

FORMULA SHEET

Constants / Conversions

$$R = 8.314 \frac{\text{kJ} \cdot \text{mol}^{-1} \cdot \text{K}^{-1}}{\text{mol} \cdot \text{K}} = 8.314 \frac{\text{J}}{\text{mol} \cdot \text{K}} \quad N_A = 6.023 \times 10^{23} \frac{\text{molecules}}{\text{mol}} \quad g = 9.81 \text{ m/s}^2$$

$$R = 0.08205 \frac{\text{atm} \cdot \text{m}^3}{\text{mol} \cdot \text{K}} \quad k = \frac{R}{N_A} = 1.3805 \times 10^{-23} \text{ J / K} \quad 1 \text{ cP} = 10^{-3} \text{ Pa} \cdot \text{s}$$

$$101.325 \text{ kPa} = 1 \text{ atm} \quad 1 \text{ bar} = 100 \text{ kPa} \quad 1 \text{ L} = 1000 \text{ cm}^3 = 1000 \text{ mL} = 0.001 \text{ m}^3$$

$$760 \text{ mmHg} = 1 \text{ atm} \quad 1 \text{ inch} = 2.54 \text{ cm}$$

Phase Rule

$$F = C - P + 2$$

Two-Point Interpolation

$$y = y_1 + \frac{(y_2 - y_1)}{(x_2 - x_1)}(x - x_1)$$

Geometric Shapes

$$V_{\text{sphere}} = \frac{4}{3} \pi r^3$$

$$SA_{\text{sphere}} = 4 \pi r^2$$

$$V_{\text{cylinder}} = \pi r^2 h$$

Ideal Gas

$$Pv = nRT$$

Kinetic Theory of Gases

$$c_{mp} = \sqrt{\frac{2RT}{M}}$$

$$P = \frac{N_A m \bar{c}^2}{3V_m}$$

$$\lambda = \frac{1}{\sqrt{2} \pi \sigma^2 \rho_N}$$

$$\sqrt{\bar{c}^2} = \sqrt{\frac{3RT}{M}}$$

$$E_k = \frac{1}{2} m \bar{c}^2$$

$$\delta = \left[\frac{kT}{P} \right]^{1/3}$$

$$\bar{c} = \sqrt{\frac{8RT}{\pi M}}$$

$$k = \frac{R}{N_A}$$

$$\rho_N = \frac{N_A}{V_m} = \frac{P}{kT}$$

Kinetic Theory of Gases - Transport Properties

$$\mu = \frac{M}{N_A \pi \sigma^2} \sqrt{\frac{RT}{\pi M}}$$

$$\mu = \frac{\rho_N \bar{c} \lambda m}{2}$$

$$F/A = -\mu \frac{du}{dz}$$

$$\kappa = \frac{C_v}{N_A \pi \sigma^2} \sqrt{\frac{RT}{\pi M}}$$

$$\kappa = \frac{\lambda \rho_N \bar{c}}{2} \frac{C_v}{N_A}$$

$$Q/A = -\kappa \frac{dT}{dz}$$

$$D_{AA} = \frac{RT}{PN_A \pi \sigma^2} \sqrt{\frac{RT}{\pi M}}$$

$$j_A = -D \frac{dC}{dz}$$

...continued

FORMULA SHEET (continued)

$$C_v = \frac{3}{2}R$$

$$C_p = \frac{5}{2}R$$

$$C_p = C_v + R$$

van der Waals EOS

$$P = \frac{RT}{V_m - b} - \frac{a}{V_m^2}$$

$$V_m^3 - [b + \frac{RT}{P}]V_m^2 + \frac{a}{P}V_m - \frac{ab}{P} = 0$$

$$P_c = \frac{a}{27b^2}$$

$$T_c = \frac{8a}{27Rb}$$

$$V_c = 3b$$

$$a = \frac{27}{64} \frac{R^2 T_c^2}{P_c}$$

$$b = \frac{RT_c}{8P_c}$$

Mixing Rules >>> $b = \sum y_i b_i$

$$a = [\sum y_i \sqrt{a_i}]^2$$

Law of Corresponding States

$$T_r = \frac{T}{T_c} \quad P_r = \frac{P}{P_c}$$

$$PV_m = ZRT$$

Pitzer-Curl

$$Z = Z^{(0)} + \omega Z^{(1)}$$

Mixtures >>> $T_{pc} = \sum_i y_i T_{ci}, \quad P_{pc} = \sum_i y_i P_{ci} \quad \bar{\omega} = \sum_i y_i \omega_i$

Volumetric Behaviour of Liquids

$$\beta_T = -\frac{1}{V} \left(\frac{\partial V}{\partial P} \right)_T$$

$$\alpha_P = \frac{1}{V} \left(\frac{\partial V}{\partial T} \right)_P$$

$$\gamma_V = \frac{1}{P} \left(\frac{\partial P}{\partial T} \right)_V$$

$$V_T = V_{T_o} (1 + A\theta + B\theta^2 + C\theta^3)$$

Tait's Equation

$$\beta_T = \frac{c}{P + d}$$

$$\frac{V_o - V}{V_o} = c \ln \left[\frac{P + d}{d} \right]$$

Vapour-Liquid Equilibrium

Raoult's Law

$$P_{v_i} x_i = P y_i = \bar{p}_i$$

Clausius-Clapeyron

$$\frac{dP}{dT} = \frac{\Delta H_v}{T(V_g - V_l)}$$

$$\ln \left(\frac{P_2}{P_1} \right) = \frac{\Delta H_v}{R} \left(\frac{1}{T_1} - \frac{1}{T_2} \right)$$

$$\ln(P) = -\frac{A}{T} + C$$

...continued

FORMULA SHEET (continued)

Viscosity of Liquids

Newtonian

$$\tau = -\mu \frac{du}{dy}$$

Non-Newtonian

$$\mu_{app} = \frac{\tau}{\left(\frac{du}{dy}\right)}$$

Power Law

$$\tau = K \left(\frac{du}{dy}\right)^n$$

Kinematic Viscosity

$$\nu = \mu / \rho$$

Temperature Dependence

$$\ln(\mu) = -\frac{A}{T} + C$$

Flow of Fluids in Pipes

$$Re = \frac{D \bar{u} \rho}{\mu}$$

$$Q = \bar{u} A = \bar{u} \frac{\pi D^2}{4}$$

$$Power = Q \Delta P$$

Ideal (Bernoulli)

$$\frac{P}{\rho} + gh + \frac{u^2}{2} = Const.$$

$$\frac{\Delta P}{\rho} + g \Delta h + \frac{\Delta u^2}{2} = 0$$

Laminar

$$-\left[\frac{\Delta P}{L} + \rho g \frac{\Delta h}{L}\right] = \frac{32 \mu \bar{u}}{D^2}$$

Turbulent

$$-\left[\frac{\Delta P}{L} + \rho g \frac{\Delta h}{L}\right] = \frac{2 f \bar{u}^2 \rho}{D}$$

Density of Solids

$$SimpleCubicMaterials = \frac{m}{d^3}$$

$$FCC materials = \frac{\sqrt{2}m}{d^3}$$

$$BCC materials = 1.299 \frac{m}{d^3}$$

$$HCP materials = \frac{\sqrt{2}m}{d^3}$$

Lennard Jones Potential

$$\Phi(r) = 4\epsilon \left[\left(\frac{\sigma}{r}\right)^{12} - \left(\frac{\sigma}{r}\right)^6 \right]$$

$$F(r) = \frac{d\Phi(r)}{dr}$$

$$\Phi(r) = \int_{\infty}^r F(r) dr$$

$$\Phi(r) = \Phi(r)_r + \Phi(r)_a$$

$$b_o = \frac{2\pi}{3} \sigma^3 N_A$$

...continued

FORMULA SHEET (continued)

Thermal Expansion of Solids

$$\alpha_L = \frac{1}{L} \frac{dL}{dT}$$

Heat Conduction

Fourier's Law

$$Q = -\kappa A \frac{dT}{dx} = -\kappa A \frac{\Delta T}{\Delta x}$$

Composite Planar Wall

$$Q = \frac{-A \Delta T}{\left[\frac{\Delta x_1}{\kappa_1} + \frac{\Delta x_2}{\kappa_2} + \frac{\Delta x_3}{\kappa_3} + \dots \right]}$$

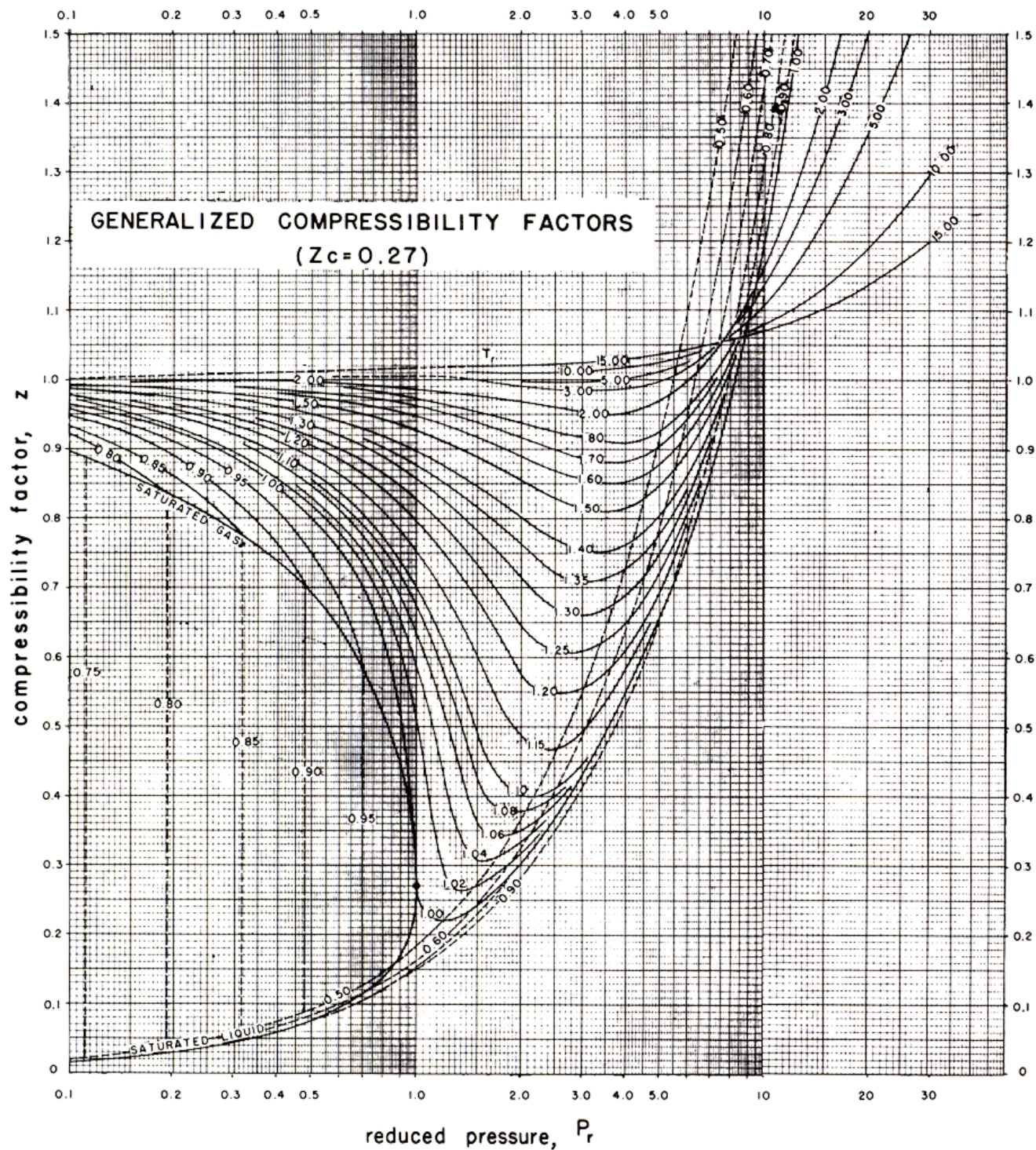
Simple Cylinder

$$Q = \frac{-2\pi\kappa L \Delta T}{\ln\left(\frac{r_2}{r_1}\right)}$$

Composite Cylinder (Pipe)

$$Q = \frac{-2\pi L \Delta T}{\frac{\ln(r_2/r_1)}{\kappa_1} + \frac{\ln(r_3/r_2)}{\kappa_2} + \frac{\ln(r_4/r_3)}{\kappa_3} + \dots}$$

GENERALIZED COMPRESSIBILITY CHART



PITZER-CURL TABLES

Table C-1
Pitzer-Curl Generalized $Z^{(0)}$

Tr	0.2	0.4	0.6	0.8	1.0	1.2	1.4	Pr 1.6	1.8	2.0	2.2	2.4	2.6	2.8	3.0
0.80	0.851	0.066	0.100	0.133	0.164	0.192	0.255	0.258	0.287	0.318	0.347	0.376	0.405	0.433	0.461
0.85	0.882	0.067	0.101	0.134	0.165	0.194	0.226	0.258	0.287	0.316	0.345	0.374	0.403	0.431	0.459
0.90	0.904	0.778	0.102	0.135	0.167	0.198	0.229	0.258	0.288	0.316	0.345	0.373	0.402	0.430	0.458
0.95	0.920	0.819	0.697	0.145	0.176	0.205	0.235	0.262	0.292	0.321	0.347	0.375	0.403	0.430	0.457
1.00	0.932	0.849	0.756	0.638	0.291	0.231	0.250	0.278	0.304	0.329	0.356	0.381	0.407	0.433	0.458
1.05	0.942	0.874	0.800	0.714	0.609	0.470	0.341	0.320	0.332	0.350	0.372	0.393	0.417	0.441	0.446
1.10	0.950	0.893	0.833	0.767	0.691	0.607	0.512	0.442	0.408	0.402	0.405	0.420	0.440	0.462	0.484
1.15	0.958	0.98	0.858	0.805	0.746	0.684	0.620	0.562	0.514	0.484	0.477	0.478	0.485	0.498	0.513
1.20	0.963	0.921	0.879	0.835	0.788	0.737	0.690	0.640	0.598	0.568	0.553	0.545	0.544	0.548	0.554
1.25	0.968	0.930	0.896	0.858	0.820	0.778	0.740	0.702	0.664	0.636	0.618	0.606	0.599	0.597	0.598
1.30	0.971	0.940	0.909	0.878	0.846	0.811	0.780	0.749	0.718	0.691	0.671	0.657	0.649	0.644	0.642
1.4	0.977	0.952	0.929	0.908	0.883	0.859	0.838	0.817	0.795	0.777	0.759	0.745	0.734	0.725	0.720
1.5	0.982	0.963	0.945	0.927	0.909	0.892	0.875	0.859	0.844	0.831	0.819	0.808	0.800	0.794	0.790
1.6	0.985	0.971	0.957	0.944	0.930	0.917	0.904	0.893	0.882	0.872	0.863	0.855	0.848	0.843	0.840
1.7	0.988	0.977	0.966	0.956	0.946	0.936	0.926	0.919	0.911	0.903	0.896	0.889	0.889	0.883	0.879
1.8	0.991	0.982	0.974	0.966	0.958	0.950	0.944	0.937	0.931	0.926	0.921	0.916	0.913	0.910	0.908
1.9	0.993	0.986	0.980	0.974	0.968	0.962	0.958	0.952	0.948	0.944	0.940	0.936	0.933	0.931	0.930
2.0	0.995	0.989	0.984	0.979	0.975	0.971	0.968	0.964	0.961	0.959	0.956	0.954	0.953	0.953	0.952

Table C-2
Pitzer-Curl Generalized $Z^{(1)}$

Tr	0.2	0.4	0.6	0.8	1.0	1.2	1.4	Pr 1.6	1.8	2.0	2.2	2.4	2.6	2.8	3.0
0.80	-0.095	-0.028	-0.044	-0.058	-0.07	-0.08	-0.10	-0.11	-0.12	-0.13	-0.14	-0.15	-0.16	-0.17	-0.18
0.85	-0.067	-0.031	-0.049	-0.064	-0.08	-0.09	-0.11	-0.12	-0.13	-0.14	-0.15	-0.16	-0.17	-0.18	-0.18
0.90	-0.042	-0.09	-0.053	-0.068	-0.085	-0.10	-0.11	-0.12	-0.13	-0.14	-0.15	-0.16	-0.17	-0.17	-0.18
0.95	-0.025	-0.050	-0.100	-0.072	-0.091	-0.10	-0.11	-0.12	-0.12	-0.13	-0.14	-0.15	-0.15	-0.16	-0.17
1.00	-0.012	-0.16	-0.20	-0.05	-0.080	-0.090	-0.099	-0.108	-0.115	-0.123	-0.13	-0.13	-0.14	-0.14	-0.15
1.05	0.000	+0.001	+0.005	+0.015	+0.02	+0.01	-0.01	-0.04	-0.06	-0.07	-0.08	-0.09	-0.10	-0.11	
1.10	+0.002	0.008	0.016	0.030	0.055	0.082	+0.11	+0.082	+0.035	0.000	-0.02	-0.03	-0.05	-0.06	-0.07
1.15	0.004	0.012	0.012	0.040	0.064	0.093	0.12	0.140	0.136	+0.100	+0.07	+0.04	+0.02	0.00	-0.01
1.20	0.009	0.018	0.028	0.044	0.069	0.10	0.13	0.16	0.17	0.17	0.16	0.14	0.12	+0.09	+0.07
1.25	0.011	0.023	0.036	0.050	0.069	0.10	0.13	0.16	0.18	0.19	0.19	0.18	0.16	0.14	0.12
1.30	0.013	0.027	0.041	0.055	0.072	0.10	0.13	0.16	0.18	0.20	0.20	0.20	0.20	0.19	0.18
1.4	0.016	0.032	0.049	0.065	0.082	0.10	0.13	0.16	0.18	0.19	0.20	0.21	0.21	0.21	0.20
1.5	0.017	0.035	0.052	0.070	0.088	0.10	0.13	0.15	0.17	0.18	0.20	0.20	0.21	0.21	0.21
1.6	0.018	0.036	0.054	0.07	0.08	0.10	0.12	0.14	0.16	0.17	0.18	0.19	0.20	0.20	0.21
1.7	0.018	0.036	0.054	0.07	0.09	0.10	0.11	0.13	0.15	0.16	0.17	0.18	0.19	0.20	0.21
1.8	0.018	0.036	0.054	0.07	0.09	0.10	0.11	0.13	0.15	0.16	0.17	0.18	0.19	0.20	0.21
1.9	0.018	0.035	0.05	0.07	0.09	0.10	0.11	0.13	0.15	0.16	0.17	0.18	0.19	0.20	0.21
2.0	0.016	0.031	0.05	0.07	0.08	0.10	0.11	0.13	0.14	0.15	0.16	0.17	0.19	0.20	0.21

FRICTION FACTOR CHART

