

Electricity and Magnetism

- Physics 259 – L02
 - Lecture 22



UNIVERSITY OF
CALGARY

Chapter 24.1: Electric Potential



Last time

- Electric potential energy of a collection of charges
- Electric potential (very important concept)



This time

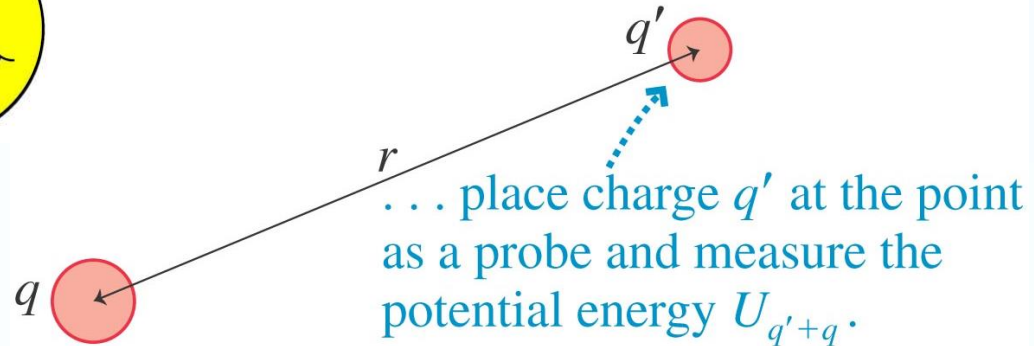
- Equipotential surfaces: visualizing electric potential
- Conductors and electric potential
- Interpreting equipotential surfaces



Starting from the end



The whole story is:



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Electric force on q' from q

$$\vec{F}_{qq'} = \frac{1}{4\pi\epsilon_0} \frac{qq'}{r^2} \hat{r}$$

Then the electric field of q is

$$\vec{E} = \frac{\vec{F}_{qq'}}{q'} = \frac{1}{4\pi\epsilon_0} \frac{q}{r^2} \hat{r}$$

Potential energy of q and q'

$$U_{q'+q} = \frac{1}{4\pi\epsilon_0} \frac{qq'}{r}$$

Then the potential of q is

$$V = \frac{U_{q'+q}}{q'} = \frac{1}{4\pi\epsilon_0} \frac{q}{r}$$

Electric Potential

source
charges



q



Point P

$$V \equiv \frac{U_{q+sources}}{q}$$

$$U_{q+sources} = qV$$

Potential Gradient -- E and V

Note: E is always \perp equipotential lines

$$\vec{E} = -\vec{\nabla}V = -\frac{\partial V}{\partial x}\hat{i} - \frac{\partial V}{\partial y}\hat{j} - \frac{\partial V}{\partial z}\hat{k}$$

In 3 dimensions we must take 3 derivatives, then add them
VECTORIALLY

Alternatively, the potential is found from the electric field integrated along any path connecting points A and B

$$V_{AB} = \int_A^B \vec{E} \cdot d\vec{s}$$

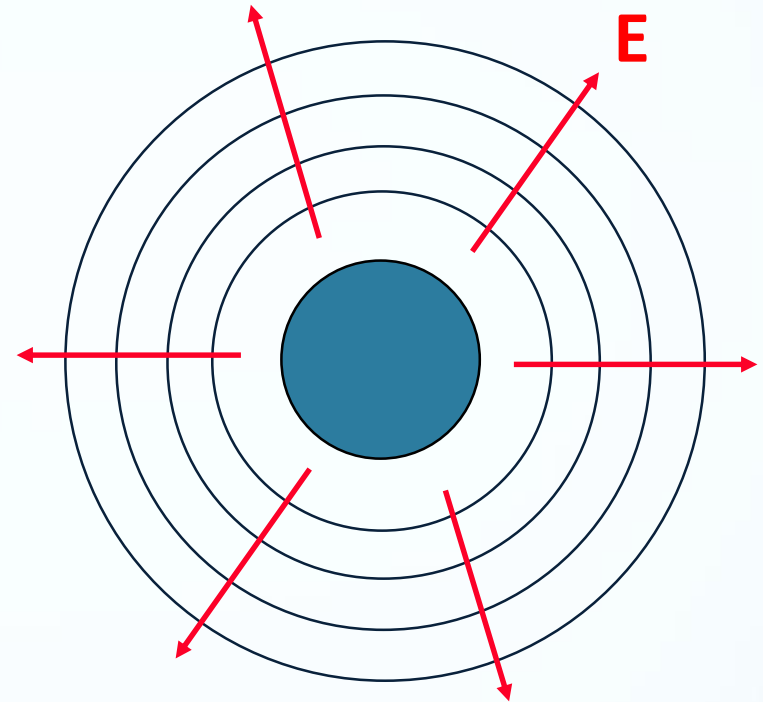
Equipotentials

Ex: For uniform spherical charge

$$V(r) = k Q/r$$

For each r , $V(r)$ is constant →

$V(r)$ is constant over any sphere concentric with the charged sphere

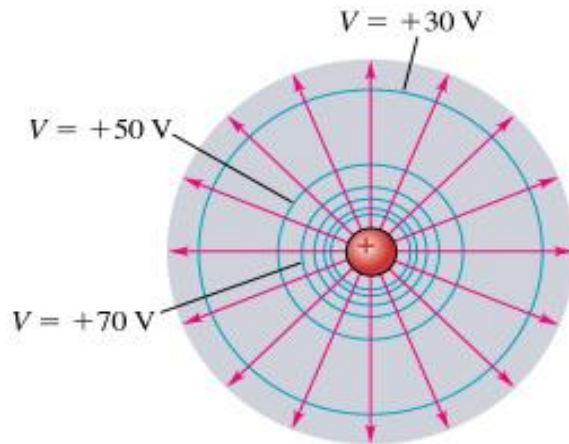


→ We have equipotential lines (or surfaces, actually, in 3-D)

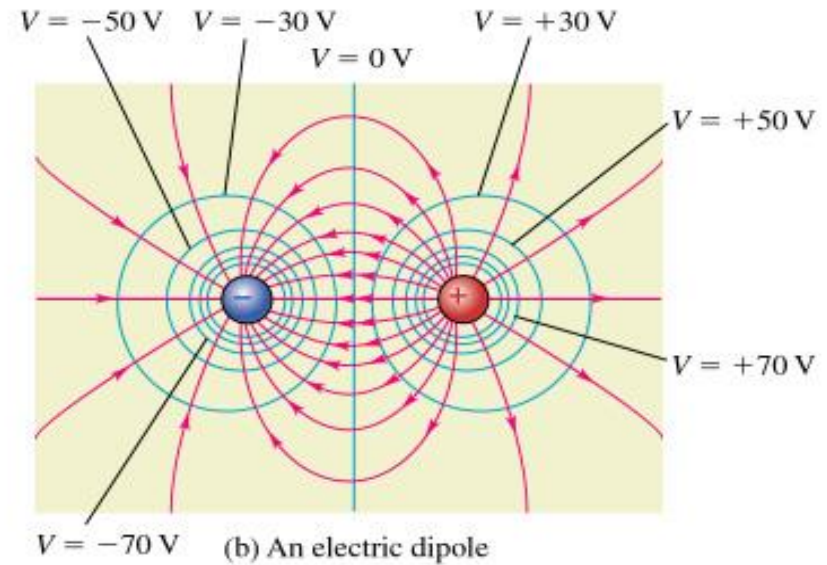
Note that if move along equipotential surface →

→ by definition $\Delta V = - \mathbf{E} \cdot \Delta \mathbf{r} = 0$ --> \mathbf{E} is \perp equipotential surface

Equipotential Surfaces

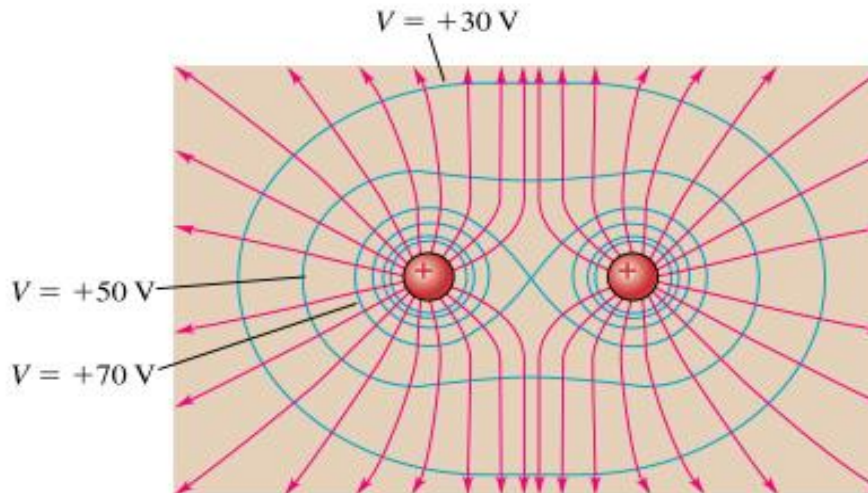


(a) A single positive charge



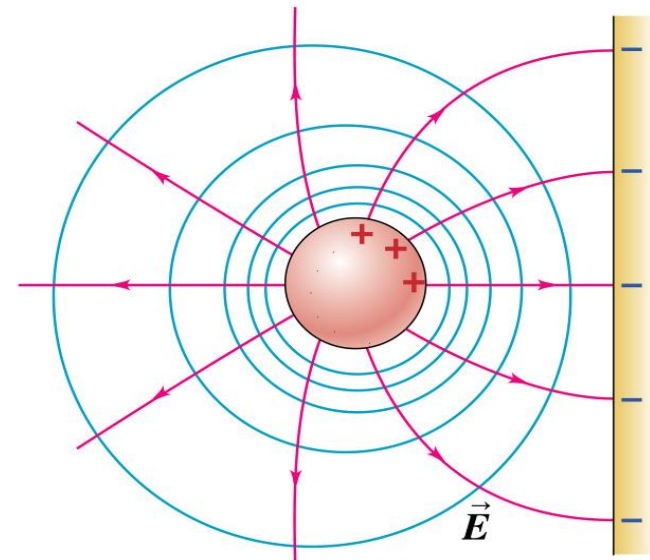
(b) An electric dipole

Note – \vec{E} is always $\perp V$!!



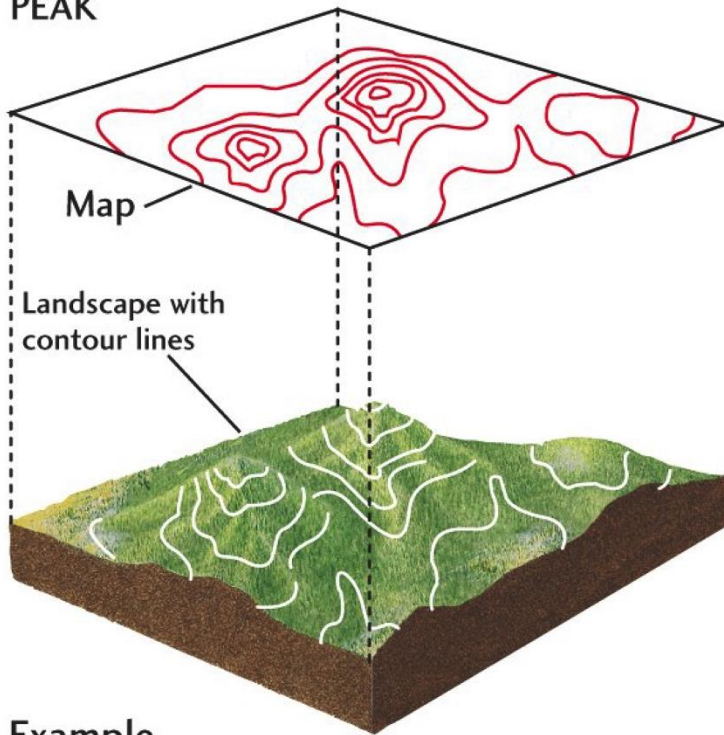
(c) Two equal positive charges

**Conducting sphere
+ sheet**

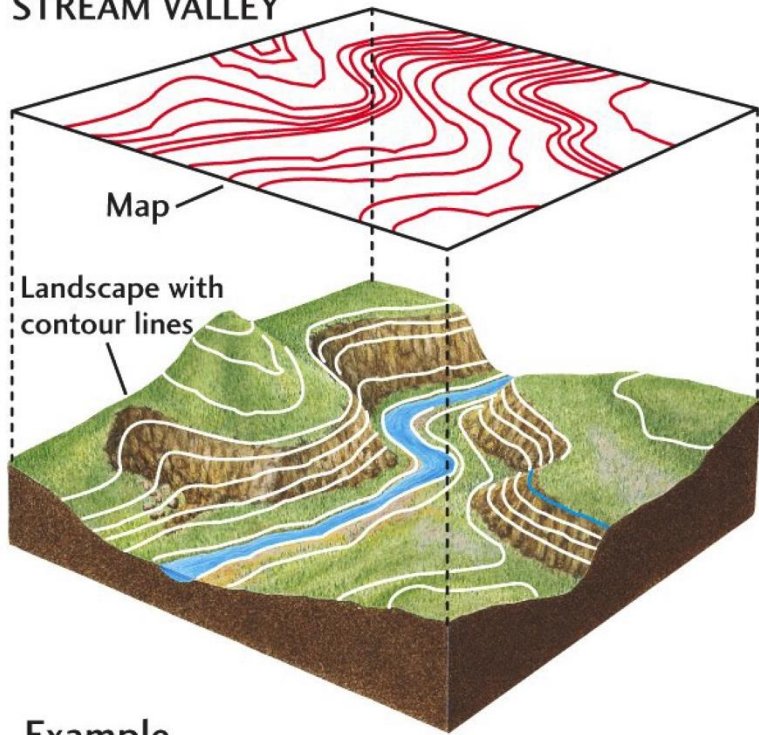


Where have you seen equipotentials before?

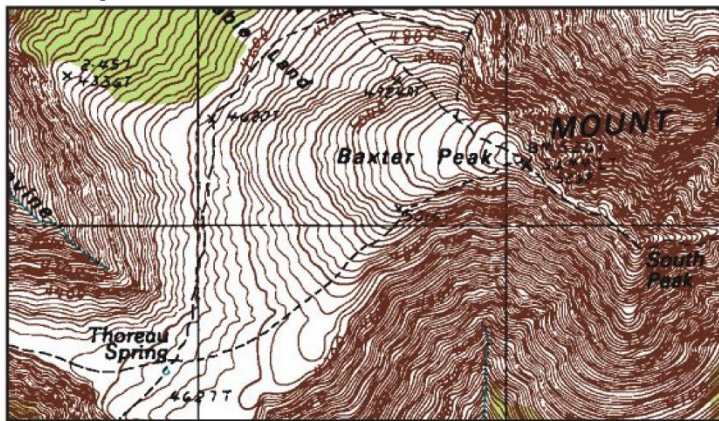
PEAK



STREAM VALLEY

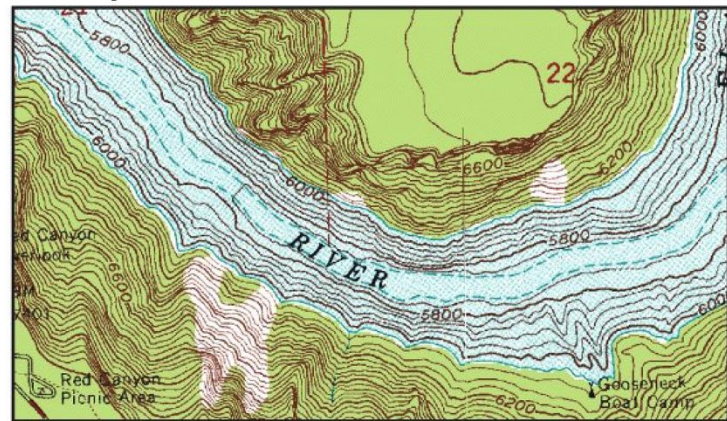


Example



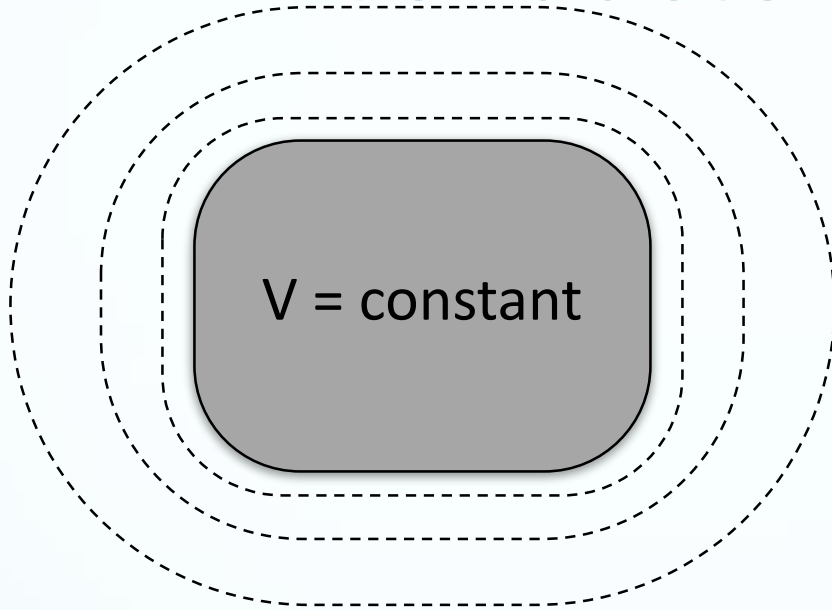
Mt. Katahdin, Maine

Example



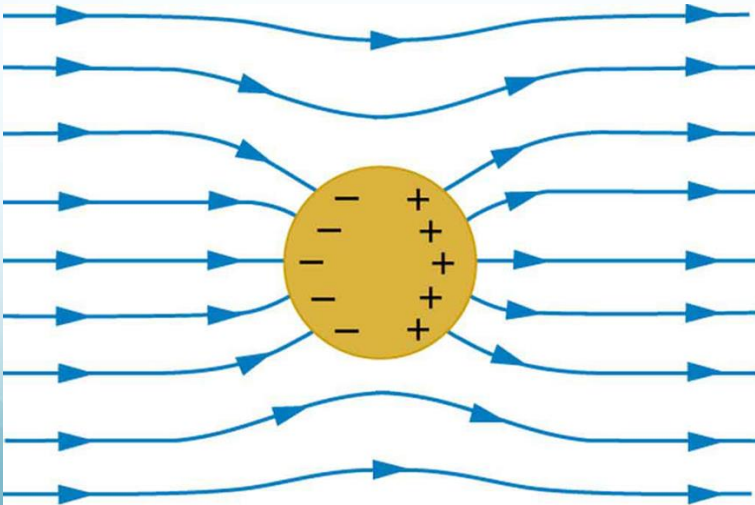
Flaming Gorge, Wyoming

Conductors and E-fields



The surface of a conductor is an equipotential. If there was a potential difference across the surface of a conductor, the freely moving charges would move around until the potential is constant.

This means that electric field lines ALWAYS must meet a conducting surface at right angles (any tangential component would imply a tangential force on the free charges).

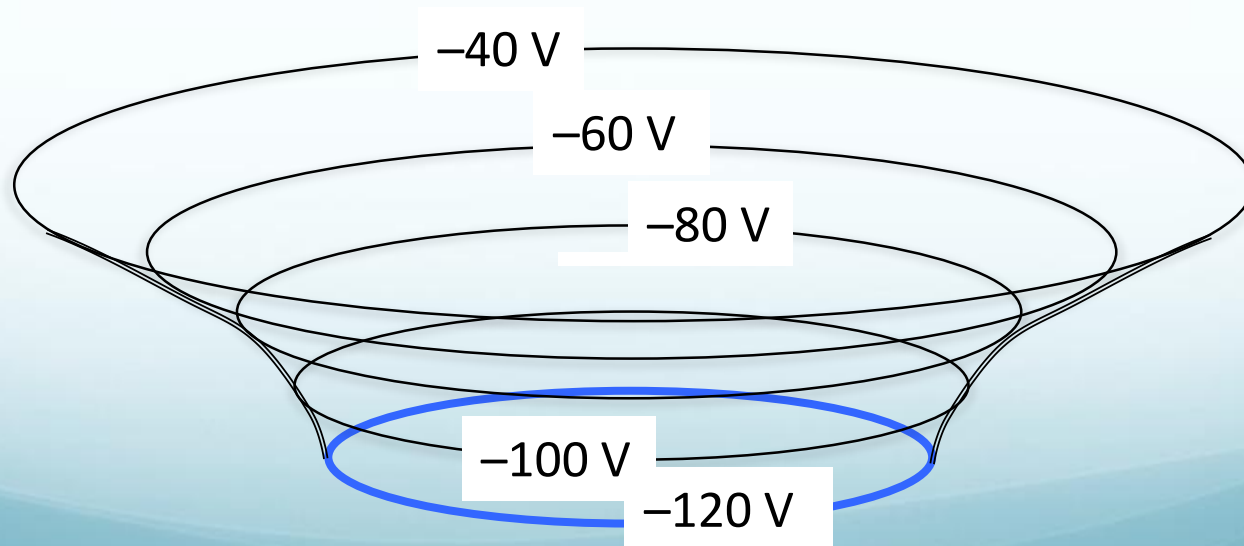


Equipotential surfaces for charged shell

Equipotential surfaces give you information about:

1. the potential energy that charged particles would have:

Think of the electric potential (V) the same way that gravitational potential (gh) is an altitude above sea level. The potential energy of a charge q is then just $U = qV$, while the potential energy of a mass is $U = mgh$.

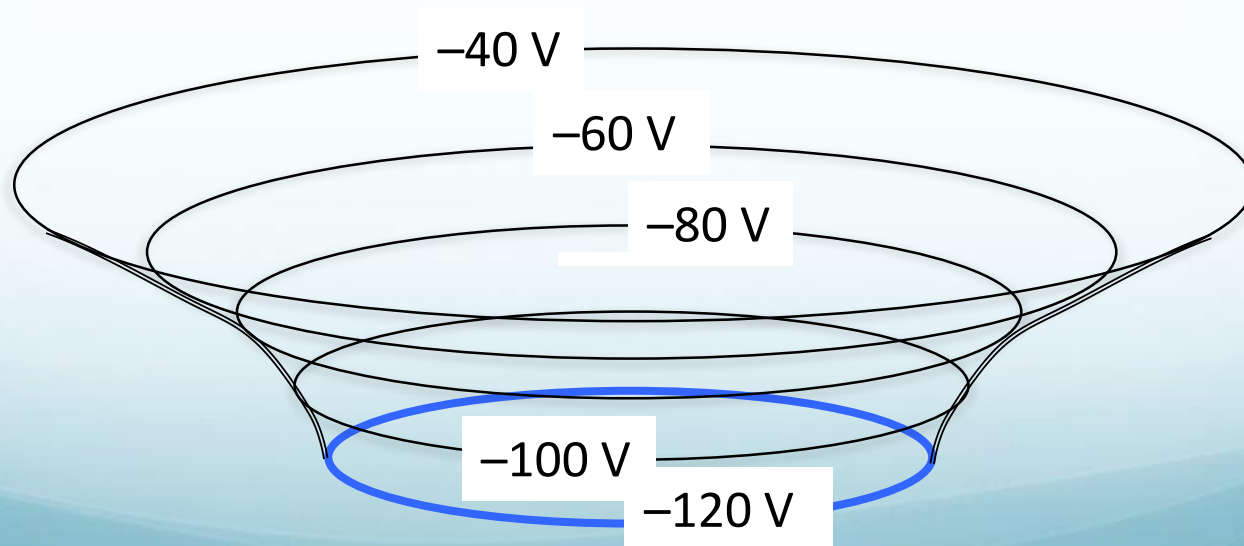


Equipotential surfaces for charged shell

Equipotential surfaces give you information about

2. **the direction of the electric field:**

Just like in the gravitational analogy, objects roll downhill (to lower gravitational potential), positive charges move “downhill” to lower electric potential; the electric field always points “downhill”.

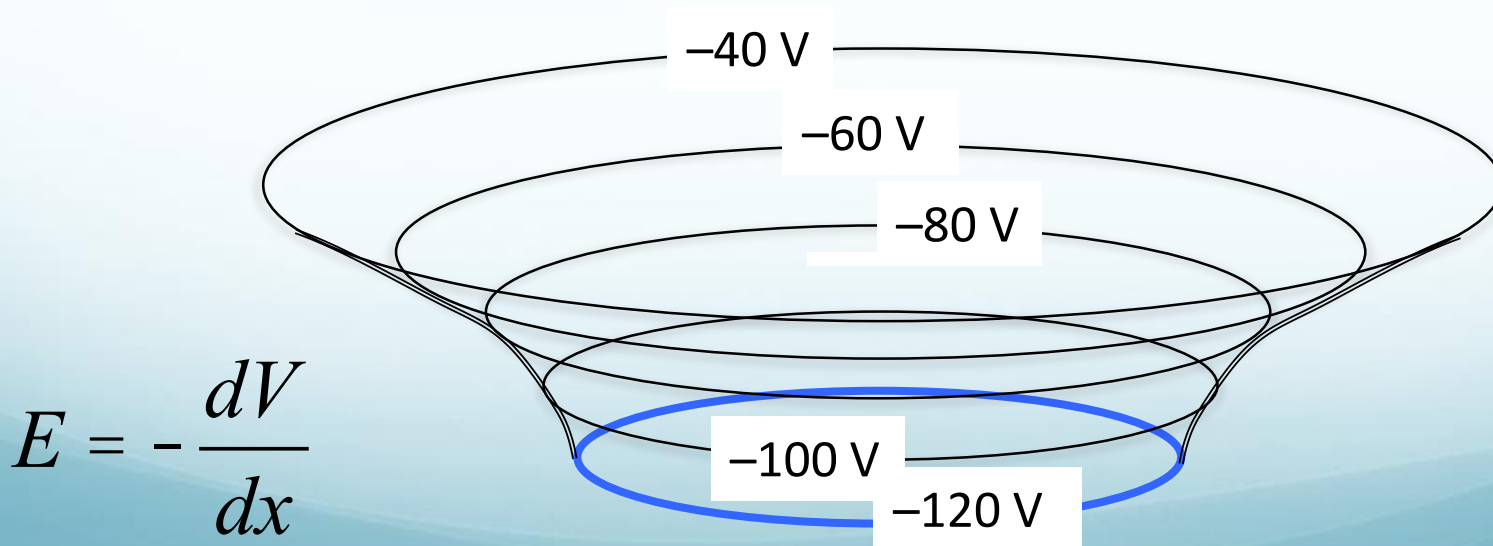


Equipotential surfaces for charged shell

Equipotential surfaces give you information about

3. **the strength of the electric field:**

We know that in the gravitational case, objects on steeper slopes will accelerate faster. Similarly here, the strength of the electric field is related to the slope of $V(x)$. The more bunched together the equipotential lines, the steeper the slope, the stronger the field.

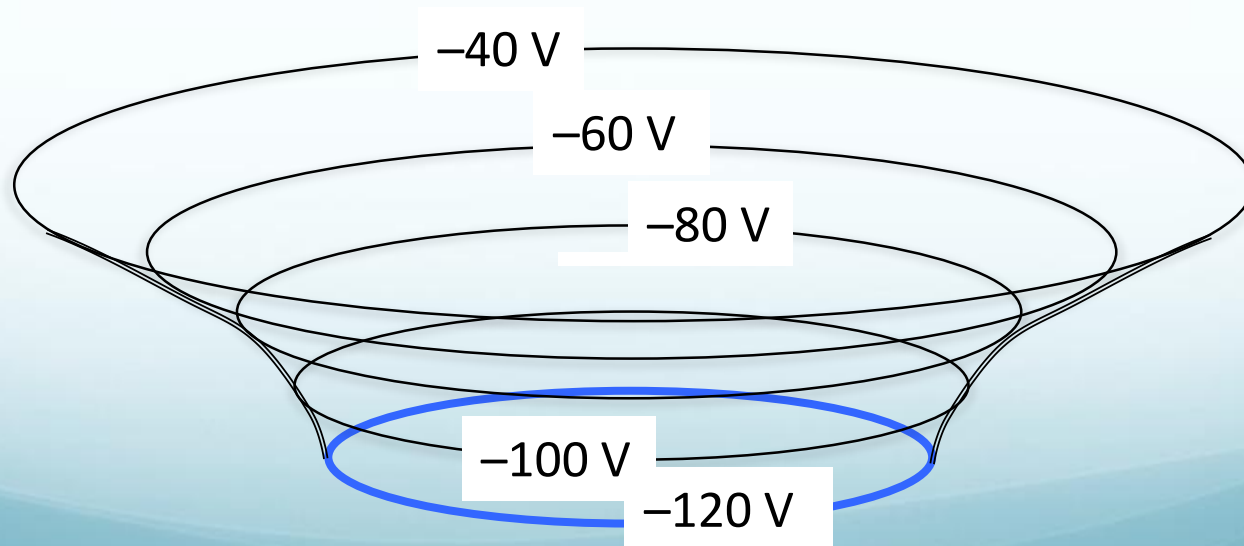


Equipotential surfaces for charged shell

Equipotential surfaces give you information about

4. **where a charged particle is allowed to go, based on its energy:**

If you release a marble in a bowl at some height h , it will never be able to reach a higher height. Similarly, if you release a positive charge from some potential, it can never reach a higher potential unless supplied with extra energy.



This section we talked about:
Chapter 24.1 and 24.2

See you on next Monday

Happy reading week

