# Predicting Lotto Numbers: A Natural Experiment on the Gambler's Fallacy and the Hot-Hand Fallacy Suetens, Galbo-Jørgensen, & Tyran (2016)

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#### Introduction: A Tale of Two Fallacies

- As discussed in our course notes, people often exhibit two seemingly contradictory biases when judging random sequences:
- The Gambler's Fallacy (GF): The belief that a recent outcome makes the opposite outcome more likely. (e.g., "Red is due after a streak of black.")
- The Hot-Hand Fallacy (HHF): The belief that a recent streak of an outcome makes that same outcome more likely. (e.g., "The player is on fire, pass him the ball!")
- The Research Question: Can these two opposing fallacies coexist?
   Specifically, do lotto players bet *less* on numbers drawn last week
   (GF), but *more* on numbers that have been drawn frequently in the recent past (HHF)?

# Background: The Law of Small Numbers

- Course Context: This paper provides field evidence for the theories
  of belief formation under uncertainty discussed in our class.
- The "Law of Small Numbers": The core idea, proposed by Tversky & Kahneman and formalized by Rabin & Vayanos (2010), is that people mistakenly believe small samples should be representative of the large population.

#### Fallacy Reversal Intuition:

- A belief in the law of small numbers leads to the **Gambler's Fallacy** in the short run (expecting reversals to maintain representativeness).
- However, a long streak violates this belief so strongly that the person starts to doubt the randomness of the process itself, inferring an underlying cause or "hotness." This leads to the Hot-Hand Fallacy.

# Data & Methodology: Danish Lotto

- A Natural Experiment: The study uses data from the Danish state lottery, a truly random process, avoiding the confound of "skill" present in studies like basketball.
- **Key Advantage:** The data is from online players who have a unique ID, allowing the researchers to track *individual betting choices* over 28 weeks in 2005. The individual analysis uses data from 7,323 players.
- Dependent Variables: Two proxies for betting confidence.
  - NumberBet: Whether a player picks a number.
  - MoneyBet: How much money a player bets on a number, weighted by the size of the set of numbers they chose.

# The Empirical Model

#### Key Independent Variables:

- Drawn<sub>t-1</sub>: = 1 if number j was drawn in week t-1.
- Hotness<sub>t-1</sub>: Count of how often number j was drawn from week t-2 to t-6.

#### Aggregate Regression Model :

$$DV_{ijt} = \beta_0 + \beta_1 \mathsf{Drawn}_{jt-1} + \beta_2 \mathsf{Hotness}_{jt-1} + \beta_3 (\mathsf{Drawn}_{jt-1} \times \mathsf{Hotness}_{jt-1}) + \dots$$

- **GF** Test:  $\beta_1 < 0$
- HHF Test:  $\beta_2 > 0$  and/or  $\beta_3 > 0$

#### • Individual-Level Model :

$$\Delta$$
MoneyBet<sub>ijt</sub> =  $\beta_{0j} + \beta_{1i}$ Drawn<sub>jt-1</sub> +  $\beta_{2i}$ Hotness<sub>jt-1</sub> + . . .

• Regressions are run for each player i to get their individual biases,  $\beta_{1i}$  and  $\beta_{2i}$ .

# Aggregate Results: Both Fallacies are Present

 The researchers run pooled regressions on different samples (all players, active players, and "changers" who alter their bets).

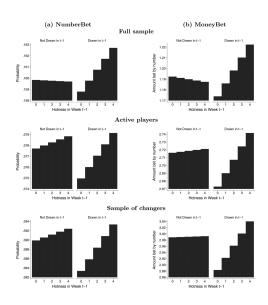
# • Evidence for Gambler's Fallacy ( $\beta_1 < 0$ ):

- On average, players bet significantly less on numbers that were drawn in the preceding week.
- The effect is strongest for active "changers", who bet about 2-3% less on a number if it was drawn last week.

#### • Evidence for Hot-Hand Fallacy ( $\beta_3 > 0$ ):

- Players bet significantly *more* on numbers as their 'Hotness' increases, but primarily if that number was also drawn last week.
- The marginal effect is about a **1% increase** in bets for each additional time the number was drawn in the recent past.

# Aggregate Results: Visualized



# Interpreting Figure 1: A Closer Look

#### • How to Read the Plots:

- Gambler's Fallacy (GF): Compare the first bar on the left ('Not Drawn') with the first bar on the right ('Drawn'). If the right bar is lower, players avoid last week's numbers.
- Hot-Hand Fallacy (HHF): Look at the trend on the right side ('Drawn'). If the bars rise with 'Hotness', players chase streaks.

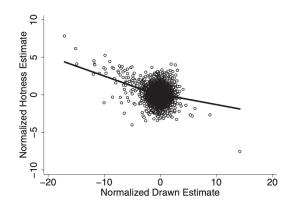
#### • Key Observation Across Samples:

- Top Row (Full Sample): Effects are small.
- Middle Row (Active Players): Effects become clearer.
- Bottom Row (Sample of Changers): The effects are strongest and most significant. This shows the biases are driven by active players who change their bets, not by people quitting after a win.

# Individual-Level Analysis: Are the Fallacies Related?

- **The Core Question:** Do the fallacies just coexist in the aggregate, or do the *same individuals* exhibit both biases?
- **Method:** The authors run separate regressions for each of the 7,323 individual players to estimate their personal sensitivity to Drawn  $(\beta_{1i})$  and Hotness  $(\beta_{2i})$ .
- **Finding:** There is a significant negative relationship between the two estimates. Players who most strongly exhibit the Gambler's Fallacy (large negative  $\beta_{1i}$ ) also tend to most strongly exhibit the Hot-Hand Fallacy (large positive  $\beta_{2i}$ ).
- **Quantitatively:** Among players with statistically significant biases, **55%** (71 out of 129) exhibit both fallacies simultaneously—more than double the 25% expected by chance.

## Individual Results: Visualized



# Upshots & Take-Aways

- Main Take-Away: This paper provides the first field evidence that the Gambler's Fallacy and the Hot-Hand Fallacy are systematically related and can coexist within the same individual.
- Link to Theory: The findings strongly support the "law of small numbers" and "fallacy reversal" models proposed by Rabin and Vayanos.

#### Broader Implications:

- This framework can help explain financial market anomalies, like short-term underreaction (GF) and long-term overreaction (HHF) to earnings news.
- It shows that even in a purely random environment, people's beliefs and behaviors are predictable and systematically biased.

## Personal Reactions & Comments

# Strengths of the Paper

• The paper is strong because it uses real-world data from the lottery. This is better than a lab experiment because people are acting naturally, and it's better than studying sports because the lottery is purely random, so there's no confusion with skill. It gives us a very clean look at people's psychology.

## Avenues for Discussion & Critique

- Heterogeneity: The paper finds the effects are strongest for male, frequent, and heavy players. This suggests the biases are not uniform.
- **Selection Bias:** People who believe they can predict lotto numbers are more likely to play. The observed biases might be stronger in this population than in the general population.

# Q&A and Discussion

# Thank you.

Questions?