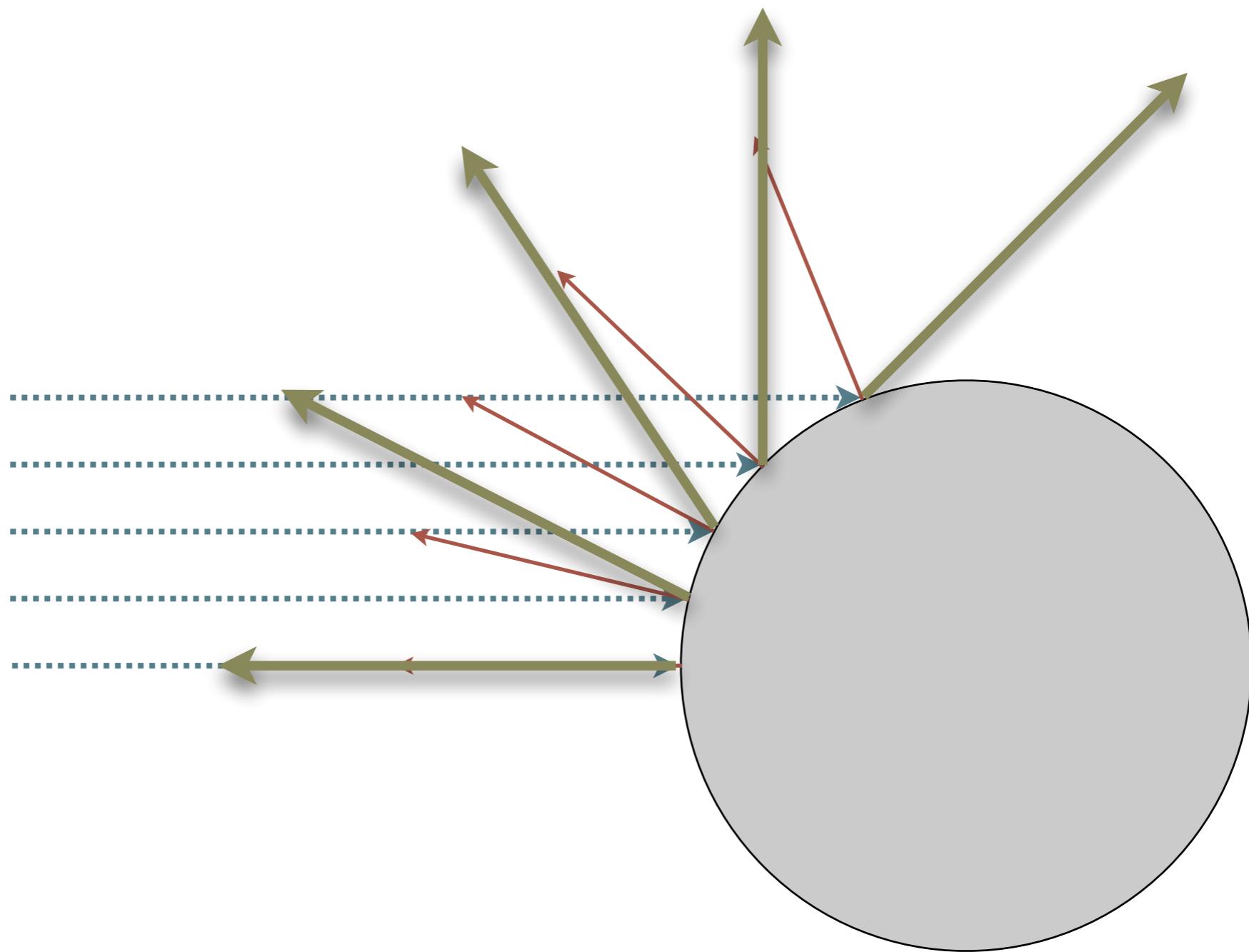
# Environment Maps

A bonus topic...

**How much can you see on this  
mirrored sphere?**

# Side View

---



# Indexing the Image

If you need a reflection over normal

$$\hat{\mathbf{n}} = (x_n, y_n, z_n),$$

read the image at

$$(x_n, y_n).$$



# Early Reflectance Map Rendering

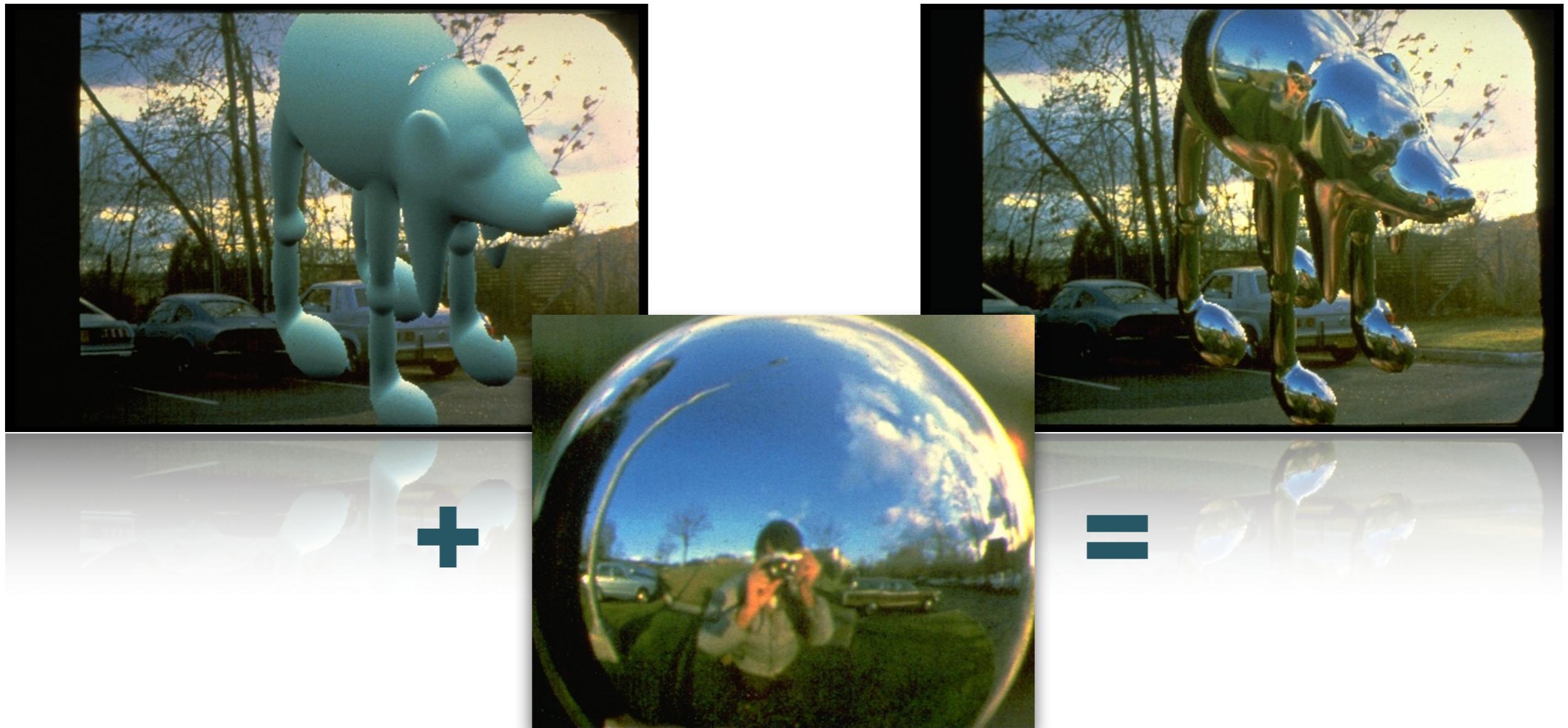
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Gene Miller, MAGI SynthaVision, 1982

# Early Reflectance Map Rendering

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[images from [pauldebevec.com](http://pauldebevec.com)] 48



Terminator 2: Judgement Day

TriStar Pictures, 1991





Gran Turismo 6

Sony Computer Entertainment

# Things to Remember

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- The appearance of a material is determined by the manner in which light is reflected from it
- The Phong lighting equation approximates material colour, diffuse and specular reflection, and ambient light
- Ideal specular reflection and refraction are relatively easy to achieve with ray tracing
- Environment mapping is a simple way to give reflective materials a realistic rendered appearance