# 4. Exercise

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## **Exercise 4.1**

#### 1.

# $T_1$ and $T_2$

 $T_1 \subseteq T_2$ ?

Find mapping 
$$h:T_2\to T_1,x\rightarrowtail \begin{cases} b_3&x=b_1\\5&x=b_2\\b_4&x=b_3\\b_3&x=b_4\\a_1&x=a_1\\a_2&x=a_2 \end{cases} \Rightarrow T_1\subseteq T_2$$

$$T_2 \subseteq T_1$$
?

Impossible since we would have to map the constant 5 to an other constant and  $T_2$  does not contain a constant. So  $T_2 \not\subseteq T_1$ 

#### **Overall**

$$\Rightarrow T_1 \subset T_2$$
, but  $T_2 \not\subseteq T_1$  and therefore  $T_1 \not\equiv T_2$ 

# $T_2$ and $T_3$

$$T_2 \subseteq T_3$$
?

When we map  $T_3$  to  $T_2$ :

$$a1 \rightarrow a1$$

$$a2 \rightarrow a2$$

$$b3 \rightarrow b4$$

$$b2 \rightarrow b3$$

 $b1 \rightarrow a1$ , but then for (b4, b1) in  $T_3$  we cannot find a matched instance in  $T_1$ 

So there can not exists a function  $h: T_3 \to T_2$ .  $\Rightarrow T_2 \not\subseteq T_3$ 

 $T_3 \subseteq T_2$ ?

When we map  $T_2$  to  $T_3$ :

 $a1 \rightarrow a1$ 

 $a2 \rightarrow a2$ 

 $b4 \rightarrow b3$ 

 $b1 \rightarrow b4$ 

 $b3 \rightarrow b2$ 

 $b2 \rightarrow b2$  (or b1)

but then for (b3,b2) in  $T_2$  we cannot find a matched instance in  $T_3$  So there can not exists a function  $h: T_2 \to T_3$ .  $\Rightarrow T_3 \not\subseteq T_2$ 

#### **Overall**

 $\Rightarrow T_2 \not\subseteq T_3, T_3 \not\subseteq T_2$  and therefore especially  $T_2 \not\equiv T_3$ 

# $T_1$ and $T_3$

$$T_1 \subseteq T_3$$
?

When we map  $T_3$  to  $T_1$ :

 $a1 \rightarrow a1$ 

 $a2 \rightarrow a2$ 

 $b3 \rightarrow b3$ 

 $b2 \rightarrow b4$ 

 $b1 \rightarrow a1$ 

 $b2 \rightarrow 5$ , because of (b2, b3) in  $T_3$  and b3 $\rightarrow$  b3, so conflict with b2 $\rightarrow$  b4

So there can not exists a function  $h: T_3 \to T_1$ .  $\Rightarrow T_1 \not\subseteq T_3$ 

$$T_3 \subseteq T_3$$
?

Analogously to  $T_2 \subseteq T_1$  we would have to map the constant 5 to an other constant and  $T_3$  does not contain a constant. So  $T_3 \not\subseteq T_1$ 

#### **Overall**

 $\Rightarrow T_1 \not\subseteq T_3, T_3 \not\subseteq T_1$  and therefore especially  $T_1 \not\equiv T_3$ 

## 2.

 $T_1$ :

 $T_1$  is minimal, because if we delete any row and so create T' we can not have a function  $h:T\to T'$  such that  $T'\subseteq T$ 

2

 $T_2$ :

1. delete row  $(b_4, a_2)$ , since we have a function  $h_1$ , with  $h_1(x) = \begin{cases} b_1 & \text{if } x = b_4 \\ x & \text{if } x \neq b_4 \end{cases}$ 

New Tableau 7		au $T_2^\prime$	
	$a_1$	$a_2$	
	$b_1$	$a_2$	(R)
	$a_1$	$b_3$	(R)
	$b_2$	$b_1$	(R)
	$b_3$	$b_2$	(R)

2. we can't minimize  $T_2^{\prime\prime}$  any further, so  $T_2^{\prime\prime}$  is the minimal tableau

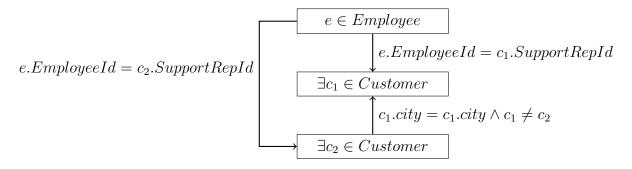
## $T_3$ :

 $T_3$  is minimal, because if we delete any row and so create T' we can not have a function  $h:T\to T'$  such that  $T'\subseteq T$ 

## Exercise 4.2

## 1.a)

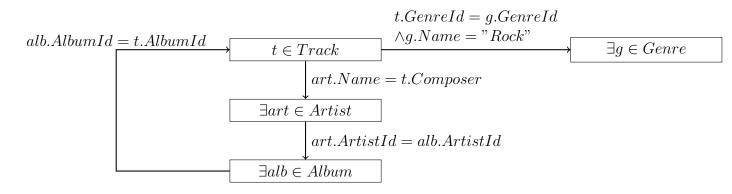
 $\{ \langle e.EmployeeId, e.LastName \rangle | e \in Employee \land \exists c_1 \in Customer \land c_1.SupportedRepId = e.EmployeeId \land \exists c_2 \in Customer \land c_2.SupportRepId = e.EmployeeId \land c_1.City = c_2.City \land c_1 \neq c_2 \}$ 



This graph is cycle free, which means the query is optimizable using semi-joins.

#### 1.b)

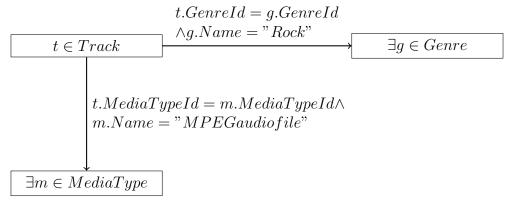
 $\{ < t.name, t.composer > | \ t \in Track \land \exists g \in Genre \land g.GenreId = t.GenreId \land g.Name = "Rock" \land \exists art \in Artist \land \exists alb \in Album \land alb.ArtistId = art.ArtistId \land t.AlbumId = alb.AlbumId \land t.Composer = art.Name \}$ 



This Graph has a cycle. This means the query is not optimizable using semi-joins.

## 2.

 $\{ \langle t.Name \rangle | \ t \in Track \land t.Miliseconds \leq 90000 \land \exists g \in Genre \land t.GenreId = t.GenreId \land g.Name = "Rock" \land \exists m \in MediaType \land t.MediaTypeId = m.MediaTypeid \land m.Name = "MPEGaudiofile" \}$ 



TODO: es fehlt das mit den ≤90000ms

The graph is cycle free, which means it can be optimized using semi-joins.

## Exercise 4.3

#### 1.

B = # buffer pages in memory = 4 N = # pages in the input file =  $\lceil \frac{7500 \cdot 36}{1024 - 64} \rceil = 282$ After the initial pass: # runs (subfiles) =  $\lceil \frac{N}{B} \rceil = \lceil \frac{282}{4} \rceil = 71$ , each subfiles: 4-pages runs

### 2.

# passes = 
$$1+\lceil\log_{B-1}\lceil\frac{N}{B}\rceil\rceil=1+\lceil\log_{4-1}71\rceil=1+4=5$$

### **3.**

Total costs =  $2N \cdot (\#passes) = 2 \cdot 282 \cdot 5 = 2820$  I/Os

### 4.

If B = 4: 
$$1+\lceil\log_3\lceil\frac{N}{B}\rceil\rceil=2\Rightarrow(\log_3\lceil\frac{N}{4}\rceil)_{max}=1\Rightarrow(\lceil\frac{N}{4}\rceil)_{max}=3\Rightarrow N_{max}=12$$
 # records in the file =  $\frac{12\cdot(1024-64)}{36}=320$  records

If B = 42: 
$$1 + \lceil \log_{41} \lceil \frac{N}{B} \rceil \rceil = 2 \Rightarrow (\log_4 1 \lceil \frac{N}{42} \rceil)_{max} = 1 \Rightarrow (\lceil \frac{N}{42} \rceil)_{max} = 41 \Rightarrow N_{max} = 41 \cdot 42 = 1722$$
 # records in the file =  $\frac{1722 \cdot (1024 - 64)}{36} = 45920$  records