

Abbott, B. and Gallipoli, G. (2019).
Permanent-Income Inequality. Working Paper

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March 26, 2019

Overview of the Paper

- Literature on income inequality focuses on measurement and understanding the forces that shape differences in economic wellbeing of individuals.
- This paper takes a broad assessment of the concept of income inequality.
 - In Milton Freedman's **permanent income hypothesis**, individuals smooth their consumption over their lifetime conditional on their expected future earnings.
- For individuals the value of their future earnings is likely to be a strong determinant of their economic wellbeing.
 - A young person who expects a strong increase in future earnings is much better off than what can be inferred from their current wealth or income.

Overview of the Paper

- This paper looks to estimate pecuniary measures of both human capital and wealth to:
 - 1 Evaluate the change of wealth over the lifecycle.
 - 2 Evaluate the change in wealth since 1989 (U.S.).
 - 3 Explore the relationship between HH consumption and permanent-income.
- This is done through nonparametric estimation of a concept the authors refer to as **Human Wealth**.
 - Estimates are obtained by combining data from the Panel Study of Income Dynamics (PSID) and the Survey of Consumer Finances (SCF).

Human Wealth

- What is **human wealth**?
 - The value to individuals of their yet-to-be realized earnings.
 - Reflects the value of an individual's human capital.
 - A recent graduate may have low current wealth but high human capital, so therefore high yet-to-be realized earnings (human wealth).
- **Human wealth + current asset wealth = lifetime wealth.**
- The age-adjusted annuity value of lifetime wealth is the **permanent income**.

Valuation of Human Wealth

- Human Capital Value:
 - Equivalent to the price of a non-traded asset that pays dividends equal to an individual's income.
- An individual's valuation of the uncertain stream of earnings their human capital produces in the future is their **human wealth** θ_{it} .
- From a standard pricing formula:

$$\theta_{it} = \mathbb{E}_{it} \left[\beta \frac{u_c(c_{it+1}, v_{it+1})}{u_c(c_{it}, v_{it})} (y_{it+1} + \theta_{it+1}) \right]$$

Estimation of Human Wealth

- 1st step: nonparametric estimates are obtained for marginal utility functions and the discount factor β .
 - β represents state-dependent stochastic discounting.
 - Being credit constrained or facing high risk decreases the valuation of future earnings (human wealth).
 - β captures the losses from incomplete markets.
- 2nd step: nonparametric estimates of human wealth θ_{it} .

1st Step - MU and β Identification

- The intertemporal Euler equation can be written as:

$$u_c(q) = \beta \mathbb{E} [u_c(q') R' | q]$$

- Replacing the expectations with an integral where utility is weighted by expected returns given Markov transitions between states:

$$u_c(q) - \beta \int u_c(q') \psi(q, q') dq' = 0$$

- This can be solved for MU given β , but we don't have β .
- Rewrite the integral as a sum and then solve the linear system:

$$(Au_c)(q) = \beta \int u_c(q') \psi(q, q') dq'$$

gives $\beta = 1/\rho(A)$, where $\rho(A)$ is the largest real eigenvalue of the linear operator A .

2nd Step - Human Wealth Identification

- Human wealth depends on the entire distribution of possible future outcomes, but this is not observed.
- Estimating the distribution of possible outcomes uses outcomes for individuals who are ex-ante the same regarding observed characteristics and unobserved types.
 - Identification relies on **conditional equivalence of expectations**:

$$\mathbb{E}_{it} \left[\beta \frac{u_c(q')}{u_c(q)} (y' + \theta') \right] = \mathbb{E} \left[\beta \frac{u_c(q')}{u_c(q)} (y' + \theta') \mid \mathbf{z} = \mathbf{z}_{it}, j = j_{it} \right]$$

- If this holds we can write the human wealth equation as:

$$\theta(j, \mathbf{z}) = \mathbb{E} \left[\beta \frac{u_c(q')}{u_c(q)} (y' + \theta(j+1, \mathbf{z}')) \mid \mathbf{z} \right]$$

and to solve for θ in a similar manner as step 1.

Estimation

- Estimation is done nonparametrically, using locally weighted average (Nadaray-Watson) estimator. Equation (1) can be estimated by using a linear estimator of the integral for expectations:

$$\left(\hat{A}u_c\right)(q) = \sum_{i=1}^N \sum_{t \in \tau_\sigma(i)} u_c(q'_{it}) R'_{it} \phi_{it}(q)$$

giving a solution for MU and the stochastic discount factor:

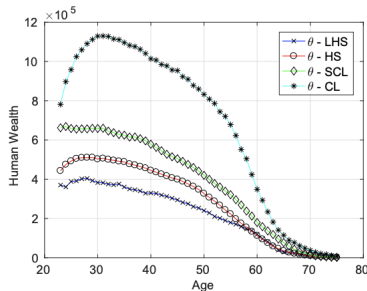
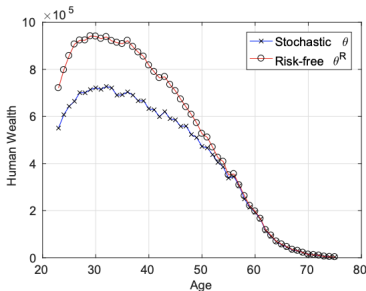
$$\hat{\beta} = \frac{1}{\lambda^*}, \quad \hat{u}_c(q) = \sum_{i=1}^N \sum_{t \in \tau_o(i)} b_{it}^* \phi_{it}(q)$$

- Human wealth can be recovered after estimating:

$$\hat{g}(j, z) = \sum_{i=1}^N \sum_{t \in \tau_o(i)} \hat{\beta}' \frac{\hat{u}_c(q'_{it})}{\hat{u}_c(q_{it})} y'_{it} \gamma_{it}(z)$$

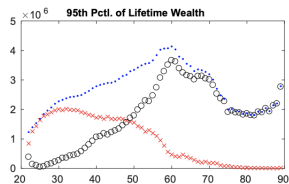
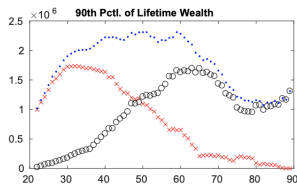
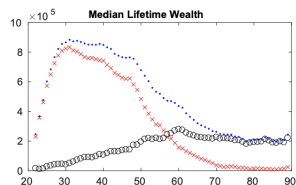
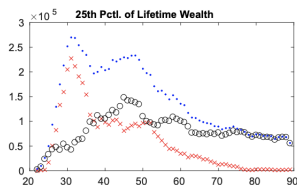
Results - Human Wealth Estimates

- Human wealth with the stochastic discount factor is compared to a risk-free discounted human wealth
 - The difference is the loss due to incomplete markets
- At the peak, college graduates hold twice as much human wealth as high-school graduates, and three times as much human wealth as high-school drop-outs.



Results - Wealth over the Life-Cycle

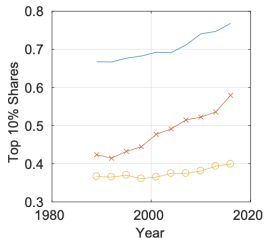
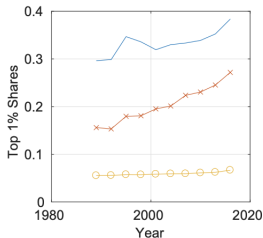
- Lifetime wealth peaks early among poorer households.
 - Human wealth does not translate into equivalent amounts of net worth later in life - suggests luck plays a role.



\times Human Wealth \circ Net Worth \bullet Lifetime Wealth

Evolution of Inequality

- Since 1989 the pace of increase in concentration of permanent income towards the richest households has been twice as fast as the increase in the share of asset wealth.
- **A pronounce growth in the share of asset wealth in household portfolios is the key driver of the sustained increase in permanent-income concentration.**



Conclusions

- Human wealth is less concentrated than net worth.
- Rich households have increased their share of permanent income over the past decades and this concentration has grown much faster than concentration of net worth.
- Effective inequality has increased more than previously thought, albeit from a lower initial level.
- The crucial driver in increasing wealth inequality is the growing value of assets as a share of lifetime wealth portfolios of the rich.
- High net worth households account for a larger share of total permanent-income in 2016 than they did in 1989.