Prof. Dr. Ir. Dr. h. c. Joost-Pieter Katoen

Christian Hensel, Matthias Volk

## Introduction to Model Checking (Summer Term 2018)

## -- Exercise Sheet 3 (due 14th May) --

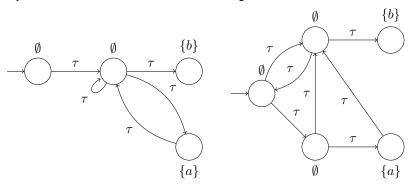
## General Remarks

- The exercises are to be solved in groups of *three* students.
- You may hand in your solutions for the exercises just before the exercise class starts at 12:15 or by dropping them into the "Introduction to Model Checking" box at our chair *before 12:00*. Do *not* hand in your solutions via L2P or via e-mail.

Exercise 1 (1+1 Points)

Consider the following transition systems. Note that the transition systems might contain terminal states.

 $TS_1:$   $TS_2:$ 



- (a) Give the traces of  $TS_1$ , i.e.,  $Traces(TS_1)$ .
- (b) Are TS<sub>1</sub> and TS<sub>2</sub> trace equivalent?

Exercise 2<sup>\*</sup> (4+4 Points)

In the following we show that LT properties are not solely a theoretical concept but have a wide range of practical applications. As proof, we apply the concept of LT properties to movie/TV series quotes.

- (a) We assume each following quote informally describes some property. Formulate these properties as LT properties over the given set AP of atomic propositions:
  - (i) "Winter is coming."  $AP = \{winter\}.$ winter will eventually by reached.
  - (ii) "Everything is awesome."  $AP = \{awesome\}.$  awesome always holds.
  - (iii) "I'll be back."  $AP = \{here\}.$

I am currently *here* but at some point I will not be *here*. However, I will be *here* again at a later time.

(iv) "You either die a hero, or you live long enough to see yourself become the villain."  $AP = \{live, hero\}.$ 

In the beginning, you *live* and are a *hero*. You either cease to *live* and die, still being a *hero*, or you *live* but become the villain, i.e., you are not a *hero* anymore.

(v) "By night one way, by day another

Thus shall be the norm

Till you receive true love's kiss

then, take love's true form."

 $AP = \{day, form_1, form_2, true\_form, kiss\}.$ 

You start by having  $form_1$  at night, i.e., not day. You alternate between  $form_1$  at night and  $form_2$  by day. This alternation goes on till at some point you receive true love's kiss and from there on have love's true form.

(vi) "A Lannister always pays his debts."

 $AP = \{in \ debt\}.$ 

Whenever a Lannister is  $in\_debt$ , he will be  $in\_debt$  as long as he has not payed back his debt. If he has payed back his debt, he is no longer  $in\_debt$ . A Lannister can be  $in\_debt$  arbitrarily (but finitely) many times.

(vii) "Anything is possible [if you just believe]."

 $AP = \{ap_1, \dots, ap_n\}.$ 

We do not consider the second part here and just concentrate on the fact, that everything is possible.

(viii) "It's gonna be legen... wait for it... dary!"

 $AP = \{legen, wait\_for\_it, dary\}.$ 

In the beginning it is legen, then we have to  $wait\_for\_it$  for some time, and then it is dary at some point.

- (b) Determine for all LT properties of (a) whether they are
  - (i) safety properties and/or
  - (ii) liveness properties.

Justify your answers.

Exercise 3 (3+3 Points)

- (a) Let P and P' be liveness properties over AP. Prove or disprove the following claims:
  - (i)  $P \cup P'$  is a liveness property,
  - (ii)  $P \cap P'$  is a liveness property.
- (b) Answer the same questions for P and P' being safety properties.

Hint: you can use the distributivity of union over closure for LT properties P, P':

 $closure(P \cup P') = closure(P) \cup closure(P')$ 

Exercise 4 (4 Points)

Let P be an LT property. Prove: pref(closure(P)) = pref(P).