Geometric Non-Termination Arguments for Integer Programs

Bachelor-Thesis

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Erklärung Ich versichere hiermit, dass ich die vorliegende Arbeit selbstständig verfasst und keine anderen als die angegebenen Quellen und Hilfsmittel benutzt sowie Zitate kenntlich gemacht habe.

Aachen, den August 6, 2017

Timo Bergerbusch

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- *AProVE* and it's way of proving

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