

# Electricity and Magnetism

- Physics 259 – L02
  - Lecture 34



UNIVERSITY OF  
CALGARY

# Chapters 26 & 27



# Last time

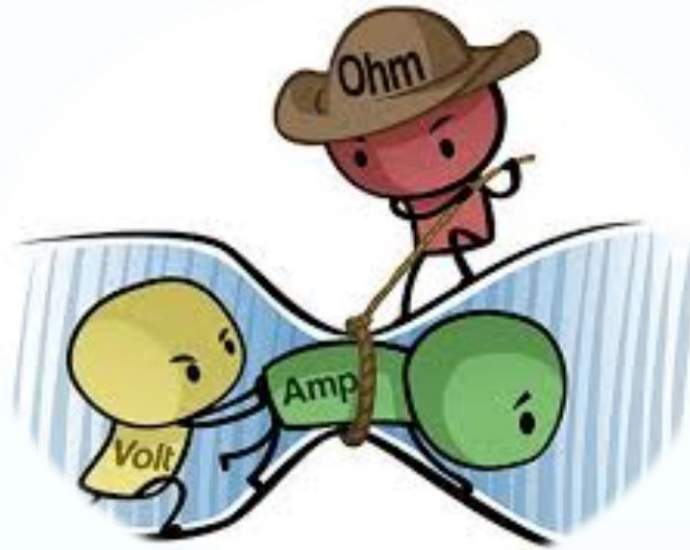
- Chapter 25- Capacitance

This time

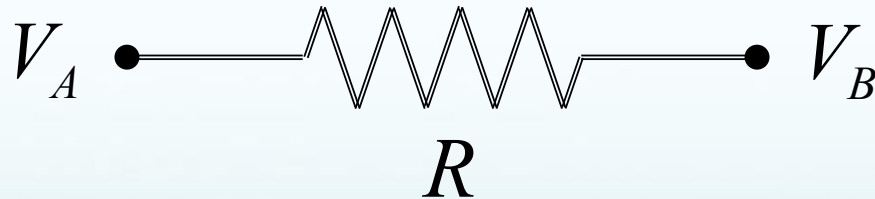


- Chapters 26 and 27

## 26-4 Ohm's Law



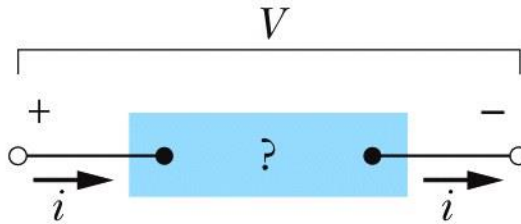
When a voltage difference  $\Delta V$  is applied across a resistor  $R$ , the voltage difference causes electrons to flow through the resistor



This flow of electrons is the electric current  $I$ . These quantities are related by Ohm's Law:

$$\Delta V = IR$$

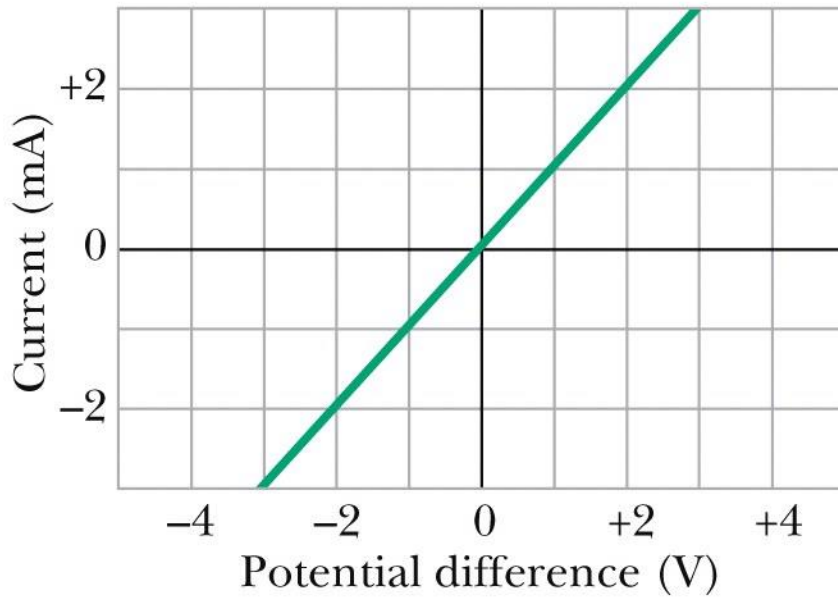
# Ohmic vs non-Ohmic devices



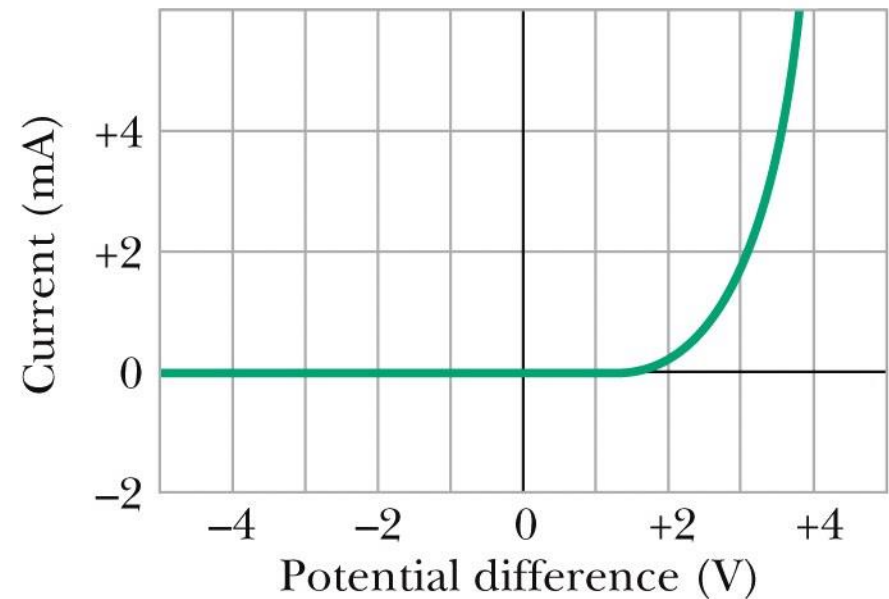
(a)

Materials with isotropic electrical properties

Materials with anisotropic electrical properties (pn junction diode)

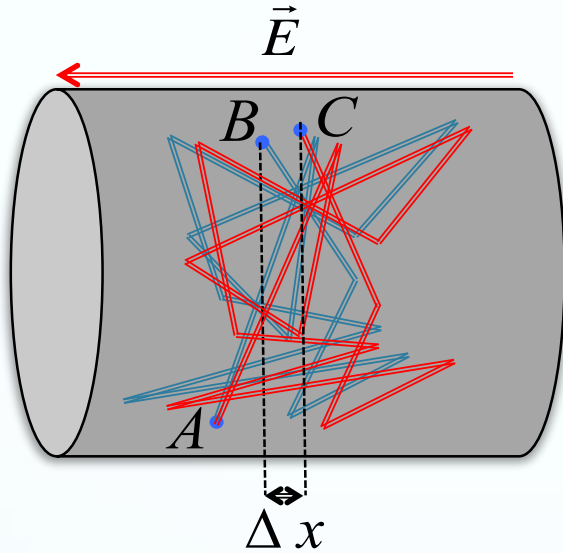


(b)



(c)

# Microscopic view of Ohm's law (resistivity)



Electrons bounce around inside the metal at speeds very high speeds on the order of 0.5% light speed.

When an electric field is applied in the conductor, there is a net force on the electrons, leading to “drift speed”

$$v_d = \frac{J}{ne}$$

microscopic picture of resistivity:

$$r = \frac{m}{ne^2 t}$$

$$r - r_0 = r_0 a (T - T_0)$$

# Temperature Dependent Resistance

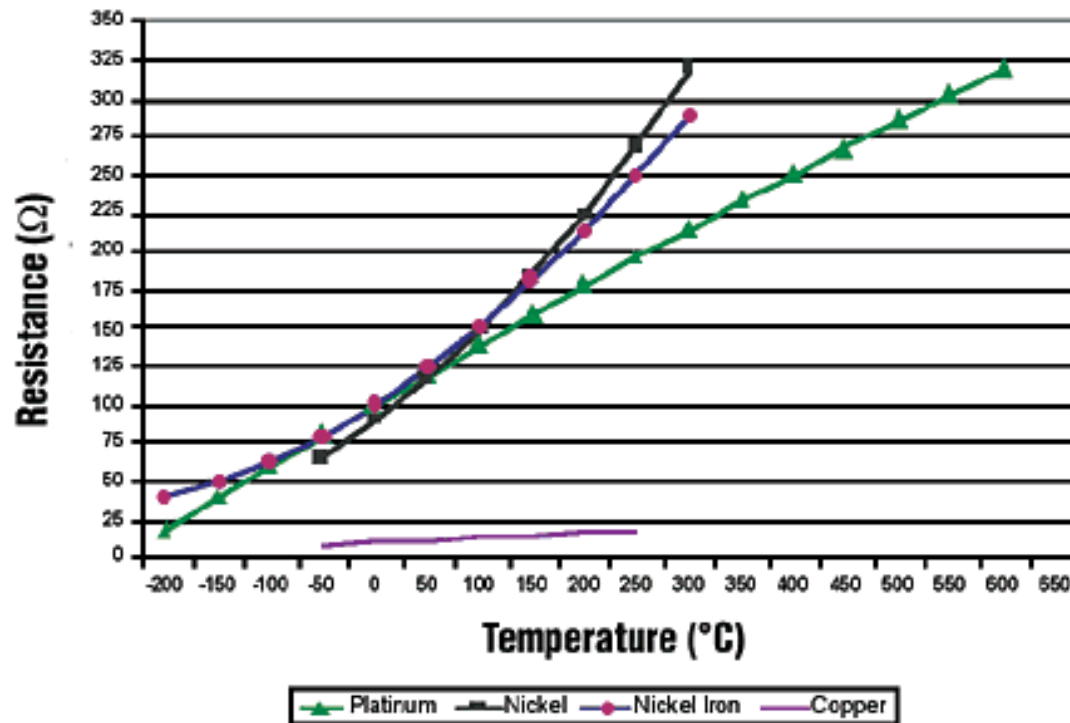


$$R - R_0 = R_0 \left( \frac{2}{3} a \right) (T - T_0)$$

Proof: Appendix 2-Chapter 26

$$r - r_0 = r_0 a (T - T_0)$$

Resistance vs. Temperature



## 26-5 Power in circuits

Recall that **POWER** is the **rate at which work is done**

$$P = \frac{W}{\Delta t}$$

A battery with voltage  $\Delta V$  raises the **potential energy** of a single charge  $q$  by an amount  $q \Delta V$ . This is the **work done** by the battery. For  $N$  charges

$$P = \frac{Nq \Delta V}{\Delta t} = \left( \frac{Nq}{\Delta t} \right) \Delta V = IV$$

**Power in circuits** →

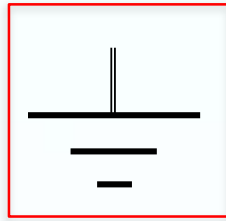
$$P = IV = RI^2 = \frac{V^2}{R}$$



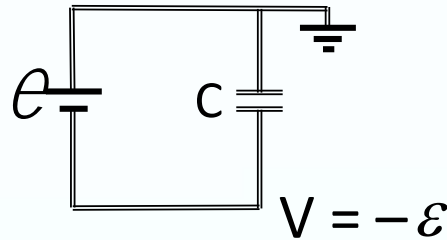
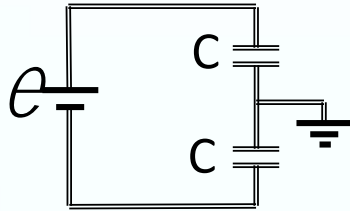
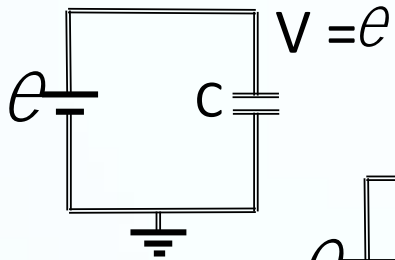
## 27 Circuits: continue of last section



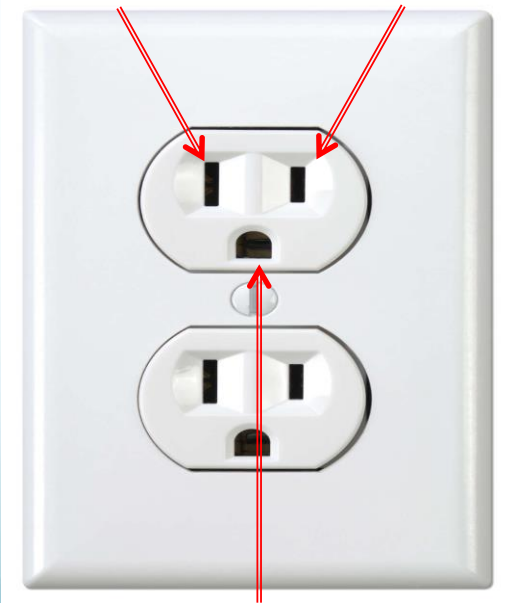
# Grounding



This symbol is called “ground” and it represents the place in the circuit where  $V=0$ .



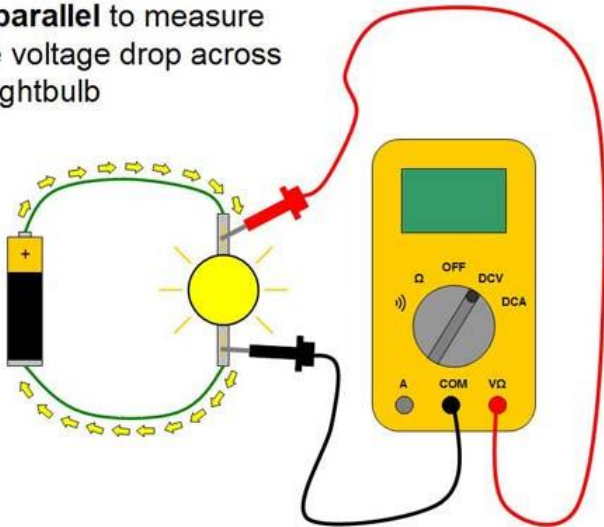
Wide slot (neutral)      Narrow slot (hot/live)



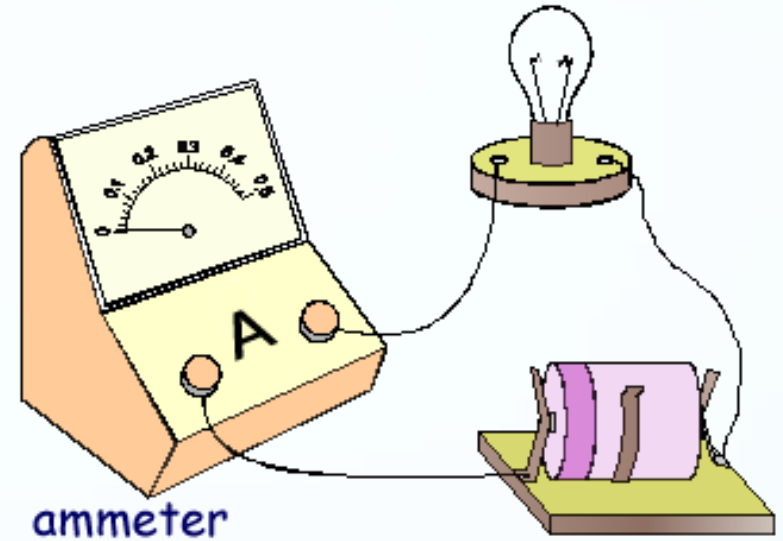
Ground

## 27-3 The Ammeter and The Voltmeter

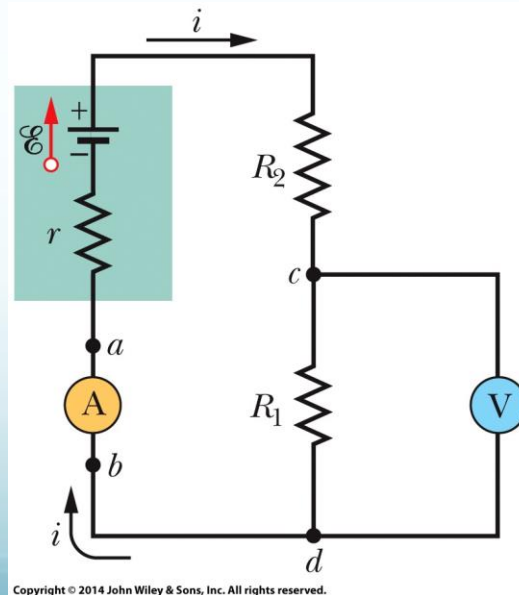
Connect a multimeter in **parallel** to measure the voltage drop across a lightbulb



<https://tinyurl.com/zpb36w>



<https://tinyurl.com/jlktro3>

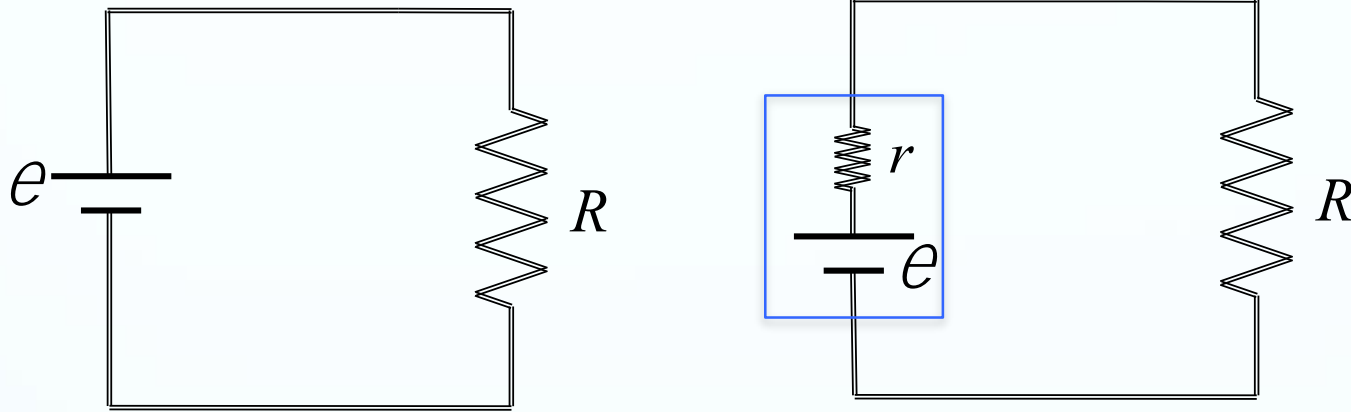


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# Non-ideal Batteries: internal resistance

## Appendix 2-Chapter 26

Every voltage source has **some** internal resistance to it. Usually this can be ignored but not always.

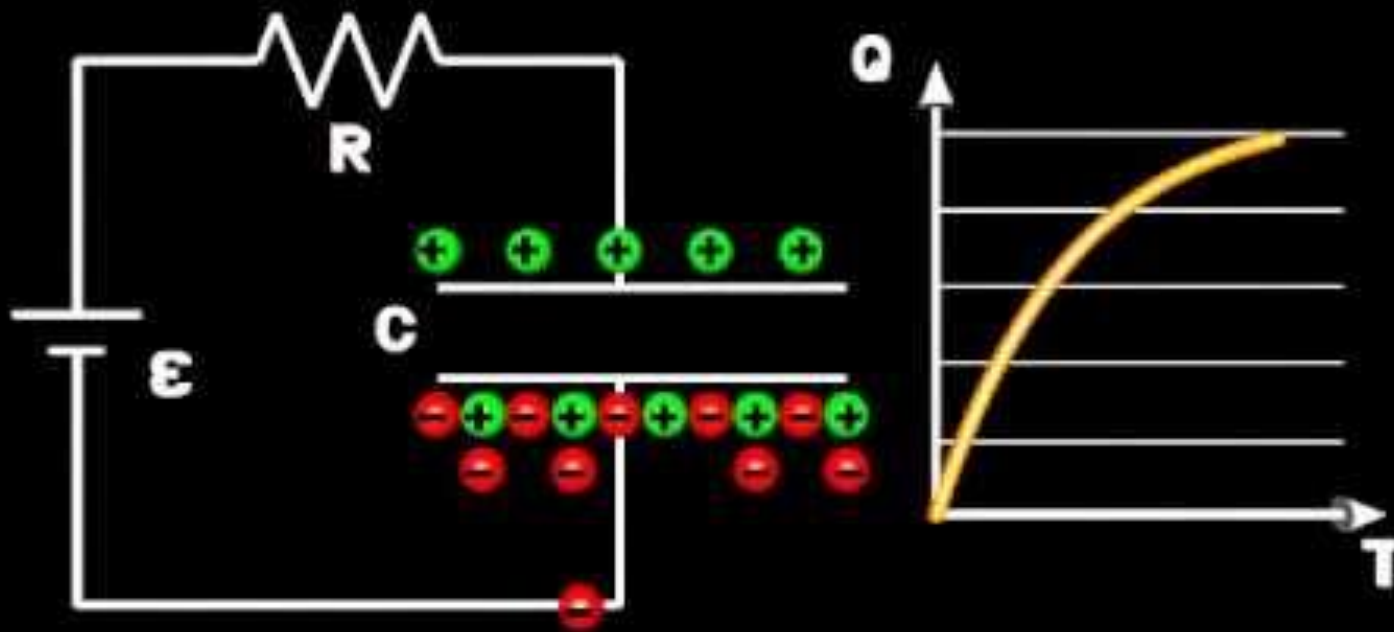


The internal resistance simply acts as a resistor in series with the rest of the circuit.

$$e - Ir - IR = 0 \quad I = \frac{e}{(r + R)}$$

$$P_e = Ie = \frac{e^2}{R + r}$$
$$P_R = I^2 R = \frac{e^2 R}{(R + r)^2}$$

## 27-4 RC Circuits (resistors + capacitors)

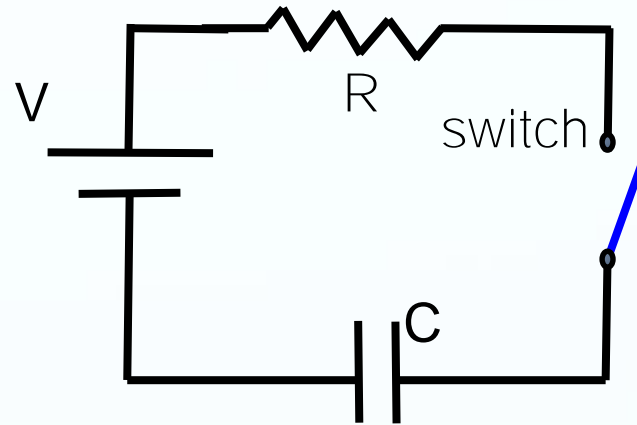


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Until now → **steady and continuous currents**  
many important circuit applications use a combination of capacitors and resistors to produce **time dependent currents**

*Examples: wireless signals in a cordless phone, remote control, etc.*

Simple RC Series Circuit



Open switch →

- ✓ no current can flow
- ✓ charge and voltage on capacitor → Zero

Closed switch for a long time →

- ✓ Charge on capacitor  $Q = CV$
- ✓ Voltage across capacitor is  $V$  and no current flows in the circuit.

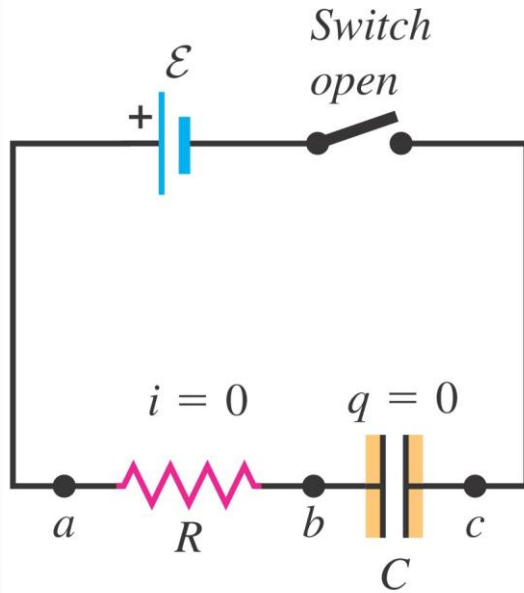
**What happens immediately after switch is closed or opened?**

**We get time dependent currents!**



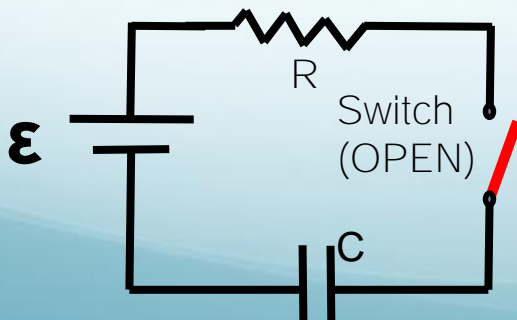
# Case 1: Charging a capacitor

(a) Capacitor initially uncharged

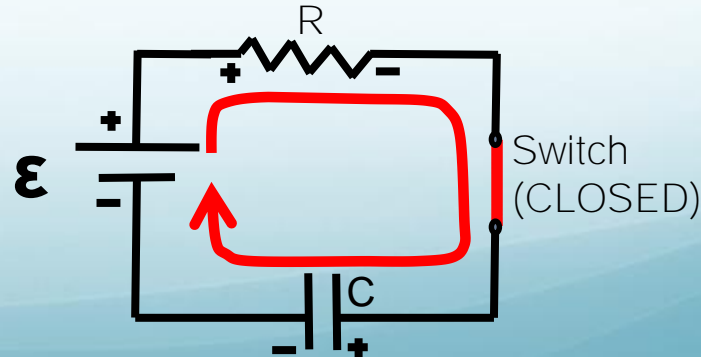


$R$  could be the internal resistance of the battery, resistance of the connecting wires, an actual resistance in the circuit or combination of all the above.

Switch is open for a long time before  $t=0$

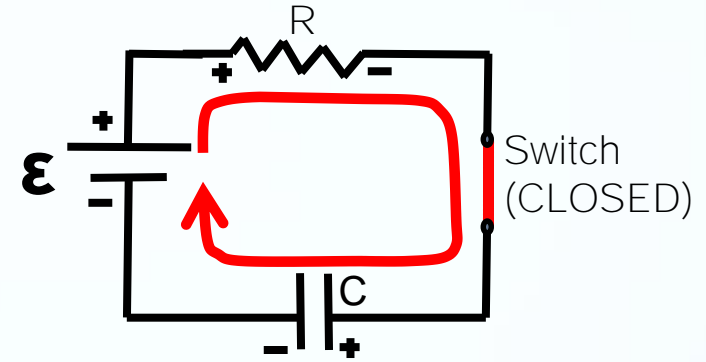


Switch is suddenly closed at  $t=0$



## Case 1: Charging a capacitor

Switch is suddenly  
closed at  $t=0$



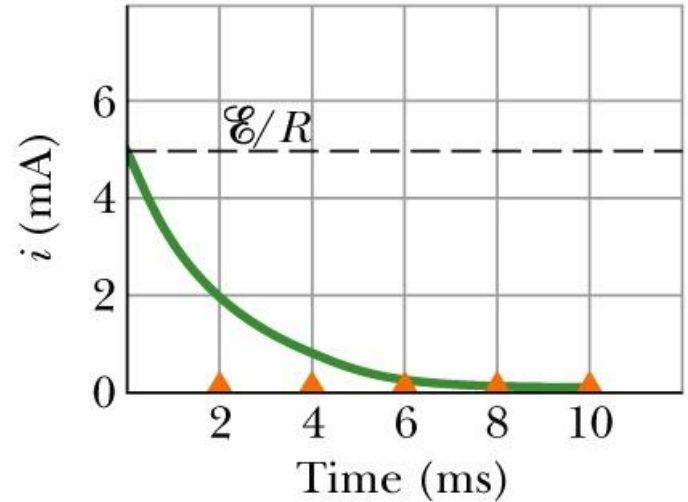


# Case 1: Charging a capacitor

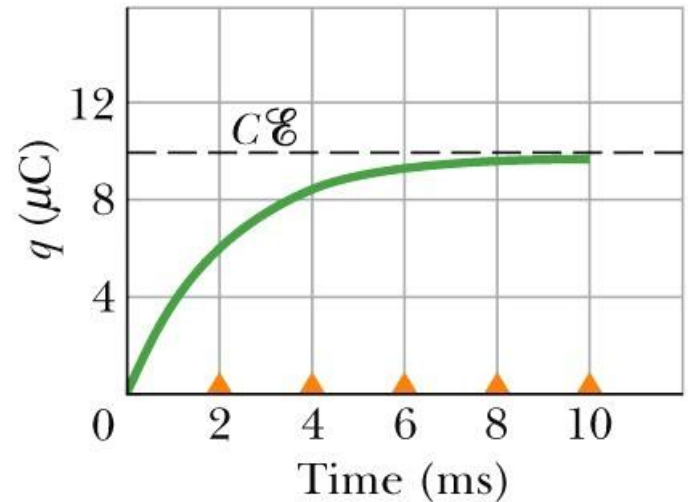


$$i = i_0 e^{-t/RC}$$

$$q = \varepsilon C (1 - e^{-t/RC}) = Q_f (1 - e^{-t/RC})$$



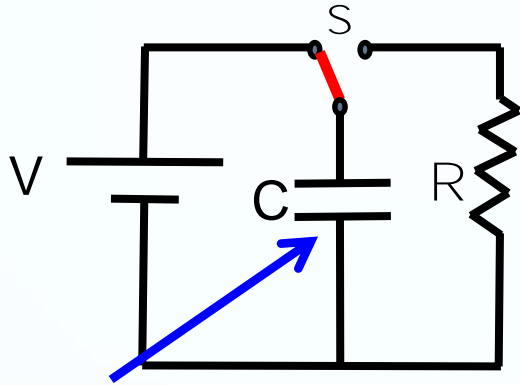
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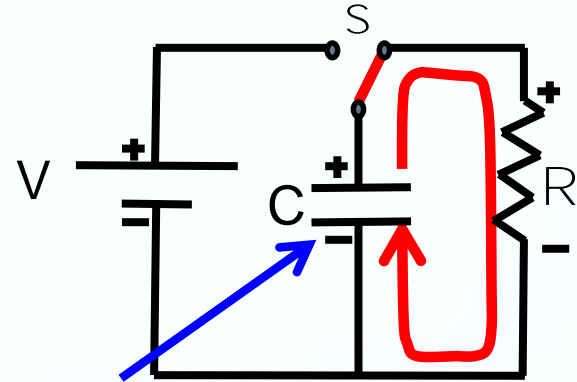
## Case 2: Discharging a capacitor

Switch is connected to the left for a long time until  $t=0^-$



Capacitor charges up to voltage  $V$

Switch is suddenly flipped to the right at  $t=0^+$



Capacitor discharges

Once the switch is flipped to right  $\rightarrow \frac{q(t)}{C} - iR = 0 \rightarrow \frac{q}{RC} = i = -\frac{dq}{dt}$

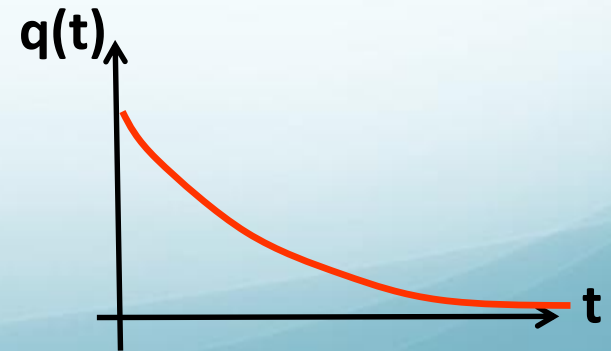
NOTE here  $dq < 0$

Solving for the charge  $q(t)$  on the capacitor  $\rightarrow$

$$q(t) = q_0 e^{-t/RC}$$

$$i(t) = i_0 e^{-t/RC}$$

$$q_0 = CV$$



This section we talked about:  
Chapters 26 and 27

*See you on Thursday*

