See the Assessment Guide for information on how to interpret this report.

## ASSESSMENT SUMMARY

```
Compilation: PASSED (0 errors, 3 warnings)
API:
             PASSED
SpotBugs:
            PASSED
PMD:
             FAILED (1 warning)
Checkstyle: PASSED
Correctness: 49/49 tests passed
Memory:
             124/124 tests passed
Timing:
             193/193 tests passed
Aggregate score: 100.00%
[ Compilation: 5%, API: 5%, Style: 0%, Correctness: 60%, Timing: 10%, Memory: 20% ]
```

## ASSESSMENT DETAILS

```
The following files were submitted:
-----
3.9K Sep 21 20:07 Deque.java
795 Sep 21 20:07 Permutation.java
4.3K Sep 21 20:07 RandomizedQueue.java
**********************************
  COMPTI TNG
% javac Deque.java
% javac RandomizedQueue.java
RandomizedQueue.java:18: warning: [unchecked] unchecked cast
       arr = (Item[]) new Object[1];
  required: Item[]
  found:
         Object[]
 where Item is a type-variable:
   Item extends Object declared in class RandomizedQueue
RandomizedQueue.java:47: warning: [unchecked] unchecked cast
       Item[] tempArr = (Item[]) new Object[size];
  required: Item[]
  found:
           Object[]
 where Item is a type-variable:
   Item extends Object declared in class RandomizedQueue
RandomizedQueue.java:94: warning: [unchecked] unchecked cast
           iterArr = (Item[]) new Object[sizeN];
 required: Item[]
  found:
           Object[]
 where Item is a type-variable:
   Item extends Object declared in class RandomizedQueue
3 warnings
```

% javac Permutation.java *
Checking the APIs of your programs.
*
Deque:
RandomizedQueue:
Permutation:
**************************************
% spotbugs *.class *
% pmd .
Permutation.java:12: Avoid unused local variables, such as 'n'. [UnusedLocalVariable] PMD ends with 1 warning.
% checkstyle *.java *
% custom checkstyle checks for Deque.java
% custom checkstyle checks for RandomizedQueue.java
% custom checkstyle checks for Permutation.java
**************************************
Testing correctness of Deque
Running 19 total tests.
Tests 1-8 make random intermixed calls to addFirst(), addLast(), removeFirst(), removeLast(), isEmpty(), and size(), and iterator(). The probabilities of each operation are (p1, p2, p3, p4, p5, p6, p7), respectively.

```
Test 1: check random calls to addFirst(), addLast(), and size()
       5 random calls (0.4, 0.4, 0.0, 0.0, 0.0, 0.2, 0.0)
      50 random calls (0.4, 0.4, 0.0, 0.0, 0.0, 0.2, 0.0)
     500 random calls (0.4, 0.4, 0.0, 0.0, 0.0, 0.2, 0.0)
  * 1000 random calls (0.4, 0.4, 0.0, 0.0, 0.0, 0.2, 0.0)
==> passed
Test 2: check random calls to addFirst(), removeFirst(), and isEmpty()
       5 random calls (0.8, 0.0, 0.1, 0.0, 0.1, 0.0, 0.0)
      50 random calls (0.8, 0.0, 0.1, 0.0, 0.1, 0.0, 0.0)
     500 random calls (0.8, 0.0, 0.1, 0.0, 0.1, 0.0, 0.0)
   1000 random calls (0.8, 0.0, 0.1, 0.0, 0.1, 0.0, 0.0)
       5 random calls (0.1, 0.0, 0.8, 0.0, 0.1, 0.0, 0.0)
      50 random calls (0.1, 0.0, 0.8, 0.0, 0.1, 0.0, 0.0)
     500 random calls (0.1, 0.0, 0.8, 0.0, 0.1, 0.0, 0.0)
  * 1000 random calls (0.1, 0.0, 0.8, 0.0, 0.1, 0.0, 0.0)
==> passed
Test 3: check random calls to addFirst(), removeLast(), and isEmpty()
       5 random calls (0.8, 0.0, 0.0, 0.1, 0.1, 0.0, 0.0)
      50 random calls (0.8, 0.0, 0.0, 0.1, 0.1, 0.0, 0.0)
     500 random calls (0.8, 0.0, 0.0, 0.1, 0.1, 0.0, 0.0)
   1000 random calls (0.8, 0.0, 0.0, 0.1, 0.1, 0.0, 0.0)
       5 random calls (0.1, 0.0, 0.0, 0.8, 0.1, 0.0, 0.0)
      50 random calls (0.1, 0.0, 0.0, 0.8, 0.1, 0.0, 0.0)
     500 random calls (0.1, 0.0, 0.0, 0.8, 0.1, 0.0, 0.0)
  * 1000 random calls (0.1, 0.0, 0.0, 0.8, 0.1, 0.0, 0.0)
==> passed
Test 4: check random calls to addLast(), removeLast(), and isEmpty()
       5 random calls (0.0, 0.8, 0.0, 0.1, 0.1, 0.0, 0.0)
      50 random calls (0.0, 0.8, 0.0, 0.1, 0.1, 0.0, 0.0)
     500 random calls (0.0, 0.8, 0.0, 0.1, 0.1, 0.0, 0.0)
   1000 random calls (0.0, 0.8, 0.0, 0.1, 0.1, 0.0, 0.0)
       5 random calls (0.0, 0.1, 0.0, 0.8, 0.1, 0.0, 0.0)
      50 random calls (0.0, 0.1, 0.0, 0.8, 0.1, 0.0, 0.0)
     500 random calls (0.0, 0.1, 0.0, 0.8, 0.1, 0.0, 0.0)
  * 1000 random calls (0.0, 0.1, 0.0, 0.8, 0.1, 0.0, 0.0)
==> passed
Test 5: check random calls to addLast(), removeFirst(), and isEmpty()
       5 random calls (0.0, 0.8, 0.1, 0.0, 0.1, 0.0, 0.0)
      50 random calls (0.0, 0.8, 0.1, 0.0, 0.1, 0.0, 0.0)
     500 random calls (0.0, 0.8, 0.1, 0.0, 0.1, 0.0, 0.0)
   1000 random calls (0.0, 0.8, 0.1, 0.0, 0.1, 0.0, 0.0)
       5 random calls (0.0, 0.1, 0.8, 0.0, 0.1, 0.0, 0.0)
      50 random calls (0.0, 0.1, 0.8, 0.0, 0.1, 0.0, 0.0)
     500 random calls (0.0, 0.1, 0.8, 0.0, 0.1, 0.0, 0.0)
  * 1000 random calls (0.0, 0.1, 0.8, 0.0, 0.1, 0.0, 0.0)
==> passed
Test 6: check random calls to addFirst(), removeFirst(), and iterator()
       5 random calls (0.8, 0.0, 0.1, 0.0, 0.0, 0.0, 0.1)
      50 random calls (0.8, 0.0, 0.1, 0.0, 0.0, 0.0, 0.1)
     500 random calls (0.8, 0.0, 0.1, 0.0, 0.0, 0.0, 0.1)
    1000 random calls (0.8, 0.0, 0.1, 0.0, 0.0, 0.0, 0.1)
       5 random calls (0.1, 0.0, 0.8, 0.0, 0.0, 0.0, 0.1)
      50 random calls (0.1, 0.0, 0.8, 0.0, 0.0, 0.0, 0.1)
     500 random calls (0.1, 0.0, 0.8, 0.0, 0.0, 0.0, 0.1)
  * 1000 random calls (0.1, 0.0, 0.8, 0.0, 0.0, 0.0, 0.1)
==> passed
Test 7: check random calls to all methods except iterator()
       5 random calls (0.3, 0.3, 0.1, 0.1, 0.1, 0.0)
      50 random calls (0.3, 0.3, 0.1, 0.1, 0.1, 0.0)
     500 random calls (0.3, 0.3, 0.1, 0.1, 0.1, 0.0)
   1000 random calls (0.3, 0.3, 0.1, 0.1, 0.1, 0.0)
       5 random calls (0.1, 0.1, 0.3, 0.3, 0.1, 0.1, 0.0)
      50 random calls (0.1, 0.1, 0.3, 0.3, 0.1, 0.1, 0.0)
```

```
500 random calls (0.1, 0.1, 0.3, 0.3, 0.1, 0.1, 0.0)
  * 1000 random calls (0.1, 0.1, 0.3, 0.3, 0.1, 0.1, 0.0)
==> passed
Test 8: check random calls to all methods, including iterator()
       5 random calls (0.2, 0.2, 0.1, 0.1, 0.1, 0.2)
      50 random calls (0.2, 0.2, 0.1, 0.1, 0.1, 0.2)
     500 random calls (0.2, 0.2, 0.1, 0.1, 0.1, 0.2)
   1000 random calls (0.2, 0.2, 0.1, 0.1, 0.1, 0.1, 0.2)
      5 random calls (0.1, 0.1, 0.2, 0.2, 0.1, 0.1, 0.2)
      50 random calls (0.1, 0.1, 0.2, 0.2, 0.1, 0.1, 0.2)
     500 random calls (0.1, 0.1, 0.2, 0.2, 0.1, 0.1, 0.2)
  * 1000 random calls (0.1, 0.1, 0.2, 0.2, 0.1, 0.1, 0.2)
==> passed
Test 9: check removeFirst() and removeLast() from an empty deque
  * removeFirst()
  * removeLast()
==> passed
Test 10: check whether two Deque objects can be created at the same time
  * n = 10
  * n = 1000
==> passed
Test 11: check iterator() after n calls to addFirst()
  * n = 10
  * n = 50
==> passed
Test 12: check iterator() after random calls to addFirst(), addLast(),
         removeFirst(), and removeLast() with probabilities (p1, p2, p3, p4)
  * 20 random operations (0.8, 0.0, 0.2, 0.0)
  * 20 random operations (0.8, 0.0, 0.0, 0.2)
  * 20 random operations (0.0, 0.8, 0.0, 0.2)
  * 20 random operations (0.0, 0.8, 0.2, 0.0)
  * 20 random operations (0.4, 0.4, 0.1, 0.1)
  * 20 random operations (0.2, 0.0, 0.8, 0.0)
  * 20 random operations (0.2, 0.0, 0.0, 0.8)
  * 20 random operations (0.0, 0.2, 0.0, 0.8)
  * 20 random operations (0.0, 0.2, 0.8, 0.0)
  * 20 random operations (0.1, 0.1, 0.4, 0.4)
  * 100 random operations (0.4, 0.4, 0.1, 0.1)
  * 1000 random operations (0.4, 0.4, 0.1, 0.1)
==> passed
Test 13: create two nested iterators to same deque of size n
  * n = 10
  * n = 50
==> passed
Test 14: create two parallel iterators to same deque of size n
  * n = 10
  * n = 50
==> passed
Test 15: create an iterator and check calls to next() and hasNext()
  * 10 consecutive calls to hasNext() on a deque of size 10
  * 10 consecutive calls to next() on a deque of size 10
  * 50 random intermixed calls to next() and hasNext() on a deque of size 10
  * 1000 random intermixed calls to next() and hasNext() on a deque of size 100
==> passed
Test 16: create Deque objects of different parameterized types
==> passed
Test 17: call addFirst() and addLast() with null argument
==> passed
```

```
Test 18: check that remove() and next() throw the specified exceptions in iterator()
==> passed
Test 19: call iterator() when the deque is empty
==> passed
Total: 19/19 tests passed!
______
Testing correctness of RandomizedQueue
*_____
Running 21 total tests.
Tests 1-6 make random intermixed calls to enqueue(), dequeue(), sample(),
isEmpty(), size(), and iterator(). The probabilities of each operation
are (p1, p2, p3, p4, p5, p6), respectively.
Test 1: check random calls to enqueue() and size()
      5 random calls (0.8, 0.0, 0.0, 0.0, 0.2, 0.0)
     50 random calls (0.8, 0.0, 0.0, 0.0, 0.2, 0.0)
    500 random calls (0.8, 0.0, 0.0, 0.0, 0.2, 0.0)
  * 1000 random calls (0.8, 0.0, 0.0, 0.0, 0.2, 0.0)
==> passed
Test 2: check random calls to enqueue() and dequeue()
      5 random calls (0.7, 0.1, 0.0, 0.1, 0.1, 0.0)
     50 random calls (0.7, 0.1, 0.0, 0.1, 0.1, 0.0)
    500 random calls (0.7, 0.1, 0.0, 0.1, 0.1, 0.0)
   1000 random calls (0.7, 0.1, 0.0, 0.1, 0.1, 0.0)
      5 random calls (0.1, 0.7, 0.0, 0.1, 0.1, 0.0)
     50 random calls (0.1, 0.7, 0.0, 0.1, 0.1, 0.0)
    500 random calls (0.1, 0.7, 0.0, 0.1, 0.1, 0.0)
  * 1000 random calls (0.1, 0.7, 0.0, 0.1, 0.1, 0.0)
==> passed
Test 3: check random calls to enqueue() and sample()
      5 random calls (0.8, 0.0, 0.2, 0.0, 0.0, 0.0)
     50 random calls (0.8, 0.0, 0.2, 0.0, 0.0, 0.0)
    500 random calls (0.8, 0.0, 0.2, 0.0, 0.0, 0.0)
   1000 random calls (0.8, 0.0, 0.2, 0.0, 0.0, 0.0)
      5 random calls (0.2, 0.0, 0.8, 0.0, 0.0, 0.0)
     50 random calls (0.2, 0.0, 0.8, 0.0, 0.0, 0.0)
    500 random calls (0.2, 0.0, 0.8, 0.0, 0.0, 0.0)
  * 1000 random calls (0.2, 0.0, 0.8, 0.0, 0.0, 0.0)
==> passed
Test 4: check random calls to enqueue() and iterator()
      5 random calls (0.8, 0.0, 0.0, 0.0, 0.0, 0.2)
     50 random calls (0.8, 0.0, 0.0, 0.0, 0.0, 0.2)
    500 random calls (0.8, 0.0, 0.0, 0.0, 0.0, 0.2)
  * 1000 random calls (0.8, 0.0, 0.0, 0.0, 0.0, 0.2)
==> passed
Test 5: check random calls to all methods except iterator()
      5 random calls (0.6, 0.1, 0.1, 0.1, 0.0)
     50 random calls (0.6, 0.1, 0.1, 0.1, 0.0)
    500 random calls (0.6, 0.1, 0.1, 0.1, 0.0)
  * 1000 random calls (0.6, 0.1, 0.1, 0.1, 0.0)
      5 random calls (0.1, 0.6, 0.1, 0.1, 0.0)
     50 random calls (0.1, 0.6, 0.1, 0.1, 0.0)
    500 random calls (0.1, 0.6, 0.1, 0.1, 0.0)
  * 1000 random calls (0.1, 0.6, 0.1, 0.1, 0.1, 0.0)
==> passed
Test 6: check random calls to all methods, including iterator()
      5 random calls (0.5, 0.1, 0.1, 0.1, 0.1)
     50 random calls (0.5, 0.1, 0.1, 0.1, 0.1)
```

```
* 500 random calls (0.5, 0.1, 0.1, 0.1, 0.1)
  * 1000 random calls (0.5, 0.1, 0.1, 0.1, 0.1, 0.1)
      5 random calls (0.1, 0.5, 0.1, 0.1, 0.1)
     50 random calls (0.1, 0.5, 0.1, 0.1, 0.1)
    500 random calls (0.1, 0.5, 0.1, 0.1, 0.1, 0.1)
  * 1000 random calls (0.1, 0.5, 0.1, 0.1, 0.1, 0.1)
==> passed
Test 7: call dequeue() and sample() from an empty randomized queue
  * dequeue()
  * sample()
==> passed
Test 8: create multiple randomized queue objects at the same time
  * n = 10
  * n = 100
==> passed
Test 9: check that iterator() returns correct items after a sequence
        of n enqueue() operations
  * n = 10
  * n = 50
==> passed
Test 10: check that iterator() returns correct items after intermixed
         sequence of m enqueue() and dequeue() operations
  * m = 10
  * m = 1000
==> passed
Test 11: create two nested iterators over the same randomized queue of size n
  * n = 10
  * n = 50
==> passed
Test 12: create two parallel iterators over the same randomized queue of size n
  * n = 10
  * n = 50
==> passed
Test 13: create two iterators over different randomized queues,
         each of length 10
==> passed
Test 14: create an iterator and check calls to next() and hasNext()
  * 10 consecutive calls to hasNext() on a deque of size 10
  * 10 consecutive calls to next() on a deque of size 10
  * 50 random intermixed calls to next() and hasNext() on a deque of size 10
  * 1000 random intermixed calls to next() and hasNext() on a deque of size 100
==> passed
Test 15: create RandomizedQueue objects of different parameterized types
==> passed
Test 16: check randomness of sample() by enqueueing n items, repeatedly calling
         sample(), and counting the frequency of each item
  * n = 3, trials = 12000
  * n = 5, trials = 12000
  * n = 8, trials = 12000
  * n = 10, trials = 12000
==> passed
Test 17: check randomness of dequeue() by enqueueing n items, dequeueing n items,
         and seeing whether each of the n! permutations is equally likely
  * n = 2, trials = 12000
  * n = 3, trials = 12000
  * n = 4, trials = 12000
  * n = 5, trials = 12000
==> passed
```

```
Test 18: check randomness of iterator() by enqueueing n items, iterating over those
        n items, and seeing whether each of the n! permutations is equally likely
 * n = 2, trials = 12000
 * n = 3, trials = 12000
 * n = 4, trials = 12000
 * n = 5, trials = 12000
==> passed
Test 19: call enqueue() with a null argument
Test 20: check that remove() and next() throw the specified exceptions in iterator()
==> passed
Test 21: call iterator() when randomized queue is empty
==> passed
Total: 21/21 tests passed!
_____
********************************

    * TESTING CORRECTNESS (substituting reference RandomizedQueue and Deque)

*******************************
Testing correctness of Permutation
Tests 1-5 call the main() function directly, resetting standard input
before each call.
Running 9 total tests.
Test 1a: check formatting for sample inputs from assignment specification
 % java Permutation 3 < distinct.txt</pre>
 C
 Α
 Ε
 % java Permutation 3 < distinct.txt</pre>
 Ι
 C
 % java Permutation 8 < duplicates.txt
 AΑ
 CC
  ВВ
  ВВ
  BB
 BB
 CC
==> passed
Test 1b: check formatting for other inputs
 % java Permutation 8 < mediumTale.txt
 was
 it
 the
 of
 the
 wisdom
 best
 age
 % java Permutation 0 < distinct.txt</pre>
```

```
==> passed
Test 2: check that main() reads all data from standard input
 * filename = distinct.txt, k = 3
 * filename = distinct.txt, k = 3
 * filename = duplicates.txt, k = 8
 * filename = mediumTale.txt, k = 8
==> passed
Test 3a: check that main() prints each item from the sequence at most once
        (for inputs with no duplicate strings)
  * filename = distinct.txt, k = 3
  * filename = distinct.txt, k = 1
 * filename = distinct.txt, k = 9
 * filename = permutation6.txt, k = 6
  * filename = permutation10.txt, k = 10
==> passed
Test 3b: check that main() prints each item from the sequence at most once
        (for inputs with duplicate strings)
 * filename = duplicates.txt, k = 8
 * filename = duplicates.txt, k = 3
 * filename = permutation8.txt, k = 6
  * filename = permutation8.txt, k = 2
  * filename = tinyTale.txt, k = 10
==> passed
Test 3c: check that main() prints each item from the sequence at most once
        (for inputs with newlines)
 * filename = mediumTale.txt, k = 10
  * filename = mediumTale.txt, k = 20
 * filename = tale.txt, k = 10
  * filename = tale.txt, k = 50
==> passed
Test 4: check main() when k = 0
  * filename = distinct.txt, k = 0
  * filename = distinct.txt, k = 0
==> passed
Test 5a: check that permutations are uniformly random
        (for inputs with no duplicate strings)
 * filename = permutation4.txt, k = 1
 * filename = permutation4.txt, k = 2
 * filename = permutation4.txt, k = 3
 * filename = permutation4.txt, k = 4
  * filename = permutation6.txt, k = 2
==> passed
Test 5b: check that permutations are uniformly random
        (for inputs with duplicate strings)
 * filename = permutation5.txt, k = 1
 * filename = permutation5.txt, k = 2
 * filename = permutation5.txt, k = 3
 * filename = duplicates.txt, k = 3
  * filename = permutation8.txt, k = 2
==> passed
Total: 9/9 tests passed!
______
*******************************
  TIMING (substituting reference RandomizedQueue and Deque)
***********************************
```

Timing Permutation

\*\_\_\_\_\_

Running 23 total tests.

Test 1: count calls to methods in StdIn

- \* java Permutation 5 < distinct.txt
- \* java Permutation 10 < permutation10.txt
- \* java Permutation 1 < mediumTale.txt
- \* java Permutation 20 < tale.txt
- \* java Permutation 100 < tale.txt
- \* java Permutation 16412 < tale.txt
- ==> passed

Test 2: count calls to methods in Deque and RandomizedQueue

- \* java Permutation 5 < distinct.txt
- \* java Permutation 10 < permutation10.txt
- \* java Permutation 1 < mediumTale.txt
- \* java Permutation 20 < tale.txt
- \* java Permutation 100 < tale.txt
- \* java Permutation 16412 < tale.txt
- ==> passed

Test 3: count calls to methods in StdRandom

- \* java Permutation 5 < distinct.txt
- \* java Permutation 10 < permutation10.txt
- \* java Permutation 1 < mediumTale.txt
- \* java Permutation 20 < tale.txt
- \* java Permutation 100 < tale.txt
- \* java Permutation 16412 < tale.txt
- ==> passed

Test 4: Time main() with k = 5, for inputs containing n random strings

	n	seconas
=> passed	1000	0.00
=> passed	2000	0.00
=> passed	4000	0.00
=> passed	8000	0.00
=> passed	16000	0.00
=> passed	32000	0.01
=> passed	64000	0.02
=> passed	128000	0.04
=> passed	256000	0.07
=> passed	512000	0.15
==> 10/10	tests passed	l

Test 5: Time main() with k = 1000, for inputs containing n random strings

		n	seconds
=>	passed	1000	0.00
=>	passed	2000	0.00
=>	passed	4000	0.00
=>	passed	8000	0.00
=>	passed	16000	0.00
=>	passed	32000	0.01
=>	passed	64000	0.02
=>	passed	128000	0.04
=>	passed	256000	0.07
=>	passed	512000	0.14
=='	10/10	tests passed	l

Total: 23/23 tests passed!

\_\_\_\_\_\_

```
**********************************
 MEMORY
********************************
Analyzing memory of Permutation
*_____
Running 2 total tests.
Test 1: check that only one Deque or RandomizedQueue object is created
 * filename = distinct.txt, n = 9, k = 1
 * filename = distinct.txt, n = 9, k = 2
 * filename = distinct.txt, n = 9, k = 4
 * filename = tinyTale.txt, n = 12, k = 10
 * filename = tale.txt, n = 138653, k = 50
==> passed
Test 2: check that the maximum size of any Deque or RandomizedQueue object
       created is between k and n
 * filename = distinct.txt, n = 9, k = 1
 * filename = distinct.txt, n = 9, k = 2
 * filename = distinct.txt, n = 9, k = 4
 * filename = tinyTale.txt, n = 12, k = 10
 * filename = tale.txt, n = 138653, k = 5
 * filename = tale.txt, n = 138653, k = 50
 * filename = tale.txt, n = 138653, k = 500
 * filename = tale.txt, n = 138653, k = 5000
 * filename = tale.txt, n = 138653, k = 50000
==> passed
Test 3 (bonus): check that maximum size of any or Deque or RandomizedQueue object
             created is equal to k
 * filename = tale.txt, n = 138653, k = 5
   - max size of RandomizedQueue object = 138653
 * filename = tale.txt, n = 138653, k = 50
   - max size of RandomizedQueue object = 138653
 * filename = tale.txt, n = 138653, k = 500
   - max size of RandomizedQueue object = 138653
 * filename = tale.txt, n = 138653, k = 5000
   - max size of RandomizedQueue object = 138653
 * filename = tale.txt, n = 138653, k = 50000
   - max size of RandomizedQueue object = 138653
==> FAILED
Total: 2/2 tests passed!
***********************************
Analyzing memory of Deque
For tests 1-4, the maximum amount of memory allowed for a Deque
containing n items is 48n + 192.
Running 49 total tests.
Test 1a-1i: total memory usage after inserting n items,
```

where n is a power of 2

	n	bytes	
=> passed	32 64 128 256 512 1024 2048 4096 8192 passed	1576 3112 6184 12328 24616 49192 98344 196648 393256	

Memory:  $48.00 \text{ n} + 40.00 \text{ (R}^2 = 1.000)$ 

Test 2a-2i: Total memory usage after inserting n items, when n is one more than a power of 2.

-> nassed 22 1624	
=> passed 33 1624 => passed 65 3160 => passed 129 6232 => passed 257 12376 => passed 513 24664 => passed 1025 49240 => passed 2049 98392 => passed 4097 196696	
=> passed 8193 393304 ==> 9/9 tests passed	

Memory:  $48.00 \text{ n} + 40.00 \text{ (R}^2 = 1.000)$ 

Test 3a-3i: Total memory usage after inserting 2n-1 items, and then deleting n-1 items, when n is one more than a power of 2.

	n	bytes	
=> passed	33	1624	
=> passed	65 129	3160 6232	
<pre>=&gt; passed =&gt; passed</pre>	257	12376	
=> passed	513	24664	
=> passed	1025	49240	
=> passed	2049	98392	
<pre>=&gt; passed =&gt; passed</pre>	4097 8193	196696 393304	
==> 9/9 tests		393304	

Memory:  $48.00 \text{ n} + 40.00 \text{ (R}^2 = 1.000)$ 

Test 4a-4e: Total memory usage after inserting n items, and then deleting all but one item (should not grow with n or be too large of a constant).

	n	bytes	
=> passed	32 64 128 256 512 1024 2048	88 88 88 88 88 88	

```
4096
                             88
=> passed
              8192
                             88
=> passed
==> 9/9 tests passed
```

Memory: 88.00 (R^2 = 1.000)

Test 5a-5e: Total memory usage of iterator after inserting n items (should not grow with n or be too large of a constant).

```
n
                   bytes
_____
=> passed 32
                   32
=> passed
           64
                     32
          128
=> passed
                     32
=> passed 256
=> passed 512
=> passed 1024
=> passed 2048
                     32
                     32
                     32
                     32
          4096
=> passed
                     32
=> passed 8192
                     32
==> 9/9 tests passed
```

Memory: 32.00 (R<sup>2</sup> = 1.000)

```
Test 6a: Insert n strings; delete them one at a time, checking for
         loitering after each deletion. The probabilities of addFirst()
         and addLast() are (p1, p2), respectively. The probabilities of
         removeFirst() and removeLast() are (q1, q2), respectively.
```

- \* 100 random insertions (1.0, 0.0) and 100 random deletions (1.0, 0.0)
- \* 100 random insertions (1.0, 0.0) and 100 random deletions (0.0, 1.0)
- \* 100 random insertions (0.0, 1.0) and 100 random deletions (1.0, 0.0)
- \* 100 random insertions (0.0, 1.0) and 100 random deletions (0.0, 1.0)
- \* 100 random insertions (0.5, 0.5) and 100 random deletions (0.5, 0.5)

==> passed

Test 6b: Perform random operations, checking for loitering after each operation. The probabilities of addFirst(), addLast(), removeFirst(), and removeLast() are (p1, p2, p3, p4), respectively.

- \* 100 random operations (0.8, 0.0, 0.2, 0.0)
- \* 100 random operations (0.8, 0.0, 0.0, 0.2)
- \* 100 random operations (0.0, 0.8, 0.2, 0.0)
- \* 100 random operations (0.0, 0.8, 0.0, 0.2)
- \* 100 random operations (0.4, 0.4, 0.1, 0.1)
- \* 100 random operations (0.2, 0.2, 0.3, 0.3)
- ==> passed

Test 7: Perform m random add/remove operations in the deque and check that only constant memory is allocated/deallocated per operation

- \* m = 128
- \* m = 256
- \* m = 512
- ==> passed

Test 8: Insert m items into deque; then iterate over deque and check that only constant memory is allocated/deallocated per operation

- \* m = 64
- \* m = 128
- \* m = 256
- ==> passed

Min observed memory for Deque:  $48.00 \text{ n} + 40.00 \text{ (R}^2 = 1.000)$ Max observed memory for Deque:  $48.00 \text{ n} + 40.00 \text{ (R}^2 = 1.000)$ 

Total: 49/49 tests passed!

\_\_\_\_\_\_

## Analyzing memory of RandomizedQueue

\*\_\_\_\_\_

For Tests 1-5, the maximum amount of memory allowed for a RandomizedQueue containing n items is 48n + 192.

For Test 6, the maximum amount of memory allowed for a RandomizedQueue iterator over n items is 8n + 72.

Test 1a-1i: Total memory usage after inserting n items when n is a power of 2.

	n	bytes	
=> passed	32 64 128 256 512 1024 2048 4096 8192	312 568 1080 2104 4152 8248 16440 32824 65592	
==> 9/9 tests	passed		

Memory:  $8.00 \text{ n} + 56.00 \text{ (R}^2 = 1.000)$ 

Test 2a-2i: Total memory usage after inserting n items, when n is one more than a power of 2.

	n	bytes	
=> passed	33	568	
=> passed	65	1080	
=> passed	129	2104	
=> passed	257	4152	
=> passed	513	8248	
=> passed	1025	16440	
=> passed	2049	32824	
=> passed	4097	65592	
=> passed	8193	131128	
==> 9/9 tests	passed		

Memory:  $16.00 \text{ n} + 40.00 \text{ (R}^2 = 1.000)$ 

Test 3a-3i: Total memory usage after inserting 2n-1 items, and then deleting n-1 items, when n is one more than a power of 2.

	n	bytes	
=> passed	33	1080	
=> passed	65	2104	
=> passed	129	4152	
=> passed	257	8248	
=> passed	513	16440	
=> passed	1025	32824	
=> passed	2049	65592	
=> passed	4097	131128	
=> passed	8193	262200	
==> 9/9 tests	passed		

Memory:  $32.00 \text{ n} + 24.00 \text{ (R}^2 = 1.000)$ 

Test 4a-4i: Total memory usage after inserting n items, deleting n items, then inserting n times, when n is a power of 2.

	n	bytes	
=> passed	32 64 128 256 512 1024 2048 4096 8192 passed	312 568 1080 2104 4152 8248 16440 32824 65592	
	-		

Memory:  $8.00 \text{ n} + 56.00 \text{ (R}^2 = 1.000)$ 

Test 5a-5i: Total memory usage after inserting n items, and then deleting all but one item.

	n	bytes	
=> passed	32 64 128 256 512 1024 2048 4096 8192	72 72 72 72 72 72 72 72 72 72	
==/ J/J CE3C3	passeu		

Memory: 72.00 (R<sup>2</sup> = 1.000)

Test 6a-6i: Total memory usage of iterator after inserting n items.

	n	bytes	
=> passed	32 64 128 256 512	320 576 1088 2112 4160 8256	
<pre>=&gt; passed =&gt; passed =&gt; passed ==&gt; 9/9 tests</pre>	2048 4096 8192 passed	16448 32832 65600	

Memory:  $8.00 \text{ n} + 64.00 \text{ (R}^2 = 1.000)$ 

Test 7a: Insert 100 strings; delete them one at a time, checking for loitering after each deletion.

==> passed

Test 7b: Perform random operations, checking for loitering after each operation. The probabilities of enqueue(), dequeue(), and sample() are (p1, p2, p3), respectively.

- \* 200 random operations (0.8, 0.2, 0.0)
- \* 200 random operations (0.2, 0.8, 0.0)
- \* 200 random operations (0.6, 0.2, 0.2)
- \* 200 random operations (0.2, 0.4, 0.4)
- ==> passed

```
Test 8: Insert m items into queue; then iterate over deque and check
        that only constant memory is allocated/deallocated per operation
  * m = 64
```

\* m = 128

\* m = 256

==> passed

Test 9: Total memory usage after inserting n items, seeking to identify values of n where memory usage is minimized as a function of n.

	n	bytes	
=> passed	32	312	
=> passed	64	568	
=> passed	128	1080	
=> passed	256	2104	
=> passed	512	4152	
=> passed	1024	8248	
=> passed	2048	16440	
==> 7/7 tests	passed		

Memory:  $8.00 \text{ n} + 56.00 \text{ (R}^2 = 1.000)$ 

Test 10: Total memory usage after inserting 4096 items, then successively deleting items, seeking values of n where memory usage is maximized as a function of n

	n	bytes	
=> passed	2049 1025 513 257 129 65 33 17 9	65592 32824 16440 8248 4152 2104 1080 568 312	

Memory:  $32.00 \text{ n} + 24.00 \text{ (R}^2 = 1.000)$ 

Min observed memory for RandomizedQueue:  $8.00 \text{ n} + 56.00 \text{ (R}^2 = 1.000)$ Max observed memory for RandomizedQueue:  $32.00 \text{ n} + 24.00 \text{ (R}^2 = 1.000)$ 

Running 73 total tests.

Total: 73/73 tests passed!

```
************************************
```

```
Timing Deque
```

Running 103 total tests.

```
Test 1a-1k: make n calls to addFirst() followed by n calls to removeFirst()
           n seconds
```

=> passed 1024 0.00

```
=> passed

=> passed 4096

=> passed 8192 0.00

=> passed 16384 0.00

=> passed 32768 0.00

=> passed 65536 0.00

=> passed 128000 0.00

=> passed 256000 0.00

512000 0.01
     ==> 11/11 tests passed
```

Test 2a-2k: make n calls to addLast() followed by n calls to removeLast()

```
n seconds
-----
=> passed 1024 0.00
=> passed
=> passed
                 2048
                            0.00
                 4096
                            0.00
=> passed 8192

=> passed 16384

=> passed 32768

=> passed 65536

=> passed 128000

=> passed 256000

=> passed 512000
                            0.00
                            0.00
                            0.00
                            0.00
                            0.01
                            0.00
=> passed 512000
=> passed 1024000
                512000
                            0.01
                             0.02
==> 11/11 tests passed
```

Test 3a-3k: make n calls to addFirst() followed by n calls to removeLast()

```
n seconds
-----
=> passed 1024 0.00
=> passed 2048 0.00
=> passed 4096 0.00
=> passed 8192
=> passed 16384
=> passed 32768
=> passed 65536
=> passed 128000
=> passed 256000
=> passed 512000
                                 0.00
                                 0.00
                                 0.00
                                 0.00
                                 0.00
                                 0.01
=> passed 512000
=> passed 1024000
                  512000
                                 0.01
                                 0.02
==> 11/11 tests passed
```

Test 4a-4k: make n calls to addLast() followed by n calls to removeFirst()

```
n seconds
=> passed 1024 0.00
=> passed 2048 0.00
=> passed 4096 0.00
=> passed 8192 0.00
=> passed 16384 0.00
=> passed 32768 0.00
=> passed 65536 0.00
=> passed 128000 0.00
=> passed 256000 0.00
=> passed
                            512000
                                                   0.01
                      1024000
                                                      0.02
=> passed
==> 11/11 tests passed
```

```
Test 5a-5g: make n random calls to addFirst(), removeFirst(), isEmpty(), and size()
            with probabilities (0.7, 0.1, 0.1, 0.1)
```

```
n seconds
```

```
1024
                       0.00
=> passed
              2048
                       0.00
=> passed
             4096
                       0.00
=> passed
              8192
                       0.00
=> passed
            16384
=> passed
                       0.00
            32768
=> passed
                      0.00
=> passed
             65536
                      0.00
           128000
                      0.00
=> passed
            256000
                      0.01
=> passed
            512000
                      0.01
=> passed
            1024000
                      0.03
=> passed
            2048000
                       0.06
=> passed
==> 12/12 tests passed
```

Test 6a-6g: make n random calls to addLast(), removeLast(), isEmpty(), and size(), with probabilities (0.7, 0.1, 0.1, 0.1)

			n	seconds
=> pa	issed		1024	0.00
=> pa	issed		2048	0.00
=> pa	ssed		4096	0.00
=> pa	ssed		8192	0.00
=> pa	ssed		16384	0.00
=> pa	issed		32768	0.00
=> pa	issed		65536	0.00
=> pa	issed		128000	0.00
=> pa	issed	2	256000	0.01
=> pa	issed		512000	0.02
=> pa	ssed	10	24000	0.03
=> pa	issed	26	948000	0.06
==> 1	2/12	tests	passe	d

Test 7a-7g: make n random calls to addFirst(), addLast(), removeFirst(), removeLast(), isEmpty(), and size() with probabilities (0.3, 0.3, 0.1, 0.1, 0.1, 0.1)

			n	seconds
=>	passed		1024	0.00
=>	passed		2048	0.00
=>	passed		4096	0.00
=>	passed		8192	0.00
=>	passed		16384	0.00
=>	passed		32768	0.00
=>	passed		65536	0.00
=>	passed	1	.28000	0.00
=>	passed	2	56000	0.01
=>	passed	5	12000	0.02
=>	passed	16	24000	0.04
=>	passed	26	48000	0.07
==)	> 12/12	tests	passed	

Test 8a-8g: make n calls to addFirst(); iterate over the n items by calling next() and hasNext()

		n	seconds
=>	passed	1024	0.00
=>	passed	2048	0.00
=>	passed	4096	0.00
=>	passed	8192	0.00
=>	passed	16384	0.00
=>	passed	32768	0.00
	passed	65536	0.00
=>	passed	128000	0.00
=>	passed	256000	0.00

```
512000
                              0.01
=> passed
=> passed 1024000
=> passed 2048000
                              0.02
                              0.04
==> 12/12 tests passed
```

Test 9a-9k: make n calls to addFirst()/addLast(); interleave n calls each to removeFirst(), removeLast(), addFirst(), and addLast()

```
n seconds
-----
=> passed 1025 0.00
=> passed
=> passed
            2049
                   0.00
            4097
                   0.00
            8193
                   0.00
=> passed
           16385
                   0.00
=> passed
          32769
65537
128001
                   0.00
=> passed
                   0.00
=> passed
                   0.01
=> passed
          256001
=> passed
                   0.01
=> passed
           512001
                   0.03
=> passed 1024001
                    0.05
==> 11/11 tests passed
```

Total: 103/103 tests passed!

\_\_\_\_\_\_

```
Timing RandomizedQueue
```

\*\_\_\_\_\_

Running 67 total tests.

Test 1: make n calls to enqueue() followed by n calls to dequeue(); count calls to StdRandom

- \* n = 10
- \* n = 100
- \* n = 1000
- ==> passed

Test 2: make n calls to enqueue() follwed by n calls to sample(); count calls to StdRandom

- \* n = 10
- \* n = 100
- \* n = 1000
- ==> passed

Test 3: make n calls to enqueue() and iterate over the n items; count calls to StdRandom

- \* n = 10
- \* n = 100
- \* n = 1000
- ==> passed

Test 4a-k: make n calls to enqueue() followed by n calls to dequeue()

		n	seconds	
=>	passed	1024	0.00	
=>	passed	2048	0.00	
=>	passed	4096	0.00	
=>	passed	8192	0.00	
=>	passed	16384	0.00	
=>	passed	32768	0.00	
=>	passed	65536	0.00	
=>	passed	128000	0.01	
=>	passed	256000	0.01	

```
0.01
=> passed
            512000
         1024000
                      0.03
=> passed
```

==> 11/11 tests passed

Test 5a-k: make n calls to enqueue() followed by n random calls to enqueue(), sample(), dequeue(), isEmpty(), and size() with probabilities (0.2, 0.2, 0.2, 0.2, 0.2)

		n	seconds
=>	passed	1024	0.00
=>	passed	2048	0.00
=>	passed	4096	0.00
=>	passed	8192	0.00
=>	passed	16384	0.00
=>	passed	32768	0.00
=>	passed	65536	0.01
=>	passed	128000	0.01
=>	passed	256000	0.02
=>	passed	512000	0.04
=>	passed	1024000	0.10
==;	> 11/11	tests passed	

Test 6a-k: make n calls to enqueue() followed by n random calls to enqueue(), sample(), dequeue(), isEmpty(), and size() with probabilities (0.6, 0.1, 0.1, 0.1, 0.1)

	n	seconds
=> passed	1024	0.00
=> passed	2048	0.00
=> passed	4096	0.00
=> passed	8192	0.00
=> passed	16384	0.00
=> passed	32768	0.00
=> passed	65536	0.00
=> passed	128000	0.01
=> passed	256000	0.01
=> passed	512000	0.03
=> passed	1024000	0.07
==> 11/11	tests passed	l

Test 7a-k: make n calls to enqueue() followed by n random calls to enqueue(), sample(), dequeue(), isEmpty(), and size() with probabilities (0.1, 0.1, 0.6, 0.1, 0.1)

	n	seconds
=> passed	1024	0.00
=> passed	2048	0.00
=> passed	4096	0.00
=> passed	8192	0.00
=> passed	16384	0.00
=> passed	32768	0.00
=> passed	65536	0.00
=> passed	128000	0.01
=> passed	256000	0.02
=> passed	512000	0.05
=> passed	1024000	0.12
==> 11/11	tests passed	

Test 8a-k: make n calls to enqueue() followed by n calls each to next() and hasNext().

n seconds

=>	passed	1024	0.00
=>	passed	2048	0.00
=>	passed	4096	0.00
=>	passed	8192	0.00
=>	passed	16384	0.00
=>	passed	32768	0.00
=>	passed	65536	0.00
=>	passed	128000	0.01
=>	passed	256000	0.01
=>	passed	512000	0.02
=>	passed	1024000	0.04
==>	11/11	tests passed	

Test 9a-i: make 100 calls to enqueue; 99 calls to dequeue; n calls to enqueue(); then call dequeue() three times, followed by enqueue() three times, and repeat n times.

	n	seconds
=> passed	1024	0.00
=> passed	2048	0.00
=> passed	4096	0.00
=> passed	8192	0.00
=> passed	16384	0.00
=> passed	32768	0.00
=> passed	65536	0.01
=> passed	128000	0.02
=> passed	256000	0.04
==> 9/9 tests	passed	

Total: 67/67 tests passed!

\_\_\_\_\_\_