

Monday March 27, 2017

# Last time:

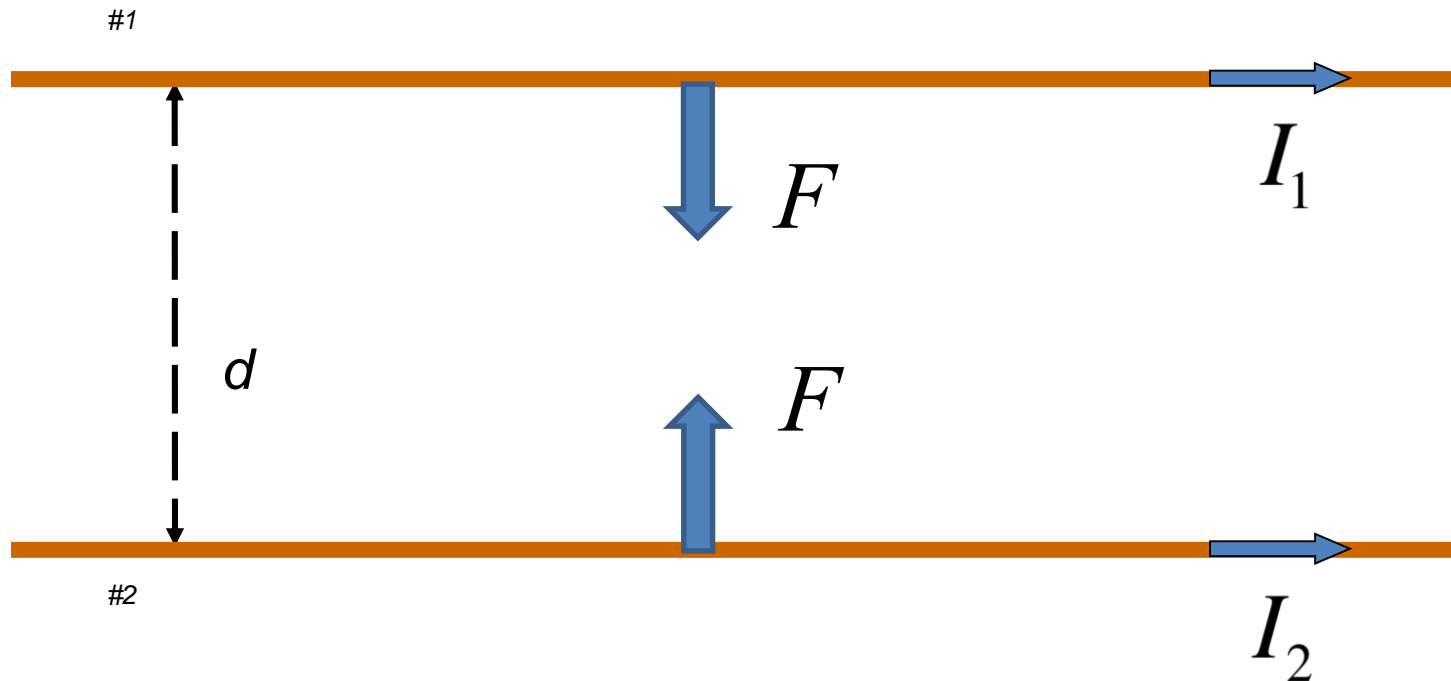
- Charge to mass apparatus demonstration
- Group activity

# Today:

- Magnetic force between parallel current-carrying wires
- Torque on a current loop
- Biot-Savart Law (like Coulomb's Law for magnetism)
- B-field of a line of current

# Force Between Two Parallel Wires

$$\vec{F}_B = i\vec{L} \times \vec{B}$$

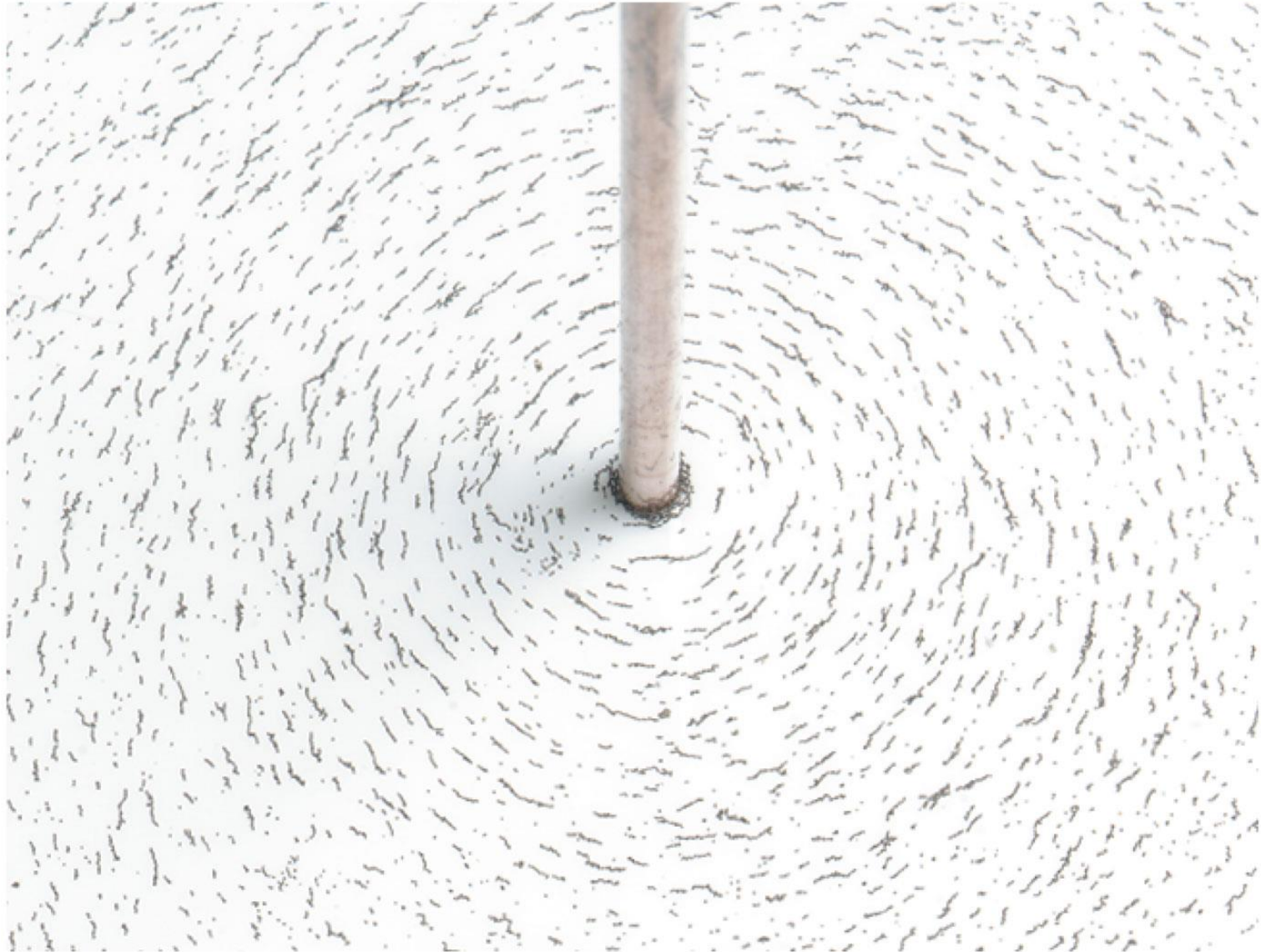


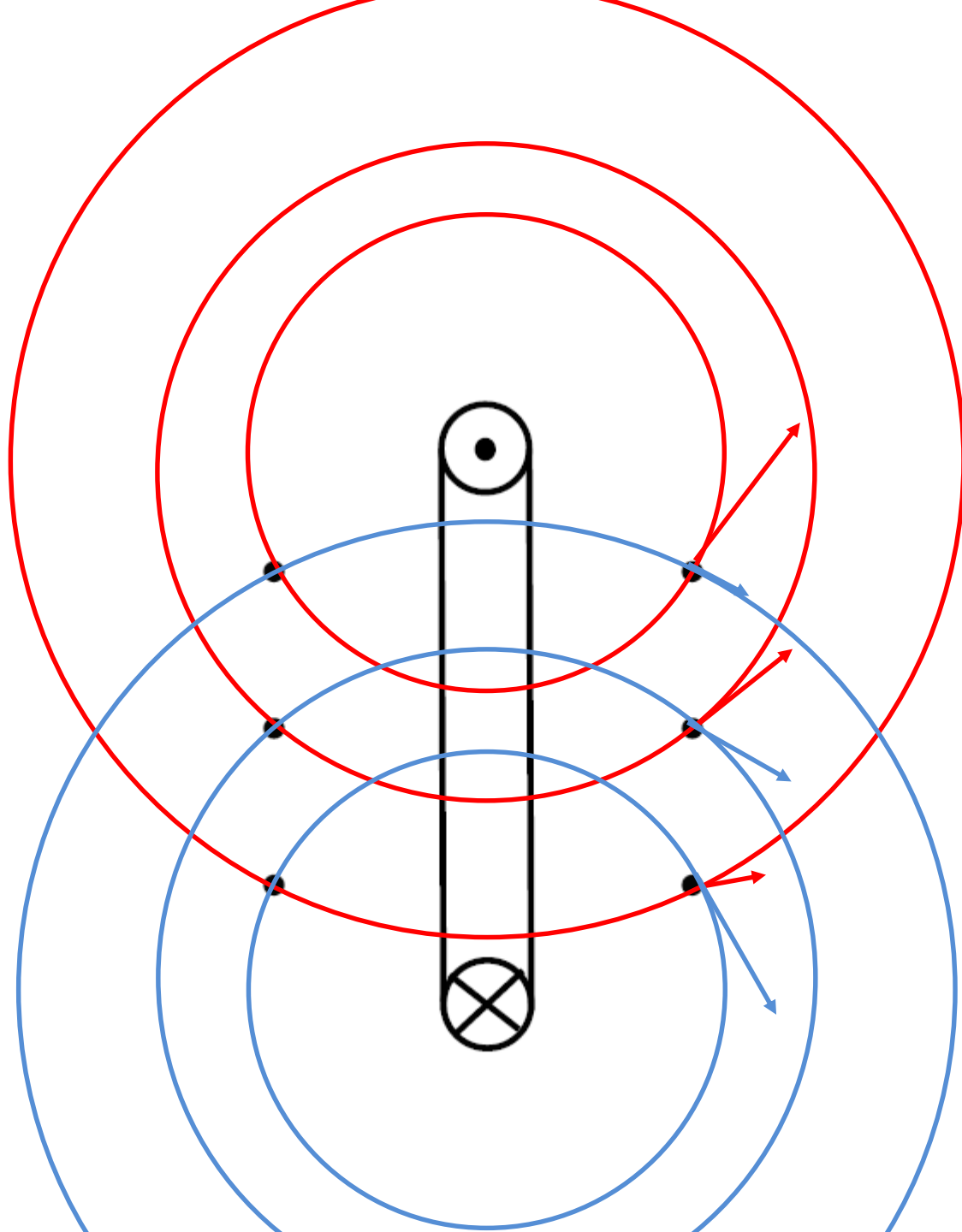
Derive an expression for the magnetic force on wire #2 due to the magnetic field created by the current flowing in wire #1.

# Demonstration wires



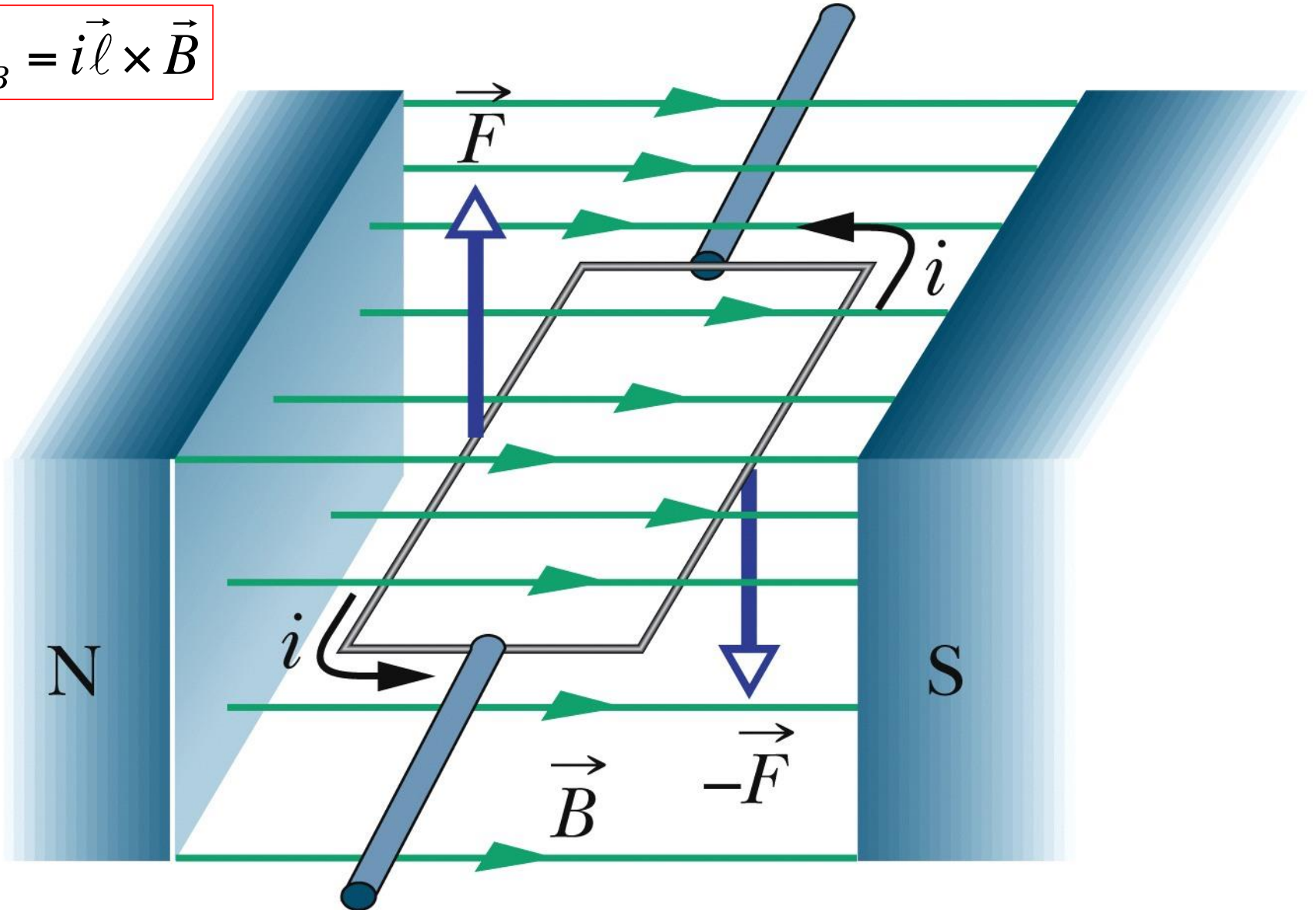
# Magnetic Field of a Long, Straight Wire





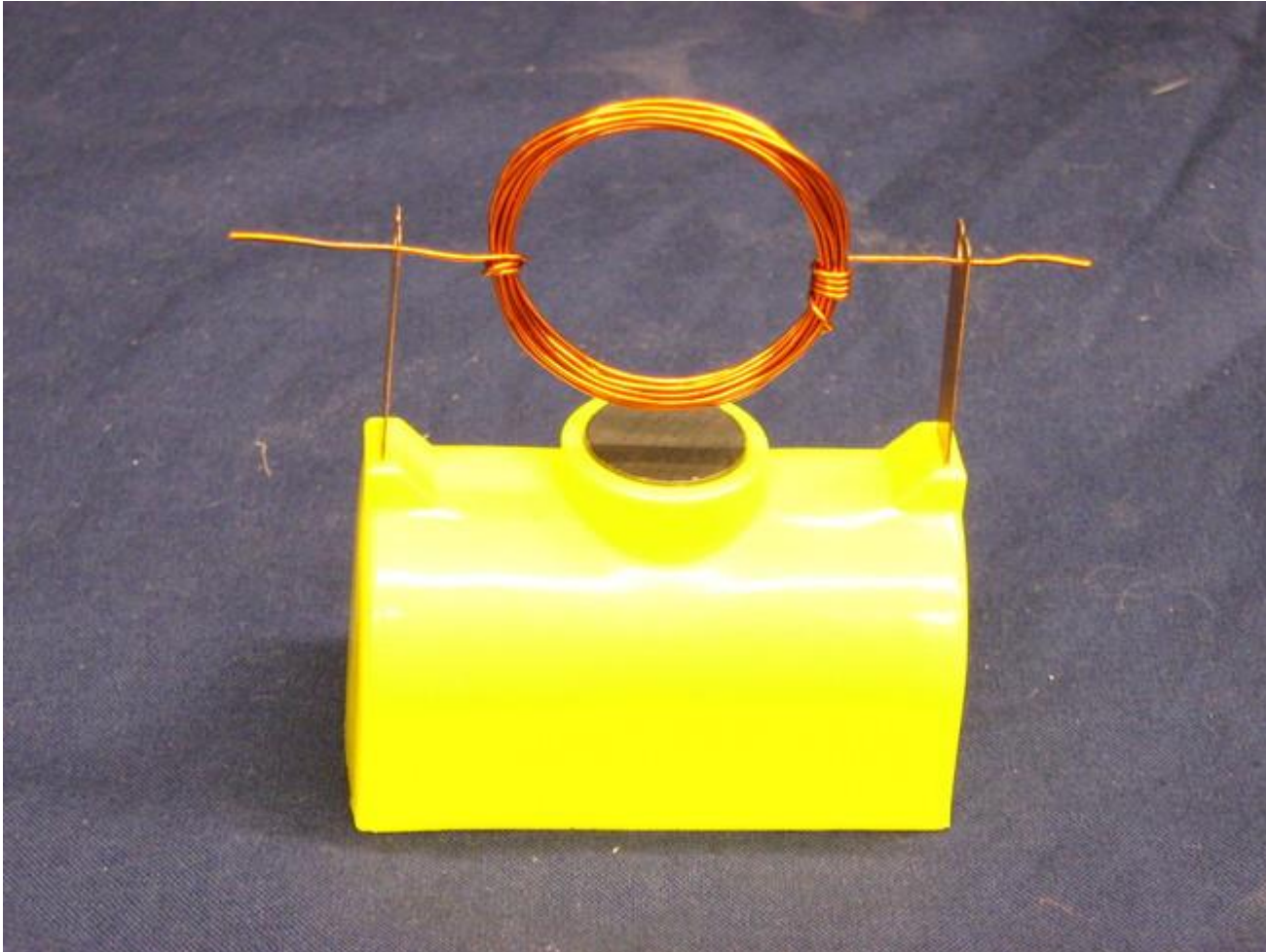
# Torque on a current loop

$$\vec{F}_B = i\vec{\ell} \times \vec{B}$$





# Demonstration

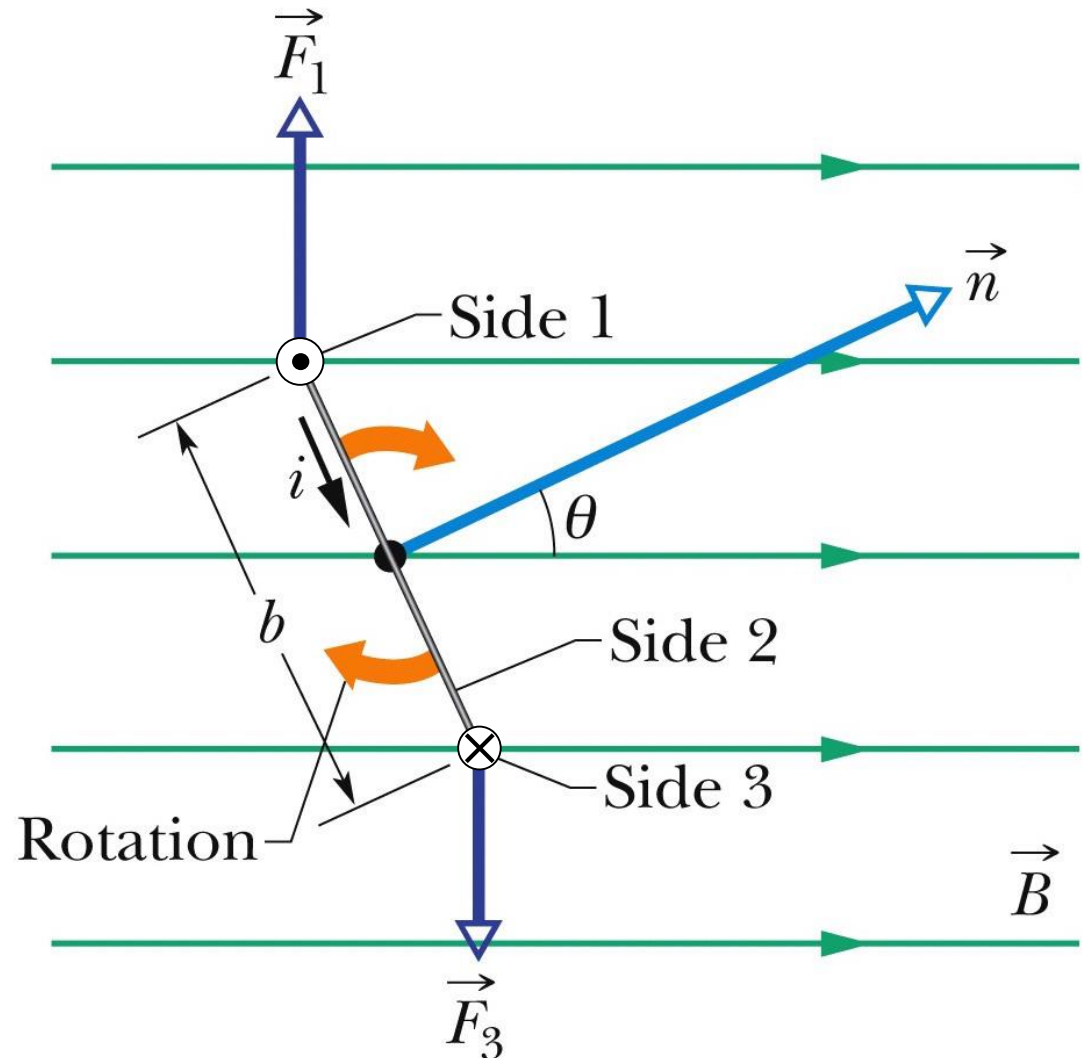
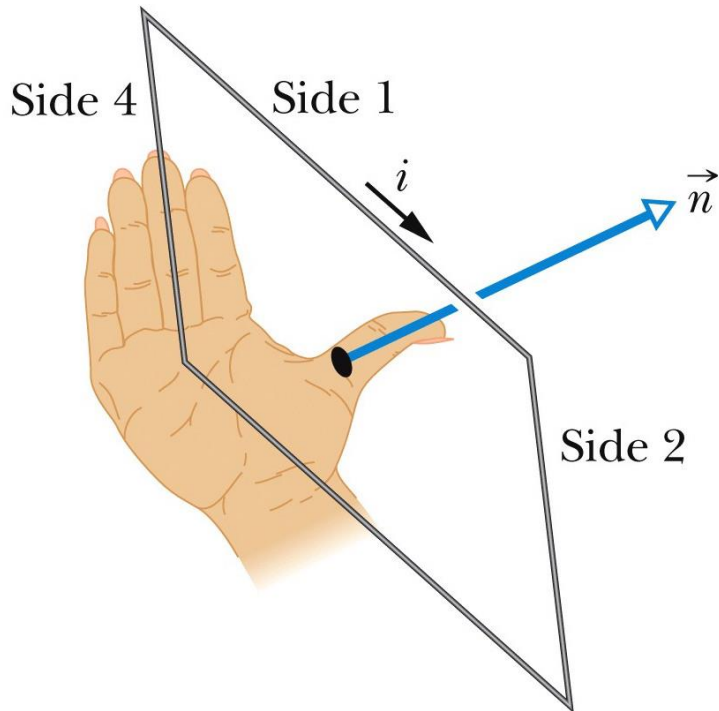


[http://www.phas.ucalgary.ca/files/phas/5k40\\_05\\_worlds\\_simplest\\_motor\\_pic1.jpg](http://www.phas.ucalgary.ca/files/phas/5k40_05_worlds_simplest_motor_pic1.jpg)

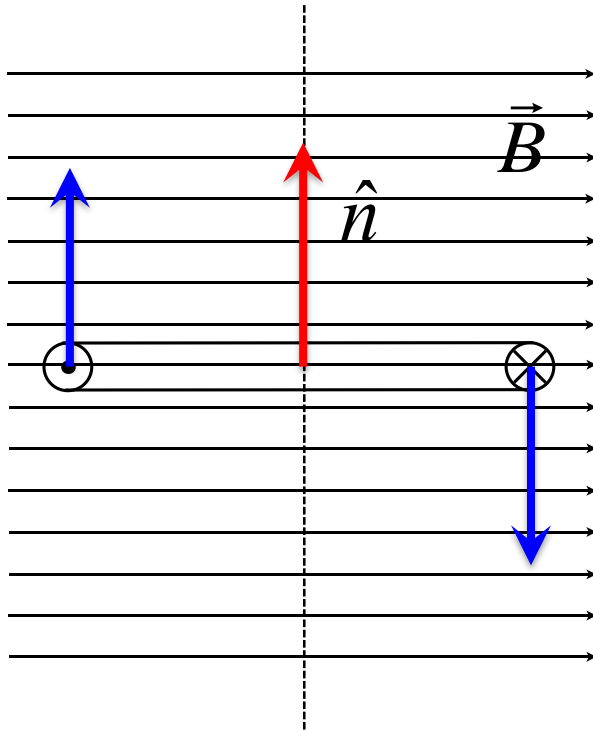


# Torque on a current loop

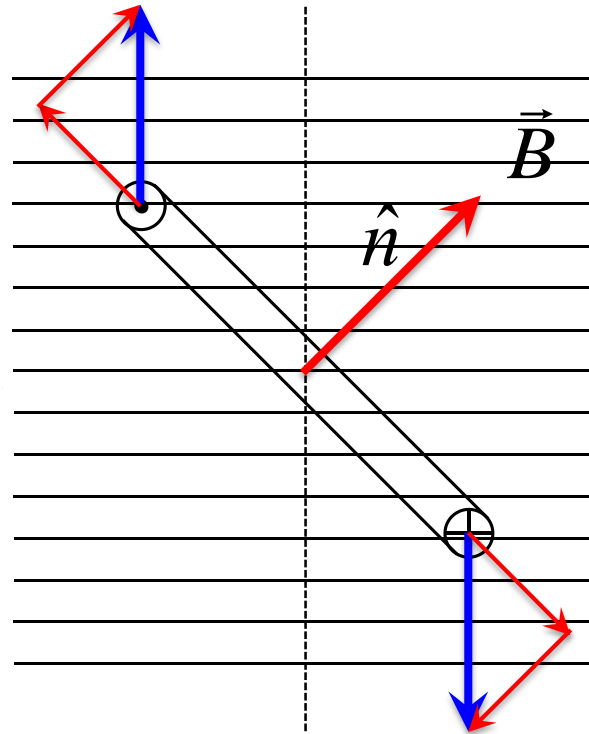
Pick the normal vector to the loop area by RHR: curl your fingers in the direction of  $i$ , thumb points in direction of  $\vec{n}$



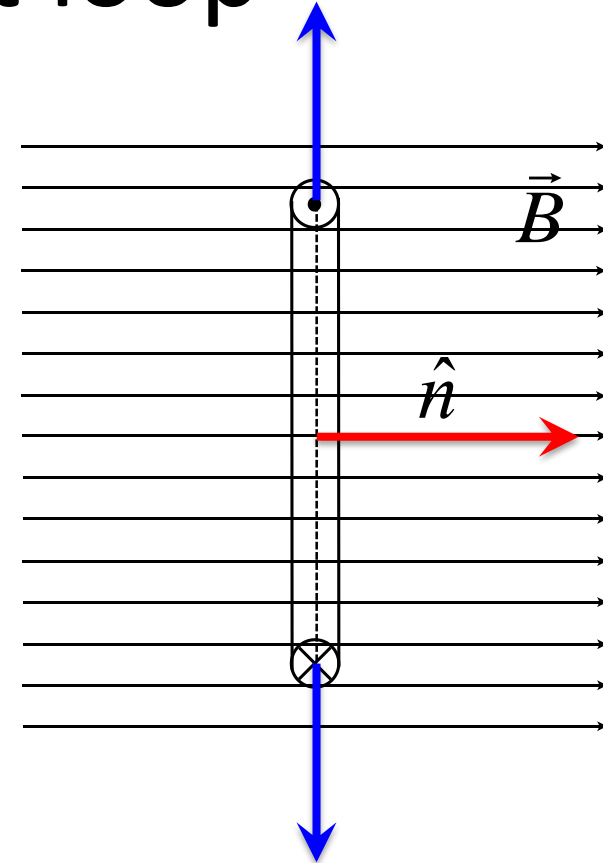
# Torque on a current loop



The normal vector is at right angles to the B-field: all magnetic force causes rotation of the loop



The normal vector is at some angle to the B-field: some of the magnetic force causes rotation of the loop



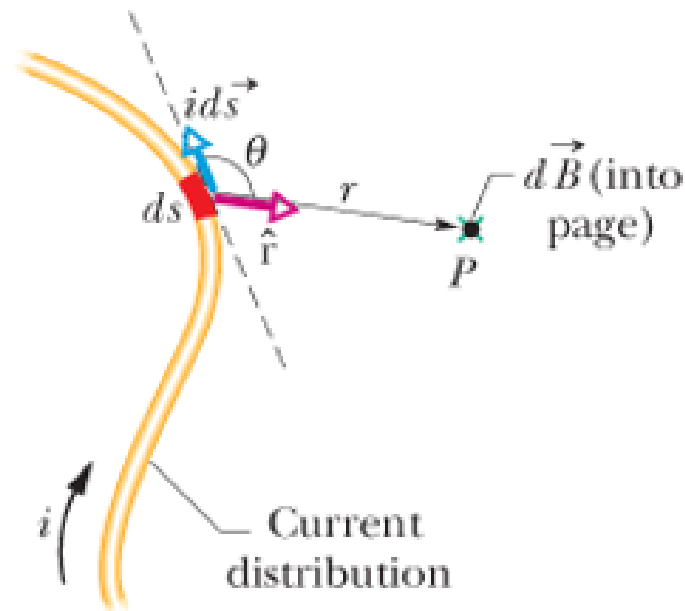
The normal vector is parallel to the B-field: none of the magnetic force causes rotation of the loop

Conclusion: components of magnetic force (anti)parallel to normal vector that cause torque

# The Biot-Savart Law

(Bee-oh Sah-var)

This element of current creates a magnetic field at  $P$ , into the page.



$$\vec{B}_{\text{current segment}} = \frac{\mu_0}{4\pi} \frac{I \Delta \vec{s} \times \hat{r}}{r^2}$$

$$\mu_0 = 4\pi \times 10^{-7} \frac{N \cdot s^2}{C^2}$$

“Permeability of free space”

# Constants of nature

“Permittivity of free space”

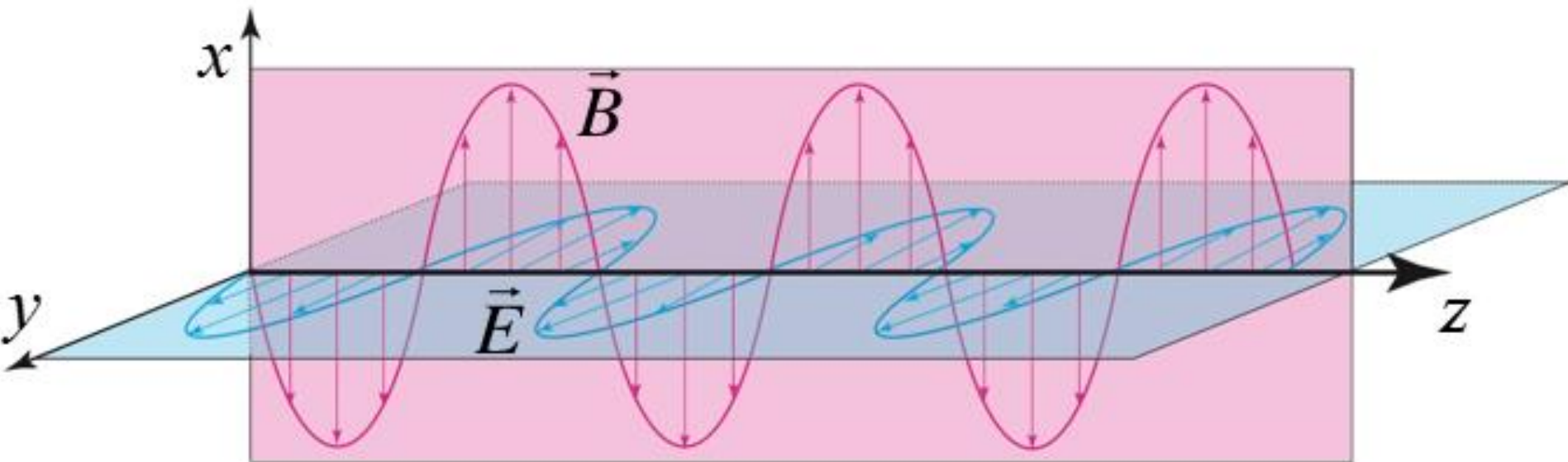
$$\epsilon_0 = 8.85418781719 \times 10^{-12} \frac{C^2}{N \cdot m^2}$$

“Permeability of free space”

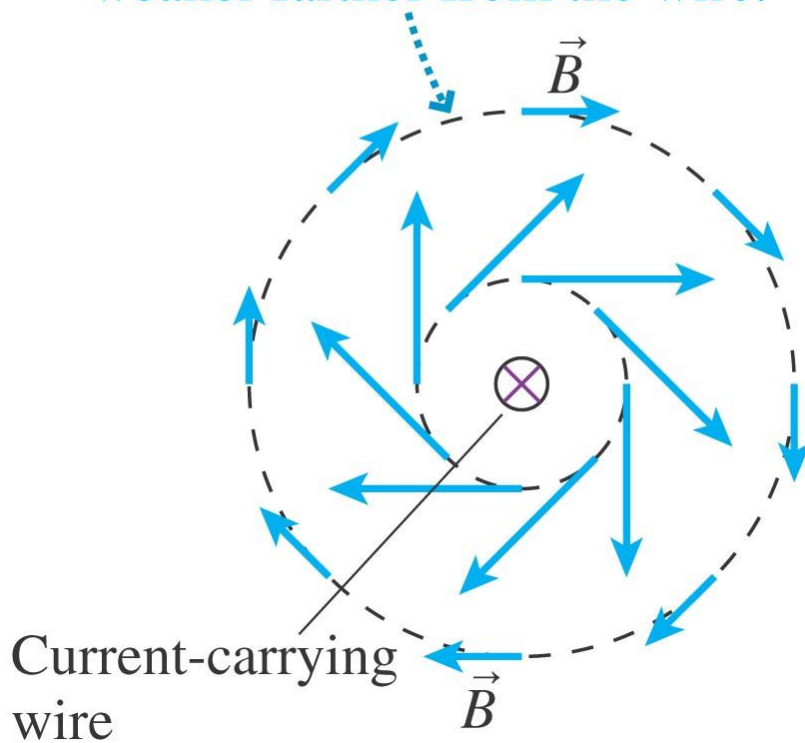
$$\mu_0 = 4\pi \times 10^{-7} \frac{N \cdot s^2}{C^2}$$

$$\frac{1}{\sqrt{\mu_0 \epsilon_0}} = 299,792,458 \text{ m/s}$$

**Speed of light!**

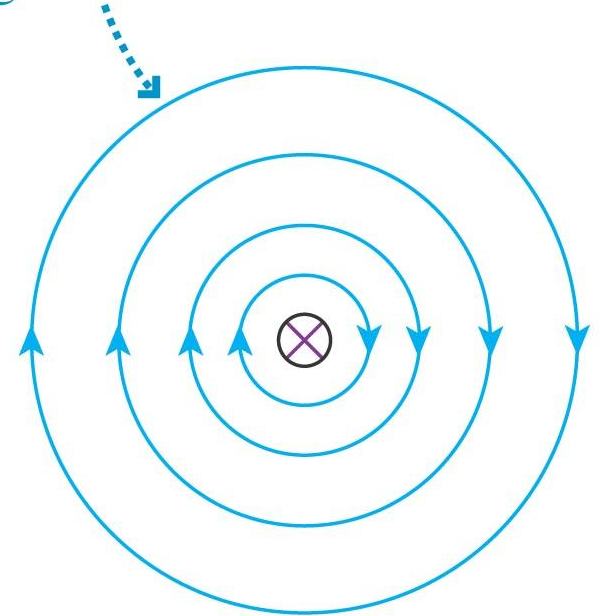


- (a) The magnetic field vectors are tangent to circles around the wire, pointing in the direction given by the right-hand rule. The field is weaker farther from the wire.



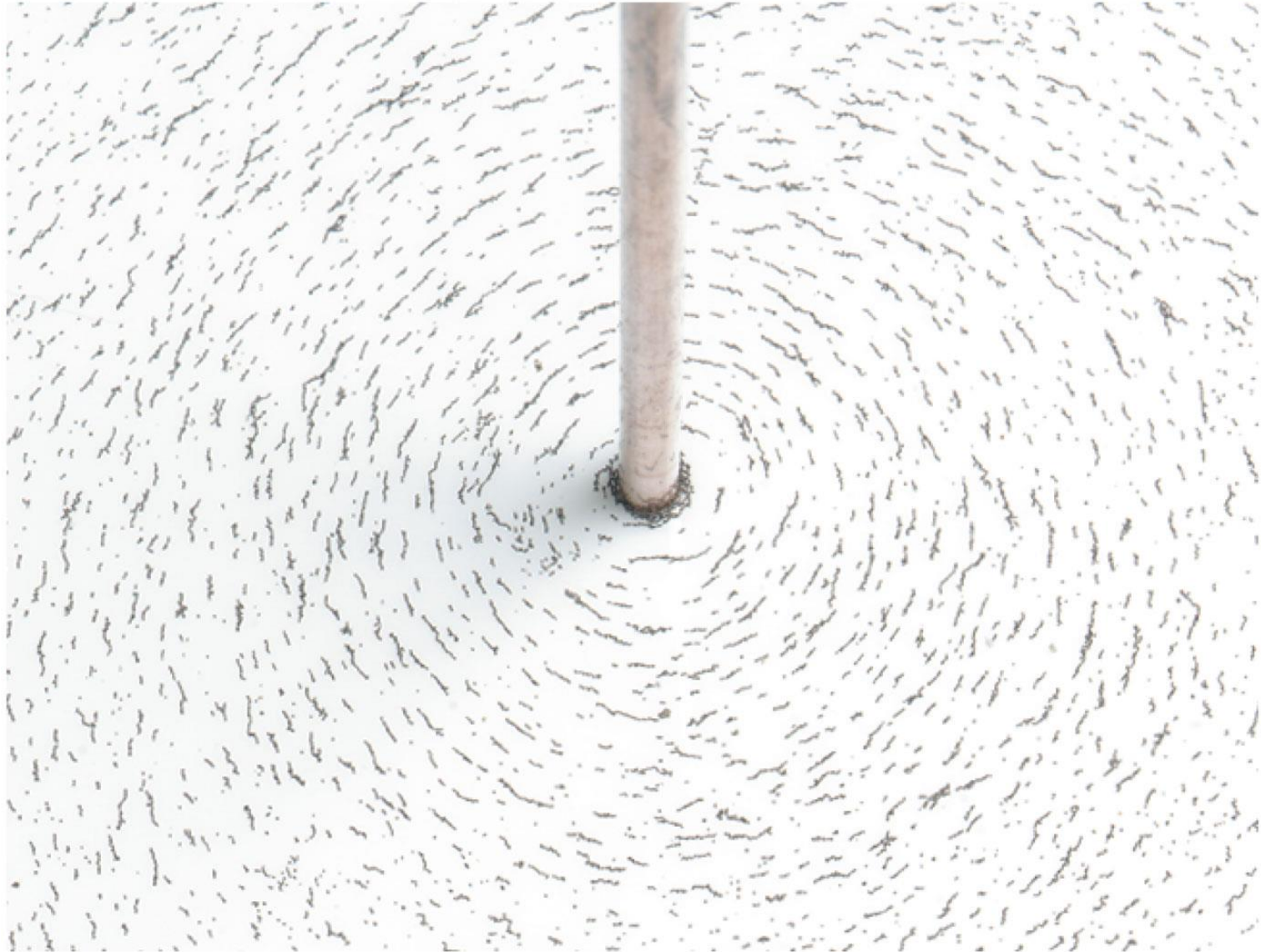
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- (b) Magnetic field lines are circles.

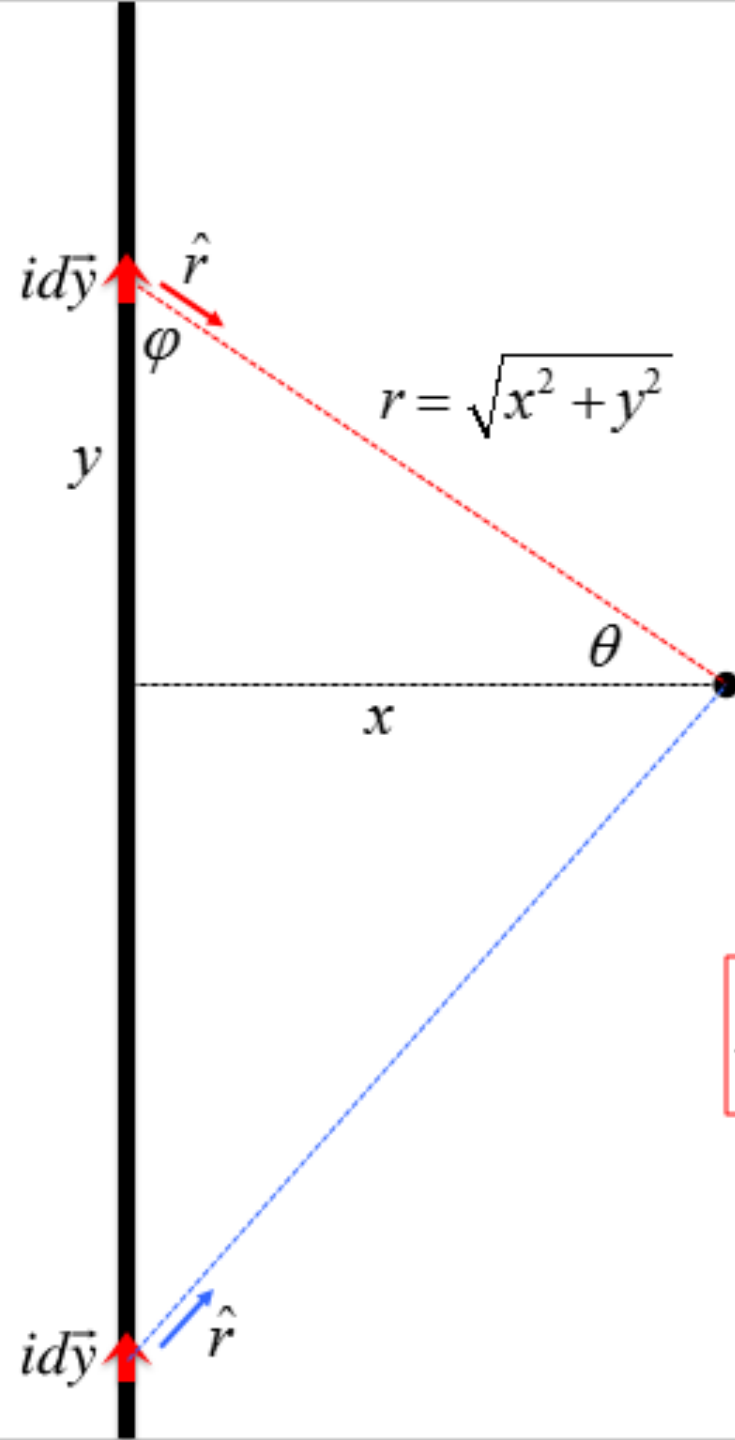


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# Magnetic Field of a Long, Straight Wire







$$d\vec{B} = \frac{\mu_0}{4\pi} \frac{id\vec{y} \times \hat{r}}{r^2}$$

$$id\vec{y} \times \hat{r} = idy \sin \varphi (-\hat{k}) = -idy \frac{x}{\sqrt{x^2 + y^2}} \hat{k}$$

$$d\vec{B} = -\frac{\mu_0}{4\pi} \frac{ixdy}{(x^2 + y^2)^{3/2}} \hat{k}$$

All contributions are in the same direction

$$B = \int_{-\infty}^{\infty} \frac{\mu_0}{4\pi} \frac{ixdy}{(x^2 + y^2)^{3/2}}$$

Can just worry about the magnitude

$$B_{\text{wire}} = \frac{\mu_0 i}{2\pi x}$$

Magnetic field strength of a long straight wire. Direction from RHR



# TopHat Question