- A Tutorial on Tailored Power Simulations for Experimental Study Designs with Generalized
- 2 Linear Mixed Models
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Abstract

[THIS WILL BE UPDATED BASED ON GOOGLE DOC] Researchers often lack the tools 19 to conduct a priori power analysis for complex experimental designs deployed in 20 human-computer interaction (HCI) studies. Generalized Linear Mixed Models (GLMMs) are 21 well-suited to analyze experiments in which subjects respond to a set of stimuli. However, existing software packages can only be used to simulate power for simple designs, which are 23 often not useful for more sophisticated investigations. This tutorial addresses this gap by providing a comprehensive tutorial to perform tailored power analyses using data simulation. 25 Our tutorial provides code for an HCI case study, empowering researchers to simulate their 26 own data and ascertain appropriate sample sizes for GLMMs. This resource should help to 27 enhance the precision of study designs and to mitigate the risk of underpowered studies. Moreover, we discuss further implications for experimental research and provide an outlook

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32 Word count: 7059

on the increasing relevance of power simulations in the field.

A Tutorial on Tailored Power Simulations for Experimental Study Designs with Generalized
Linear Mixed Models

35 Introduction

When planning experimental research, it is essential to determine an appropriate sample size (Lakens, 2022b) to ensure that the results obtained are both robust and informative, and to use appropriate statistical models to analyze the data. However, the recent replication crisis in experimental research, such as in Human-Computer Interaction (HCI), has illustrated many challenges surrounding the reproducibility and reliability of findings (Robertson & Kaptein, 2016). As a result, there is a growing need for rigorous statistical methodology and the adoption of well-powered experimental designs. While software solutions exist for simple statistical models and experimental designs, many researchers lack the skills and tools to conduct power analyses for more complex research designs using the flexible generalized linear mixed models (GLMM) framework. In the present work, we provide a tutorial comprised of a concrete example for custom a priori power analyses using data simulations based on GLMMs.

## 48 Statistical power

In empirical research relying on hypothesis testing, the most common strategy for
determining an adequate sample size is based on statistical power (Lakens, 2022b).

Statistical power is defined as the probability that a hypothesis test has a significant p-value
when analyzing repeated samples from a population with a true effect of some pre-specified
size. Less formally, power is described as the probability that a hypothesis test accepts the
alternative hypothesis  $H_1$  if  $H_1$  is indeed true. If the sample size (i.e., the number of
participants and/or stimuli) used for data collection is insufficient to detect the effects with
high probability the effects or relationships being investigated, this particular study would
be considered "underpowered".

Conducting underpowered research has many negative consequences. First, relying on underpowered experiments may yield inconclusive (if low power is taken into account) or misleading (if low power is ignored) results, hindering the accumulation of knowledge. Second, underpowered studies waste resources by consuming time, effort, and funding without delivering meaningful results.

### A priori power analysis

A power analysis represents the act of calculating the statistical power for a given true effect and sample size. By running the calculation for a range of sample sizes "a priori" (i.e., before data collection), the required sample size can be determined so that researchers find an assumed true effect with the desired statistical power. Thereby, power analysis offers a valuable contribution to the research process by allowing researchers to estimate the appropriate sample sizes required to achieve sufficient statistical power for results with high evidential value.

Conducting a careful a priori power analysis helps researchers decide which
experimental design and statistical models are both feasible and appropriate for analyzing
the data and answering their research questions. Also, when conducting a proper power
analysis, researchers have to consider every aspect of the experimental design and will notice
statistical or design challenges before starting with data collection. Especially in fast-moving
research fields, adding a solid sample size calculation to the process can act as a safeguard
for ensuring high-quality research.

Moreover, many journals and funding agencies now require that a power analysis is included in study protocols and grant proposals, recognizing its significance in ensuring robust and meaningful findings. By incorporating power analysis into research planning, researchers can enhance the replicability and credibility of their work, contributing to the advancement of the respective research field through more robust insights. For simple statistical models, like t-tests, ANOVA, and linear regression, with common study designs (e.g., mean comparison between two groups), user-friendly software for power analysis is readily available (Faul, Erdfelder, Buchner, & Lang, 2009).

# Generalized linear mixed models (GLMM)

As study designs become more complex, researchers require more sophisticated statistical models to capture the nuanced relationships and hierarchical structures introduced by their study designs (Yarkoni, 2022). GLMMs (also called multilevel models) are gaining increasing popularity in analyzing data from experimental research, such as in HCI, because they offer a flexible framework for analyzing data with non-normal and categorical outcomes while accounting for both fixed and random effects (Fahrmeir, Kneib, Lang, & Marx, 2021; Kaptein, 2016).

GLMMs are an extension of LMMs (Linear Mixed Models), which are, in turn, 94 extensions of classic linear regression models that account for correlated data and hierarchical structures (Fahrmeir et al., 2021). In this context, correlated data means that observations within a given dataset are not independent of each other. In other words, the 97 values of the dependent variable for one observation may be related to the values of the dependent variable for other observations in a systematic way. This correlation can arise for various reasons, such as repeated measurements on the same subjects over time, observations 100 clustered within certain groups or locations, or data collected at different levels of 101 granularity. Hierarchical structures can be found in datasets that have a nested or 102 hierarchical organization. For example, one might have data on students nested within schools, employees nested within departments, or patients nested within hospitals. In such cases, the observations within each higher-level grouping (e.g., school, department, hospital) 105 tend to be more similar to each other than to observations in other groups. LMMs are used 106 when the outcome variable is continuous and follows a normal distribution (when 107 conditioned on the predictor variables). They allow for the modelling of fixed effects, which 108

capture the relationships between predictors and the outcome, as well as random effects, 109 which account for the correlation and variability within groups or subjects. Random effects 110 are typically assumed to follow a normal distribution with a mean of zero and a variance 111 that quantifies the heterogeneity across the groups or subjects. As mentioned, GLMMs 112 extend the LMM framework to accommodate non-normal and categorical outcome variables. 113 They are used when the outcome variable does not follow a normal distribution but instead 114 belongs to a different distribution family (e.g., binomial). GLMMs incorporate both fixed 115 and random effects, similar to LMMs, but also involve a link function that connects the 116 linear predictor to the expected value of the outcome variable. The link function allows for 117 modelling the relationship between predictors and the outcome in a non-linear way that is 118 appropriate for the specific distribution family of the response variable. 119

### 20 Power simulations for GLMMs

Currently available software packages for power simulations do not include GLMMs, 121 making it necessary to build data simulations tailored specifically to the study design 122 (Murayama, Usami, & Sakaki, 2022; Westfall, Kenny, & Judd, 2014). A number of tutorials 123 have been published describing how to perform such power simulation for multilevel models 124 (Arend & Schäfer, 2019; Brysbaert & Stevens, 2018; DeBruine & Barr, 2021; Kumle, Võ, & 125 Draschkow, 2021; Lafit et al., 2021; Zimmer, Henninger, & Debelak, 2022). However, most of 126 these tutorials only cover linear mixed models (LMMs) and focus on the most common 127 designs (e.g., INSERT EXAMPLE). This narrow focus provides little guidance for 128 researchers faced with more complex study designs (e.g., INSERT EXAMPLE), which are very common (Brown, 2021). The necessary assumptions for power simulations in GLMMs include assumptions about the distributional form of the outcome variable, the random effects, and the error structure. The distributional assumption specifies the family of 132 distributions for the outcome variable, such as Gaussian, Poisson, or binomial. Assumptions 133 about the random effects include the assumption of normality and the covariance structure

among the random effects. Additionally, assumptions about the error structure, such as 135 independence or correlation, must be specified. Interpreting these assumptions entails 136 understanding the underlying assumptions of the model and ensuring they align with the 137 characteristics of the data being analyzed. Existing tutorials often rely on heuristics for 138 specifying variance components (e.g., the standard deviation of random intercepts) or 139 assume that results from meta-analyses or data from pilot studies are available to determine 140 plausible values for all model parameters. However, in practice, knowledge about those 141 parameters from prior studies is often limited, specifying assumptions a practical challenge 142 (Maxwell, Kelley, & Rausch, 2008). 143

Based on the need for well-powered experimental research using GLMMs and the lack
of tools to conduct corresponding power analyses, in this tutorial paper, we present a case
study that serves as a practical demonstration of how to perform a data simulation and an a
priori power simulation for a more complex study design. Thereby, we aim to equip
researchers with the tools needed to simulate their own data and determine appropriate
sample sizes for their own research.

#### The present case study

In this section, we outline the steps for performing data simulation and a priori power analysis for GLMMs using a case study based on a specific experimental study design from the area of human-AI (artificial intelligence) interaction research.

### Experimental study design

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In the present case study, we simulate the data for an experiment where the diagnostic performance of users of an AI-enabled diagnostic decision support system is to be evaluated.

The goal is to understand how AI advice influences medical decision-making. Participants, radiologists (task experts) and students/interns (non-task experts), review head computer tomography (CT) scans to assess the presence of bleeding, more specifically, intracranial

haemorrhage (ICH). To support their decision-making, in two experimental conditions, an AI model provides initial diagnostic advice, which can be used as guidance by the 161 participants. This AI advice can be either correct (80% of cases) or incorrect (20%). In the 162 control condition, no AI advice is presented, meaning that the participants have to read the 163 CT scan without any support. After reviewing the CT scan, participants deliver a medical 164 diagnosis (bleeding or no bleeding), which may be either accurate or inaccurate. This 165 experimental design introduces some missing values by design since the advice is neither 166 correct nor incorrect when no advice is present, which must be taken into account when 167 simulating and analyzing the data. With this experiment, we want to determine if (a) 168 experts are better than non-experts in reading head CT scans, (b) correct AI advice leads to 169 better diagnostic accuracy than incorrect AI advice, and (c) different presentations of AI 170 advice influence performance. In this example, recruiting task experts (i.e., radiologists) is more challenging due to their limited availability, while non-experts (i.e., students/interns) 172 are more readily accessible. The goal of the power simulation is to determine how many task experts and non-experts must be recruited to achieve sufficient statistical power in the planned experiment. 175

#### 176 The lme4 package in R

In our case study, we use the lme4 R package (Bates, Mächler, Bolker, & Walker, 2015)
which is a state-of-the-art tool for fitting frequentist GLMMs.<sup>1</sup>

The lme4 package includes a function called simulate that allows researchers to simulate the dependent variable based on the same model formula used for model fitting, enabling power simulations and other related analyses.

However, the model parameterization used by the lme4 package is quite technical, making it difficult for applied researchers to determine whether their specified population

<sup>&</sup>lt;sup>1</sup> For Bayesian GLMMs, the brms R package is currently the most prominent option (Bürkner, 2017).

model (i.e., the theoretical model that describes the underlying data generation process for a specific population of interest) implies plausible associations in their simulated data.

Therefore in this tutorial, we simulate data for GLMMs from first principles (i.e., creating synthetic data step by step instead of using black box functions) to assist applied researchers in better understanding all model assumptions and then use lme4 to analyze the simulated data sets.<sup>2</sup>

## 190 Our specific GLMM

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In a GLMM, the expected value of the dependent variable Y conditioned on the vector of predictor variables  $\mathbf{X}$  and random effects  $\mathbf{U}$ , transformed by a link function g() is modeled as a linear combination  $\eta$  of the predictor variables  $\mathbf{X}$ , the random effects  $\mathbf{U}$  and the model parameters  $\beta$  (Fahrmeir et al., 2021).

 $g(E(Y|\mathbf{X}=\mathbf{x},\mathbf{U}=\mathbf{u})) = \eta < !--SG: Sorry formay be a stupid question, but what does Est and for ?and why determined to the standard of the standard of$ 

Equivalently, the conditional expected value is modelled as the linear combination  $\eta$ ,

transformed by the inverse link function  $g^{-1}()$ .

$$E(Y|\mathbf{X} = \mathbf{x}, \mathbf{U} = \mathbf{u})) = g^{-1}(\eta)$$

If the dependent variable (i.e., diagnostic decision) Y is a binary variable with values 0 (i.e. inaccurate), or 1 (i.e., accurate), the conditional expected value is equivalent to the probability:

$$P_{si} := P(Y = 1 | \mathbf{X} = \mathbf{x}, \mathbf{U} = \mathbf{u})$$

In our case study,  $P_{si}$  is the conditional probability that a subject s gives the correct response to item (i.e., CT scan) i.

In such a setting, we model this probability as

$$P_{si} = inverse\_logit(\eta_{si})$$

<sup>&</sup>lt;sup>2</sup> A less flexible alternative would be to use the simr package (Green & MacLeod, 2016), which can be used to both simulate data and perform power analysis for models supported by the lme4 package.

with the inverse-logit link  $g^{-1}(\eta_{si}) = inverse\_logit(\eta_{si}) = \frac{exp(\eta_{si})}{1 + exp(\eta_{si})}$  or equivalently

$$logit(P_{si}) = \eta_{si}$$

with the logit link  $g(P_{si}) = logit(P_{si}) = ln(\frac{P_{si}}{1 - P_{si}}).$ 

In our case study, the probability of giving a correct response is assumed to depend on the predictors:

- $advice\_present_{si}$ : whether subject s was presented with AI advice (1) or not (0) when asked to asses item i
- $advice\_correct_{si}$ : whether this advice was correct (1) or not (0)
- $expert_s$ : whether subject s was a task expert (1) or not (0)
- and the random effects:
- $u_{0s}$ : the deviation of subject s from the average ability to solve an item (i.e., CT scan)
  with average difficulty; assumed to be distributed as  $u_{0s} \sim N(0, \sigma_S^2)$
- $u_{0i}$ : the deviation of item (i.e., CT scan) i from the average difficulty to be solved by a person with average ability; assumed to be distributed as  $u_{0i} \sim N(0, \sigma_I^2)$
- In total, we assume the model

$$logit[P_{si}] = (\beta_0 + u_{0s} + u_{0i}) +$$

$$\beta_a \cdot advice\_present_{si} + \beta_c \cdot advice\_correct_{si} + \beta_e \cdot expert_s +$$

$$\beta_{ea} \cdot expert_s \cdot advice\_present_{si} + \beta_{ec} \cdot expert_s \cdot advice\_correct_{si}$$

217 or equivalently

$$P_{si} = inverse\_logit[(\beta_0 + u_{0s} + u_{0i}) +$$
 
$$\beta_a \cdot advice\_present_{si} + \beta_c \cdot advice\_correct_{si} + \beta_e \cdot expert_s +$$
 
$$\beta_{ea} \cdot expert_s \cdot advice\_present_{si} + \beta_{ec} \cdot expert_s \cdot advice\_correct_{si}]$$

with model parameters  $\beta_0, \beta_e, \beta_a, \beta_c, \beta_{ea}, \beta_{ec}, \sigma_S, \text{ and } \sigma_I$ .

In the GLMM literature, this would be called a binomial GLMM with two random intercepts (for subjects and items), two level-1 predictors (advice\_present, advice\_correct), one level-2 predictor (expert) and two cross-level interactions (expert · advice\_present, expert · advice\_correct).

To limit complexity, we do not consider random slopes, additional predictors or higher-level interactions here.

# 25 Data simulation

The following R function simulates a full dataset structured according to the design of our case study. The faux package (DeBruine, 2023) contains useful functions when simulating factorial designs, including random effects.

```
# compute dependent variable

mutate(linpred = b_0 + u0i + u0s +

    b_e * expert + b_a * advice_present + b_c * advice_correct +

    b_ea * expert * advice_present + b_ec * expert * advice_correct) %>%

mutate(y_prob = plogis(linpred)) %>%

mutate(y_bin = rbinom(n = n(), size = 1, prob = y_prob))

dat
}
```

In the first six lines of the function definition, we set some default parameter values 229 (which we will explain in a later section) and load the packages we use to manipulate and 230 simulate data. In our case study, each subject (n subjects in total) is assumed to respond 231 to each item (i.e., CT scan; n items in total). Thus, the add random command creates a 232 fully-crossed data.frame with n subjects  $\times$  n items rows. We add a between-subject 233 effect with the add\_between command, simulating that about 25% of subjects are experts. 234 The next two lines simulate that in  $\frac{2}{3}$  of trials, subjects will be presented with AI advice, and 235 if advice is presented, the advice will be correct in about 80% of cases (the variable 236 advice\_correct is always 0 when no advice is presented). Next, we simulate one random 237 effect for each subject (u0s) and for each item (u0i). As assumed by standard GLMMs, the 238 add ranef function draws the random effects from a normal distribution with a mean 0 and 239 a standard deviation specified by the user. With all design variables done, we are ready to 240 simulate our model equation as outlined in equation X. The linear predictor variable lingred ( $\eta$  in the GLMM model equations) combines the predictor variables, random effects and model parameters as assumed by our model. We then transform the linear predictor with the inverse-link function to compute y prob, the probability that the subject correctly solved the item (in R, the inverse-logit link is computed with plogis and the logit link with 245 qlogis). In the final step, we simulate the binary dependent variable y\_bin (i.e., whether 246

the subject chooses the accurate diagnosis for the CT scan) by – for each trial – drawing from a Bernoulli distribution with success probability y\_prob.

# $_{^{249}}$ Model fitting

In this section, we show how to fit a GLMM with lme4, interpret the model and test hypotheses derived from a research question.

We simulate data according to our model, in which 100 subjects respond to 50 items

(we use set.seed to make the simulation reproducible). However, for the sake of the

exercise, we can imagine that this would be real data resulting from our future experiment

and think about how we would analyse this data.

```
library(tidyverse)
set.seed(1)
dat <- simulate(n_subjects = 100, n_items = 50)</pre>
```

The lme4 package uses a special syntax for model specification. Our specific GLMM is represented by the formula:

```
library(lme4)

f <- y_bin ~ 1 + expert + advice_present + advice_correct +
    expert:advice_present + expert:advice_correct +
    (1|subject) + (1|item)</pre>
```

The first two lines look similar to any linear model in R (general intercept indicated by
1; main effects indicated by variable names in the dataset; interactions indicated by
variable1:variable2). The third line specifies a random intercept for each subject
(1|subject) and for each item (1|item). The complete set of rules for the syntax is
outlined in Bates et al. (2015) and in the documentation of the lme4 package.

In lme4, a GLMM is fitted with the glmer function. By setting family =

"binomial", we request a binomial GLMM appropriate for our binary dependent variable

y\_bin (the binomial GLMM uses the canonical logit link by default), which is defined as an

accurate (1) vs. inaccurate (0) diagnosis.

# 267 Model interpretation

We can inspect the estimates for all model parameters with the summary command:

### summary(fit)

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In the output, the Estimate column in the Fixed effects table contains the estimates for the  $\beta$  parameters, while the Std.Dev. column in the Random effects table contains the estimates for  $\sigma_S$  and  $\sigma_I$ .

Unfortunately, the model parameters in a binomial GLMM are hard to interpret because 1) the  $\beta$  parameters are connected to the modelled probability via the non-linear inverse-logit link, and 2) we also have to consider the random effects. The most simple interpretation works by imagining a subject with average ability ( $u_{0s} = 0$ ) responding to an item (i.e., CT scan) with average difficulty ( $u_{0i} = 0$ ). Then the model implied probability that such a person solves such an item accurately is given by:

$$P(Y = 1 | \mathbf{X} = \mathbf{x}, \mathbf{U} = \mathbf{0}) =$$

$$= inverse\_logit[\beta_0 + \beta_a \cdot advice\_present_{si} + \beta_c \cdot advice\_correct_{si} + \beta_e \cdot expert_s +$$

$$\beta_{ea} \cdot expert_s \cdot advice\_present_{si} + \beta_{ec} \cdot expert_s \cdot advice\_correct_{si}]$$

In fact, we would only need the full equation if the subject is an expert and correct advice is presented. In all other experimental conditions, some terms drop from the equation because they are multiplied by 0. The other extreme case would be the probability that a

non-expert with average ability solves an item with average difficulty when no advice is presented:

$$P(Y = 1 | expert = 0, advice\_present = 0, advice\_correct = 0, u_{0s} = 0, u_{0i} = 0) = inverse\_logit[\beta_0]$$

Due to this complicated relationship, we argue not to focus too much on interpreting single model parameters when working with GLMMs. Instead, it can be more intuitive to consider model predictions and the model-implied distribution of the dependent variable for each experimental condition across all subjects and items.

With the marginal effects package (Arel-Bundock, 2023), we can easily compute
predictions for all observations in the dataset based on the fitted GLMM (including all fixed
and random effects), and plot the average probability with confidence intervals for each
experimental condition:

```
library(marginaleffects)
plot_predictions(fit, by = c("advice_present", "advice_correct", "expert"),
   type = "response") + ylim(c(0.3, 1))
```

# $_{\scriptscriptstyle 11}$ Hypothesis testing

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However, we need to think about the model parameters again when we want to test hypotheses that we have theoretically derived from some research question. Because the inverse-logit link is still a continuously increasing function, positive parameter values always correspond to increases in probability and vice versa.

The Fixed effects table in Figure X also includes p-values for hypothesis tests with null hypotheses of the style  $H_0: \beta = 0$ . However, for many research questions of interest, we are not interested in these two-sided tests that refer to only a single parameter.

For our case study, imagine the following combined hypothesis: We expect that for both

experts and non-experts, correct advice leads to a higher probability of accurately diagnosing a

CT scan compared to no advice presented, AND, we expect that for both experts and

non-experts, incorrect advice leads to a lower probability of accurately diagnosing a CT scan

compared to no advice presented.

This combined hypothesis leads to the following four separate null hypotheses to be tested:

$$H_{01}: \beta_a + \beta_c + \beta_{ea} + \beta_{ec} \le 0$$

$$H_{02}: \beta_a + \beta_c \leq 0$$

$$H_{03}: \beta_a + \beta_{ea} \geq 0$$

$$H_{04}: \beta_a \geq 0$$

We arrive at these inequalities based on the following logic, exemplified here only for  $H_{01}$ : The first null hypothesis states that an expert responding to an item while presented with correct advice has a lower or equal probability of solving the item compared to the same expert facing the same item without any advice. This implies the following inequality for each subject s and item i

 $inverse\_logit[(\beta_0 + u_{0s} + u_{0i}) + \beta_e + \beta_a + \beta_c + \beta_{ea} + \beta_{ec}] \leq inverse\_logit[(\beta_0 + u_{0s} + u_{0i}) + \beta_e]$ which simplifies to  $\beta_a + \beta_c + \beta_{ea} + \beta_{ec} \leq 0$ .

We can specify and test hypotheses like these with the multcomp package (Hothorn, Bretz, & Westfall, 2008a) as follows:

```
library(multcomp)
null_hypotheses <- c(
    "advice_present + advice_correct + expert:advice_present +
    expert:advice_correct <= 0",
    "advice_present + advice_correct <= 0",
    "-1 * (advice_present + expert:advice_present) <= 0",</pre>
```

```
"-1 * (advice_present) <= 0")
glht <- glht(fit, linfct = null_hypotheses)
summary(glht, test = univariate())$test$pvalues</pre>
```

Because all hypotheses tested simultaneously with the glht function must have the 314 same direction, we flip the sign of inequalities three and four by multiplying them with -1. 315 The multcomp package automatically adjusts p-values when multiple hypotheses are tested 316 simultaneously (Hothorn, Bretz, & Westfall, 2008b). However, the combined null hypothesis 317 in our exemplary research question should only be rejected if all individual null hypotheses 318 are rejected [i.e. intersection-union setting; Dmitrienko and D'Agostino (2013)]. In such 319 cases, the error probabilities do not accumulate, and we would waste power when correcting 320 for multiple tests. Thus, we request unadjusted p-values by setting test = univariate() 321 in the summary command. With a standard significance level of  $\alpha = 0.05$ , we would not 322 reject all four null hypotheses (the p-value for hypothesis  $H_{03}$  is not significant) and 323 therefore also not reject the combined null hypothesis for this simulated dataset. Note that 324 this decision would be wrong because we have simulated the data such that the combined 325 alternative hypothesis is actually true in the population. 326

#### 327 Specification of plausible parameter values

When introducing our simulation function and simulating data for the above example, we have used theoretically plausible values as defaults for all model parameters ( $\beta_0$ ,  $\beta_e$ ,  $\beta_a$ ,  $\beta_c$ ,  $\beta_{ea}$ ,  $\beta_{ec}$ ,  $\sigma_S$ , and  $\sigma_I$ ), but have not talked about where these numbers came from.

Often no meta-analytic results or conclusive data from pilot studies are available. All parameter values in our present case study have been determined based on results from prior own work and from the literature. Additionally, we had repeated exchanges with our affiliated domain experts from radiology.

We now outline a few strategies on how to determine plausible parameter values. We have already seen in our discussion of model interpretation how we can derive the model implied probability for each experimental condition, that a subject with average ability solves an item with average difficulty. We can revert this perspective by choosing plausible probability values and deriving the parameter values implied by these probabilities (for an average subject and an average item).

Table X shows our set of assumptions concerning the probability that an average 341 subject solves an average item for each experimental condition, as well as the corresponding 342 equations implied by the model: | Experimental condition |  $P(Y = 1 | \mathbf{X} = \mathbf{x}, \mathbf{U} = \mathbf{0})$  | 343 344 expert | 0.70 |  $logit(0.70) = \beta_0$  | | no advice, expert | 0.90 |  $logit(0.90) = \beta_0 + \beta_e$  | | false 345 advice, no expert | 0.40 |  $logit(0.40) = \beta_0 + \beta_a$  | | false advice, expert | 0.85 | 346  $logit(0.85) = \beta_0 + \beta_e + \beta_a + \beta_{ea} \mid |$ correct advice, no expert  $| 0.90 \mid logit(0.90) = \beta_0 + \beta_a + \beta_c$ 347 | | correct advice, expert | 0.95 |  $logit(0.95) = \beta_0 + \beta_e + \beta_a + \beta_c + \beta_{ea} + \beta_{ec}$  | 348

This table can be used to compute the implied values for the  $\beta$  parameters, starting with the first equation and reinserting the computed  $\beta$  values in all following equations:

```
b_0 <- qlogis(0.7)

b_e <- qlogis(0.9) - b_0

b_a <- qlogis(0.4) - b_0

b_ea <- qlogis(0.85) - b_0 - b_e - b_a

b_c <- qlogis(0.9) - b_0 - b_a

b_ec <- qlogis(0.95) - b_0 - b_e - b_a - b_c - b_ea

c(b_0 = b_0, b_e = b_e, b_a = b_a, b_c = b_c, b_ea = b_ea, b_ec = b_ec)</pre>
```

It is always possible to double-check these computations by transforming the

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parameter values back to probabilities, e.g.

$$P(Y = 1 | expert = 1, advice\_present = 1, advice\_correct = 1, u_{0s} = 0, u_{0i} = 0) =$$

$$= inverse\_logit[\beta_0 + \beta_e + \beta_a + \beta_c + \beta_{ea} + \beta_{ec}]$$

Although the derivations above are straightforward, it is important not to misinterpret 353 their implications: In binomial GLMMs, the average probability to solve an item (averaged 354 across persons of varying ability and items of varying difficulty) is **not** equal to the 355 probability that a person with average ability solves an item with average difficulty. The first 356 perspective implies a so-called marginal interpretation, while the second one implies a 357 conditional interpretation. For example, we determined the  $\beta$  parameters in a way that 358 corresponds to a desired conditional probability of 0.95, that an expert with average ability 359 solves an item with average difficulty when presented with correct advice. However, even if 360 the model were true, we would not observe this probability value if we estimated the 361 marginal probability in a group of experts responding to items presented with correct advice from a big sample of subjects drawn from their natural distribution of ability and items drawn from their natural distribution of difficulty.

The inequality of conditional and marginal effects in GLMMs (Fahrmeir et al., 2021)
makes their interpretation more difficult. One must be careful when specifying parameter
values based on previous studies or pilot data that use the marginal interpretation (e.g., a
pilot study providing an estimate of how often neurologists make an accurate diagnosis based
on brain scans). However, this does not mean that we cannot use the marginal interpretation
(average probability across persons and items) to inform plausible parameter values: When
parameter values have been selected, we can compute the implied marginal distributions and
compare this information to our domain knowledge. Then, we can iteratively adjust the
parameter values until we are satisfied with the implied distributions.

Earlier, we have already encountered one way to visualize the implied marginal
distributions: We can fit our model to a simulated dataset and use the convenience functions
from the marginaleffects package to compute averaged predictions that correspond to our
quantities of interest. However, the model predictions will only be close to the true
distribution if the simulated dataset is very large, but then the model fitting consumes a lot
of time and memory. A more sophisticated strategy is to simulate a large dataset and
directly compute the averages, contrasts and distributions we are interested in.

```
library(tidyverse)

library(ggdist)

dat <- simulate(n_subjects = 2000, n_items = 2000, sd_u0s = 0.5, sd_u0i = 0.5)

dat %>%

mutate(condition = fct_cross(
    factor(expert), factor(advice_present), factor(advice_correct))) %>%

mutate(condition = fct_recode(condition,
    "no expert, no advice" = "0:0:0", "expert, no advice" = "1:0:0",
    "no expert, wrong advice" = "0:1:0", "expert, wrong advice" = "1:1:0",
    "no expert, correct advice" = "0:1:1", "expert, correct advice" = "1:1:1")) %>%

ggplot(aes(x = y_prob, y = condition)) +

stat_histinterval(point_interval = "mean_qi", slab_color = "gray45") +

scale_x_continuous(breaks = seq(0, 1, 0.1), limits = c(0, 1))
```

Figure X shows the model implied marginal distributions, including the mean, 66% and 95% intervals. We can see that, indeed, the average probabilities (black dots) slightly differ from the probabilities of average subjects and items considered in the previous section. This difference increases with the variability of the random effects.

Up to this point, we have not talked about plausible values for the standard deviations of the subject and item random intercepts ( $\sigma_S$  and  $\sigma_I$ ). Plots like the one above are a useful tool to decide whether the specified standard deviations are reasonable by comparing the ranges and overlap between conditions to domain knowledge.

In the next plot, we have set the item standard deviation to almost zero ( $\sigma_I = 0.01$ ).

This gives us a better way to see the variability between persons.

As an example, this presentation reveals a number of implicit assumptions about the 391 comparison between experts and non-experts: With wrong advice, virtually all experts have 392 a higher probability of making a correct diagnosis compared to non-experts when considering 393 only items with average difficulty. In contrast, there is considerable overlap in probability 394 between experts and non-experts with no advice and even higher overlap with correct advice. 395 Patterns like these should be considered carefully and discussed with the domain experts. 396 Parameter values ( $\beta$  parameters, and  $\sigma_S$ ) should be adjusted if the implications do not seem 397 reasonable. 398

We could also have a closer look at variability between items by setting the subject standard deviation to almost zero ( $\sigma_S = 0.01$ , see Figure X in Appendix X).

The final plot demonstrates that these plots are also useful for spotting standard deviations that are specified too high. For this example, we have set  $\sigma_S = 3$  and  $\sigma_I = 3$ .

This implies that in each experimental condition, the probabilities that a subject solves an item are usually close to either 0 or 1, which is not a plausible assumption. For example, we would expect even experts with low ability to solve a difficult item with a probability substantially larger than zero even when presented with wrong advice.

407 Results

With all these considerations addressed, we are finally ready to perform a power
analysis. Wrapping the simulate function already constructed earlier, the helper function
sim\_and\_analyse performs all previous steps (simulate a dataset, fit a GLMM, compute

p-values) in a single command.

```
sim and analyse <- function(</pre>
  formula chr = "y bin ~ 1 + expert + advice present + advice correct +
    expert:advice present + expert:advice correct + (1|subject) + (1|item)",
  null hypotheses = c("advice present + advice correct +
    expert:advice present + expert:advice correct <= 0",</pre>
    "advice present + advice correct <= 0",</pre>
    "-1 * (advice present + expert:advice present) <= 0",
    "-1 * (advice present) <= 0"), ...){
  require(lme4)
  require(multcomp)
  # simulate data
  dat <- simulate(...)</pre>
  # fit model
  model <- glmer(as.formula(formula_chr), data = dat, family = "binomial")</pre>
  # compute p-values
  glht <- glht(model, linfct = null hypotheses)</pre>
  pvalues <- summary(glht, test = univariate())$test$pvalues</pre>
  setNames(pvalues, paste0("p H0", 1:length(null hypotheses)))
}
```

Power analysis can quickly become computationally intensive when we repeatedly simulate data and fit models for different parameter combinations or sample sizes. Thus, we use the future (Bengtsson, 2021) and furrr (Vaughan & Dancho, 2022) packages to perform computations in parallel. First, we enable parallelization and specify how many parallel cores ("workers") of our computer to use (users can find out the maximum number of cores on their computer with the command parallel::detectCores()), and set a seed to make the

simulation reproducible.

```
library(future)
plan("multisession", workers = 6)
set.seed(2)
```

The next code chunk specifies a simulation grid with different settings for both the
number of subjects (n\_subjects) and the number of items (n\_items), each combination
being repeated rep times. We chose 300 repetitions for the data simulation at hand as it
strikes a balance between achieving a robust statistical estimate and remaining
computationally feasible. With the current settings, this simulation takes about X minutes
on a MacBook Pro from 2020 with M1 chip and 16 GB working memory. If you want to
quickly experiment with the code yourself, a setting with workers = 4 and rep = 5 should
finish in less than 5 minutes, even on smaller machines.

The result of the computation is a data frame that contains the p-values of all tested hypotheses for each simulated dataset. In some iterations (predominantly in conditions with small sample sizes), model estimation did not converge with the lme4 package. We do not remove these results because non-convergence can also happen when analyzing the real data we plan to collect, thus, we want to factor in this possibility to keep our simulation more realistic.

For our exemplary combined hypothesis, power is defined as the (long-run) percentage of simulations in which all four p-values of our component hypotheses are significant at the  $\alpha = 0.05$  level. Based on our simulation outcomes, we compute a power estimate for each combination of n\_subjects  $\times$  n\_items (including 95% confidence intervals) and visualize the results with the following code.

```
library(binom)
alpha \leftarrow 0.05
power <- sim design %>%
  group_by(n_subjects, n_items) %>%
  summarise(power = mean(p H01 < alpha & p H02 < alpha &</pre>
                           p_H03 < alpha & p_H04 < alpha),
    n_sig = sum(p_H01 < alpha & p_H02 < alpha &
                  p HO3 < alpha & p HO4 < alpha),
    n = n(),
    ci.lwr = binom.confint(n sig, n, method = "wilson")$lower,
    ci.upr = binom.confint(n sig, n, method = "wilson")$upper,
    .groups = "drop")
power %>%
  mutate(across(c(n subjects, n items), factor)) %>%
  ggplot(aes(n subjects, n items, fill = power)) +
  geom_tile() +
  geom_text(aes(label = sprintf("%.2f \n [%.2f; %.2f]",
```

<sup>&</sup>lt;sup>3</sup> This code was inspired by the "Mixed Design Simulation" vignette of the faux package at https://debruine.github.io/faux/articles/sim\_mixed.html.

```
power, ci.lwr, ci.upr)),
color = "white", size = 4.5) +
scale_fill_viridis_c(limits = c(0, 1)) +
xlab("number of subjects") + ylab("number of items")
```

As should be the case, power estimates increase with both the number of subjects and 438 the number of items. The confidence intervals indicate how precisely power was estimated by our simulation. Higher precision (which would be reflected in narrower confidence intervals) could be obtained by increasing the number of repetitions (rep) in the simulation. In practice, power simulations are often run multiple times with adjusted combinations of sample sizes. When running for the first time, it might be revealed that power is way too low (or much higher than required) for some combinations of n subjects and n items. When 444 narrowing down the best combination that achieves sufficient power while at the same time 445 striking a good balance of how many subjects and items are practically feasible, later rounds 446 of power simulation will typically include a smaller grid of sample sizes combined with a 447 higher number of repetitions. This will assure high precision for the final power estimates, 448 which are then used for the sample size justification of the future study. 440

Much has been written on the optimal amount of power to target in empirical research. 450 The most prominent heuristic is to target a power of 0.8 (when combined with a type I error 451 rate of  $\alpha = 0.05$ ), but depending on the research goals of the study, there are often good 452 reasons to move away from this standard (Lakens, 2022b; Lakens et al., 2018). When target 453 power has been specified, the number of subjects and the number of items in our study design can be traded against each other based on practical considerations. For the sake of the example, let the targeted power be indeed about 0.8, using an  $\alpha$  of 0.05 to detect an effect of the expected size implied by our data simulation. This could be achieved by 457 collecting data from 200 subjects (about 25% of which will be experts), each completing the 458 same 50 items (with advice present in about 67% of cases, which is correct in about 80% of 459

cases with present advice). If collecting data from 200 subjects is not feasible, an alternative 460 would be to recruit 150 subjects but increase the length of the experiment to over 70 items. 461 However, 70 items might take too long to complete for the radiologists participating in the 462 study, who have a busy schedule. The simulation suggests that it might also be possible to 463 plan a shorter experiment with only 30 items if it is feasible to recruit an even higher 464 number of subjects (> 250, to be determined by additional rounds of power analysis). 465 Design parameters that also affect power, and which could be investigated in the simulation 466 to find a more optimal trade-off, are the ratio of experts, the frequency of whether advice is 467 presented and whether it is correct. 468

469 Discussion

Experimental research requires careful planning and consideration of statistical power to ensure robust and meaningful results. While heuristics and user-friendly software can be useful for simple designs and models, they often fall short when more complex and customized simulations are required. The present tutorial presents a specific example of how to run power simulations for experimental designs with GLMMs.

## Expected effect size vs. smallest effect size of interest: sensitivity power analysis

In our case study, we have performed power simulations based on a single set of 476 parameter values that reflect our assumptions of an expected effect size. Instead of extracting 477 this expected effect size from meta-analyses or pilot data, which has been the main focus of 478 previous tutorials, we have demonstrated some strategies to determine plausible parameter 479 values in GLMMs based on domain knowledge. Domain knowledge can be considered a vague theoretical model about the data-generating process that is less formal and can only be accessed by a back-and-forth exchange in which domain experts assess the plausibility of simulated data. When sample sizes are chosen based on the results of our power simulations, 483 a future study will be informative to reject the null hypothesis if an effect of our expected 484 size is present. However, if the true effect is indeed smaller, the power will be lower, and the 485

study might not be sufficiently informative. A common, more conservative strategy for 486 sample size justification is to perform power analysis for the smallest effect size of interest 487 (SESOI). An effect smaller than the SESOI would be considered too small to be interesting or 488 practically meaningful, even if the effect is not actually zero (King, 2011). For strategies on 489 the even more difficult task of specifying a plausible SESOI, as well as a thorough discussion 490 of various topics concerning power analysis, see (Lakens, 2022a). When domain knowledge or 491 formal theories about the research topic of interest are too vague to specify a meaningful 492 SESOI, it is still recommended to demonstrate power for different effect sizes in what is 493 called sensitivity power analysis. By simulating power for different effect sizes (in addition to 494 the different number of subjects and items), one can make sure that power would still be 495 sufficient to detect smaller effect sizes than our expected effect or at least get an impression 496 of how strongly power depends on the size of the true effect. In simple study designs, it is possible to perform sensitivity power analysis based on a single standardized effect size (e.g., analyse power in a two-sample t-test for a standardized mean difference varying between 0.1 and 0.8). However, for our case study that investigates combined hypotheses in a GLMM 500 modelling framework, the effect size is implicitly represented by the complex distribution of 501 probabilities within and between experimental conditions. In this setting, sensitivity power 502 analysis would require manually specifying additional sets of plausible parameter values that 503 reflect scenarios with smaller or larger differences between groups with respect to our specific 504 research question. Power could then be simulated for several of these scenarios (across 505 different numbers of subjects and items, as considered earlier). 506

#### 507 Outlook

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Beyond the specifics of our concrete case study, we want to outline six avenues regarding the future of power simulations in experimental research:

1. The need for power simulations in experimental research: Experimental research often involves intricate designs and complex models that cannot be adequately addressed by

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- heuristics or user-friendly software. Power simulations offer a solution by providing 512 experimental researchers with a tailored approach to estimating statistical power. 513 These simulations take into account the specific study design, account for the 514 underlying assumptions, and offer more accurate power estimates. 515
- 2. Managing simulations with discrete predictor variables: Power simulations become 516 more manageable when all predictor variables are discrete (like in the presented case 517 study) and fixed by the study design. This allows researchers to focus on simulating 518 outcome variables while avoiding the need for complex simulations of predictor values, 519 which would introduce additional assumptions. By simplifying the simulation process, 520 researchers can obtain reliable power estimates without compromising accuracy.
- 3. Teaching power simulation skills: The ability to conduct power simulations is a 522 valuable skill that should be taught to experimental researchers. By incorporating this 523 training into research methods courses and workshops, researchers can gain a deeper 524 understanding of statistical power and improve the quality of their experimental 525 designs. Equipping researchers with the knowledge and tools to perform power 526 simulations enables them to make informed decisions and enhance the rigor of their 527 studies. The need to reason about how to simulate plausible data that is in line with 528 the research hypothesis, while not violating domain expertise on how plausible data 529 should look like, might also contribute to planning more insightful studies that can 530 answer more precise research questions (Yarkoni, 2022). 531
- 4. Addressing the mismatch in effort perception: There is often a significant disconnect 532 between the amount of effort required to perform power analysis and the perceived 533 effort estimated by researchers and collaborators in experimental research. Many 534 researchers request power simulations from statisticians or methodological experts 535 without fully comprehending the complexity and time-consuming nature of these 536 tailored simulations. It is crucial to raise awareness about the effort involved in power 537

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- simulations to ensure realistic expectations and effective collaboration between researchers and methodological experts.
- 5. Recognizing the value of power simulations: Power simulations are not mere 540 technicalities; they are valuable research contributions that deserve recognition in experimental research. They offer insights into the robustness and sensitivity of experimental designs, helping researchers make informed decisions about sample sizes, 543 effect sizes, and statistical power. The importance of power simulations can be 544 reflected by allocating them a separate publication or incorporating them as a 545 significant component of stage 1 preregistered reports. 546
  - 6. Integration with Open Science and preregistration practices: Power simulations align well with the principles of Open Science and preregistration in experimental research. When researchers have access to simulated data based on their pre-specified model, analyzing the collected dataset becomes straightforward and unambiguous. By preregistering their power simulations, researchers enhance transparency and accountability of their experimental procedures, contributing to the credibility and reproducibility of research.

Conclusion 554

Power simulations play a critical role in experimental research, allowing investigators to 555 tailor power estimation to the unique aspects of their experiments. Through this tutorial, we 556 aim to provide researchers with the necessary skills and tools to perform these simulations for GLMMs themselves. By incorporating GLMMs and power analysis into research planning, 558 researchers can enhance the replicability and credibility of their work (Yarkoni, 2022).

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