

Wednesday, April 6, 2016

Therefore, the total input power :  $P_{in} = P_{total} = 40,650 \text{ W}$

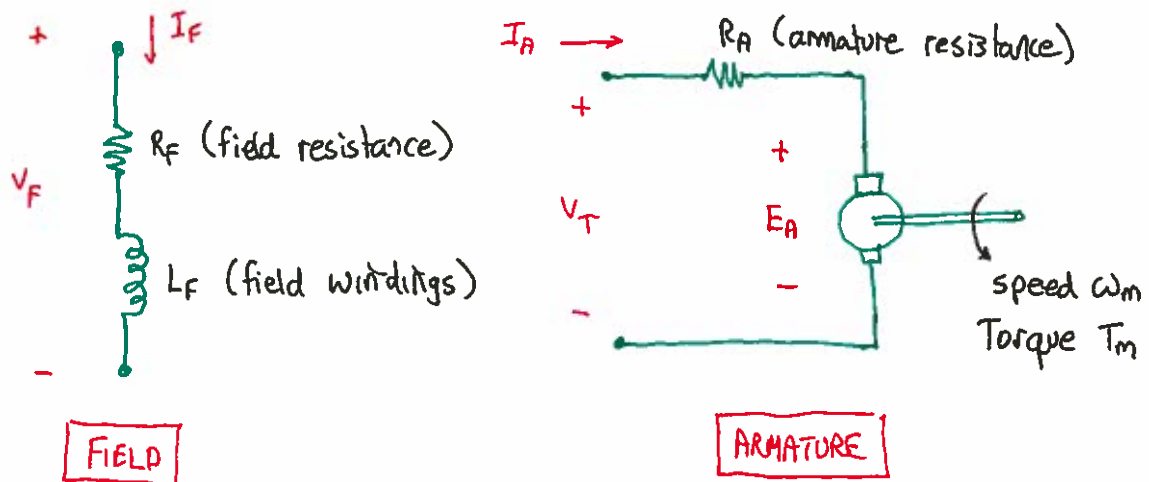
$$\eta = \frac{P_{out}}{P_{in}} = \frac{37,300}{40,650} \times 100\% \\ = 91.76\%$$

Input current:  $i = \frac{P_{in}}{V} = \frac{40,650}{220} = 184.77 \text{ A}$

Speed regulation:  $SR = \frac{n_{no-load} - n_{full-load}}{n_{full-load}} \times 100\% \\ = \frac{1200 - 1150}{1150} \times 100\% = 4.35\%$

### Electric circuit of DC motors

DC motors can be modeled with two simple circuits

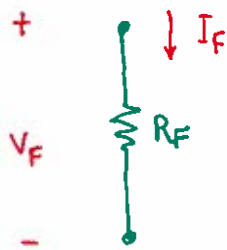


For a rotating DC machine, we have

$\omega_m$  — rotational speed, rad/sec

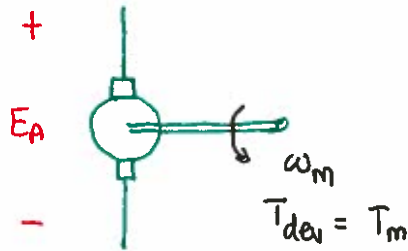
$T_m$  — torque, Nm (Newton-meters)

Since we are operating at DC, the field circuit reduces to.



( $L_F$  is acting like a short circuit)

The induced armature voltage



$$E_A = K \phi \omega_m,$$

$\phi$  = magnetic flux

$K$  = machine constant

And total developed mechanical torque

$$T_{dev} = K \phi I_A$$

And total developed mechanical power

$$P_{dev} = T_{dev} \omega_m$$

Together, these three equations are key to analyzing DC motor/generator circuits.

$$\begin{aligned} E_A &= K \phi \omega_m \\ T_{dev} &= K \phi I_A \\ P &= T \omega_m \end{aligned}$$

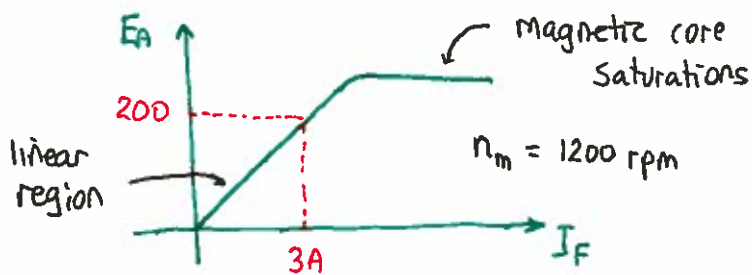
KEY MACHINE  
EQUATIONS

Normally, we lump  $K$  and  $\phi$  together

$$K \phi$$

MACHINE  
CONSTANT

The magnetization curve



Typical magnetization curve for a given speed

- A point on this curve gives us  $K\phi$

—  $K\phi$  tells us everything,

Note: may not always get such a curve, but  $K\phi$  can almost always be calculated from info' given.

Example: We have a DC motor that obeys the above curve.

- $n_m = 1500 \text{ rpm}$
- $P_{dev} = 10 \text{ HP}$
- $I_F = 3 \text{ A}$
- $R_A = 0.3 \Omega$
- $R_F = 50 \Omega$

Find developed torque, armature  $I_A$ , applied voltage  $V_T$ , efficiency.

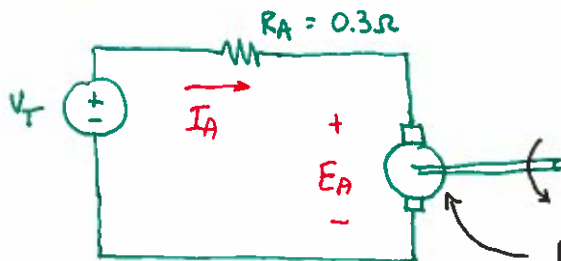
We have

$$\omega_m = n_m \times \frac{2\pi}{60} = 157.1 \text{ rads/sec}$$

$$P_{dev} = 10 \text{ HP} \times 746 = 7460 \text{ W}$$

$$T_{dev} = \frac{P_{dev}}{\omega_m} = 47.49 \text{ Nm}$$

The armature circuit:



$$P_{dev} = E_A I_A = 7460 \text{ W}$$

(electrical world meets the mechanical world)

Machine equations:

$$E_A = K\phi \omega_m$$

$$T_{dev} = K\phi I_A$$

We need  $E_A$  to find  $I_A = P_{dev} / E_A$

From information given

$$E_A = 200 \text{ v when } I_F = 3 \text{ A}$$

$$\text{and at } n_m = 1200$$

Using  $E_A$  and  $n_m$

$$E_A = K\phi \omega_m, \quad \text{so } K\phi = \frac{E_A}{\omega_m}$$

$$K\phi = \frac{200}{1200 \times \frac{2\pi}{60}} = 1.59$$

The motor is run at  $n_m = 1500 \text{ rpm}$ , so

$$\begin{aligned} E_A &= K\phi \omega_m = 1.59 \times 1500 \times \frac{2\pi}{60} \\ &= 250 \text{ v.} \end{aligned}$$