

Last Name Instructor solution First Name _____ ID _____

ENGG 201 – WINTER 2017 – QUIZ (January 31, 2017)

Total marks: 60

Time allowed: 60 minutes

- Closed book, closed notes
- Schulich calculators only
- Show all work, and box the final answer

Question 1

PART A

In distillation column, vapour and liquid are contacted for separation of a mixture. The velocity of small liquid droplets carried-up by vapour jets is given by the following equation:

$$\rho_L \left(\frac{\pi d^3}{6} \right) g - \rho_V \left(\frac{\pi d^3}{6} \right) g = C_D \left(\frac{\pi d^2}{4} \right) \frac{u^2}{2} \rho_V \quad \dots (1)$$

A capacity parameter is defined in the following manner

$$C = \left(\frac{4dg}{3C_D} \right)^{1/2} \quad \dots (2)$$

where, ρ_L = Density of liquid

d = Diameter of liquid droplet

ρ_V = Density of vapour

u = Velocity of liquid droplet

g = Gravitational acceleration

C_D = Drag coefficient

C = Capacity parameter

(i) Determine the dimensions of drag coefficient (/4)

Each additive term has same dimensions.

$$\left[C_D \frac{\pi d^2}{4} \frac{u^2}{2} \rho_V \right] = \left[\rho_V \frac{\pi d^3}{6} g \right]$$

$$\Rightarrow [C_D u^2] = [dg]$$

$$\Rightarrow [C_D] = \left[\frac{dg}{u^2} \right] = \left[\frac{L \cdot \frac{L}{t^2}}{L^2} \right] = [1] , \boxed{C_D \text{ is dimensionless.}}$$

(ii) Determine the dimensions of capacity parameter (C) in terms of fundamental dimensions. Also give its typical units. (/4)

$$[C] = \left[\left(\frac{dg}{C_D} \right)^{1/2} \right] = [dg]^{1/2} = \left[\left(L \cdot \frac{L}{t^2} \right)^{1/2} \right] = \left[\frac{L}{t} \right] = \boxed{[L][t]^{-1}}$$

PART B

(iii) Determine the dimensions of thermal diffusivity in terms of fundamental dimensions from the following heat transfer equation. (/3)

$$\frac{1}{r} \frac{\partial}{\partial r} \left(r \frac{\partial T}{\partial r} \right) = \frac{1}{\alpha} \frac{\partial T}{\partial t}$$

Where,

T = Temperature

t = Time

r = Radial distance

α = Thermal diffusivity

$$\left[\frac{1}{L} \cdot \frac{1}{L} \cdot L \cdot \frac{T}{L} \right] = \left[\frac{1}{\alpha} \cdot \frac{T}{t} \right]$$

$$\Rightarrow \left[\frac{1}{L^2} \right] = \left[\frac{1}{t \alpha} \right]$$

$$\Rightarrow [t \alpha] = [L^2]$$

$$\Rightarrow [\alpha] = [L]^2 [t]^{-1}$$

(iv) If the following quantity is dimensionless, determine the dimensions of the quantity k in terms of fundamental dimensions. (/3)

$$k \left(\frac{\rho}{\mu g} \right)^{1/3}$$

Where,

ρ = Density

g = Gravitational acceleration

μ = Viscosity $\left(\frac{kg}{m.s} \right)$

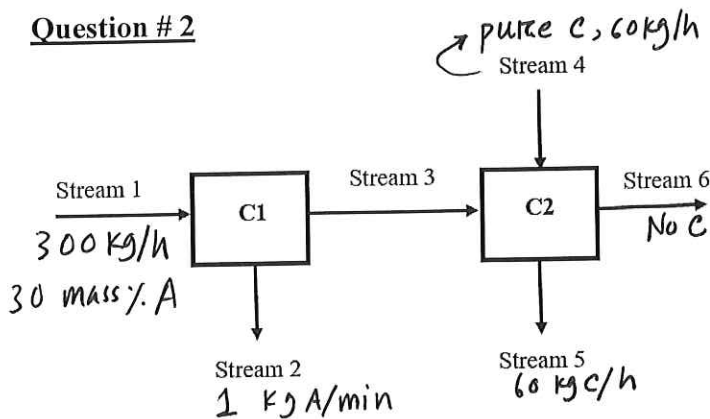
$$\left[k \left(\frac{\rho}{\mu g} \right)^{1/3} \right] = [1]$$

$$\Rightarrow [k] = \left[\left(\frac{\mu g}{\rho} \right)^{1/3} \right]$$

$$= \left[\left(\frac{M}{L \cdot t} \cdot \frac{L}{t^2} \cdot \frac{L^3}{M} \right)^{1/3} \right]$$

$$= \left[\frac{L}{t} \right]$$

$$= [L] [t]^{-1}$$

Question # 2

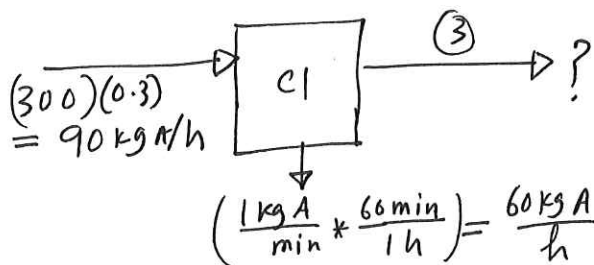
The schematic of a steady-state separation process, for the separation of a gas mixture of components A and B, is shown to the left. Stream 1, which contains 30 mass percent component A, with the balance being component B, is fed to a cooler (C1) at a rate of 300 kg/h. Pure Component A leaves the cooler (C1) as liquid condensate via Stream 2 at a rate of 1 kg/min. Stream 3 is sent to an extraction column (C2). Stream 4 which contains a pure component C also enters into the extraction

column (C2) at a rate of 60 kg/h. Stream 5 contains 25 mass percent A, and the balance C. Stream 6 contains no C.

(i) Determine the mass flow rate (kg/h) of component B in stream 1 (1/2)

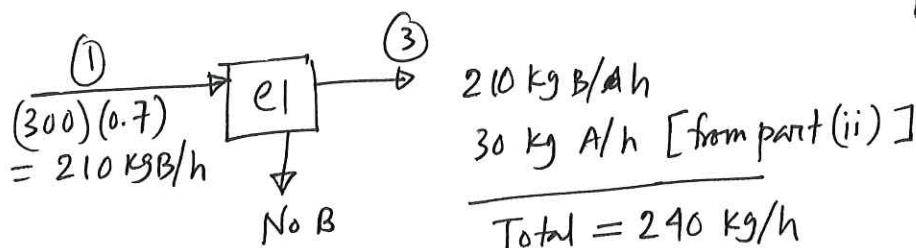
$$(300 \frac{\text{kg}}{\text{h}})(70\%) = (300 \frac{\text{kg}}{\text{h}})(0.7) = \boxed{210 \text{ kg B/h}}$$

(ii) Calculate the mass flow rate (kg/h) of component A in stream 3. (1/2)



$$\text{Flow rate of A in (3)} = 90 - 60 = \boxed{30 \frac{\text{kg A}}{\text{h}}}$$

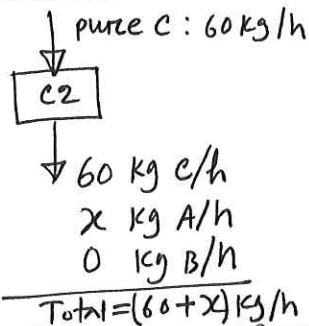
(iii) Calculate the mass fraction of component B in stream 3. (1/2)



$$B \text{ in (1)} = B \text{ in (3)}$$

$$\text{Mass fraction of B} = \frac{210 \text{ kg B/h}}{240 \text{ kg total/h}} = \frac{7}{8} = \boxed{0.875}$$

(iv) Calculate the total mass flow rate (kg/h) of stream 5. (/4)



$$25\% = 0.25 = \frac{x}{60+x}$$

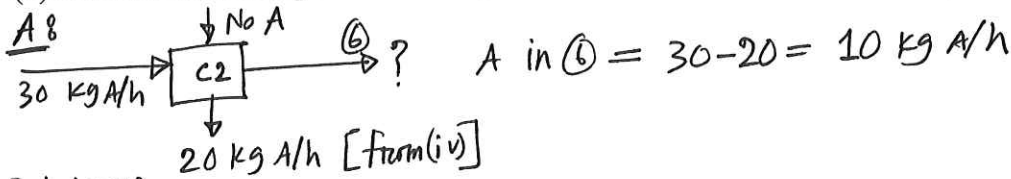
$$\Rightarrow 15 + 0.25x = x \Rightarrow 15 = 0.75x$$

$$\Rightarrow \boxed{x = 20 \text{ kg/h}}$$

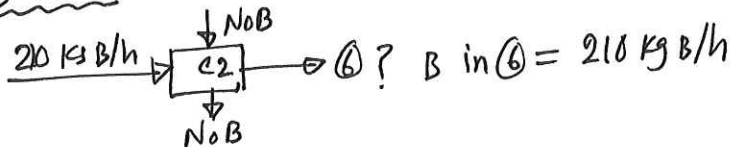
Alternatively: $\frac{x}{60} = \frac{25\%}{75\%} = \frac{1}{3}$

$$\Rightarrow \boxed{x = 20 \text{ kg A/h}}$$

(v) Calculate the mass percent of component A in stream 6. (/4)



B balance:



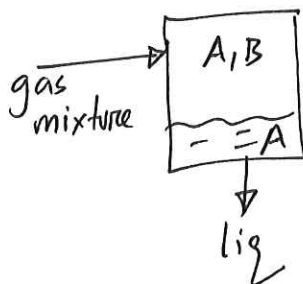
$$\text{Total } 6 = 10 + 210 = 220 \text{ kg total/h}$$

$$\text{Mass\% A} = \frac{10 \text{ kg/h}}{220 \text{ kg/h}} \times 100\% = \boxed{4.545\%}$$

(vi) Calculate the molar flow rate (in mol /min) of stream 4. The molar mass of component C is 18 kg/kmol. (/2)

$$\frac{60 \text{ kg}}{\text{h}} \times \frac{1 \text{ h}}{60 \text{ min}} \times \frac{\text{kmol}}{18 \text{ kg}} \times \frac{10^3 \text{ mol}}{1 \text{ kmol}} = \boxed{55.56 \frac{\text{mol}}{\text{min}}}$$

(vii) Calculate the degree of freedom in the cooler (C1) assuming the phases present in the cooler are in equilibrium. (/2)



$$C = 2$$

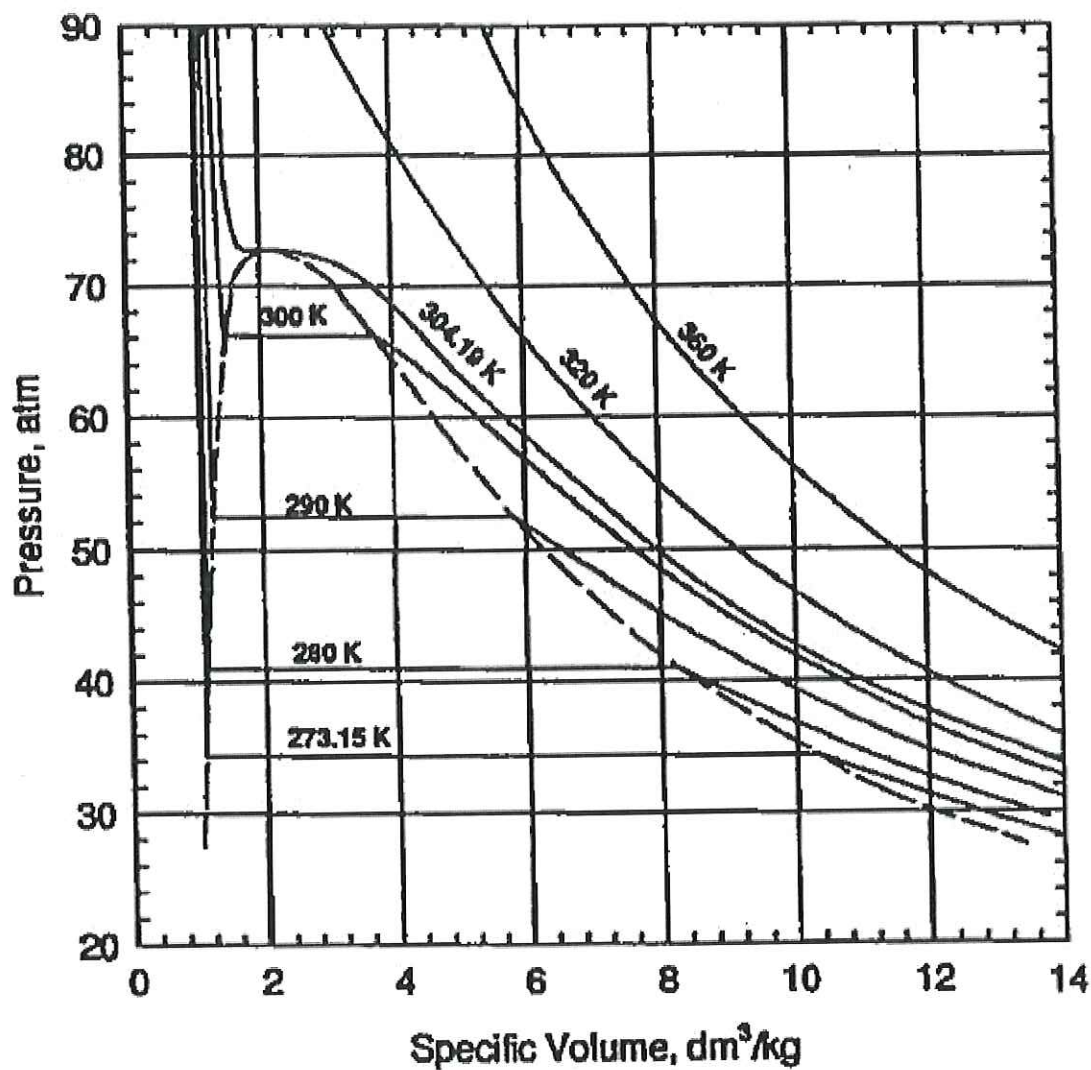
$$P = 2$$

$$F = 2 + C - P = 2 + 2 - 2 = 2$$

$$\boxed{F = 2}$$

Question 3

Use the phase diagram for the vapour-liquid region of CO₂ to answer the following questions. Show all your work for full marks.



Pressure - Volume Diagram for CO₂

PART A (/10)

(i) What is the critical temperature of CO₂. (1)

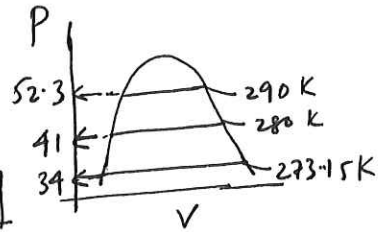
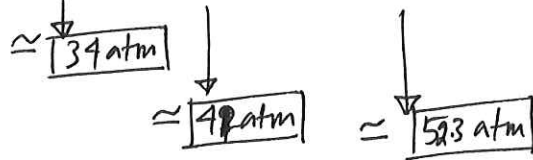
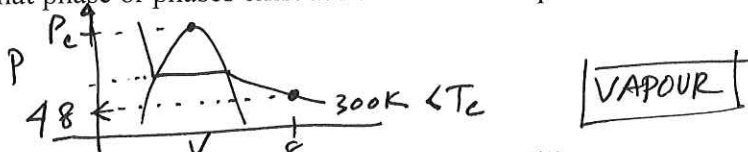
$$\boxed{304.19 \text{ K}}$$

(ii) At critical conditions, what is the volume of 2 kg carbon dioxide? (/2)

$$\left(2 \cdot 1 \frac{\text{dm}^3}{\text{kg}}\right) (2 \text{ kg}) \simeq \boxed{4.2 \text{ dm}^3} \pm \text{error in reading graph.}$$

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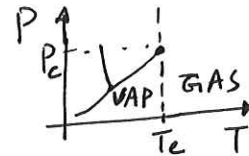
(iii) Estimate the vapor pressure of CO₂ at 273.15 K, 280 K, and at 290 K. (/3)(iv) What phase or phases exist at 300 K and at a specific volume of 8 dm³/kg? (/2)

(v) What is the equilibrium pressure in part (iv)? (/1)

$$\approx \boxed{48 \text{ atm}}$$

(vi) What phase or phases exist at 360 K and at 60 atm? (/1)

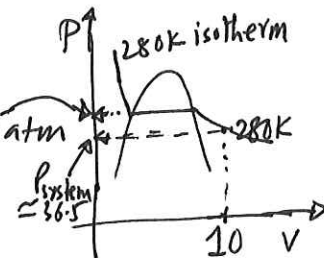
$$\cancel{360} \quad 360 > T_c \quad 60 < P_c \Rightarrow \boxed{\text{GAS}}$$

**PART B (/18)**(vii) Is the pressure of the system at the following conditions ($T = 280 \text{ K}$, specific volume = $10 \text{ dm}^3/\text{kg}$) greater or less or equal to the vapor pressure of CO₂ at 280 K? (/4)

$$T = 280 \text{ K}, V = 10 \text{ dm}^3/\text{kg} \Rightarrow P_{\text{sys}} \approx 36.5 \text{ atm}$$

$$\text{VAPOUR pressure of CO}_2 \text{ at } 280 \text{ K} \Rightarrow P_{\text{vap}} \approx 41.5 \text{ atm}$$

$$\boxed{P_{\text{system}} \text{ is LESS than } P_{\text{vap}}}$$

(viii) A rigid container of volume 600 dm³ contains 100 kg of CO₂ at a temperature of 280 K. Determine how much CO₂ (kg) would have to be added or removed to the container at the same temperature so that the specific volume of CO₂ become equal to the bubble point specific volume at 280 K? (/4)

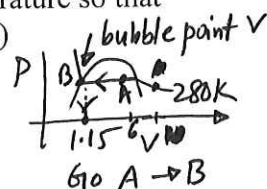
$$\text{Bubble point specific volume at } 280 \text{ K} \approx 1.15 \text{ dm}^3/\text{kg}$$

$$(1.15 \frac{\text{dm}^3}{\text{kg}}) * (m_{\text{new}} \text{ kg}) = 600 \text{ dm}^3 \quad [mV = v]$$

$$\Rightarrow m_{\text{new}} = \frac{600}{1.15} = 522 \text{ kg} > 100 \text{ kg}$$

$$\text{So, } \boxed{422 \text{ kg have to be added.}}$$

[± error reading graph]



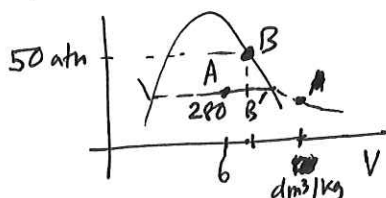
(ix) Another rigid container of volume 600 dm^3 contains 100 kg of CO_2 at a temperature of 280 K . Determine how much CO_2 (kg) would have to be added or removed to the container so that the specific volume of CO_2 become equal to the dew point specific volume at 50 atm ? (4)

Dew point specific volume at $50 \text{ atm} \approx 6.3 \text{ dm}^3/\text{kg}$
 Then, $(6.3 \frac{\text{dm}^3}{\text{kg}}) * (m_{\text{new}} \text{ kg}) = 600 \text{ dm}^3$ [\pm error in reading graph]

$$\Rightarrow m_{\text{new}} = 600/6.3 \approx 95.2 \text{ kg} < 100 \text{ kg}$$

So, $100 - 95.2 \approx 4.8 \text{ kg}$ have to be REMOVED

point A \rightarrow B'



(x) A separate variable-volume container contains 100 kg of CO_2 . The volume of the container is adjusted isothermally at 300 K and the substance is allowed to reach equilibrium. The density of the substance at equilibrium is 0.167 kg/dm^3 . What is the internal volume of the container at these conditions? (2)

$$V = \frac{1}{\rho} = \frac{1}{0.167 \text{ kg/dm}^3} = 5.988 \text{ dm}^3/\text{kg}$$

$$V = mV = (100 \text{ kg}) (5.988 \frac{\text{dm}^3}{\text{kg}}) = 598.8 \text{ dm}^3$$

(xi) Following part (x) the temperature of the container is brought to 273.15 K . What is the specific volume of each phase present inside the container at these new conditions at equilibrium? (4)

part (x) : $V = 5.988 \text{ dm}^3/\text{kg}$, $T = 300 \text{ K}$, $P \approx 57 \text{ atm}$

solution #1: Go to 273.15 K isobarically. New conditions: $T = 273.15$, $P \approx 57 \text{ atm}$

Then, only liquid is present, $V_{\text{liq}} \approx 0.9 \text{ dm}^3/\text{kg}$

Alternatively,

solution #2: Go to 273.15 K keeping specific volume constant.
 New conditions: $T = 273.15 \text{ K}$, $V = 5.988 \text{ dm}^3/\text{kg}$

Then, both liquid and vapour are present, with

$$\begin{aligned} V_{\text{liq}} &\approx 1 \text{ dm}^3/\text{kg} \\ V_{\text{vap}} &\approx 10.2 \text{ dm}^3/\text{kg} \end{aligned}$$

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Question	Total Marks	Marks Obtained
1	14	
2	18	
3	28	