

Summary__week7

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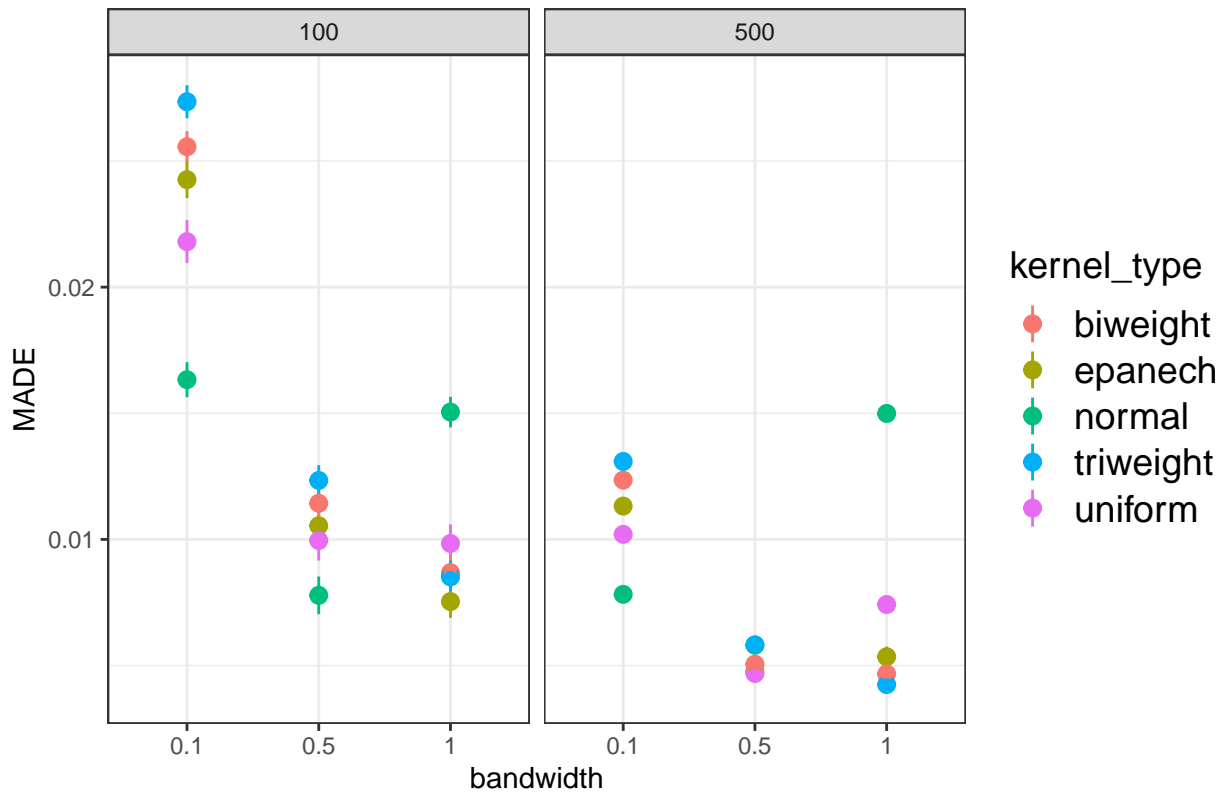
```
library(tidyverse)
library(here)
library(ggplot2)
library(purrr)
devtools::load_all()
```

Simulation result with different sample sizes & kernels & bandwidths(randomly selected)

```
made_comapre <- read_rds(here("results", "week7-sim-1-plot.rds"))
#png(here("plots", "KDE_big_xkernel.png"),width=1600, height=900)

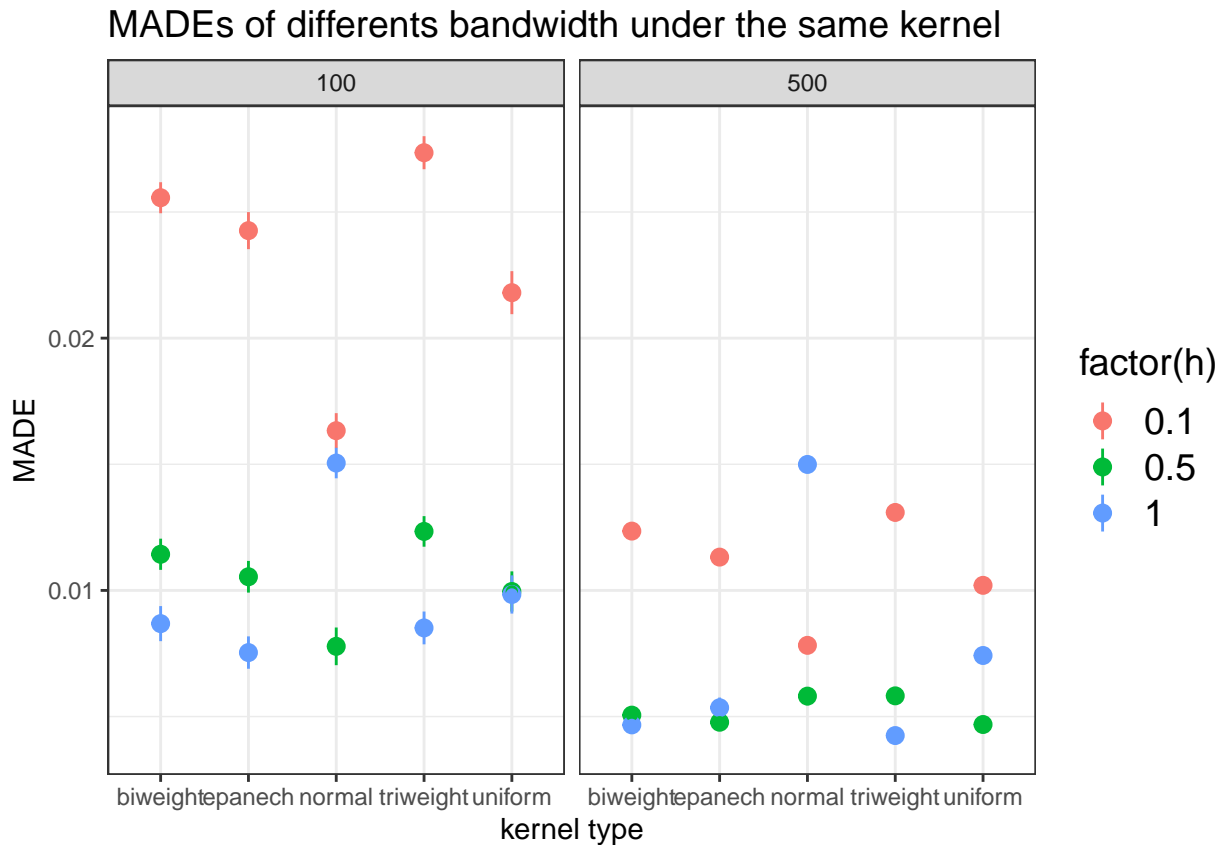
made_comapre %>%
  ggplot(aes(x = factor(h), y = made_mean, color = kernel_type)) +
    geom_pointrange(aes(
      ymin = made_mean - 1.96*made_sd/sqrt(n.sim),
      ymax = made_mean + 1.96*made_sd/sqrt(n.sim))) +
    geom_point() +
    facet_wrap(~ n) +
    theme_bw() +ggtitle("MADEs of different kernels under the same bandwidth")+
    xlab("bandwidth")+
    ylab("MADE")+
    theme( legend.title = element_text(size = 14),
           legend.text = element_text(size = 14),
           plot.title = element_text(size=14))
```

MADEs of different kernels under the same bandwidth



```
#dev.off()

#png(here("plots", "KDE_big_xbandwidth.png"),width=1600, height=900)
made_comapre %>%
  ggplot(aes(x =kernel_type, y = made_mean, color = factor(h))) +
    geom_pointrange(aes(
      ymin = made_mean - 1.96*made_sd/sqrt(n.sim),
      ymax = made_mean + 1.96*made_sd/sqrt(n.sim))) +
    geom_point() +
  facet_wrap(~ n)+
  theme_bw() +ggtitle("MADEs of differents bandwidth under the same kernel")+
  xlab("kernel type")+
  ylab("MADE")+
  theme( legend.title = element_text(size = 14),
        legend.text = element_text(size = 14),
        plot.title = element_text(size=14))
```



```
#dev.off()
```

From the above two plots, we can get the following conclusion:

1. Large sample size tends to have smaller MADE, that is, smaller estimation biases.
2. Under the same bandwidth, some of MADEs of different kernel functions are close to each other. That is, their estimation results using will be similar.
3. Under the same kernel function, the MADEs with different choice of bandwidth are quite different.
4. There's no guarantee that a particular kernel or bandwidth is better than others. To achieve the best estimation results, we need to find the best combinations of kernel and bandwidth. And large sample size will achieve more accurate estimation.

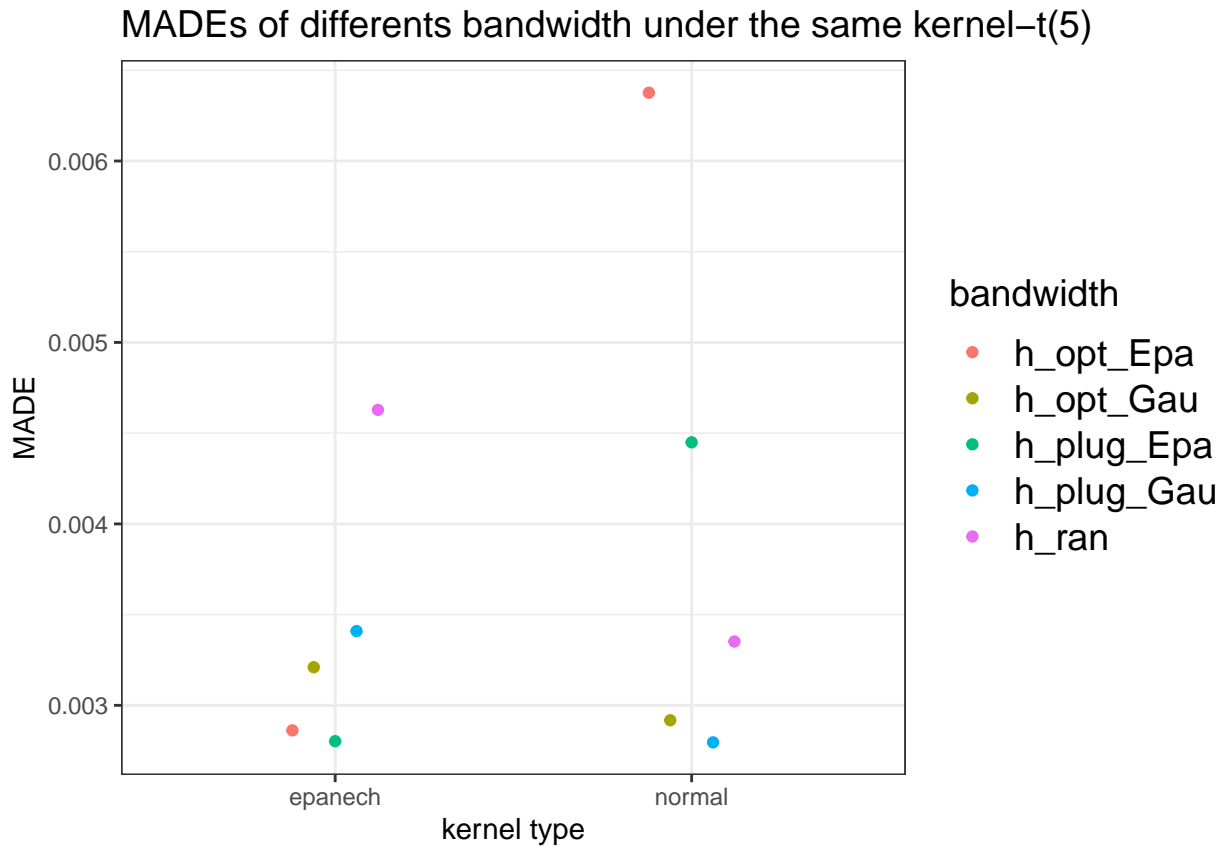
Simulation results for different distribution with different ways of choosing the optimal bandwidth

t(5)

```
comapre_bdwt_t <- read_rds(here("results", "week78-sim-t-plot.rds"))

#png(here("plots", "KDE_t.png"),width=1600, height=900)
comapre_bdwt_t %>%
ggplot(aes(x =kernel_type, y = made_mean, color = bandwidth)) +
  geom_point(position=position_dodge(width=0.3)) +
```

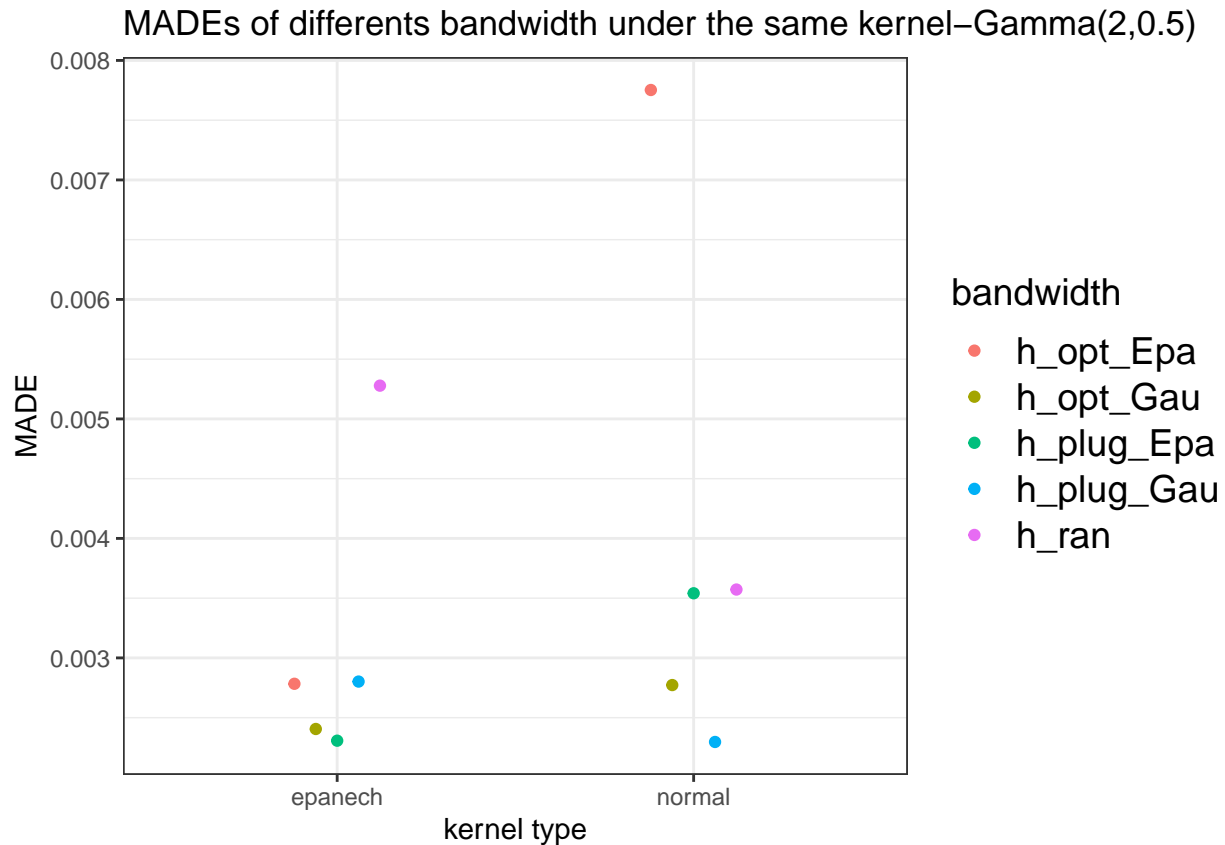
```
theme_bw() + ggtitle("MADEs of differents bandwidth under the same kernel-t(5)") +
  xlab("kernel type") + ylab("MADE") +
  theme( legend.title = element_text(size = 14),
        legend.text = element_text(size = 14),
        plot.title = element_text(size=14))
```



```
#dev.off()
```

Gamma(2,0.5)

```
comapre_bdwt_gamma <- read_rds(here("results", "week78-sim-gamma-plot.rds"))
#png(here("plots", "KDE_gamma.png"),width=1600, height=900)
comapre_bdwt_gamma %>%
  ggplot(aes(x=kernel_type, y = made_mean, color = bandwidth)) +
  geom_point(position=position_dodge(width=0.3)) +
  theme_bw() + ggtitle("MADEs of differents bandwidth under the same kernel-Gamma(2,0.5)") +
  xlab("kernel type") + ylab("MADE") +
  theme( legend.title = element_text(size = 14),
        legend.text = element_text(size = 14),
        plot.title = element_text(size=13))
```



```
#dev.off()
```

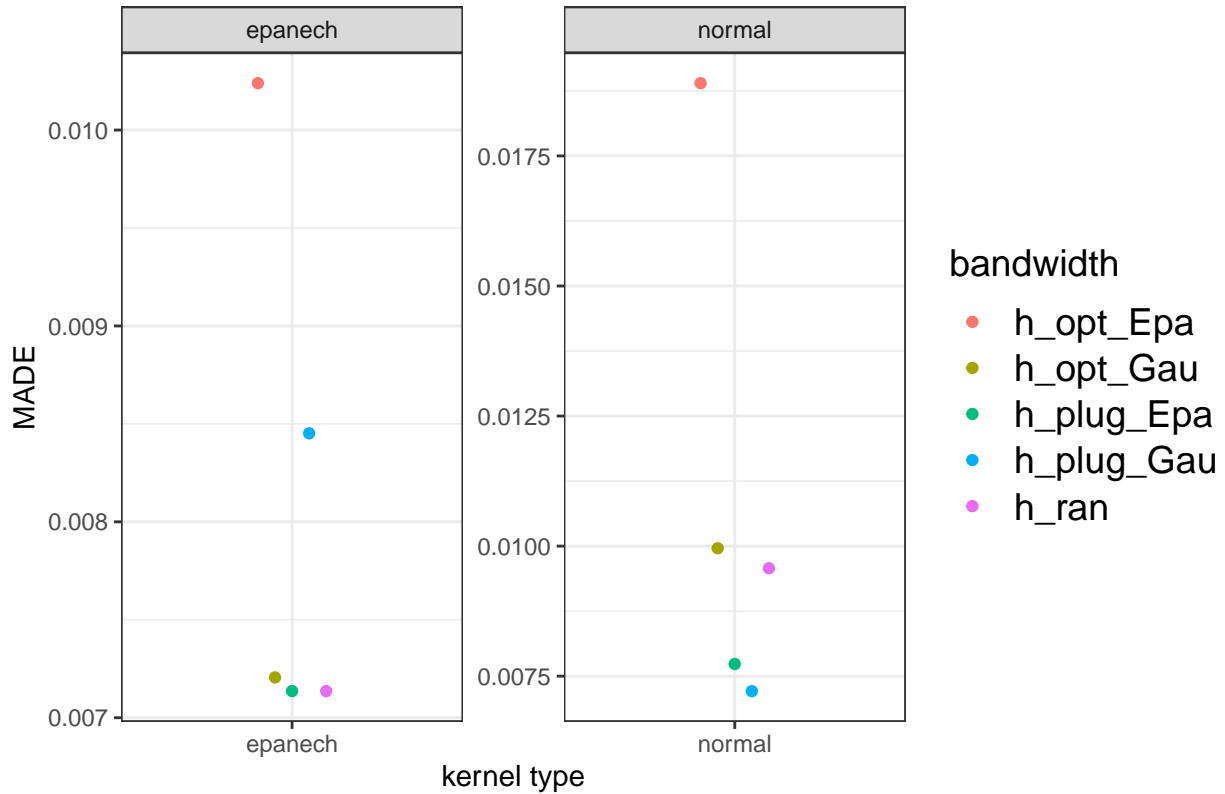
```
exp(2)
```

```
comapre_bdwt_exp <- read_rds(here("results", "week78-sim-exp-plot.rds"))

#png(here("plots", "KDE_exp.png"),width=1600, height=900)
comapre_bdwt_exp %>%
ggplot(aes(x =kernel_type, y = made_mean, color = bandwidth)) +
  geom_point(position=position_dodge(width=0.3)) +

  facet_wrap(~ kernel_type, scales = "free")+
  theme_bw() + ggtitle("MADEs of differents bandwidth under the same kernel-exp(2)")+
  xlab("kernel type")+ylab("MADE")+
  theme( legend.title = element_text(size = 14),
        legend.text = element_text(size = 14),
        plot.title = element_text(size=14))
```

MADEs of different bandwidth under the same kernel-exp(2)



#dev.off()

Results show that under different distributions, the plug-in bandwidths may or may not have the smallest MADE (under the corresponding kernels). If the data is quite close to normal distribution, maybe the Normal reference bandwidth selector is the best choice. If the data is far away from the normal distribution, the plug-in bandwidth selector is a better choice. So, how to choose the best bandwidth with the most accurate estimation result is still a tough task.