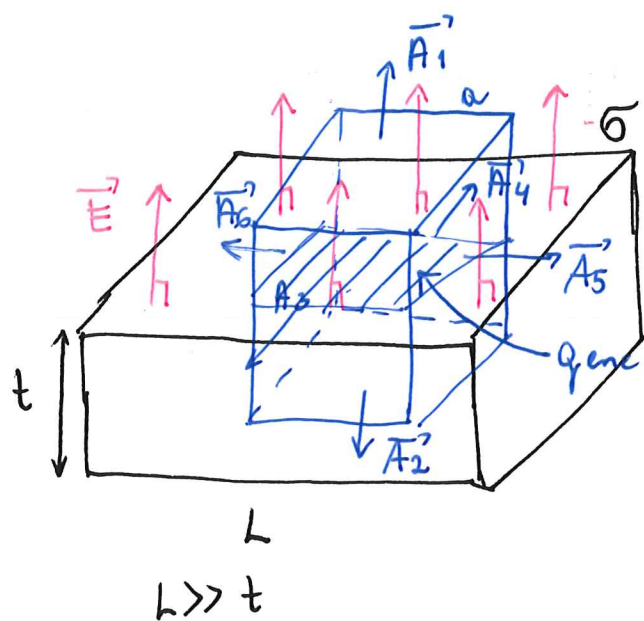


Electric field near a conductor



$\vec{E} = 0$ inside

$\vec{E} \perp$ surface outside.
has constant magnitude at constant height.

Planar symmetry.

Choose Gaussian surface
→ pillbox (side a)
half inside & half
outside the conductor

$$\oint \vec{E} \cdot d\vec{A} = \frac{q_{enc}}{\epsilon_0}$$

$$\underbrace{\int_{\text{bottom } A_2} \vec{E} \cdot d\vec{A}}_{\text{Zero because } \vec{E} = 0 \text{ inside}} + \underbrace{\int_{\text{top } A_1} \vec{E} \cdot d\vec{A}}_{\text{Zero because } \vec{E} \perp \vec{A}_3 - \vec{A}_6} + 4 \int_{\text{sides } (A_3 - A_6)} \vec{E} \cdot d\vec{A} = E \cdot A = E a^2$$

Find charge enclosed:

$$q_{enc} = \sigma \cdot a^2$$

From Gauss' Law: $\oint \vec{E} \cdot d\vec{A} = \frac{q_{enc}}{\epsilon_0}$

$$E \cdot a^2 = \frac{\sigma \cdot a^2}{\epsilon_0}$$

$$E = \frac{\sigma}{\epsilon_0}$$

→ relationship between the strength of electric field near a conductor and the local surface charge density.

This relationship is what ensures that $\vec{E} = 0$ inside the conductor.