# **Electricity and Magnetism**

- Physics 259 L02
  - •Lecture 38

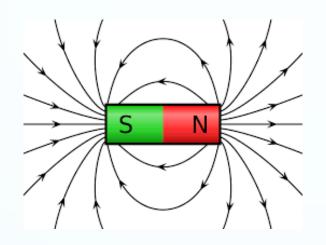


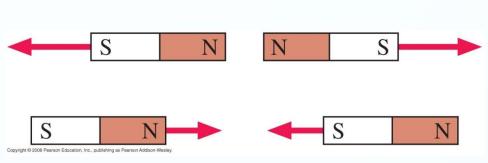
## **Chapter 28: Magnetic fields**



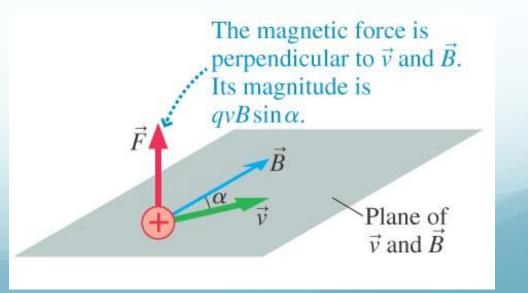
### 28.1: Magnetic fields







$$\vec{F}_B = q \vec{v} \times \vec{B}$$

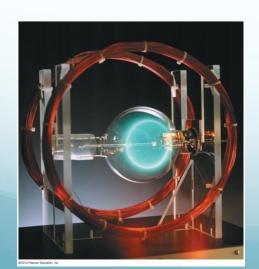


### 28.4: A circulating charged particle

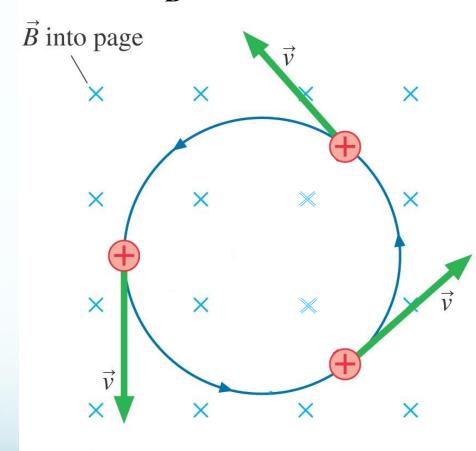
Charged particles in uniform magnetic fields undergo uniform circular motion.

The radius of the circle depends on how fast the particle is moving:

$$R = \frac{mv}{|q|B}$$



$$\vec{F}_B = q \vec{v} \times \vec{B}$$



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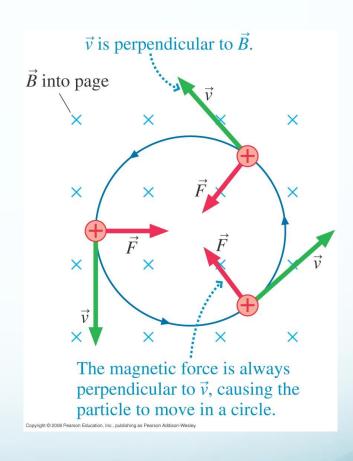
$$v = \frac{2\rho R}{T_{cvc}}$$

 $T_{cyc}$  is period (time it takes to make one cycle)

$$R = \frac{mv}{|q|B}$$

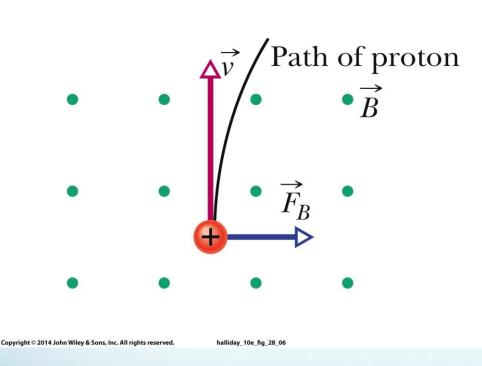
$$T_{cyc} = \frac{2\rho m}{|q|B}$$

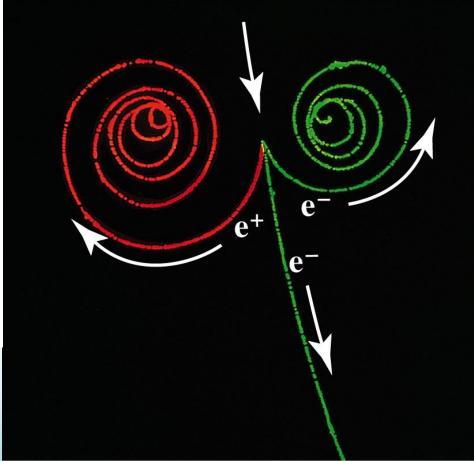
$$f_{cyc} = \frac{|q|B}{2\rho m}$$



The period (and also the frequency of the circular motion) depend on the B-field strength and the charge-to-mass ratio q/m

# Motion of charges in B-field

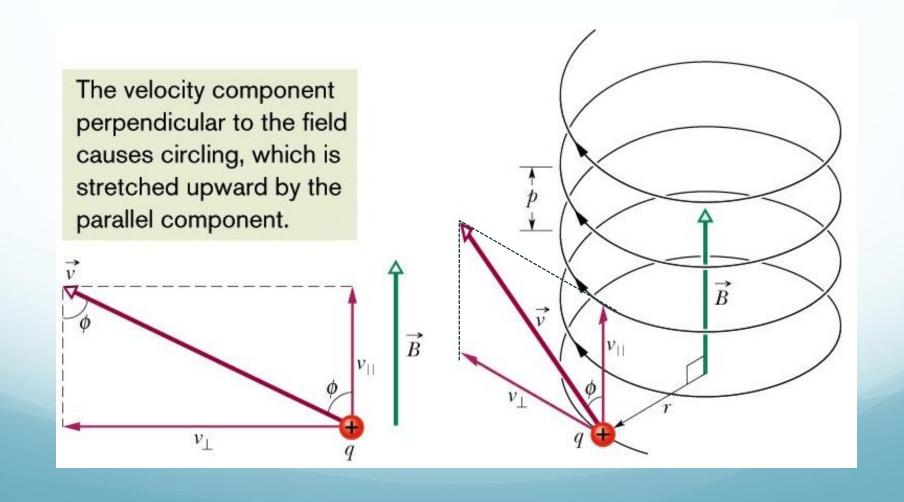




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#### Helical Paths Through a B-field

Splitting up the velocity into a component parallel to B-field and a component perpendicular to B-field immediately leads to helical motion



#### 28.5: Cyclotrons and Synchrotrons

#### We need beams of high-energy particles >

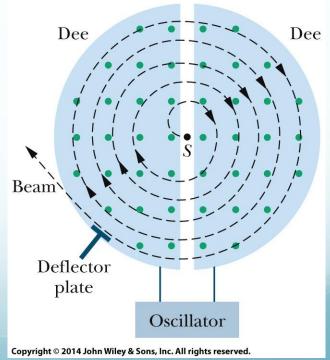
Two accelerators that employ a magnetic field to repeatedly bring

particles back to an accelerating region are:

✓ The Cyclotron

✓ The proton Synchrotron

The protons spiral outward in a cyclotron, picking up energy in the gap.



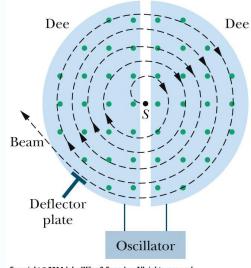
#### ✓ The Cyclotron

The key to the operation of the cyclotron is that the frequency f at which the proton circulates in the magnetic field (and that does not depend on its speed) must be equal to the fixed frequency  $f_{osc}$  of the electrical oscillator, or

$$f = f_{\text{osc}}$$
 (resonance condition).

## ✓ The proton Synchrotron

The protons spiral outward in a cyclotron, picking up energy in the gap.



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Magnetic field  ${\it B}$  and the oscillator frequency  $f_{osc}$ , instead of having fixed values as in the conventional cyclotron, are made to vary with time during the accelerating cycle  $\rightarrow$ 

- (1) the frequency of the circulating protons remains in step with the oscillator at all times
- (2) the protons follow a circular not a spiral path. Thus, the magnet need extend only along that circular path, not over some  $4 \times 10^6$  m<sup>2</sup>.

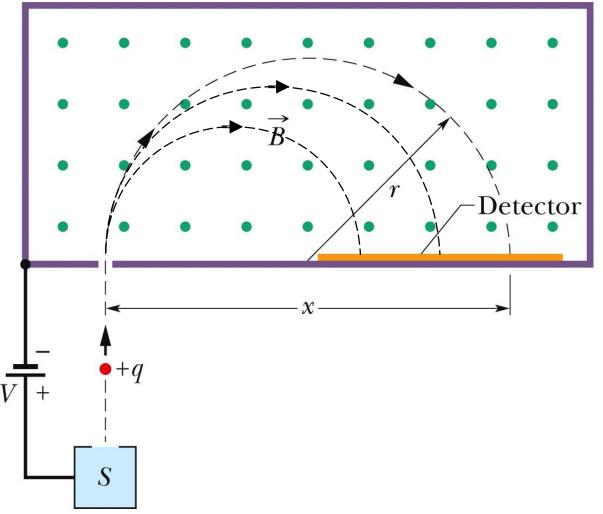
$$R = \frac{mv}{|q|B}$$

$$T_{cyc} = \frac{2\rho m}{|q|B}$$

$$f_{cyc} = \frac{|q|B}{2\rho m}$$

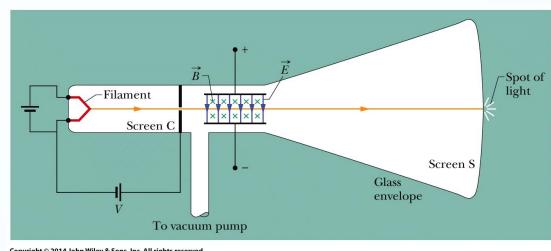
### **Application: Mass Spectrometer**

$$R = \frac{mv}{|q|B}$$



#### 28-2 Crossed Fields: Discovery of The Electron

A modern version of J.J. Thomson's apparatus for measuring the ratio of mass to charge for the electron



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If a charged particle moves through a region containing both an electric field and a magnetic field, it can be affected by both an electric force and a magnetic force.

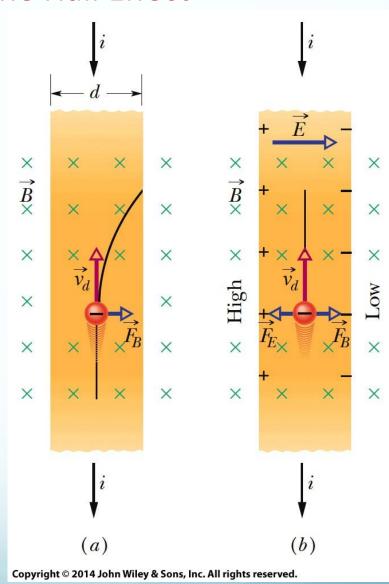
When the two fields are perpendicular to each other, they are said to be crossed fields.

#### 28-3 Crossed Fields: The Hall Effect

A beam of electrons in a vacuum can be deflected by ad magnetic field.

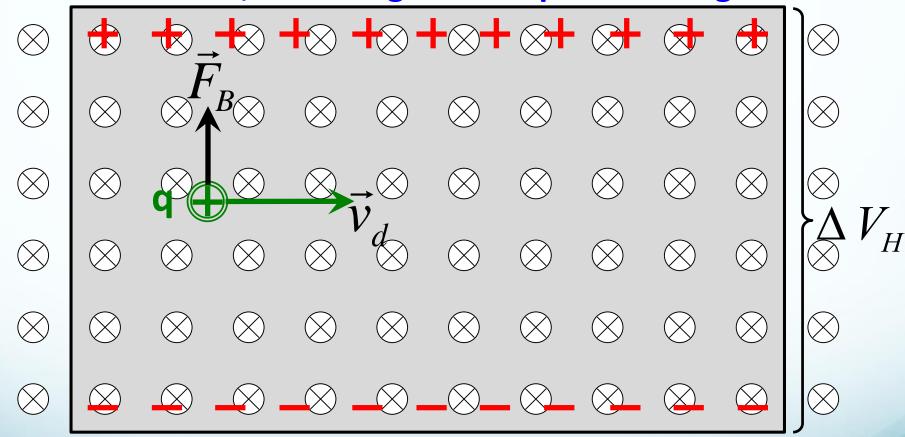
Can the drifting conduction electrons in a copper wire also be deflected by a magnetic field?

In 1879, Edwin H. Hall, then a 24-year-old graduate student at the Johns Hopkins University, showed that they can.



#### **Explanation: Let's talk about positive charge**

Due to the B-field, net charge build up on the edges.



In equilibrium, current still flows. Need to balance the magnetic and electric forces on the charge carriers.

$$F_B = q v_d B$$

$$F_E = q \frac{\Delta V_H}{d}$$

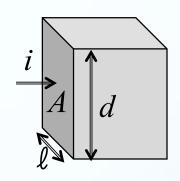
$$q\frac{\Delta V_H}{d} = q v_d B$$

$$\Delta V_H = v_d B d$$

→ Voltage established across a conductor carrying a current in a magnetic field  $\rightarrow$ 

$$\Delta V_H = v_d B d$$

We previously related the drift speed to the current via



$$v_d = \frac{i}{neA}$$

where  $A = \ell d$  and n is a material property

We can then relate the Hall voltage to known quantities:

$$\Delta V_H = \frac{i}{neld}Bd = \frac{iB}{nel}$$

In practical applications, you measure  $\Delta V_H$  to find B:

$$B = \frac{ne\ell}{i} \Delta V_H$$

 $B = \frac{ne\ell}{i} \Delta V_H$  How the B-field probe used in the next lab works

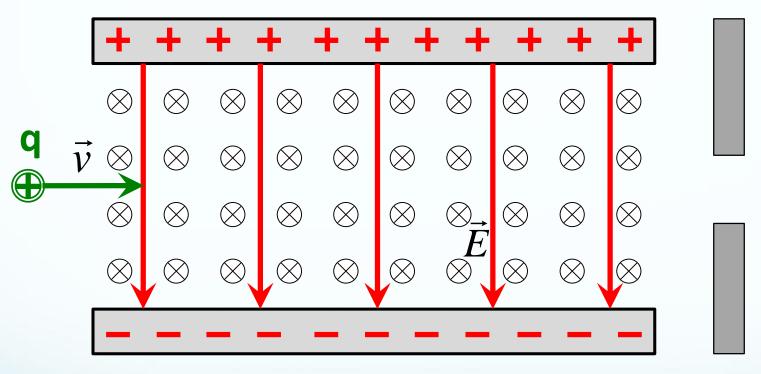
This section we talked about:

Chapter 28.2, 28.4, 28.3, 28.5

See you on Thursday



## Similar concept: velocity selector

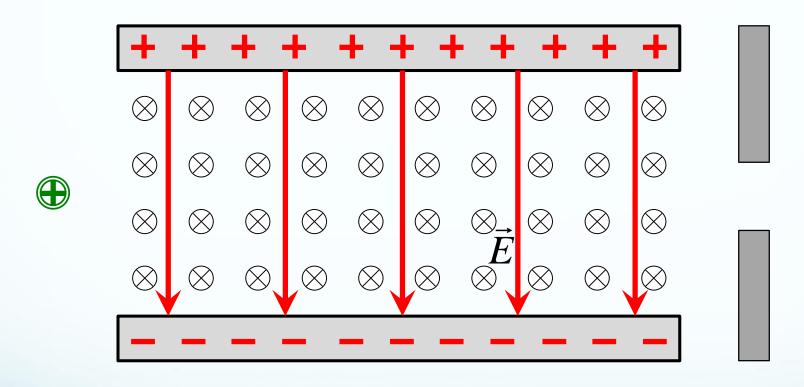


In a velocity selector, you send a charge through a region with crossed E and B fields, which leads to electric and magnetic forces:

$$\vec{F}_e = q\vec{E}$$
  $\vec{F}_B = q\vec{v} \times \vec{B}$   $qE = qvB$   $v = \frac{E}{R}$ 

If the forces balance  $(F_{net} = 0)$  the charge makes it through the slit

## Similar concept: velocity selector



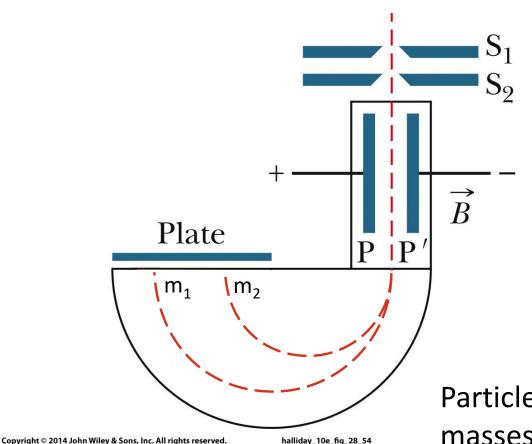
If the forces don't balance the charge hits the wall

$$qE - qvB = ma$$

We pick the E and B magnitudes to select the speeds we want

## Bainbridge Mass Spectrometer

Accelerate charges through  $\Delta V$  so they all have same Kinetic Energy



The slits  $S_1$  and  $S_2$  ensure the beam of particles is collimated.

The beam enters a region of crossed E and B-fields

A narrow slit ensures only particles with a specific speed enter

Particles with same KE but different masses and charges will have different radius in B field