

(Array)

Static v/s Dynamic Array

```
void main ()
```

```
{
```

```
int A[5];
```

```
// can use VLA
```

```
int * p;
```

```
p = new int[5]; // In C++
```

```
p = (int *) malloc (5 * sizeof(int))
```

```
// In C
```

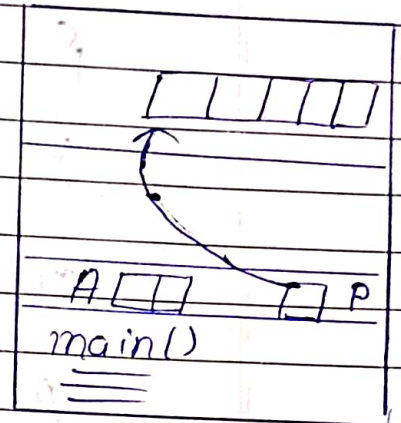
```
delete [] p; // In C++
```

```
free (p); // In C
```

```
}
```

Heap

Stack



* Increasing Array Size

```
int *p = new int[5];
```

```
int *q = new int[10];
```

```
for (int i=0; i<5; i++)
```

```
{
```

```
    (*q[i]) = (*p[i]);
```

```
}
```

```
delete [] p;
```

```
p = q;
```

```
q = NULL;
```

* 2-D Array

Ex-1 : $\text{int } A[3][4] = \{ \{1, 2, 3, 4\}, \{2, 4, 6, 8\}, \{3, 5, 7, 9\} \}$

	0	1	2	3
0				
1			15	
2				

$\{ \{1, 2, 3, 4\}, \{2, 4, 6, 8\}, \{3, 5, 7, 9\} \}$

$A[1][2] = 15$

M-2 $\text{int}^* A[3]$

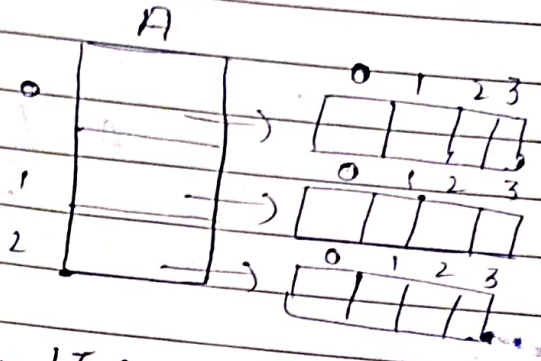
{ Array of Integer pointers }

$A[0] = \text{new int}[4];$

$A[1] = \text{new int}[4];$

$A[2] = \text{new int}[4];$

$A[1][2] = 15;$



M-3

{ Everything will be in heap }

$\text{int}^{**} A;$

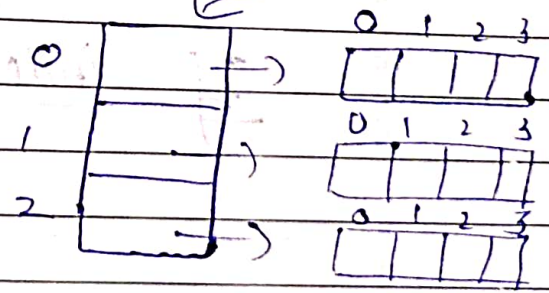
$A = \text{new int}^*[3];$

$A[0] = \text{new int}[4];$

$A[1] = \text{new int}[4];$

$A[2] = \text{new int}[4];$

A



{ for accessing, we have to use two for loops }

* Array in compilers

int A[5] = { 3, 5, 8, 4, 2 }

	0	1	2	3	4
A	3	5	8	4	2
	200/1	2/3	4/5	6/7	208/9

A[3] = 10;

$$\text{Addr}(A[3]) = 200 + 3 * 2 = 206$$

$$\text{Addr}(A[3]) = L_0 + 3 * 2 = 206$$

if $L_0 = 200$

$$\text{Addr}(A[i]) = L_0 + i * \text{size of (data-type)}$$

$$\boxed{\text{Addr}(A[i]) = L_0 + i * w}$$

Base

Addr

index

Size of
data
type

If index starts from 1 :-

int A[1..5]

	1	2	3	4	5
A					

↘
 L_0

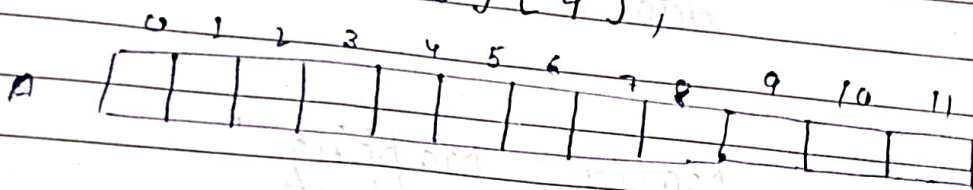
A[3] = 10;

$$\text{Addr}(A[3]) = 200 + (3-1) * 2 = 204$$

$$\boxed{\text{Addr}(A[i]) = 200 + (i-1) * W}$$

2D Array in compiler

int A[3][4];



Representation :-

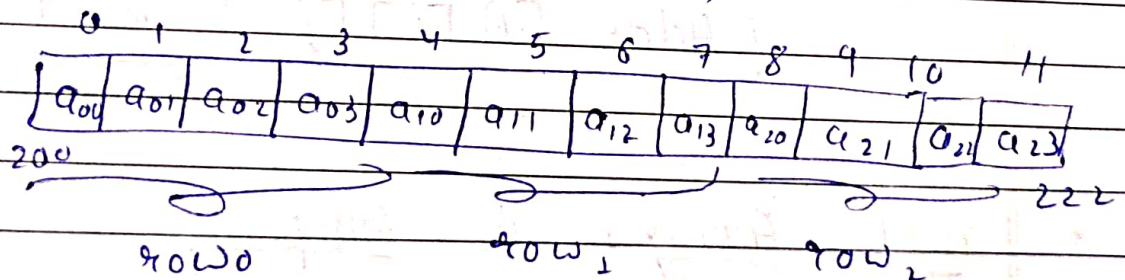
	0	1	2	3
0	a_{00}	a_{01}	a_{02}	a_{03}
1	a_{10}	a_{11}	a_{12}	a_{13}
2	a_{20}	a_{21}	a_{22}	a_{23}

1. Row-major Mapping

2. Column-major Mapping

① Row-major Mapping :-

int A[3][4];



$$\begin{aligned} \text{Add}(A[1][2]) &= 200 + [4 + 2] * 2 \\ &= 200 + 6 * 2 = 212 \end{aligned}$$

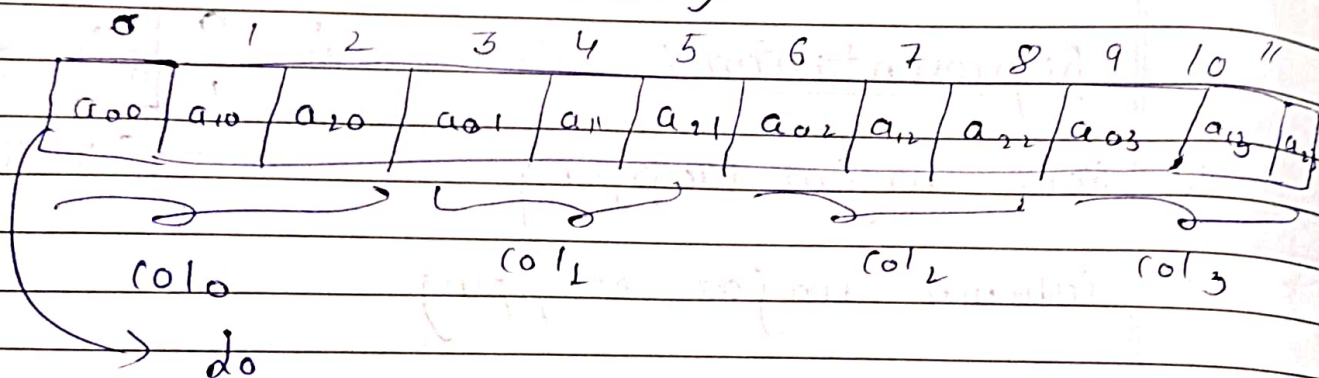
$$\text{Addr} (A[2][3]) = 200 + [2 * 4 + 3] * 2 \\ = 222$$

$$\boxed{\text{Addr} (A[i][j]) = \alpha_0 + [i * n + j] * w}$$

If array starts from 1 onwards :-

$$\text{Addr} (A[i][j]) = \alpha_0 + [(i-1) * n + (j-1)] * w$$

② Column - Major Mapping :-



$$\text{Addr} (A[1][2]) = 200 + (2 * 3 + 1) * 2$$

$$\boxed{\text{Addr} (A[i][j]) = \alpha_0 + [j * m + i] * w}$$

n-D Arrays in compiler

Type $A[d_1][d_2][d_3][d_4]$

Row - Major :-

$$\text{Addr} (A [i_1] [i_2] [i_3] [i_4]) = L_0 + [i_1 * d_2 * d_3 * d_4 + i_2 * d_3 * d_4 + i_3 * d_4 + i_4] * w$$

Column - major :-

$$\text{Addr} (A [i_1] [i_2] [i_3] [i_4]) = L_0 + [i_4 * d_1 * d_2 + i_3 * d_1 * d_2 + i_2 * d_1 + i_1] * w$$

Generalising :-

$$\boxed{\text{Row-Major} = L_0 + \sum_{p=1}^n \left(i_p * \prod_{q=p+1}^n d_q \right) * w}$$

$$\boxed{\text{Column-Major} = L_0 + \sum_{p=n}^1 \left[i_p * \prod_{q=p-1}^1 d_q \right] * w}$$

Multiplications : $4D \rightarrow 3 + 2 + 1$
 $5D \rightarrow 4 + 3 + 2 + 1$
 $nD \rightarrow (n-1) + (n-2) + \dots + 1$

$$\Rightarrow \frac{n(n-1)}{2} = O(n^2)$$

Reducing the no of multiplications :-

HORNER'S
RULE

$$\Rightarrow i_4 + i_3 * d_4 + i_2 * d_3 * d_4 + i_1 * d_2 * d_3 * d_4$$

$$\Rightarrow i_4 + d_4 + [i_3 + i_2 * d_3 + i_1 * d_2 * d_3]$$

$$\Rightarrow i_4 + d_4 \text{ (1)} [i_3 + d_3 \text{ (2)} [i_2 + i_1 * d_2 \text{ (3)}]]$$

No. of Multiplications = 3

$$O(n)$$

$$4D \rightarrow 3$$

$$5D \rightarrow 4$$

$$nD \rightarrow n-1$$