Electricity and Magnetism

- Physics 259 L02
 - Lecture 11



Chapter 23: Gauss's Law



Last time

• Chapters 21 and 22

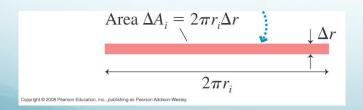
This time

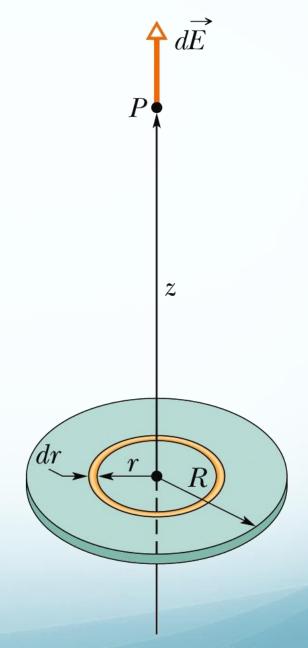
Continue Disk of Charge Chapter 23.1: Electric Flux

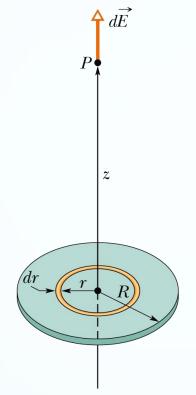
A disk of charge

$$\sigma = \frac{Q}{A} = \frac{Q}{\pi R^2} = \frac{\Delta Q}{\Delta A_i} = \frac{dQ}{dA_i}$$

$$dQ = \sigma dA_i = \sigma 2\pi r_i dr$$







Limiting cases?



$$E_{disk,z} = \frac{\sigma}{2\varepsilon_o} \left[1 - \frac{z}{\sqrt{z^2 + R^2}} \right]$$

$$E_{disk,z} = \frac{\sigma}{2\varepsilon_o} \left| 1 - \frac{z}{\sqrt{z^2}} \right| = 0????$$

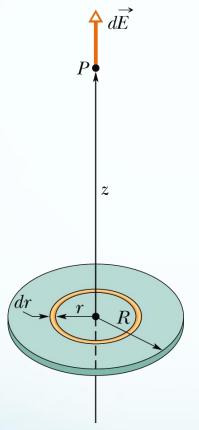
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$$E_{disk,z} = \frac{\sigma}{2\varepsilon_o} \left[1 - \frac{1}{\sqrt{1 + \frac{R^2}{z^2}}} \right] = \frac{\sigma}{2\varepsilon_o} \left[1 - \left(1 + \frac{R^2}{z^2} \right)^{-\frac{1}{2}} \right] = \frac{\sigma}{2\varepsilon_o} \left[1 - \left(1 - \frac{1}{2} \frac{R^2}{z^2} \right) \right]$$

$$\approx \frac{\sigma}{2\varepsilon_0} \frac{R^2}{2z^2} = \frac{Q/A}{2\varepsilon_0} \frac{\pi R^2}{2\pi z^2} = \frac{Q}{4\pi\varepsilon_0 z^2}$$

Limiting cases?

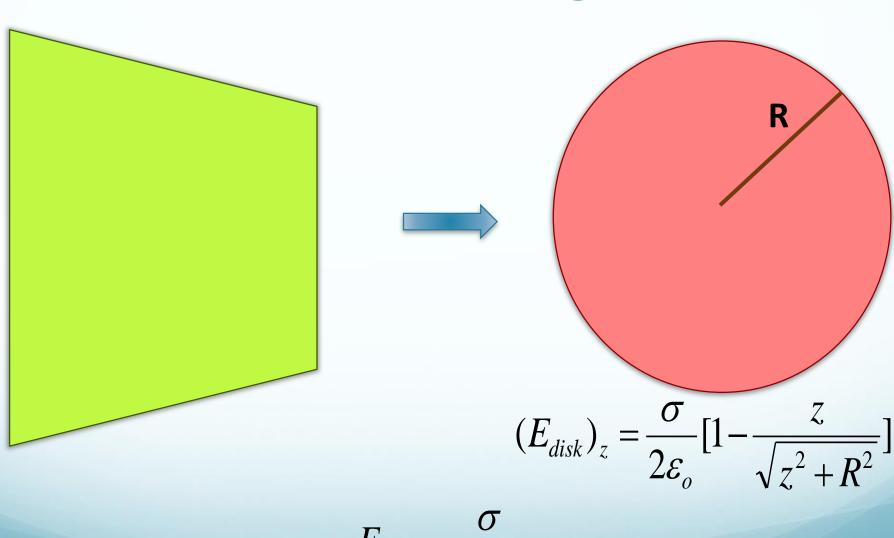




$$E_{disk,z} = \frac{\sigma}{2\varepsilon_o} \left[1 - \frac{z}{\sqrt{z^2 + R^2}} \right]$$

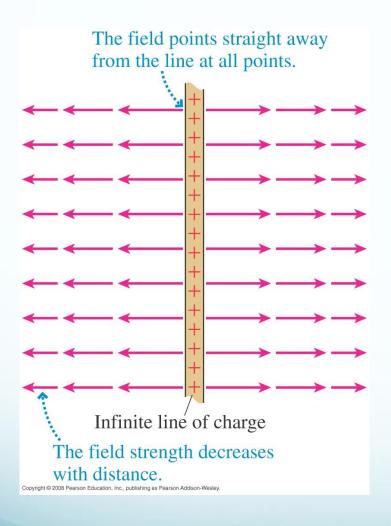
$$E_{disk,z} = \frac{\sigma}{2\varepsilon_o}$$

Plane of charge



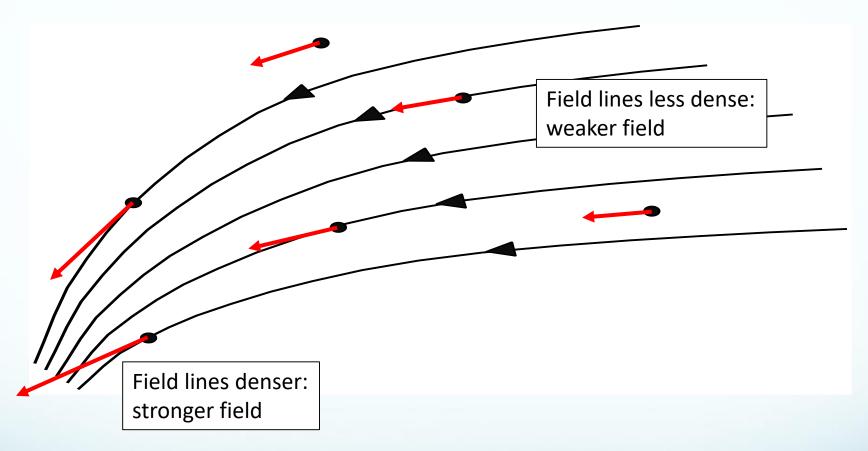
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This is the result for a plane of charge



$$E_{plane,z} = egin{cases} \dfrac{\sigma}{2arepsilon_o}, z > 0 \ -\dfrac{\sigma}{2arepsilon_o}, z < 0 \end{cases}$$

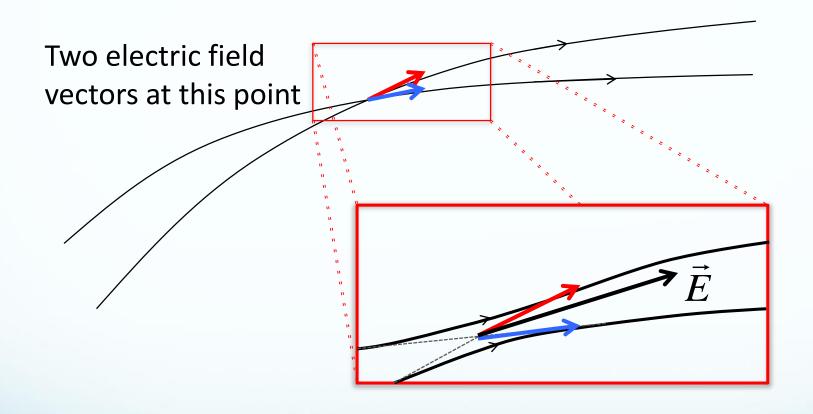
Electric Field Lines



Electric field lines are continuous curves. The electric field vectors are tangent to the field lines

The denser the field lines, the stronger the field (magnitude of E)

Electric Field Lines Can't Cross



If field lines crossed, the electric field at that point would not be defined: superposition saves the day.

Sources and Sinks of Field Lines

Two charges of equal magnitude and opposite sign.

Field lines start on + Field lines end on –

Positive charge called "source" **Negative** charge called "sink"

halliday_10e_fig_22_08

Electric force on q:
$$\vec{F}_{onq} = q\vec{E}$$

Newton's 2nd Law: $\sum \vec{F} = m\vec{a}$

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So if the electric force is the only force acting, then

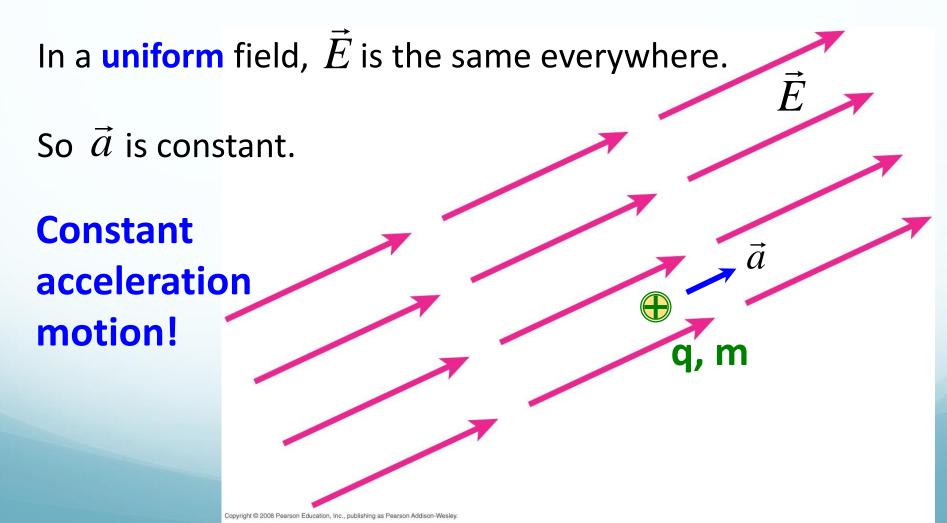
$$\vec{F}_{onq} = m\vec{a}$$

$$q\vec{E} = m\vec{a}$$

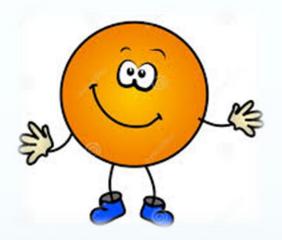
$$q\vec{E} = m\vec{a}$$

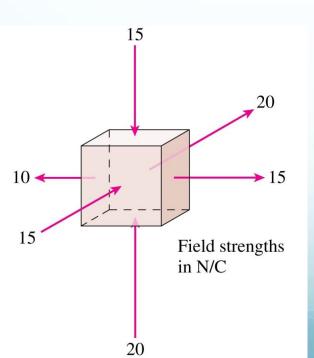


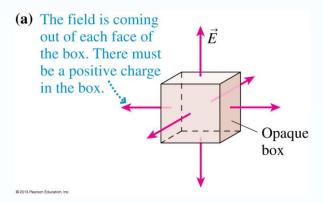
$$\vec{a} = \frac{q\vec{E}}{m}$$

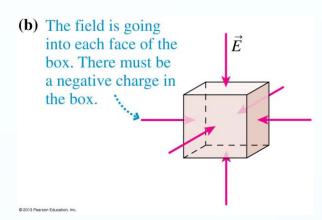


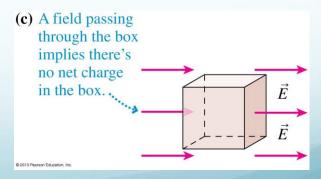
23-1: The Electric Flux











A closed surface through which an electric field passes is called **Gaussian surface**

An imaginary mathematical surface

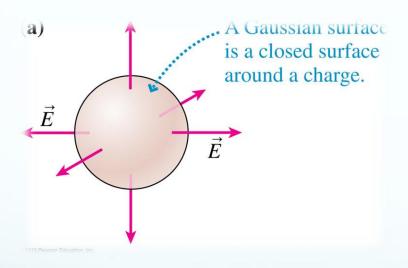


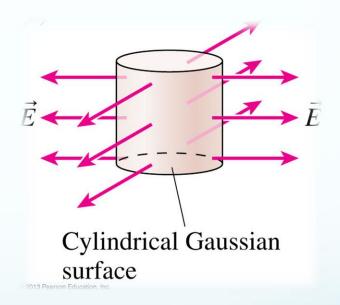
Electric Flux; Gauss' Law

Gauss' Law is equivalent to Coulomb's law. It will provide us:

- (i) an easier way to calculate the electric field in specific circumstances (especially situations with a high degree of symmetry)
- (ii) a better understanding of the properties of conductors in electrostatic equilibrium (more on this as we go)
- (iii) It is valid for moving charges not limited to electrostatics.

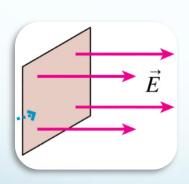
The Gaussian surface is most useful when it matches the shape of the field

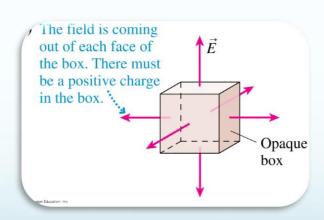


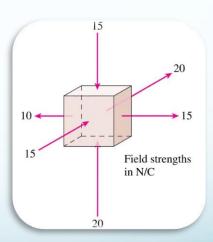


Electric Flux (Φ_e)

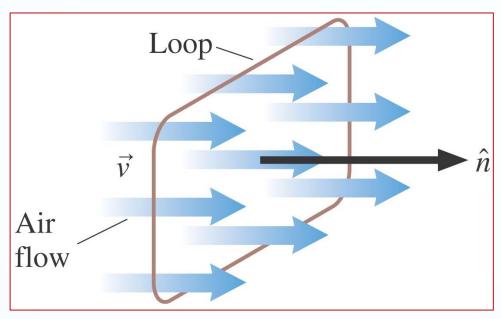
- Amount of electric field going through a surface
- The number of field lines coming through a surface

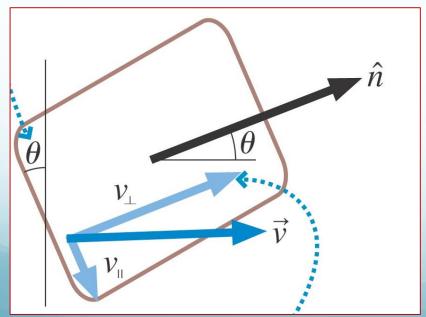


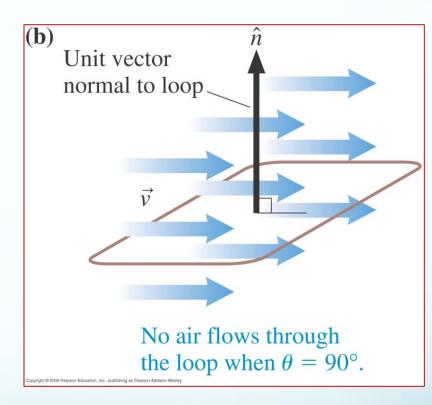




Wind going through a loop







The Electric Flux

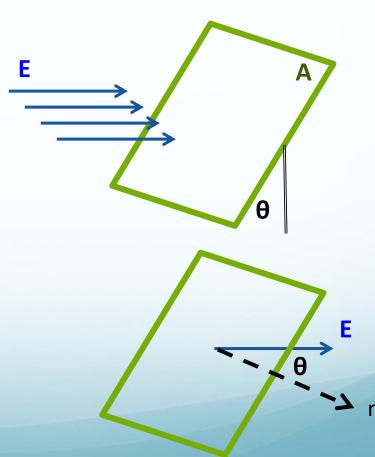
Amount of electric field going through a surface

$$\begin{array}{l} \Phi_e\,\alpha\;\text{E} \\ \Phi_e\,\alpha\;\text{A} \end{array}$$

$$\Phi_{\rho} \alpha A$$

$$\Phi_e \alpha \theta$$

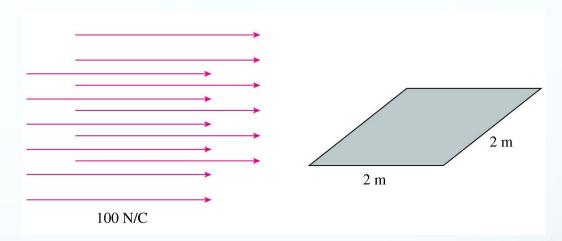
$$\Phi_{\rm e} = E_{\perp}A = EA\cos\theta$$



QuickCheck 27.2

The electric flux through the shaded surface is

- A. 0.
- B. 200 N m/C.
- C. $400 \text{ N m}^2/\text{C}$.
- D. Some other value.



This section we talked about:

Chapter 23.1

See you on Friday

