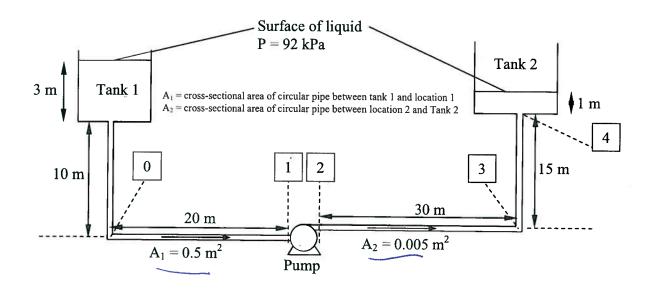
Question Number IV (22 Marks ~ 40 minutes)

PART A

A pumping station is displayed in the following Figure.



The mass flow rate through the system is 1320 kg/h. The density and viscosity of the liquid are 980 kg/m³ and 1.2 mPa s, respectively. The pipes can be treated as rough commercial steel.

a) Is the flow laminar or turbulent at location 1? (2) $M = \rho Q \rightarrow Q = \frac{M}{\rho} = \frac{1320 \text{ ks/h}}{480 \text{ ks/m}^3} = 1.347 \frac{\text{m}^3}{\text{h}} \times \frac{1 \text{h}}{36005} = 3.74 \times 10^{-4} \frac{\text{m}^3}{5}$

 $Q = UA \rightarrow \overline{U} = \frac{Q}{A} = \frac{3.74 \times 10^{-4} \text{m}^3/\text{s}}{0.5 \text{ m}^2} = 7.48 \times 10^{-4} \text{m/s} \qquad \text{Re} = \frac{DUP}{1.2 \times 10^{-3}} = \frac{(0.7979 \text{m})(7.48 \times 10^{-3})}{1.2 \times 10^{-3}}$ b) At location 1, what is the maximum velocity in the circular pipe?

Unax = \overline{U} \rightarrow \text{Umax} = \overline{U} \rightarrow \text{Umax} = \overline{U} \rightarrow \text{Umax} = \overline{U} \rightarrow \text{Umax} \left\ \text{Umax} \rightarrow \text{Umax} \left\ \text{Umax} \right\ \text{Umax} \ri

c) Is the flow laminar or turbulent at location 2?(/2)

- D location 2 - D Q = Qpipe1 = 3.74x10-4m3/s

 $\overline{V}_2 = \frac{Q}{A} = \frac{3.74 \times 10^{-4} \text{m}^3 \text{/s}}{0.005 \text{m}^2} = 0.0748 \text{m/s}$ $A = \frac{\pi}{4} D^2 - D = \int_{\overline{\pi}}^{4A} = 0.07979 \text{m}$

Re = Dop = 0.07979 x 0.0748 x 980 112 x 10-3 = 4874 Turbulent continued... **Question Number IV** (Continued)

d) What is the pressure at location (1?) (3)

section #1 - pressure @ bottom of Touk! = 92000 Pn + (980)(3)(9.81)

LAMINAR FLOW (bottom of Touk! to []) = 120841 Pa

$$-\left(\frac{\Delta P}{L} + PS \frac{\Delta h}{L}\right) = \frac{32 n \bar{\nu}}{D^2} \qquad \Delta h = 0 - 10 m$$

$$\Delta P = P_1 - 120841 Pa$$

$$-\left[\frac{\Delta P}{30} + 980 \times 9.81 \left(\frac{-10}{30}\right)\right] = 32 \times 1.2 \times 10^{-3} \times 7.48 \times 10^{-4} = 4.51166 \times 10^{-5}$$

$$\Delta P + 980 \times 9.81 \times (-10) = 1.35 \times 10^{-3}$$

 96138
 $\Delta P = 96137.99865 = P_1 - 120841$

- P, = Z16978.9986 Pa (216.98 Wa)
- e) What is the pressure at location (2) (14)

 section #2 -> pressur @ bottom of Tank Z = 92000 Pa + 980x 1x9.81

TURBULENT FLOW (bottom of Tout 2 to (2)) = 101613.8 Pa = P4

$$-\left[\frac{\Delta P}{45} + 980x9.81\frac{15}{45}\right] = \frac{2 \times 0.012 \times (0.0748 \, \text{m/s})^2 \times 980}{0.07979} = 1.649$$

$$\frac{DP}{RR} + 980 \times 9.81 \times 15 = -74.217$$

$$\frac{DP}{P} = -144132 Pa = 101613.8 - P_2$$

$$\boxed{P_2 = 245746.6 Pa}$$

f) What is the power of the pump? (/2)

Question Number IV (Continued)

PART B - In a bearing, the gap between the moving surface and a stationary surface is 0.05 mm. The lubrication liquid is at 80°C and has density equal to 870 kg/m³ and viscosity equal to 140 cP. The moving surface slides past the stationary one at 0.778 m/s. The contact area between the surfaces is 0.78 cm².

a) If the flow is laminar between the two surfaces, what is the shear stress exerted by the steel part on the liquid in the gap? (/2)

b) What is the force applied to the steel part to keep it in motion? (/2)

$$T = \frac{F}{A}$$
 $A = 0.78 \text{ m}^2 \times \left(\frac{1 \text{ m}}{100 \text{ cm}}\right)^2 = 7.8 \times 10^{-5} \text{ m}^2$
 $F = TA = \left(2178.4 \text{ Pn}\right) \left(7.8 \times 10^{-5} \text{ m}^2\right) = 0.1699 \text{ N}$

c) The lubricant is mixed with another liquid. Viscometer tests of the liquid mixture yield the following data:

T	90(30
Shear Stress, Pa	Shear Rate, s ⁻¹
510.29	10.9
1370.23	38.7

46.82 Pus 35.41 Pus

i. Does this liquid exhibit power-law behaviour? (/1)

ii. What is the apparent viscosity at a shear rate of 20 s⁻¹? (/3)