### 7. Exercise

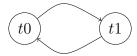
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## Exercise 7.1(Schedules, Serializability, and Locking)

#### 7.1.1

The schedule is not conflict serializable, because its corresponding conflict graph is cyclic. With the  $conflict(s_0)=\{(w_0(A),r_1(A)),(r_1(B),w_0(B))\}$ :



### 7.1.2

Using 2PL, we need to make sure that  $wl_i(X) < wu_i(Y), i \in \{0, 1\}, X, Y \in \{A, B\}$ . So we got the following schedule s':

$t_0$	$t_1$
$\overline{wl_0(A)}$	
$r_0(A)$	
$w_0(A)$	
	$wl_1(A) \to blocks$
$wl_0(B)$	
$r_0(B)$	
$w_0(B)$	
$wu_0(A)$	
$wu_0(B)$	
$c_0$	
	$wl_1(A) \rightarrow granted$
	$r_1(A)$
	$wl_1(B)$
	$r_1(B)$
	$wu_1(A)$
	$wu_1(B)$
	$c_1$

where the  $DT(s') = r_0(A)w_0(A)r_0(B)w_0(B)c_0r_1(A)r_1(B)c_1$ , and its conflict graph is acyclic with  $conflict(DT(s')) = \{(w_0(A), r_1(A)), (w_0(B), r_1(B))\}$ , so the schedule now is conflict serializable.:



#### 7.1.3

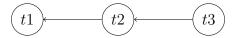
If we use locks without 2PL, we got the schedule s'':

$t_0$	$\mid t_1 \mid$
$wl_0(A)$	
$r_0(A)$	
$w_0(A)$	
$wu_0(A)$	
	$wl_1(A)$
	$r_1(A)$
	$wu_1(A)$
	$wl_1(B)$
	$r_1(B)$
	$wu_1(B)$
	$c_1$
$wl_0(B)$	
$r_0(B)$	
$w_0(B)$	
$wu_0(B)$	
$c_0$	

where  $DT(s'') = r_0(A)w_0(A)r_1(A)r_1(B)c_1r_0(B)w_0(B)c_0$ , and its conflict graph is cyclic with  $conflict(DT(s'')) = \{(w_0(A), r_1(A)), (r_1(B), w_0(B))\}$ . So the lock leads to a not conflict serializable schedule.

#### 7.1.4

$$s_1 = r_1(z)r_2(x)w_1(x)r_3(y)w_3(y)r_2(z)w_2(y)w_1(z)c_1c_2c_3$$



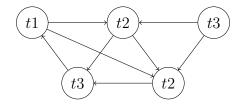
The conflict graph is acyclic, so  $s_1 \in CSR$ . There is no non-overlapped transactions in  $s_1$ , so  $s_1 \in OCSR$ . Commits in  $s_1$  is  $c_1c_2c_3$ , not in the "conflict order"  $t_3t_2t_1$ , so  $s_1 \notin CO$ .

$$s_2 = r_3(y)w_3(y)r_2(x)r_2(z)w_2(y)r_1(z)w_1(x)w_1(z)c_3c_2c_1$$



The conflict graph is acyclic, so  $s_2 \in CSR$ . Commits in  $s_2$  is  $c_3c_2c_1$ , in the "conflict order"  $t_3t_2t_1$ , so  $s_1 \in CO$ , and also  $s_1 \in OCSR$ .

 $s_3 = r_1(z)r_3(z)w_3(x)w_2(z)c_3r_4(x)w_4(z)c_2r_5(z)c_4w_5(y)w_1(y)c_1c_5$ 



The conflict graph contains cycles, so  $s_3 \notin CSR$ , as well as  $s_3 \notin OCSR$ ,  $s_3 \notin OC$ .

 $s_4 = r_1(z)r_3(z)w_3(x)w_2(z)r_4(x)c_2w_4(z)c_4r_5(z)c_3w_5(y)c_5w_1(y)c_1$ 

The order of actions except for commits in  $s_4$  is same with this in  $s_3$ , so they have same conflict graph. Thus,  $s_4 \notin CSR$ , as well as  $s_4 \notin OCSR$ ,  $s_4 \notin OC$ .

## Exercise 7.2(Recovery)

- 7.2.1
- 7.2.2
- 7.2.3

# **Exercise 7.3(B+-tree Locking)**

- 7.2.1
- 7.2.2
- 7.2.3