# simulation\_week6

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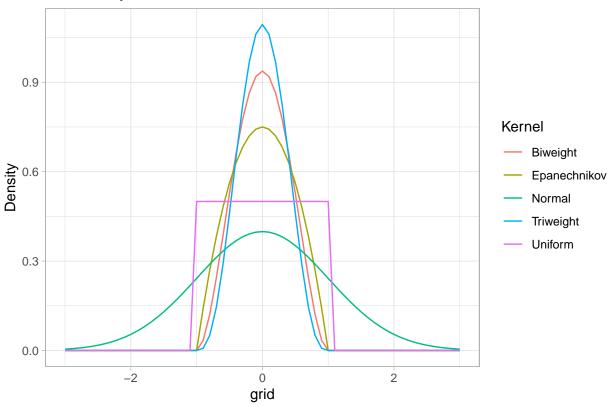
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```
library(tidyverse)
library(purrr)
library(ggplot2)
library(here)
devtools::load_all()
set.seed(1222)
```

## Commonly used kernel functions

In the beta family kernel density, lambda=0,1,2,3 correspond to the uniform, the Epanech- nikov, the biweight, and the triweight kernel functions, respectively.

# Commonly used kernel functions



# Compute the MADE (Mean Absolute Deviation Errors)

The Mean Absolute Deviation Errors for  $\hat{f}(\cdot)$  is defined as

$$MADE = \frac{1}{n} \sum_{k=1}^{n} |(\hat{f}(u_k) - f(u_k))|$$

, where  $\hat{f}(u_k)$  is the kernel estimate of  $f(u_k)$ , and  $\{u_k\}$  are the frid points taken to be arbitrary within the range of data.

When the sample is generated from the known distribution like exp,beta, gamma, etc., we can use corresponding built-in functions (dexp(), dgamma, etc.) to calculated the true densities of the grid points. If the sample is not from the familiar distributions, we can use the built-in function "denstiy()" in R to get the value of  $f(u_k)$ )s.

### Simulation

Explore the simulation results with different sample sizes & kernels

#### Build simulation functions that can save the MADE.

Note: The following functions are similar to kde\_est\_big, sim\_big\_made, and save\_made that are used in week 7, which are listed in the kde\_est\_functions.R. However, they are the first versions and are much simpler. Thus, we will not modify this part and keep those functions here as the records.

Here  $kde_n_ker_est()$  is used to simulate over different sample size and kernels for a given bandwidth  $h=1.06*100^{\circ}(-0.2)$ , the output is the estimated densities.

sim\_made is used to first generate combination of parameters, and then for each combination of parameters, using kde\_n\_ker\_est() to generate the estimated densities, and the corresponding true densities. Then, made() is used to compute the MADE. The out out is the MADEs under different combination of parameters.

```
# Define some functions for gievn h=1.06*100^{-0.2},
# simulate over different sample size and kernels
kde_n_ker_est <- function(x, n, ker, grid){</pre>
  # x large population
  # n sample sizes
  # ker name of kernels
  # grid grid points
 map2(.x = n, .y = ker,
        ~KDE_est(sample(x, .x, replace = FALSE),
                  grid, h= 1.06*100^{(-0.2)}, ker = .y)$f est)
}
sim_made <- function(ns, kes, x, grid, true_f){</pre>
  # generates every combination of parameters (ns:kers)
  simulation_params_big <- list(</pre>
  n = ns,
  kernel_type = kers)
  n_ker_est_big <- cross_df(simulation_params_big)</pre>
  n_ker_est_big <- n_ker_est_big %>%
  mutate(
    # for each combination of the paras, using the kde_n_ker_est()
    f_ests = kde_n_ker_est(x, n, kernel_type, grid),
    f_true = map(1:length(n), ~true_f) # save the corresponding true density
  ) %>%
  mutate(
    MADE = map2_dbl(.x = f_ests, .y = f_true, ~made(.x,.y)) # calculate the MADE
  )
  return(n_ker_est_big$MADE)
}
```

#### Simulation

Generate samples from t(3) distribution. Then, using five types of kernel function and different size of samples that are drawn from the large population.

Simulation is repeated n.sim times.

```
# population
x <- rt(50000, df=3)

# simulaiton parameters
ns <- c(100, 500, 1000, 1500) # sample sizes</pre>
```

```
kers <- c("normal", "uniform", "epanech", "biweight", "triweight") # kernel functions
grid <- seq(-5,15, 0.1)

# true density
true_f <- dt(grid, df=3)

# simulation
n.sim <- 100 # number of replicates
sim_rlt <- map(1:n.sim, ~sim_made(ns, kers, x, grid,true_f))</pre>
```

#### Save result

```
made_mat <- matrix(unlist(sim_rlt), nrow = length(ns)*length(kers) )

made_comapre <- tibble(
    n =rep(ns, time=length(kers)),
    kernel_type = rep(kers, each=length(ns)),
    made_mean = apply(made_mat, 1, mean),
    made_sd = apply(made_mat, 1, sd)
)

write_rds(made_mat , here("results", "week6-sim.rds"))
write_rds(made_comapre, here("results", "week6-sim-plot.rds"))</pre>
```

### Analysis

Results and plots are documented in Summary\_week6 in the analysis file.