3. Exercise

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Exercise 3.1

1. a)

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\pi_{A,B}(R) \bowtie \pi_{B,C}(\pi_{A,C}(\sigma_{B=1}(R)) \bowtie \pi_{A,B}(R))
S_{1} := \{[a,b] \mid \exists c \ R(a,b,c)\}
S_{2} := \{[a,c] \mid \exists a,c \ R(a,1,c)\}
\pi_{B=1}(S_{2} \bowtie S_{1}) := \{[b,c] \mid \exists a,c_{1},c_{2} \ R(a,b,c_{1}) \land R(a,1,c_{2})\}
Insgesamt := \{[a,b,c] \mid \exists a_{1},c_{1},c_{2} \ R(a,b,c_{1}) \land R(a_{1},1,c) \land R(a_{1},b,c_{2})\}
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1.b)

$$\begin{array}{c|cccc} T_1 & & & & \\ \hline a & b & c_1 & \mathbf{R} \\ a_1 & 1 & c & \mathbf{R} \\ a_1 & b & c_2 & \mathbf{R} \\ \end{array}$$

2)

$$h_1: T_2 \to T_1: a \to a, b \to b, a_5 \to a_1, b_5 \to b_1, c_4 \to c_1$$

 $\Rightarrow T_2 \subseteq T_1$ (1)

$$h_2: T_1 \to T_2: a \to a, b \to b, b_1 \to b, c_1 \to c_4, a_1 \to a, b_2 \to b_5, c_2 \to c_4, b_3 \to b_5, c_3 \to c_4$$

$$\Rightarrow T_1 \subseteq T_2 \qquad (2)$$

$$(1)\&(2) \Rightarrow T_1 \equiv T_2$$

Exercise 3.2