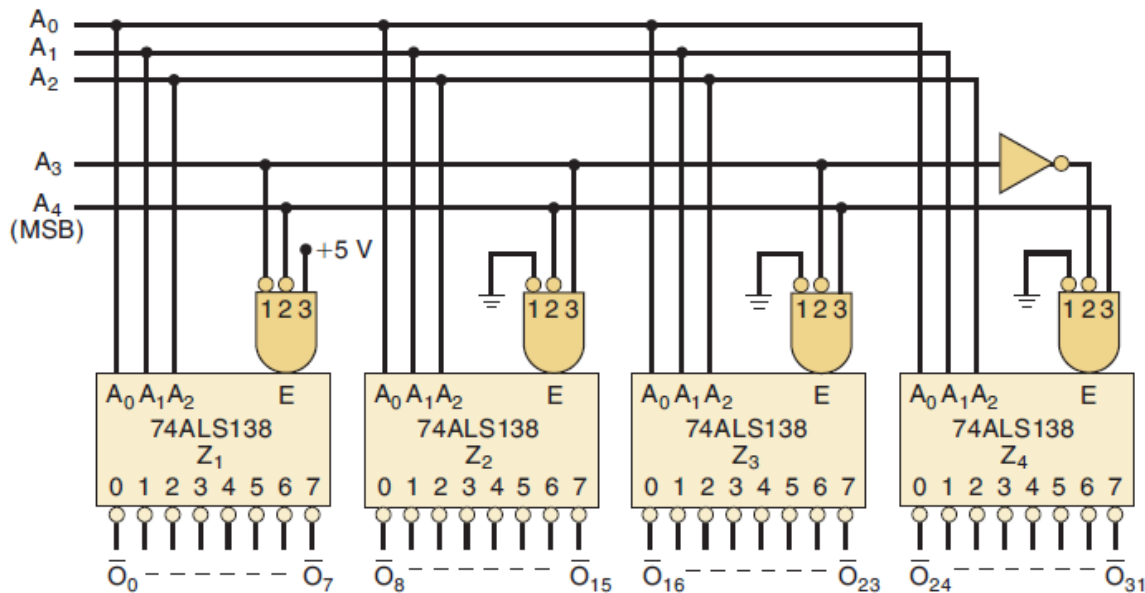


DECODER CIRCUIT

EXAMPLE 9-2

Figure 9-4(a) shows how four 74ALS138s and an INVERTER can be arranged to function as a 1-of-32 decoder. The decoders are labeled Z_1 to Z_4 for easy reference, and the eight outputs from each one are combined into 32 outputs. Z_1 's outputs are \bar{O}_0 to \bar{O}_7 ; Z_2 's outputs \bar{O}_0 to \bar{O}_7 are renamed \bar{O}_8 to \bar{O}_{15} , respectively; Z_3 's outputs are renamed \bar{O}_{16} to \bar{O}_{23} ; and Z_4 's are renamed \bar{O}_{24} to \bar{O}_{31} . A five-bit input code $A_4A_3A_2A_1A_0$ will activate only one of these 32 outputs for each of the 32 possible input codes.

- (a) Which output will be activated for $A_4A_3A_2A_1A_0 = 01101$?
- (b) What range of input codes will activate the Z_4 chip?
- (c) Create a megafunction circuit in Quartus that will implement a 1-of-32 decoder with active-HIGH outputs.

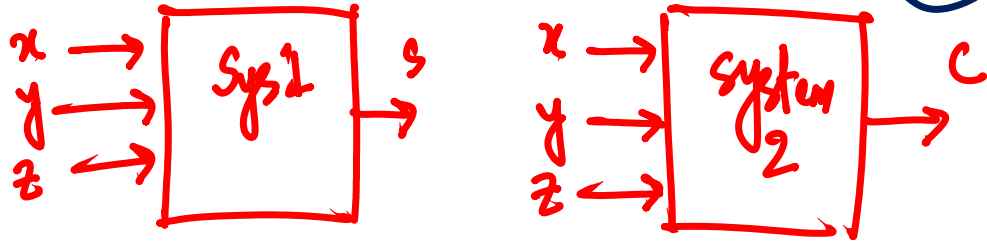


DECODER CIRCUIT

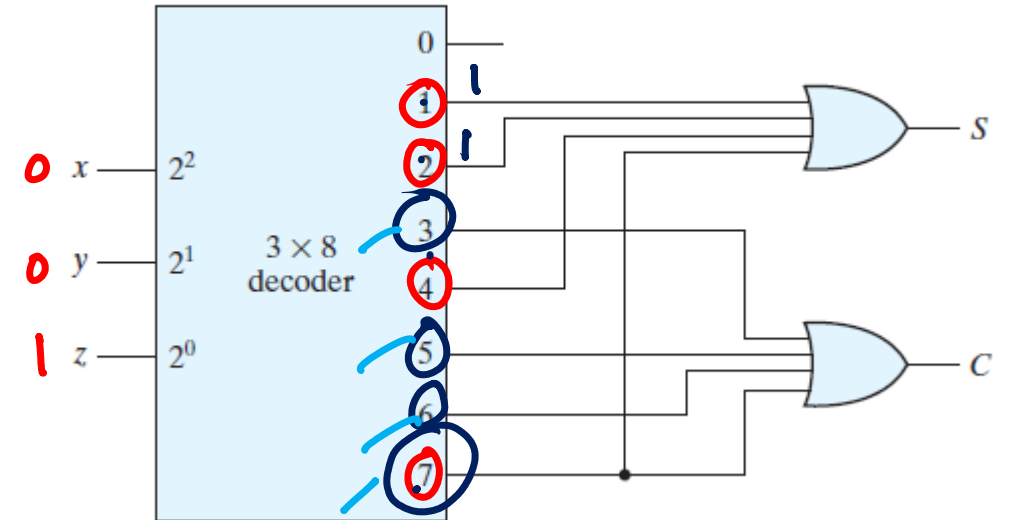
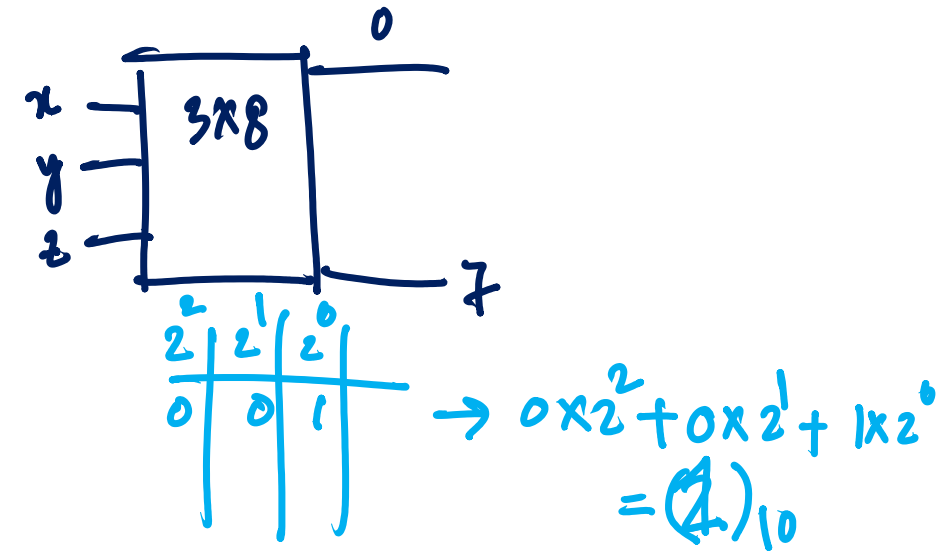
- Combinational logic implementation:

$$S(x, y, z) = \Sigma(1, 2, 4, 7) = m_1 + m_2 + m_4 + m_7$$

$$C(x, y, z) = \Sigma(3, 5, 6, 7) = m_3 + m_5 + m_6 + m_7$$



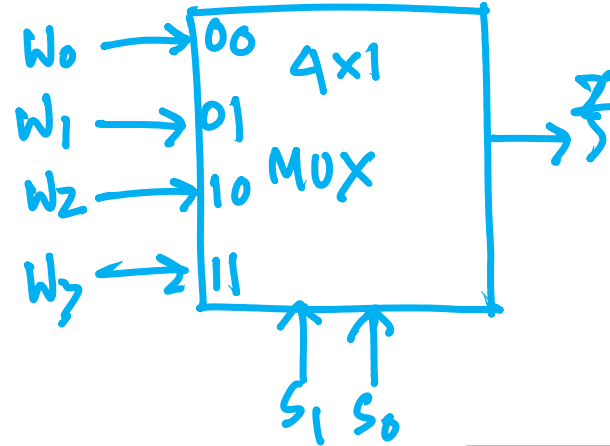
x	y	z	S	C
0	0	0	0	0
0	0	1	1	0
0	1	0	0	0
0	1	1	1	0
1	0	0	0	1
1	0	1	1	1
1	1	0	1	1
1	1	1	1	1



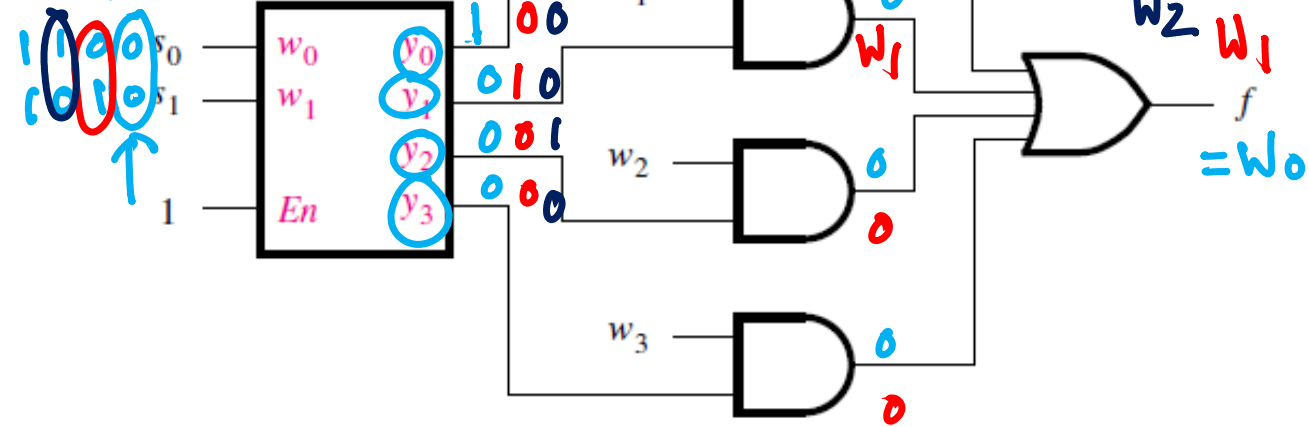
DECODER CIRCUIT

- Multiplexer circuit using decoder:

s_1	s_0	f
→ 0	0	w_0
→ 0	1	w_1
→ 1	0	w_2
1	1	w_3



$$f = \bar{s}_1 \bar{s}_0 w_0 + \bar{s}_1 s_0 w_1 + s_1 \bar{s}_0 w_2 + s_1 s_0 w_3$$



DECODER CIRCUIT

$$+V_{CC} = 5V \rightarrow 1$$

$$\frac{1}{\text{ground}} = 0V \rightarrow 0$$

LED \rightarrow Light emitting diode.

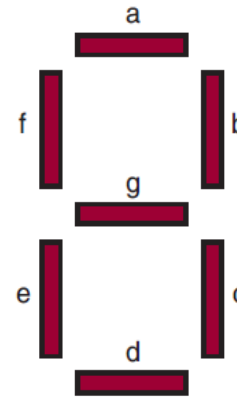
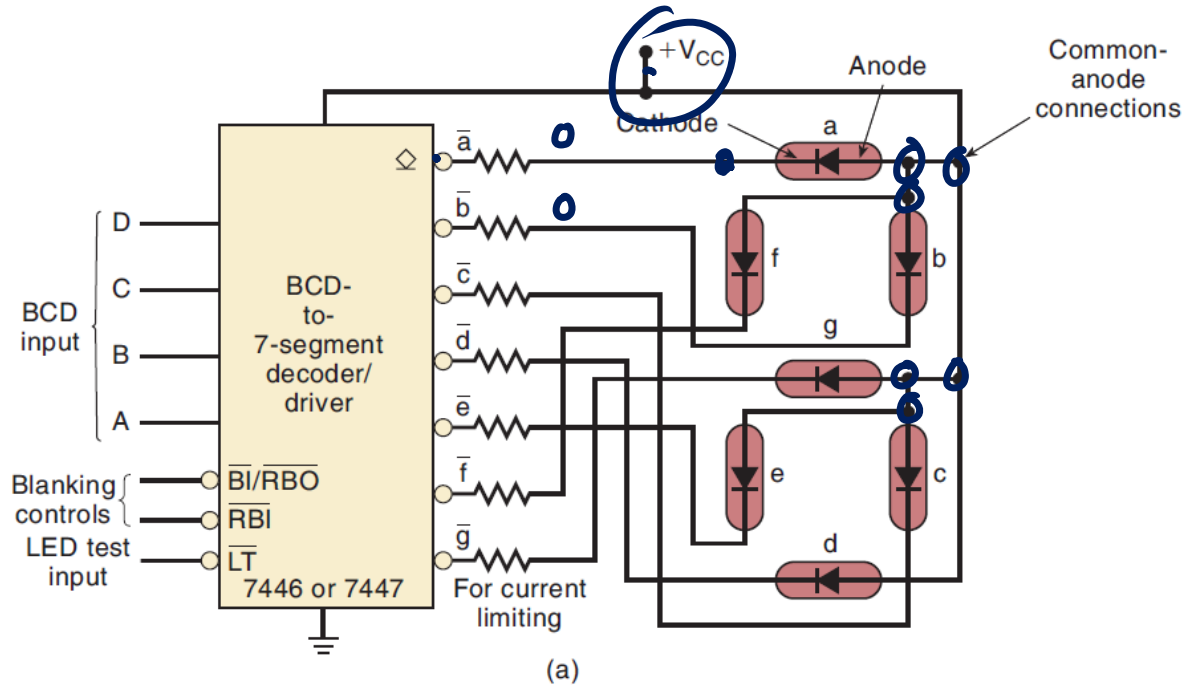
- BCD to 7 segment decoder (common anode connection):



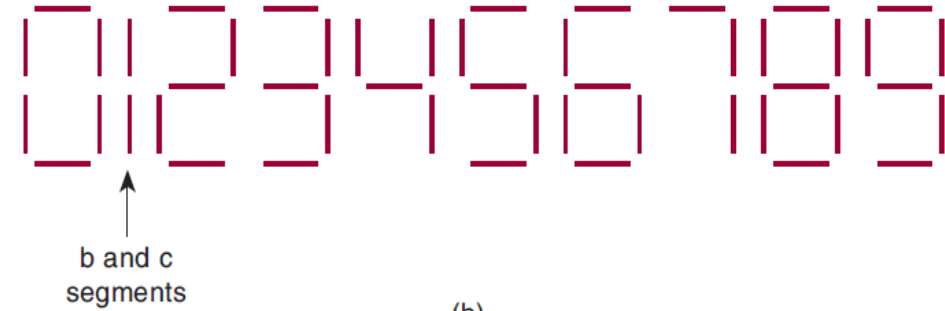
$$V_A > V_K$$

$$V_A = +V_{CC} = 1$$

$$V_K = \frac{1}{\text{ground}} = 0$$



(a)

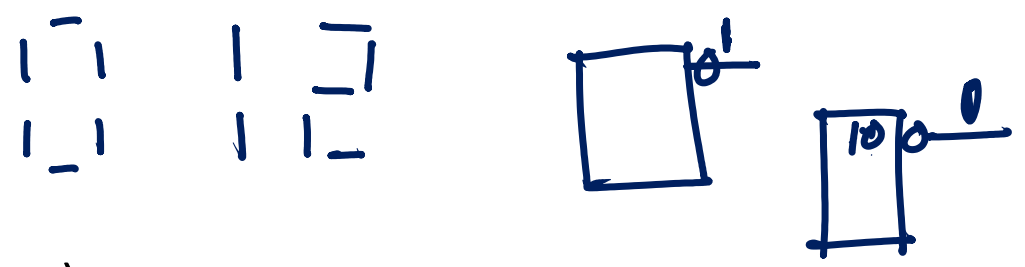


(b)

0	1	2	3	4	5	6	7	8	9	c	3	4	5	6	7	8	9
0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15		

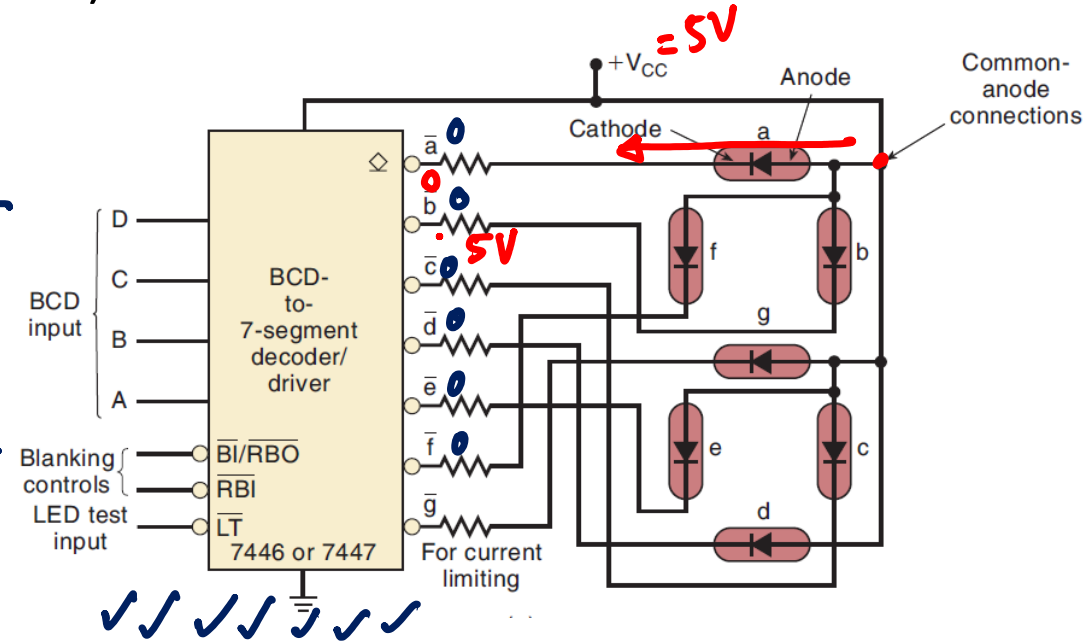
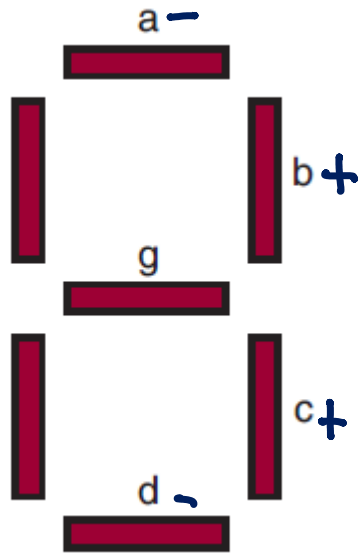


DECODER CIRCUIT



- BCD to 7 segment decoder (common anode connection):

Decimal	a	b	c	d	e	f	g
0	0	0	0	0	0	0	1
1	1	0	0	1	1	1	1
2	0	0	1	0	0	1	0
3	0	0	0	0	1	1	0
4	1	0	0	1	1	0	0
5	0	1	0	0	1	0	0
6	1	1	0	0	0	0	0
7	0	0	0	0	1	1	1
8	0	0	0	0	0	0	0
9	0	0	0	0	1	0	0



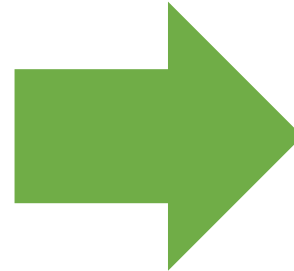
Decimal	A	B	C	D	a	b	c	d	e	f	g
10	1	0	1	0	X	X	X	X	X	X	X
11	1	0	1	1	X	X	X	X	X	X	X
12	1	1	0	0	X	X	X	X	X	X	X
13	1	1	0	1	X	X	X	X	X	X	X
14	1	1	1	0	X	X	X	X	X	X	X
15	1	1	1	1	X	X	X	X	X	X	X

$$\begin{aligned}
 a &= \prod M(0, 2, 3, 5, 7, 8, 9) \prod d(10, 11, 12, 13, 14, 15) \\
 b &= \prod M(0, 1, 2, 3, 4, 7, 8, 9) \prod d(10, 11, 12, 13, 14, 15) \\
 c &= \prod M(0, 1, 3, 4, 5, 6, 7, 8, 9) \prod d(10, 11, 12, 13, 14, 15) \\
 d &= \prod M(0, 2, 3, 5, 6, 8) \prod d(10, 11, 12, 13, 14, 15) \\
 e &= \prod M(0, 2, 6, 8, 9) \prod d(10, 11, 12, 13, 14, 15) \\
 f &= \prod M(0, 4, 5, 6, 8, 9) \prod d(10, 11, 12, 13, 14, 15) \\
 g &= \prod M(2, 3, 4, 5, 6, 8, 9) \prod d(10, 11, 12, 13, 14, 15)
 \end{aligned}$$

DECODER CIRCUIT

- BCD to 7 segment decoder (common anode connection):

$$\begin{aligned}
 a &= \prod M(0, 2, 3, 5, 7, 8, 9) \prod d(10, 11, 12, 13, 14, 15) \\
 b &= \prod M(0, 1, 2, 3, 4, 7, 8, 9) \prod d(10, 11, 12, 13, 14, 15) \\
 c &= \prod M(0, 1, 3, 4, 5, 6, 7, 8, 9) \prod d(10, 11, 12, 13, 14, 15) \\
 d &= \prod M(0, 2, 3, 5, 6, 8) \prod d(10, 11, 12, 13, 14, 15) \\
 e &= \prod M(0, 2, 6, 8, 9) \prod d(10, 11, 12, 13, 14, 15) \\
 f &= \prod M(0, 4, 5, 6, 8, 9) \prod d(10, 11, 12, 13, 14, 15) \\
 g &= \prod M(2, 3, 4, 5, 6, 8, 9) \prod d(10, 11, 12, 13, 14, 15)
 \end{aligned}$$



$$\begin{aligned}
 a &= A(B + D)(B + C)(B + D) \\
 b &= B(\bar{C} + \bar{D})(C + D) \\
 c &= \bar{B}C\bar{D} \\
 d &= (\bar{C} + D)(B + \bar{C})(\bar{B} + C + \bar{D})(B + D) \\
 e &= (\bar{C} + D)(B + D) \\
 f &= \bar{A}(C + D)(\bar{B} + C)(\bar{B} + D) \\
 g &= \bar{A}(\bar{B} + C)(\bar{C} + D)(B + \bar{C})
 \end{aligned}$$

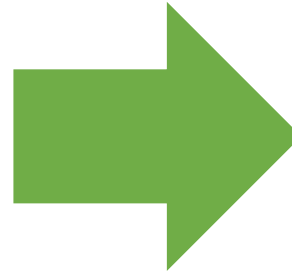
A \ B	CD			
	00	01	11	10
00				
01				
11				
10				

A \ B	CD			
	00	01	11	10
00				
01				
11				
10				

DECODER CIRCUIT

- BCD to 7 segment decoder (common anode connection):

$$\begin{aligned}
 a &= \prod M(0, 2, 3, 5, 7, 8, 9) \prod d(10, 11, 12, 13, 14, 15) \\
 b &= \prod M(0, 1, 2, 3, 4, 7, 8, 9) \prod d(10, 11, 12, 13, 14, 15) \\
 c &= \prod M(0, 1, 3, 4, 5, 6, 7, 8, 9) \prod d(10, 11, 12, 13, 14, 15) \\
 d &= \prod M(0, 2, 3, 5, 6, 8) \prod d(10, 11, 12, 13, 14, 15) \\
 e &= \prod M(0, 2, 6, 8, 9) \prod d(10, 11, 12, 13, 14, 15) \\
 f &= \prod M(0, 4, 5, 6, 8, 9) \prod d(10, 11, 12, 13, 14, 15) \\
 g &= \prod M(2, 3, 4, 5, 6, 8, 9) \prod d(10, 11, 12, 13, 14, 15)
 \end{aligned}$$



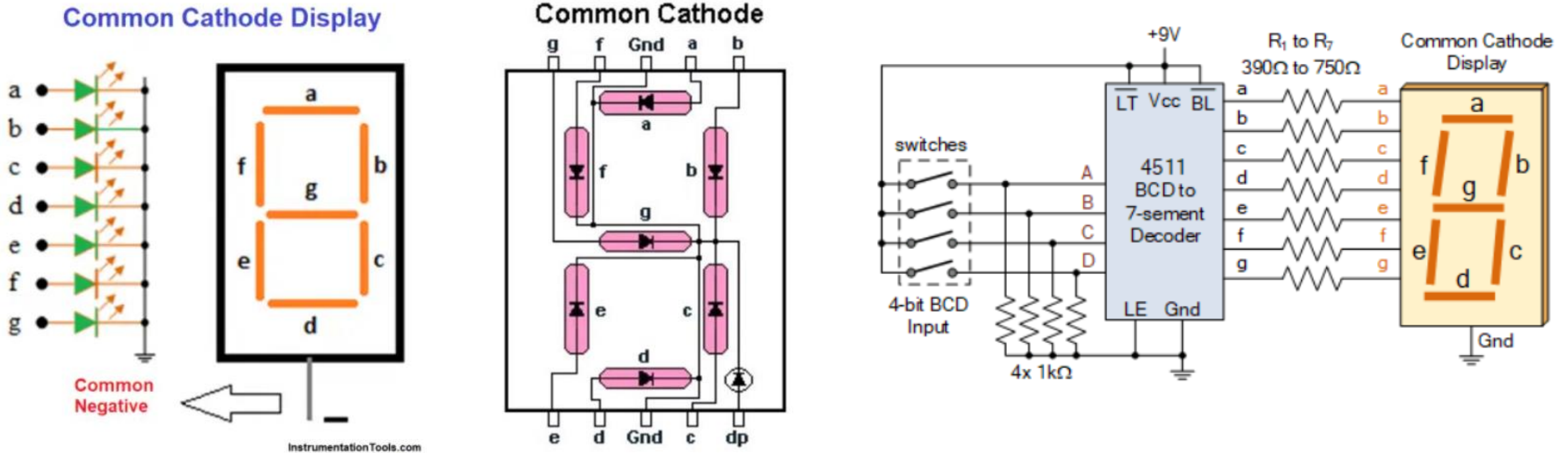
$$\begin{aligned}
 a &= A(B + D)(B + C)(B + D) \\
 b &= B(\bar{C} + \bar{D})(C + D) \\
 c &= \bar{B}C\bar{D} \\
 d &= (\bar{C} + D)(B + \bar{C})(\bar{B} + C + \bar{D})(B + D) \\
 e &= (\bar{C} + D)(B + D) \\
 f &= \bar{A}(C + D)(\bar{B} + C)(\bar{B} + D) \\
 g &= \bar{A}(\bar{B} + C)(\bar{C} + D)(B + \bar{C})
 \end{aligned}$$

A \ B	CD			
	00	01	11	10
00				
01				
11				
10				

A \ B	CD			
	00	01	11	10
00				
01				
11				
10				

DECODER CIRCUIT

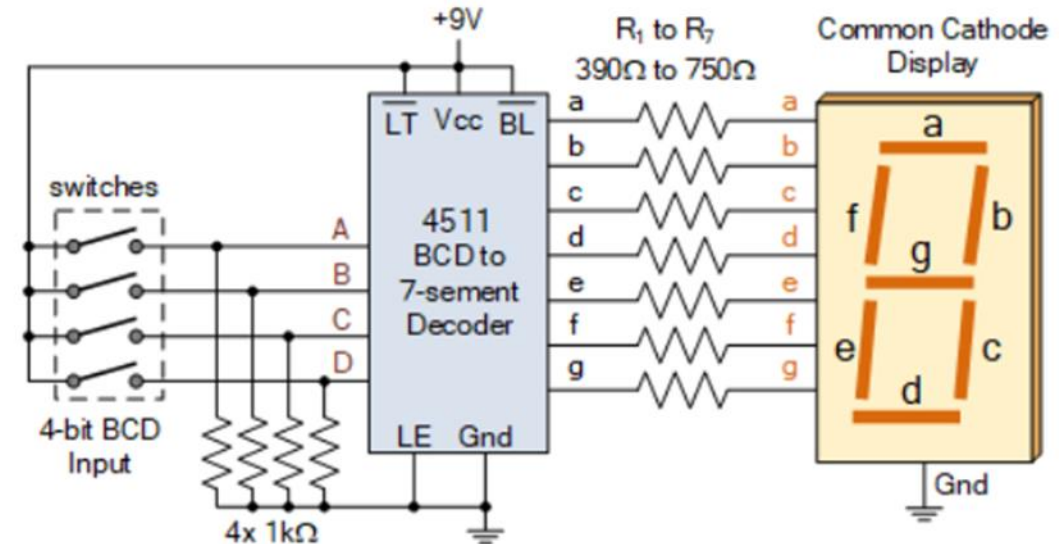
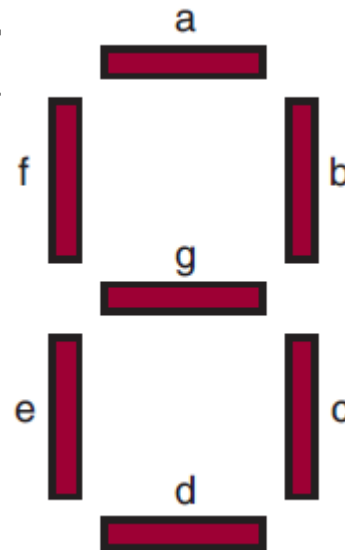
- BCD to 7 segment decoder (common cathode connection):



DECODER CIRCUIT

- BCD to 7 segment decoder (common cathode connection):

Decimal	<i>a</i>	<i>b</i>	<i>c</i>	<i>d</i>	<i>e</i>	<i>f</i>	<i>g</i>
0	1	1	1	1	1	1	0
1	0	1	1	0	0	0	0
2	1	1	0	1	1	0	1
3	1	1	1	1	0	0	1
4	0	1	1	1	0	1	1
5	1	0	1	1	0	1	1
6	1	0	1	1	1	1	1
7	1	1	1	1	0	0	0
8	1	1	1	1	1	1	1
9	1	1	1	1	0	1	1



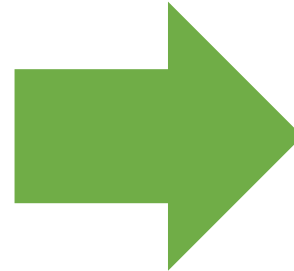
Decimal	<i>A</i>	<i>B</i>	<i>C</i>	<i>D</i>	<i>a</i>	<i>b</i>	<i>c</i>	<i>d</i>	<i>e</i>	<i>f</i>	<i>g</i>
10	1	0	1	0	X	X	X	X	X	X	X
11	1	0	1	1	X	X	X	X	X	X	X
12	1	1	0	0	X	X	X	X	X	X	X
13	1	1	0	1	X	X	X	X	X	X	X
14	1	1	1	0	X	X	X	X	X	X	X
15	1	1	1	1	X	X	X	X	X	X	X

$$\begin{aligned}
 a &= \sum m(0, 2, 3, 5, 7, 8, 9) + \sum d(10, 11, 12, 13, 14, 15) \\
 b &= \sum m(0, 1, 2, 3, 4, 7, 8, 9) + \sum d(10, 11, 12, 13, 14, 15) \\
 c &= \sum m(0, 1, 3, 4, 5, 6, 7, 8, 9) + \sum d(10, 11, 12, 13, 14, 15) \\
 d &= \sum m(0, 2, 3, 5, 6, 8) + \sum d(10, 11, 12, 13, 14, 15) \\
 e &= \sum m(0, 2, 6, 8) + \sum d(10, 11, 12, 13, 14, 15) \\
 f &= \sum m(0, 4, 5, 6, 8, 9) + \sum d(10, 11, 12, 13, 14, 15) \\
 g &= \sum m(2, 3, 4, 5, 6, 8, 9) + \sum d(10, 11, 12, 13, 14, 15)
 \end{aligned}$$

DECODER CIRCUIT

- BCD to 7 segment decoder (common anode connection):

$$\begin{aligned}
 a &= \sum m(0, 2, 3, 5, 7, 8, 9) + \sum d(10, 11, 12, 13, 14, 15) \\
 b &= \sum m(0, 1, 2, 3, 4, 7, 8, 9) + \sum d(10, 11, 12, 13, 14, 15) \\
 c &= \sum m(0, 1, 3, 4, 5, 6, 7, 8, 9) + \sum d(10, 11, 12, 13, 14, 15) \\
 d &= \sum m(0, 2, 3, 5, 6, 8) + \sum d(10, 11, 12, 13, 14, 15) \\
 e &= \sum m(0, 2, 6, 8) + \sum d(10, 11, 12, 13, 14, 15) \\
 f &= \sum m(0, 4, 5, 6, 8, 9) + \sum d(10, 11, 12, 13, 14, 15) \\
 g &= \sum m(2, 3, 4, 5, 6, 8, 9) + \sum d(10, 11, 12, 13, 14, 15)
 \end{aligned}$$



$$\begin{aligned}
 a &= A + BD + \overline{B}\overline{D} + \overline{B}C \\
 b &= B + \overline{C}\overline{D} + CD \\
 c &= B + \overline{C} + D \\
 d &= \overline{C}\overline{D} + \overline{B}C + B\overline{C}D + \overline{B}\overline{D} \\
 e &= \overline{C}\overline{D} + \overline{B}\overline{D} \\
 f &= A + \overline{C}\overline{D} + B\overline{C} + B\overline{D} \\
 g &= A + B\overline{C} + C\overline{D} + \overline{B}C
 \end{aligned}$$

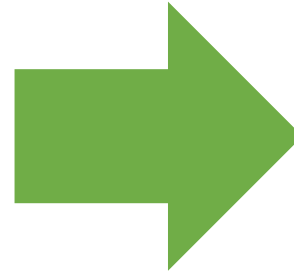
A \ B	CD			
	00	01	11	10
00				
01				
11				
10				

A \ B	CD			
	00	01	11	10
00				
01				
11				
10				

DECODER CIRCUIT

- BCD to 7 segment decoder (common anode connection):

$$\begin{aligned}
 a &= \sum m(0, 2, 3, 5, 7, 8, 9) + \sum d(10, 11, 12, 13, 14, 15) \\
 b &= \sum m(0, 1, 2, 3, 4, 7, 8, 9) + \sum d(10, 11, 12, 13, 14, 15) \\
 c &= \sum m(0, 1, 3, 4, 5, 6, 7, 8, 9) + \sum d(10, 11, 12, 13, 14, 15) \\
 d &= \sum m(0, 2, 3, 5, 6, 8) + \sum d(10, 11, 12, 13, 14, 15) \\
 e &= \sum m(0, 2, 6, 8) + \sum d(10, 11, 12, 13, 14, 15) \\
 f &= \sum m(0, 4, 5, 6, 8, 9) + \sum d(10, 11, 12, 13, 14, 15) \\
 g &= \sum m(2, 3, 4, 5, 6, 8, 9) + \sum d(10, 11, 12, 13, 14, 15)
 \end{aligned}$$



$$\begin{aligned}
 a &= A + BD + \overline{B}\overline{D} + \overline{B}C \\
 b &= B + \overline{C}\overline{D} + CD \\
 c &= B + \overline{C} + D \\
 d &= \overline{C}\overline{D} + \overline{B}C + B\overline{C}D + \overline{B}\overline{D} \\
 e &= \overline{C}\overline{D} + \overline{B}\overline{D} \\
 f &= A + \overline{C}\overline{D} + B\overline{C} + B\overline{D} \\
 g &= A + B\overline{C} + C\overline{D} + \overline{B}C
 \end{aligned}$$

A \ B	CD			
	00	01	11	10
00				
01				
11				
10				

A \ B	CD			
	00	01	11	10
00				
01				
11				
10				