

This gives

$$K\phi = \frac{EA}{\omega_m} = \frac{300}{1200 \times \frac{2\pi}{60}} = 2.387$$

Friday, April 8,  
2016

Total torque required is  $T_{\text{out}} = 200 \text{ Nm}$ . Add rotational losses

$$T_{\text{dev}} = T_{\text{out}} + T_{\text{rot}}$$

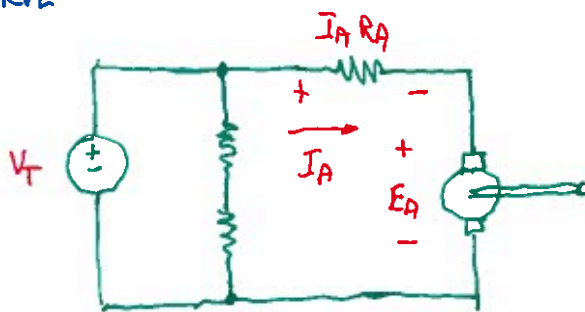
total developed torque      torque required by load      due to rotational losses

$$T_{\text{dev}} = 200 + 12 = 212 \text{ Nm}$$

Strategy: Find  $I_A$ , then  $E_A$ , then speed.

$$I_A = \frac{T_{\text{dev}}}{K\phi} = \frac{212}{2.387} = 88.8$$

From KVL



$$-V_T + I_A R_A + E_A = 0$$

$$\begin{aligned} E_A &= V_T - I_A R_A \\ &= 300 - 88.8(0.065) \\ &= 294.2 \text{ V} \end{aligned}$$

$$\text{So } \omega_m = \frac{E_A}{K\phi} = \frac{294.2}{2.387} = 123.6 \text{ rad/sec}$$

$$n_m = \omega_m \times \frac{60}{2\pi} = 1177 \text{ rpm}$$

And efficiency :

$$\begin{aligned} P_{\text{out}} &= T_{\text{out}} \omega_m = 200 \times 123.6 \\ &= 24,652 \text{ W} \end{aligned}$$

$$\begin{aligned} P_{\text{in}} &= V_T I_L = 300(I_F + I_A) \\ &= 300(10 + 88.8) \\ &= 29,640 \text{ W} \end{aligned}$$

$$\eta = \frac{P_{out}}{P_{in}} \times 100\% = \frac{24,632}{29,640} \times 100\% = 83.2\%$$

Example: Suppose fan blades are attached to the shaft of the above motor.

- this adds 15 Nm of additional torque loss, independent of speed.

What is the new speed?

The total developed torque:  $T_{dev} = \underbrace{200}_{\text{load}} + \underbrace{12 + 15}_{\text{rotational losses}} = 227 \text{ Nm}$

Armature current increases:  $I_A = \frac{T_{dev}}{K\phi} = \frac{227}{2.387} = 95.1.$

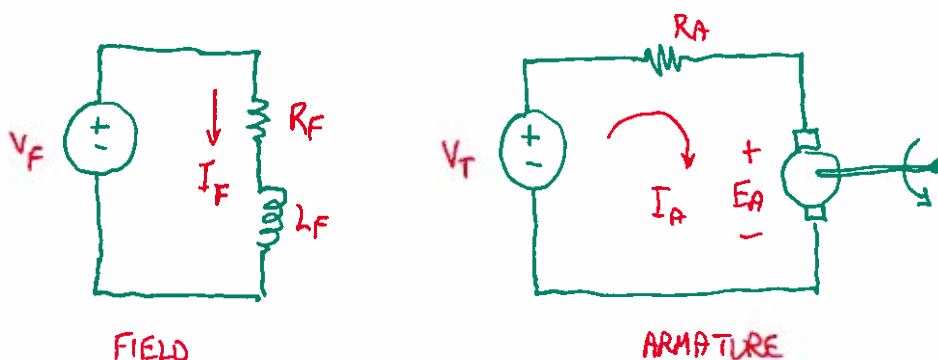
By KVL,  $E_A = V_T - I_A R_A = 300 - (95.1)(0.065) = 293.82$

Then,  $\omega_m = \frac{E_A}{K\phi} = \frac{293.82}{2.387} = 123.09 \text{ rad/sec}$

So  $n_m = \omega_m \times \frac{60}{2\pi} = 1175.4 \text{ rpm}$

### Separately excited DC machines

This configuration is similar to shunt-connected, except field and armature have separate sources.



$$\eta = \frac{P_{out}}{P_{in}} \times 100\% = \frac{24652}{29640} \times 100\% = 83.2\%$$

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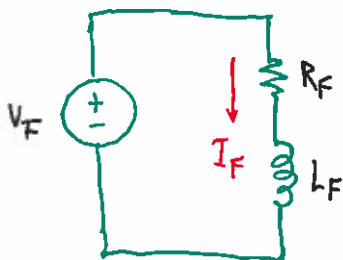
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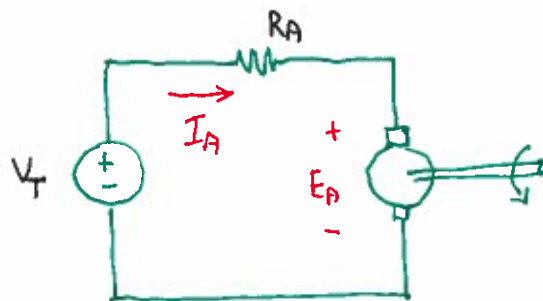
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### Separately excited DC machines

This configuration is similar to shunt-connected, except field and have separate sources.



FIELD



ARMATURE

## Permanent - magnet DC motors

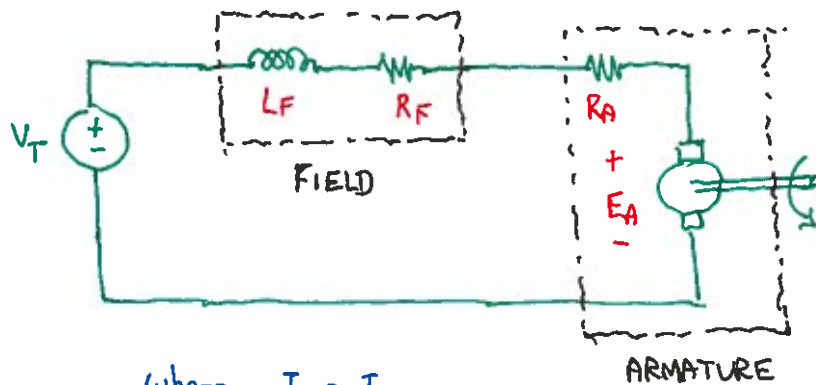
Similar to separately excited, except field is produced by permanent magnets.

Useful in fractional-horsepower applications

- small fans
- power windows, windshield wipers
- servos

## Series - connected DC motors

Field and armature connected in series



Series-connected motors have high torque at low speeds.

Suitable for many applications

- electric automotive starter motors
- electric drills, screwdrivers
- handheld mixers.

## Torque - speed characteristics

All motors are characterized by torque-speed characteristics.