

Chapter 2: Data structures

Contents

1	Vectors	1
1.1	Vector arithmetic	2
1.2	Logical vectors	4
1.3	Character vectors	5
1.4	Coercing	5
1.5	Missing values	6
1.6	Subset of a vector	6
1.7	Give names to elements of a vector	6
2	Factors	6
3	Matrices	7
3.1	Creating a matrix in R	7
3.2	Adding labels	8
3.3	Calculations on matrices	8
3.4	Subset of a matrix	10
4	Data frame	11
4.1	Creating a data frame	11
4.2	Taking a subset from a data frame	13
5	List	14
5.1	Creating a list	15
5.2	Named list	15
5.3	Accessing elements of a list	15
6	Exercises	16
6.1	Vectors	16
6.2	Creating sequences	16
6.3	Matrix creation	16
6.4	Working with data frames	16

R operates on data structures. There are different data structures: vector, factor, matrix, data frame and list.

1 Vectors

- Simplest type of data structure
- **Vector creation:** with function `c`:

```
vec <- c(5, 8, 4.6, 21)
```

- To **see** the content of a vector created and assigned to an object, call the name of this object:

```
vec
```

```
## [1] 5.0 8.0 4.6 21.0
```

OR

use an extra pair of brackets during the creation and assignment of the object:

```
(vec <- c(5, 8, 4.6, 21)) # Note the extra brackets!
```

```
## [1] 5.0 8.0 4.6 21.0
```

1.1 Vector arithmetic

1.1.1 Useful functions for vectors

1 vector: x	2 vectors: x, y
length(x)	
sum(x)	sum(x, y)
prod(x)	prod(x, y)
max(x)	max(x, y)
min(x)	min(x, y)
sort(x)	sort(x, y)
rev(x)	
diff(x, lag =)	
unique(x)	
order(x)	

Creating a vector `x` with 10 random elements drawn from a normal distribution. Some of the above listed functions will be afterwards applied on this vector

```
x <- rnorm(10)
x
```

```
## [1] 1.16380713 -2.02159814 0.25914675 -0.40558169 0.27371012 1.30685921
## [7] -0.07173989 1.02192342 -0.37770545 -1.86810075
```

The function `order()` applied on a vector `x` returns a vector with indices. The indices reveal which element of the original vector `x` needs to be put first, second ... in order to sort the vector `x` in ascending (default) or descending order.

```
z <- order(x)
z
```

```
## [1] 2 10 4 9 7 3 5 8 1 6
```

The function `sort()` gives the elements itself instead of the index.

```
sort(x)
```

```
## [1] -2.02159814 -1.86810075 -0.40558169 -0.37770545 -0.07173989 0.25914675
## [7] 0.27371012 1.02192342 1.16380713 1.30685921
```

OR, alternative way to obtain the same result

```
sort(x, decreasing = FALSE)
```

```
## [1] -2.02159814 -1.86810075 -0.40558169 -0.37770545 -0.07173989 0.25914675
## [7] 0.27371012 1.02192342 1.16380713 1.30685921
```

The function `rev()` returns a reversed version of its argument.

```
rev(sort(x))
```

```
## [1] 1.30685921 1.16380713 1.02192342 0.27371012 0.25914675 -0.07173989
```

```
## [7] -0.37770545 -0.40558169 -1.86810075 -2.02159814
```

OR, alternative way to obtain the same result

```
sort(x, decreasing = TRUE)
```

```
## [1] 1.30685921 1.16380713 1.02192342 0.27371012 0.25914675 -0.07173989
## [7] -0.37770545 -0.40558169 -1.86810075 -2.02159814
```

Creation of a vector y which will be used as argument for some other examples.

```
y <- c(1, 3, 8, 3, 7, 21)
```

The function `unique()` extracts unique elements.

```
unique(y)
```

```
## [1] 1 3 8 7 21
```

The function `diff()` returns suitably lagged and iterated differences.

```
diff(y, lag = 2)
```

```
## [1] 7 0 -1 18
```

1.1.2 Mathematical functions on numerical vectors

`abs`, `exp`, `log`, `floor`, `ceiling`, `trunc`, `gamma`, `log10`, `round`, `sin`, `cos`, `tan`, `sqrt`

1.1.3 Generating vectors

How to create regular sequences?

Colon operator :	→ To create a regular sequence
<code>seq</code>	→ To create a regular sequence
<code>rep</code>	→ To replicate value

Use of the colon operator (`:`) to create a regular sequence:

```
y <- 1:8
y
```

```
## [1] 1 2 3 4 5 6 7 8
```

To obtain a descending sequence

```
x <- 20:1
```

Use of the function `seq`

```
z <- seq(from = -2, to = 5, by = 0.5)
z
```

```
## [1] -2.0 -1.5 -1.0 -0.5 0.0 0.5 1.0 1.5 2.0 2.5 3.0 3.5 4.0 4.5 5.0
```

Use of the function `rep`

```
u <- rep(2:5, 2)
u
```

```
## [1] 2 3 4 5 2 3 4 5
```

```
v <- rep(2:5, 2:5)
v
```

```
## [1] 2 2 3 3 3 4 4 4 4 5 5 5 5 5
```

1.2 Logical vectors

The elements of a logical vector can have the values T (TRUE) or F (FALSE).

```
x <- c(9, 10, 8, 5, 9) # numerical vector
y <- x < 9 # logical vector
y
```

```
## [1] FALSE FALSE TRUE TRUE FALSE
```

1.2.1 Logical expressions

Expression	Meaning
<	Smaller than
<=	Smaller than or equal to
>	Larger than
>=	Larger than or equal to
==	Equal to
!=	Unequal to

1.2.2 Logical operators

Operator	Meaning
&	And
	Or

1.2.3 Examples

```
T + T
```

```
## [1] 2
```

```
T - F
```

```
## [1] 1
```

```
x <- rnorm(100)
y <- x > 0
y
```

```
## [1] FALSE TRUE FALSE FALSE TRUE TRUE FALSE FALSE TRUE TRUE TRUE FALSE
## [13] TRUE TRUE TRUE TRUE TRUE FALSE TRUE TRUE TRUE FALSE FALSE TRUE
## [25] TRUE FALSE FALSE FALSE TRUE TRUE FALSE TRUE TRUE TRUE TRUE TRUE
## [37] FALSE TRUE TRUE FALSE TRUE FALSE FALSE TRUE TRUE TRUE TRUE FALSE
## [49] FALSE FALSE FALSE TRUE TRUE FALSE TRUE FALSE TRUE FALSE TRUE TRUE
## [61] TRUE FALSE TRUE TRUE FALSE FALSE FALSE FALSE TRUE TRUE FALSE TRUE
## [73] TRUE TRUE TRUE FALSE TRUE FALSE TRUE FALSE TRUE TRUE FALSE TRUE
## [85] TRUE TRUE FALSE FALSE TRUE TRUE TRUE TRUE FALSE FALSE FALSE TRUE
## [97] FALSE FALSE TRUE TRUE
```

```
sum(y)
```

```
## [1] 59
```

1.3 Character vectors

```
test <- c("Leuven Statistics Research Centre", "2020-2021")
test
```

```
## [1] "Leuven Statistics Research Centre" "2020-2021"
```

1.3.1 Character vector operations

some character functions:

1. **nchar(text)**

This function returns a vector with number of characters in each element of the argument **text**

```
x <- c("start", "student")
nchar(x)
```

```
## [1] 5 7
```

2. **paste**

Concatenate vectors after converting to character.

```
paste(c("X", "Y"), 1:4, sep=" ")
```

```
## [1] "X 1" "Y 2" "X 3" "Y 4"
```

3. **substring(text, start, stop)**

Extract substrings in a character vector.

```
x <- c("start", "student")
substring(x, 1, 3)
```

```
## [1] "sta" "stu"
```

1.4 Coercing

Logical, numerical and character values can be used in one and the same vector.

```
vector <- c(TRUE, -6.05, "Leuven")
vector
```

```
## [1] "TRUE" "-6.05" "Leuven"
```

Data type	Example
Logical	T or F
Numeric	-6.05, 86.06, ...
Character	Alabama, Leuven, ...

When values of different modes are combined into one object, then R converts all values to a single mode in a way that preserves as much information as possible.

Increasing order information: logical, numeric, character

1.5 Missing values

NA (Not Available) is the symbol used in R to represent missing data (for logical, numerical or character values).

```
y <- c(1,2,3, NA)
is.na(y)
```

```
## [1] FALSE FALSE FALSE  TRUE
```

```
z <- c("Ward", "Wouter", "Lucas", NA)
!is.na(z)
```

```
## [1]  TRUE  TRUE  TRUE FALSE
```

```
x <- c(5,3,8,NA, 6)
is.na(x>5)
```

```
## [1] FALSE FALSE FALSE  TRUE FALSE
```

1.6 Subset of a vector

A part of a vector **x** can be selected by **x[subscript]**

```
y <- c(33, 55, 4, 22, 89)
y[c(2,3)]
```

```
## [1] 55  4
```

```
y[-5]
```

```
## [1] 33 55  4 22
```

```
y[y>30]
```

```
## [1] 33 55 89
```

```
x <- c(5, 9, NA)
y <- x[!is.na(x)]
y
```

```
## [1] 5 9
```

1.7 Give names to elements of a vector

```
y <- c(33, 55, 4, 22, 89)
names(y) <- 1:5
y
```

```
##  1  2  3  4  5
## 33 55  4 22 89
```

2 Factors

- A factor is a vector that contains predefined values. This type of data structure is used to store categorical data. The set of allowed values in a factor are defined by the levels.
- How to create?
 - `factor()`: To create a factor
 - `as.factor()`: To encode a vector as a factor

```
directions <- c("North", "East", "South", "South") # This is a character vector
directions
```

```
## [1] "North" "East" "South" "South"
```

```
directions.f <- as.factor(directions) # This is a factor
directions.f
```

```
## [1] North East South South
```

```
## Levels: East North South
```

To create a factor with labels

```
status <- factor(c("Medium", "Low", "High", "Medium", "Medium", "High"),
                 levels = c("Low", "Medium", "High"),
                 labels = c("Lo", "Me", "Hi"))
status
```

```
## [1] Me Lo Hi Me Me Hi
```

```
## Levels: Lo Me Hi
```

3 Matrices

All the values need to be of the same type.

3.1 Creating a matrix in R

How to create?:

- `matrix()`: To create a matrix
- `rbind()`: To add rows
- `cbind()`: To add columns

Example of the use of function `matrix()`

```
x <- matrix(1:8, nrow = 2, ncol = 4, byrow = FALSE)
x
```

```
##      [,1] [,2] [,3] [,4]
## [1,]    1    3    5    7
## [2,]    2    4    6    8
```

Some properties of objects in R are stored as attributes. Examples of attributes are `dim` (the dimension of the object), `dimnames` (the names associated with the dimension of the object.) The attributes of an object can be accessed with the function `attributes`.

```
attributes(x)
```

```
## $dim
## [1] 2 4
```

Example of the use of function `rbind()`

`rbind()` combines the arguments row-wise.

```
x <- rbind(1:4, 5:8)
x
```

```
##      [,1] [,2] [,3] [,4]
## [1,]    1    2    3    4
## [2,]    5    6    7    8
```

```
dim(x)

## [1] 2 4

dimnames(x)

## NULL

attributes(x)

## $dim
## [1] 2 4
```

Example of the use of function cbind()
 cbind() combines the arguments column-wise.

```
x <- cbind(1:4, 5:8)
x

##      [,1] [,2]
## [1,]    1    5
## [2,]    2    6
## [3,]    3    7
## [4,]    4    8
```

3.2 Adding labels

Adding labels to the rows and to the columns of a matrix:

```
dimnames(x) <- list(paste("row", 1:2), paste("col", LETTERS[1:4]))
paste("row", 1:2)

## [1] "row 1" "row 2"

paste("col", LETTERS[1:4])

## [1] "col A" "col B" "col C" "col D"
```

The row variable names comes first, then the column variable names.

```
x <- rbind(1:4, 5:8) # Creating matrix
dimnames(x) <- list(paste("row", 1:2), paste("col", LETTERS[1:4])) # Adding labels
x

##      col A col B col C col D
## row 1    1    2    3    4
## row 2    5    6    7    8
```

3.3 Calculations on matrices

```
x <- matrix(1:4, nrow = 2) # Creating a matrix x
x

##      [,1] [,2]
## [1,]    1    3
## [2,]    2    4

nrow(x) # Returns number of rows present in x

## [1] 2
```



```
ncol(x) # Returns number of columns present in x
```

```
## [1] 2
```

```
x+x
```

```
##      [,1] [,2]  
## [1,]    2    6  
## [2,]    4    8
```

Element-wise product:

```
x*x # Elementwise product
```

```
##      [,1] [,2]  
## [1,]    1    9  
## [2,]    4   16
```

Element-wise division:

```
x/x # Elementwise division
```

```
##      [,1] [,2]  
## [1,]    1    1  
## [2,]    1    1
```

```
x^2
```

```
##      [,1] [,2]  
## [1,]    1    9  
## [2,]    4   16
```

Matrix multiplication: %*%

```
x%*%x # Matrix product
```

```
##      [,1] [,2]  
## [1,]    7   15  
## [2,]   10   22
```

```
y <- c(1,5)
```

```
y
```

```
## [1] 1 5
```

xy^T :

```
y%*%x%*%y
```

```
##      [,1]  
## [1,]  126
```

```
z <- rbind(x, y)
```

```
z
```

```
##      [,1] [,2]  
##      1    3  
##      2    4  
## y      1    5
```

```
z <- cbind(x, y)
```

```
z
```

```
##          y
## [1,] 1 3 1
## [2,] 2 4 5
a <- rbind(1:4, 5:8)
b <- cbind(1:4, 5:8)
a%*%b # Matrix multiplication
```

```
##          [,1] [,2]
## [1,]      30  70
## [2,]      70 174
```

Matrix specific operations

Function	Function returns
chol(x)	Choleski decomposition of \mathbf{x}
col(x)	Matrix of which the elements corresponds to the column number of the elements
row(x)	Matrix of which the elements corresponds to the row numbers of the elements
diag(x)	Diagonal matrix from vector \mathbf{x}
ncol(x)	Number of columns of matrix \mathbf{x}
nrow(x)	Number of rows of matrix \mathbf{x}
qr(x)	QR matrix decomposition
solve(x)	Inverse
svd(x)	Singular value decomposition
var(x)	Covariance matrix of the columns
t(x)	Transpose
eigen(x)	Eigenvalues and eigenvectors of \mathbf{x}

Functions for mathematical computing

Function	Action
solve(a, b)	Solve the system $\mathbf{ax} = \mathbf{b}$ for \mathbf{x}
integrate(f, low = a, high = b)	Integration
polyroot	Optimization: Find zeros of a real or complex polynomial.
uniroot	Optimization: Search in a interval for a root (i.e., zero) of a function.
optimize	Optimization: Search in a interval for a minimum or maximum of a function.
approx	Interpolation
rnorm, pnorm, dnorm, qnorm	Random generation, distribution function, density and quantile function for the normal distribution

3.4 Subset of a matrix

```
x <- matrix(1:100, ncol = 5) # Creating a matrix x
x
```

```
##          [,1] [,2] [,3] [,4] [,5]
## [1,]      1  21  41  61  81
```

```
## [2,] 2 22 42 62 82
## [3,] 3 23 43 63 83
## [4,] 4 24 44 64 84
## [5,] 5 25 45 65 85
## [6,] 6 26 46 66 86
## [7,] 7 27 47 67 87
## [8,] 8 28 48 68 88
## [9,] 9 29 49 69 89
## [10,] 10 30 50 70 90
## [11,] 11 31 51 71 91
## [12,] 12 32 52 72 92
## [13,] 13 33 53 73 93
## [14,] 14 34 54 74 94
## [15,] 15 35 55 75 95
## [16,] 16 36 56 76 96
## [17,] 17 37 57 77 97
## [18,] 18 38 58 78 98
## [19,] 19 39 59 79 99
## [20,] 20 40 60 80 100
```

```
x[8:12, 3:4] # Returns subset with rows from 8- 12 and columns 3-4
```

```
##      [,1] [,2]
## [1,] 48 68
## [2,] 49 69
## [3,] 50 70
## [4,] 51 71
## [5,] 52 72
```

```
x[2,] # Returns 2nd row of the matrix
```

```
## [1] 2 22 42 62 82
```

```
x[,2] # Returns 2nd column of the matrix
```

```
## [1] 21 22 23 24 25 26 27 28 29 30 31 32 33 34 35 36 37 38 39 40
```

4 Data frame

- Data frames are an extension of matrices. **Data frames can have columns of different data types.** Most statistical routines require a data frame as input.

4.1 Creating a data frame

- To create or change a data frame:
 - `data.frame`: Create data frames
 - `cbind`: Combine data frames by column (add new variables to existing data frame, merge data frames with same individuals)
 - `rbind`: Combine data frames by row (add new individuals to existing data frame, merge data frames with same variables)
 - `merge`: Join data frames by their common data

Create a data frame from vectors by using `data.frame`

```
employee <- c("John", "Peter", "Sylvie") # Data type = character
salary <- c(21000, 23400, 26800) # Data type = numeric
```

```
employ.df <- data.frame(employee, salary) #Creation of a data frame with two columns.
#These columns have a different data type.
employ.df
```

```
##   employee salary
## 1    John  21000
## 2   Peter  23400
## 3  Sylvie  26800
```

Adding a new row by rbind function

```
new.df <- data.frame(employee = "Katrien", salary = 25000)
employ2 <- rbind(employ.df, new.df)
head(employ2)
```

```
##   employee salary
## 1    John  21000
## 2   Peter  23400
## 3  Sylvie  26800
## 4 Katrien  25000
```

Adding a new column by cbind function

```
age <- c(40, 23, 31)
employ3 <- cbind(employ2, age)
head(employ3) # This gives an error
```

```
age <- c(40, 23, 31, NA) #Note the extra element in this vector (i.e. NA) which is
#crucial, otherwise an error is generated.
employ3 <- cbind(employ2, age)
head(employ3)
```

```
##   employee salary age
## 1    John  21000  40
## 2   Peter  23400  23
## 3  Sylvie  26800  31
## 4 Katrien  25000  NA
```

Create a data frame by using merge function

```
authors <- data.frame(
  ## I(*) : use character columns of names to get sensible sort order
  surname = I(c("Tukey", "Venables", "Tierney", "Ripley", "McNeil")),
  nationality = c("US", "Australia", "US", "UK", "Australia"),
  deceased = c("yes", rep("no", 4)))

books <- data.frame(
  name = I(c("Tukey", "Venables", "Tierney",
    "Ripley", "Ripley", "McNeil", "R Core")),
  title = c("Exploratory Data Analysis",
    "Modern Applied Statistics ...",
    "LISP-STAT",
    "Spatial Statistics", "Stochastic Simulation",
    "Interactive Data Analysis",
    "An Introduction to R"),
  other.author = c(NA, "Ripley", NA, NA, NA, NA,
    "Venables & Smith"))
```

Examples where the data frames `authors` and `books` are merged with the `merge` function.

`authors`

```
##      surname nationality deceased
## 1      Tukey           US       yes
## 2 Venables   Australia       no
## 3 Tierney     US       no
## 4 Ripley      UK       no
## 5 McNeil     Australia       no
```

`books`

```
##      name                title      other.author
## 1      Tukey   Exploratory Data Analysis      <NA>
## 2 Venables Modern Applied Statistics ...      Ripley
## 3 Tierney                LISP-STAT      <NA>
## 4 Ripley         Spatial Statistics      <NA>
## 5 Ripley         Stochastic Simulation      <NA>
## 6 McNeil      Interactive Data Analysis      <NA>
## 7 R Core          An Introduction to R Venables & Smith
```

```
m1 <- merge(authors, books, by.x = "surname", by.y = "name")
# by.x and by.y specify the columns used for merging
m1
```

```
##      surname nationality deceased                title other.author
## 1      McNeil   Australia       no   Interactive Data Analysis      <NA>
## 2      Ripley      UK       no         Spatial Statistics      <NA>
## 3      Ripley      UK       no   Stochastic Simulation      <NA>
## 4 Tierney      US       no         LISP-STAT      <NA>
## 5      Tukey      US       yes   Exploratory Data Analysis      <NA>
## 6 Venables   Australia       no Modern Applied Statistics ...      Ripley
```

```
m2 <- merge(books, authors, by.x = "name", by.y = "surname")
m2
```

```
##      name                title other.author nationality deceased
## 1      McNeil   Interactive Data Analysis      <NA>   Australia       no
## 2      Ripley         Spatial Statistics      <NA>      UK       no
## 3      Ripley         Stochastic Simulation      <NA>      UK       no
## 4 Tierney                LISP-STAT      <NA>      US       no
## 5      Tukey   Exploratory Data Analysis      <NA>      US       yes
## 6 Venables Modern Applied Statistics ...      Ripley   Australia       no
```

4.2 Taking a subset from a data frame

1. Take a subset from a data frame like a **matrix**

```
sub1 <- authors[1:3, 1:2]
sub1
```

```
##      surname nationality
## 1      Tukey           US
## 2 Venables   Australia
## 3 Tierney     US
```

2. Taking a subset from a data frame like a **list** (to be explained later)

```
sub2 <- authors$nationality
sub2
```

```
## [1] US      Australia US      UK      Australia
## Levels: Australia UK US
```

Remark:

To sort the data frame `airquality` by two variables, use the function `orderBy` from the package `doBy`.

More information about the `airquality` data:

```
?airquality
```

```
## starting httpd help server ... done
```

```
airquality {datasets}
```

R Documentation

New York Air Quality Measurements

Description

Daily air quality measurements in New York, May to September 1973.

Usage

```
airquality
```

Format

A data frame with 153 observations on 6 variables.

```
[,1] Ozone   numeric Ozone (ppb)
[,2] Solar.R numeric Solar R (lang)
[,3] Wind    numeric Wind (mph)
[,4] Temp    numeric Temperature (degrees F)
[,5] Month    numeric Month (1--12)
[,6] Day     numeric Day of month (1--31)
```

Details

Daily readings of the following air quality values for May 1, 1973 (a Tuesday) to September 30, 1973.

- **Ozone:** Mean ozone in parts per billion from 1300 to 1500 hours at Roosevelt Island
- **Solar.R:** Solar radiation in Langleys in the frequency band 4000–7700 Angstroms from 0800 to 1200 hours at Central Park
- **Wind:** Average wind speed in miles per hour at 0700 and 1000 hours at LaGuardia Airport
- **Temp:** Maximum daily temperature in degrees Fahrenheit at La Guardia Airport.

```
sort_air <- orderBy(~Month + Temp, data = airquality)
head(sort_air)
```

```
##      Ozone Solar.R Wind Temp Month Day
## 5      NA      NA 14.3  56     5    5
## 18     6      78 18.4  57     5   18
## 25     NA     66 16.6  57     5   25
## 27     NA     NA  8.0  57     5   27
## 15     18     65 13.2  58     5   15
## 26     NA    266 14.9  58     5   26
```

5 List

- A **list** can contain elements of different data types.

- It is an ordered collection of components.

5.1 Creating a list

Creation of a list with the function `list`.

```
employee <- c("John", "Peter", "Sylvie") # creation of a character vector
salary <- c(21000, 23400, 26800) # creation of a numeric vector
employ.df <- data.frame(employee, salary) # creation of a data frame

y <- letters[1:5] # creation of a character vector
z <- 1:3 # creation of a numeric vector

list(employ.df, y, z)
```

```
## [[1]]
##   employee salary
## 1     John  21000
## 2    Peter  23400
## 3   Sylvie  26800
##
## [[2]]
## [1] "a" "b" "c" "d" "e"
##
## [[3]]
## [1] 1 2 3
```

5.2 Named list

The elements of a list can have a name, i.e., named lists have the attributes `names`.

```
mixlist <- list(logica = c(T, T, T, F),
                plant = c("tree", "bush", "grass"),
                comment = "these components are unrelated")
mixlist
```

```
## $logica
## [1] TRUE TRUE TRUE FALSE
##
## $plant
## [1] "tree" "bush" "grass"
##
## $comment
## [1] "these components are unrelated"
```

```
attributes(mixlist)
```

```
## $names
## [1] "logica" "plant" "comment"
```

5.3 Accessing elements of a list

To access a list component: use component number or component name.

```
mixlist$plant # Returns a character vector

## [1] "tree" "bush" "grass"
```

```
mixlist[[2]] # Returns a character vector
```

```
## [1] "tree" "bush" "grass"
```

```
mixlist[2] # Returns a list
```

```
## $plant
```

```
## [1] "tree" "bush" "grass"
```

6 Exercises

6.1 Vectors

- Create the object `test1` with numbers 1.5, 0.7, 45.6.
- Create a vector `y1` with the numbers from 1 to 10.
- Create a logical vector `y2` from `y1`. An element of `y2` should be `TRUE` if the corresponding element of `y1` is larger than 5.
- How many elements from `y1` has a value larger than 5?

6.2 Creating sequences

- Create a vector `x` with elements (1, 2, 3, ..., 100)
- Create a vector `y` with elements (0, 5, 10, 15, ..., 500)
- Create a vector `z1` with elements (1, 1, 1, 2, 2, 2, ..., 50, 50, 50)
- Create a vector `z2` with elements (1, 2, 2, 3, 3, 3, ..., 10)
- Create a vector `z3` with elements (1, 2, 2, 3, 4, 4, 5, 6, 6, ..., 50, 50)

6.3 Matrix creation

- Create a vector with 100 random normal numbers and use that to generate a 10 by 10 matrix. Call this matrix `mat1`.
Hint: to generate a random normal vector, use the function `rnorm()`.
- Add an extra row to `mat1` with the numbers 1 to 10 which will be the new first row. Also add the row with numbers 10 to 1 which will be the last row.
- Add an extra column to the matrix obtained in step *b* with the number 1 to 12 (as first column).

6.4 Working with data frames

`tips` (reshape package) One waiter recorded information about each tip he received over a period of a few months working in one restaurant. He collected several variables:

- tip in dollars
- bill in dollars
- sex of the bill payer
- whether there were smokers in the party
- day of the week
- time of the day
- size of the party

In all he recorded 244 tips.

- Install and load the package `reshape`.
- Check the data description of this data frame.
- Ask for the names of the variables in this data frame.
- Take a subset of data `tips` which contains the observations from 1 until 20 and only the variables `tip`, `sex` and `day`.