

$V = 100 \text{ m}^3$ n_2 $P = 10 \text{ MPa}$ $T = 65^\circ\text{C}$ (condition 1)

condition 2: $V = 100 \text{ m}^3$ n_2 $P = 18 \text{ MPa}$ $T = 85^\circ\text{C} = 358.15 \text{ K}$
 calculate mass of nitrogen added to tank

a) IGL: $n_1 = \frac{PV}{RT} = \frac{(10,000 \text{ kPa})(100 \text{ m}^3)}{(8.314)(338.15 \text{ K})}$

$n_1 = 355.7 \text{ kmoles}$

$n_2 = \frac{(18,000)(100 \text{ m}^3)}{8.314(358.15)} = 604.5$

$\Delta n = 604.5 - 355.7$

$\Delta n = 248.8 \text{ kmoles}$

$\Delta m = 248.8 \text{ kmoles} \left(\frac{28 \text{ kg}}{\text{kmol}} \right) = \underline{6966 \text{ kg}}$

c) vDW: $a = 1.38 \text{ atm} \left(\frac{\text{m}^3}{\text{kmol}} \right)^2$ $b = 3.94 \times 10^{-2} \frac{\text{m}^3}{\text{kmol}}$

$P = \frac{RT}{V_m - b} - \frac{a}{V_m^2}$ $V_m = \frac{V}{n}$ $V_{m,old,1} = \frac{100 \text{ m}^3}{355.7 \text{ kmol}} = 0.281$

$V_m = \frac{RT}{P + \frac{a}{V_m^2}} + b$

$V_{m,old,2} = \frac{100 \text{ m}^3}{604.5} = 0.1654$

$V_{m(new)} = \frac{(8.314)(358.15 \text{ K})}{(10,000) + \frac{(1.38 \text{ atm})(101.325 \text{ kPa})}{V_m^2}} + 0.0394 = 0.278 \frac{\text{m}^3}{\text{kmol}}$
 iteration 2 = $\boxed{0.2775 \frac{\text{m}^3}{\text{kmol}}}$

$V_{m(new),2} = \frac{(8.314)(358.15 \text{ K})}{18000 + \frac{1.38(101.325)}{V_m^2}} + 0.0394 = 0.1682 \frac{\text{m}^3}{\text{kmol}}$
 iteration 2 = $\boxed{0.1692 \text{ m}^3/\text{kmol}}$

$m = \left[\frac{100 \text{ m}^3}{0.1692 \text{ m}^3/\text{kmol}} - \frac{100 \text{ m}^3}{0.2775 \text{ m}^3/\text{kmol}} \right] \left(\frac{28 \text{ kg}}{\text{kmol}} \right) = \boxed{6458 \text{ kg}}$

could also use cubic form of the vDW equation