

# LECTURE 3

# ARRAYS AND PLOTS

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Fundamentals of Programming - COMP1005

Department of Computing

Curtin University

Updated 16/8/2019

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# Learning Outcomes

- Understand and use Python arrays implemented in NumPy
- Understand and use simple plotting techniques using matplotlib
- Apply arrays and plotting to more complex systems dynamics problems

# The story so far...

- We have looked at **simple data types**:  
integers, floating point  
complex numbers,  
bool (True/False) values
- We can assign these values to **variables**
- We can use **operations** on variables and values and combine them together into **expressions**
- **Control structures** provide choice and repetition (if/elif/else, for and while loops)

# The story so far...

- We've also looked at more **complex datatypes**: strings and lists  
    greeting = 'hello'  
    bucket = ['Visit Stonehenge', 'Skydiving']
- Strings and lists are **ordered sequences**
- **Strings** hold characters and are **immutable**
- **Lists** can hold anything (including sub-lists) and can be updated/changed (**mutable**)
- We can access elements in strings and lists using **indexes**, e.g. instring[0], bucket[5]

# The story so far...

- Strings and lists have operators and functions, they include:
- String operators: `+`, `*`, `<`, `>`, `==`, `in`...
- String functions: `len`, `upper()`, `lower()`, `min()`, `max()`, `count()`...
- List operators: `+`, `*`, `<`, `>`, `in`
- List functions: `len`, `append()`, `extend()`, `del`
- Select parts of a string using slicing  
`[start: stop: step]`

# ARRAYS

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# Arrays

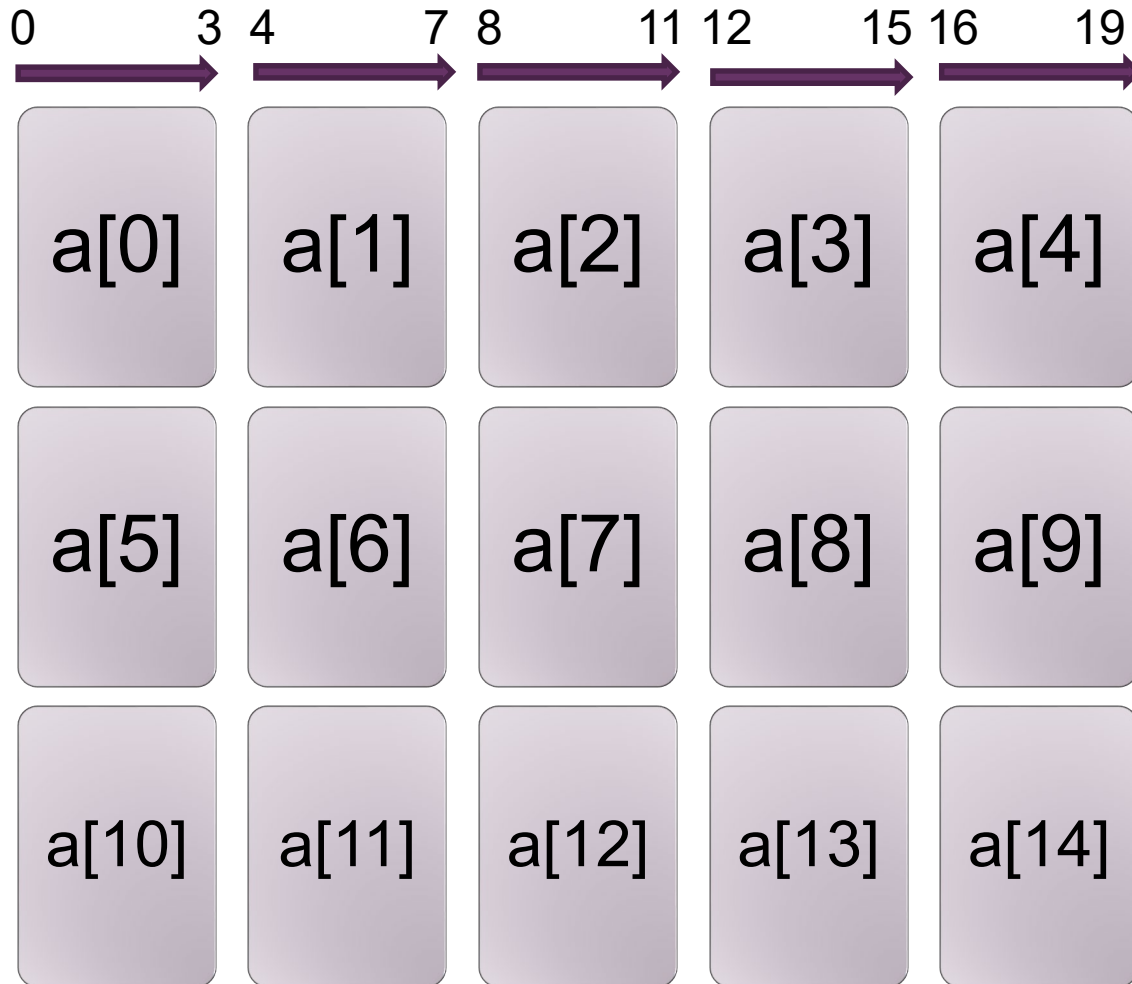
- Arrays are common across almost all programming languages
- They hold an ordered **sequence** of values
- All values must be of the same type, e.g.:
  - an array of temperatures, stored as floats
  - an array of attendance values, stored as ints
  - an array of responses, stored as bools (True/False)
  - an array of names, stored as strings



# Array implementation

- If you know the size of each element, and how many elements you have, then:
  1. The total size of the array can be calculated
  2. The array can be stored as a single block in memory
  3. Simple maths can be used to find each element
  4. Moving from element to element will be fast
- Compare this to a dynamic **list** where you add and delete elements of different types

# Array implementation



- If each element is 4 bytes long...
  - a[0] is at offset 0
  - a[1] is at offset 4
  - a[n] is at offset  $n * 4$
- Size in bytes is  
size \* # elements  
 $= 4 * 15$   
 $= 60$  bytes

# Arrays are Awesome!

- They are fast
- They make sense
- They don't take any more space than they need
- They can store lots of useful data

## **BUT**

- They are not part of "standard" Python
- We need to use a package...

# NumPy

- Pronounced "num-pai"
- This is the core library for scientific computing in Python – everything else builds upon it
- Provides high-performance N-dimensional arrays
- Includes:
  - Operations and functions to manipulate arrays
  - Sophisticated (broadcasting) functions
  - Tools for integrating C/C++ and Fortran code
  - Useful linear algebra, Fourier transform, and random number capabilities

# NUMPY ARRAYS

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# NumPy arrays

- To use an external package, we have to import it
- The convention with NumPy is to give it a new, shorter name `np`

```
import numpy as np
```

- Then we can refer to NumPy functions and create arrays with `np`

```
myarray = np.array([1, 2, 3])
```

- `np.array` is a function to create an array

# Creating arrays

- Directly:

```
array1 = np.array([1, 2, 3, 4, 5])  
[1, 2, 3, 4]
```

- From a list:

```
templist = [1.0, 2.0, 3.0, 4.0]  
array2 = np.array( templist )  
[1.0, 2.0, 3.0, 4.0]
```

```
templist2 = [1, 2, 3, 4, 5]  
array2 = np.array(templist2, dtype=float)  
[1.0, 2.0, 3.0, 4.0]
```

# Accessing/updating elements

- As with lists and strings, we use an **index** to access array elements

e.g.

```
print('Element zero is: ', array1[0])
```

```
array1[2] = 5
```

```
sumoftwo = array1[1] + array1[2]
```

- Access parts of the array with **slicing**:

```
array1 = np.array([1, 2, 3, 4, 5])
```

```
print(array1[1:3])
```

[2, 3]



# Preset arrays

- Create an array of 100 float (default), all = 0

```
zeroarray = np.zeros(100)
```

- Create an array of 100 integers, all set to 1

```
onesarray = np.ones(100, dtype=int)
```

- Array of 50 floats, each set to 100

```
hundreds = np.fill(50, 100)
```

- Array of 50 random numbers

```
randarray = np.random.random(50)
```

```
array([ 0.41976329,  0.52865412,  0.55652662, ...,  
        0.55957403,  0.03146015,  0.49496509])
```

# Arrays with ranges of numbers

- Similar to using range to create a sequence for a for loop...
- Create an array of integers, going from 0 to 50, increasing by 5 each time

```
fives = np.arange(0, 55, 5)
print(fives)
array([ 0,  5, 10, ..., 40, 45, 50])
```

```
tens = np.arange(0, 55, 10)
print(tens)
array([0, 10, 20, 30, 40, 50])
```

# Arrays with ranges of numbers

- An alternative is to give the start and stop values, and indicate how many values should be in between
- Create an array of integers, going from 0 to 50 (inclusive), increasing by 5 each time

```
tofifty = np.linspace(0, 50, 5)
print(tofifty)
array([ 0. , 12.5, 25. , 37.5, 50. ])
```

```
toten = np.linspace(0, 10, 10)
print(toten)
array([ 0., 1.11111111, 2.22222222, 3.33333333, 4.44444444, 5.55555556, 6.66666667, 7.77777778, 8.88888889, 10. ])
```

# Looping through arrays

- As with strings, there are multiple ways to go through the elements of an array...

```
index = 0
while index < len(tofifty):
    print('Element ', index, ' is: ', tofifty[index])
    index = index + 1
```

**Or...**

```
for index in range(0, len(tofifty) ):
    print('Element ', index, ' is: ', tofifty[index])
```

**Or...**

```
for item in tofifty:
    print('Element is: ', item)
```

# Slicing arrays

- Arrays can be sliced in the same way as strings and lists: `myarray[start:stop:step]`
- If a slice term is missing, it will default to:
  - `start = 0`
  - `stop = len(myarray)`
  - `step = 1`
- `myarray[1:3]` will give elements 1 and 2
- `myarray[:3]` will give elements 0, 1 and 2
- `myarray[3:]` will give elements 3, 4, 5, ...
- `myarray[3::2]` will give elements 3, 5, 7, ...
- `myarray[:,2]` will give elements 0, 2, 4, ...

# Slicing to make new arrays

- The result of a sliced array is an array, so we can use slicing to make new arrays

```
toifty = np.linspace(0, 50, 5)
```

```
print(toifty)
```

```
array([ 0. , 12.5, 25. , 37.5, 50. ])
```

```
toifty2 = toifty[1:3]
```

```
print(toifty2)
```

```
array([ 12.5, 25. ])
```

```
toifty3 = toifty[:,2]
```

```
print(toifty3)
```

```
array([ 0. , 25. , 50. ])
```

# MANIPULATING ARRAYS

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# Manipulating arrays

- So far arrays look pretty good – but not that different to strings and lists
- It's the tools for manipulation of arrays that make them powerful
- Many maths and science applications use matrix operations
- NumPy provides fast and easy implementation of matrix algebra



# Operations

- Arithmetic operations are carried out on **each element** of an array

```
a = np.array([1, 2, 3])
```

```
b = np.array([4, 5, 6])
```

```
c = a + b
```

```
array([5, 7, 9])
```

```
c = a + 1
```

```
array([2, 3, 4])
```

```
c = a - b
```

```
array([-3, -3, -3])
```

```
c = a * b
```

```
array([4, 10, 16])
```

```
c = a / b
```

```
array([0.25, 0.4, 0.5])
```

# Comparisons

- Can do element-wise comparisons of values using `<`, `<=`, `>`, `>=`, `==`, `!=`
- Result is an array

```
a = np.array([1, 2, 3])
b = np.array([4, 5, 6])
c = np.array([6, 5, 4])
```

```
d = a < b          array([True, True, True], dtype=bool)
d = a < 2          array([True, False, False], dtype=bool)
d = b == c         array([False, True, False], dtype=bool)
d = b <= c         array([True, True, False], dtype=bool)
```

# Element-wise Functions

- These functions are carried out on **each element** of an array

```
a = np.array([1, 2, 3])  
b = np.array([4, 5, 6])  
c = np.sqrt(a)  
    array([ 1.,  1.4142,  1.7320])  
c = np.sin(a)  
    array([ 0.8414,  0.9092,  0.1411])
```

Also... `exp()`, `cos()`, `log()`, `add()`, `multiply()` etc.

# Array-wise Functions

- These functions return a single result across the array (or a dimension of the array)

```
a = np.array([1, 2, 3])
```

```
b = np.array([4, 5, 6])
```

```
a.sum()
```

6

```
b.min()
```

4

```
b.max()
```

6

```
a.mean()
```

2.0

# EXAMPLES

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# Exchange rates

```
usdprices = np.array([10, 20, 30 , 40, 50])  
exchrates = 1.3  
audprices = usdprices * 1.3  
print(audprices)
```

```
[ 13.,  26.,  39.,  52.,  65.]
```

# Adding GST

```
prices = np.array([10, 20, 30, 40, 50])  
gstprices = prices * 1.1  
print(gstprices)
```

```
[ 11.,  22.,  33.,  44.,  55.]
```

# Conversion miles to km

```
distmiles = np.array([100, 150, 200, 250])  
mileskm = 1.60934  
distkm = distmiles * mileskm  
print(distkm)
```

```
[ 160.934,   241.401,   321.868,   402.335]
```



# Temperatures

```
march2017 = np.array([37.7, 29.9, 35.2, 36.1,  
36.2, 34.7, 33.8, 34.5, 31.9, 29.9, 30.9,  
24.8, 24.2, 24.1, 24.0])
```

```
print(march2017.min())  
24.0
```

```
print(march2017.max())  
37.70000000000000003
```

```
print(march2017.mean())  
31.1933333333333332
```

<http://www.bom.gov.au/climate/dwo/201703/html/IDCJDW6111.201703.shtml>

# PLOTTING WITH MATPLOTLIB

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# Plotting with Matplotlib

- Visualising data is one of the best tools for gaining insight and understanding
- Matplotlib is the preferred package for 2D graphics in Python
- Matplotlib tries to "make easy things easy and hard things possible"
- Includes plots, histograms, power spectra, bar charts, errorcharts, scatterplots, etc.,
- Originally aligned to MATLAB plotting
- Plots are production-quality, so can be included in research papers
- <http://matplotlib.org/>

# Matplotlib, origins

- When I went searching for a Python plotting package, I had several requirements:
  - Plots should look great - publication quality. One important requirement for me is that the text looks good (antialiased, etc.)
  - Postscript output for inclusion with TeX documents
  - Embeddable in a graphical user interface for application development
  - Code should be easy enough that I can understand it and extend it
  - Making plots should be easy
- Finding no package that suited me just right, I did what any self-respecting Python programmer would do: rolled up my sleeves and dived in.

John D. Hunter

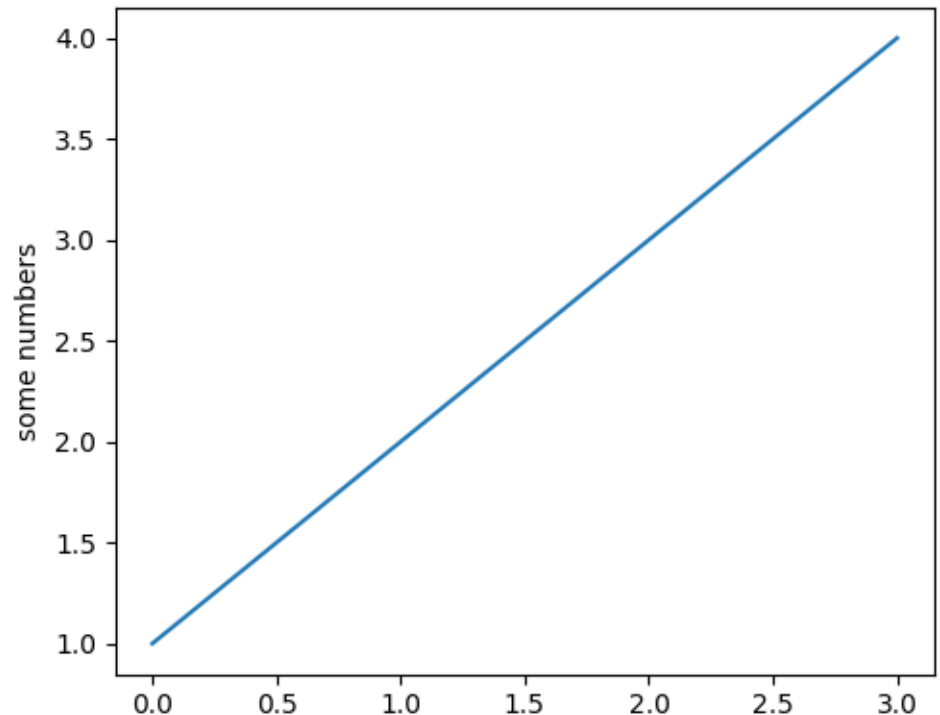
# matplotlib.pyplot

- This is a collection of functions inside matplotlib that make it work like MATLAB
- Each pyplot function makes some change to a figure, e.g.
  - create a figure, create a plotting area, plot lines
- matplotlib.pyplot keeps track of the figure you are working on
- functions calls are directed to the current figure

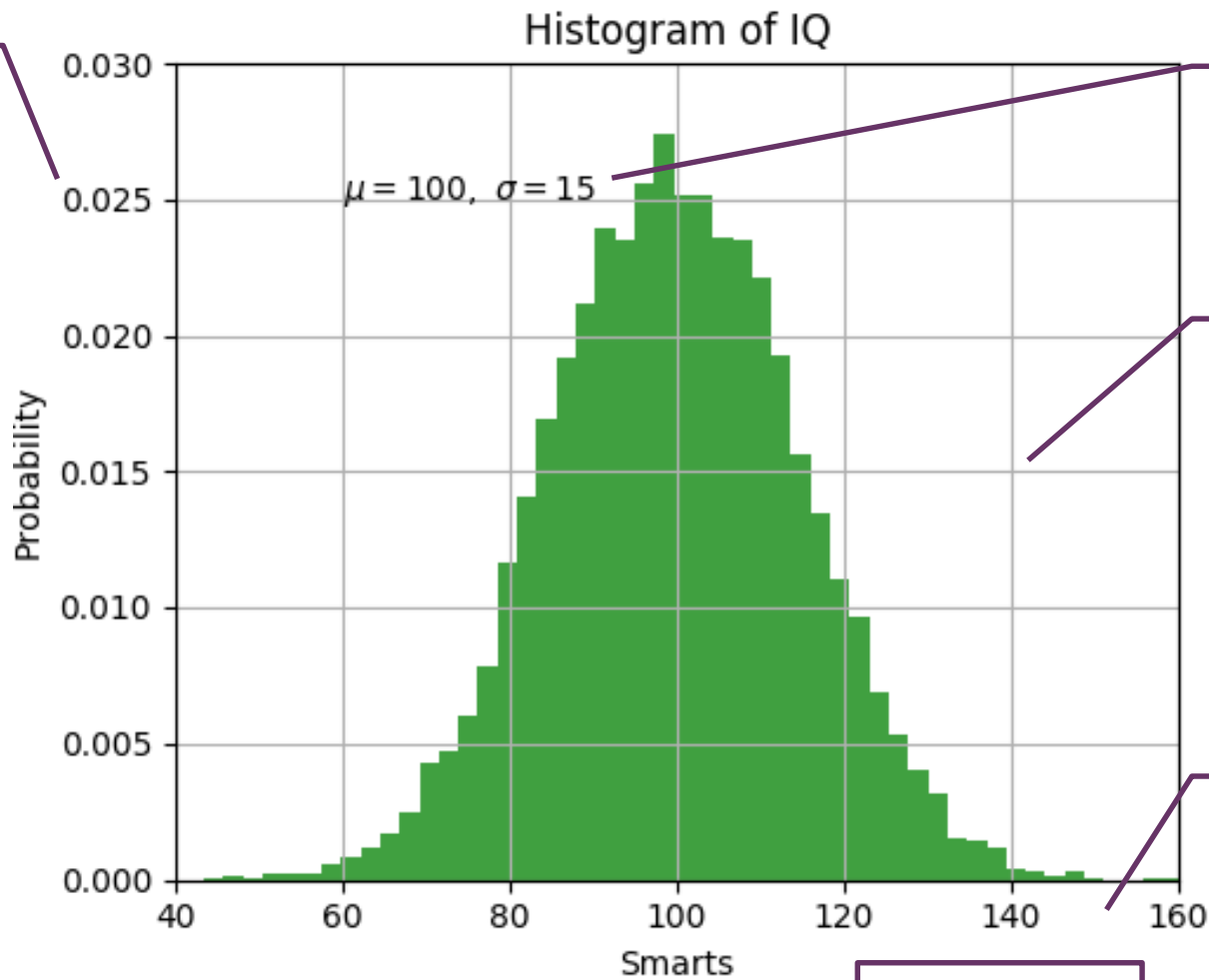
# Line Plot

```
import matplotlib.pyplot as plt
plt.plot([1,2,3,4])
plt.ylabel('Some Numbers')
plt.show()
```

- Assumes supplied values are y-values
- Uses default values for x-values



# Anatomy of a plot



y axis  
0-0.3

Title

text at  
60, 0.025

grid = True

x axis  
40-160

ylabel

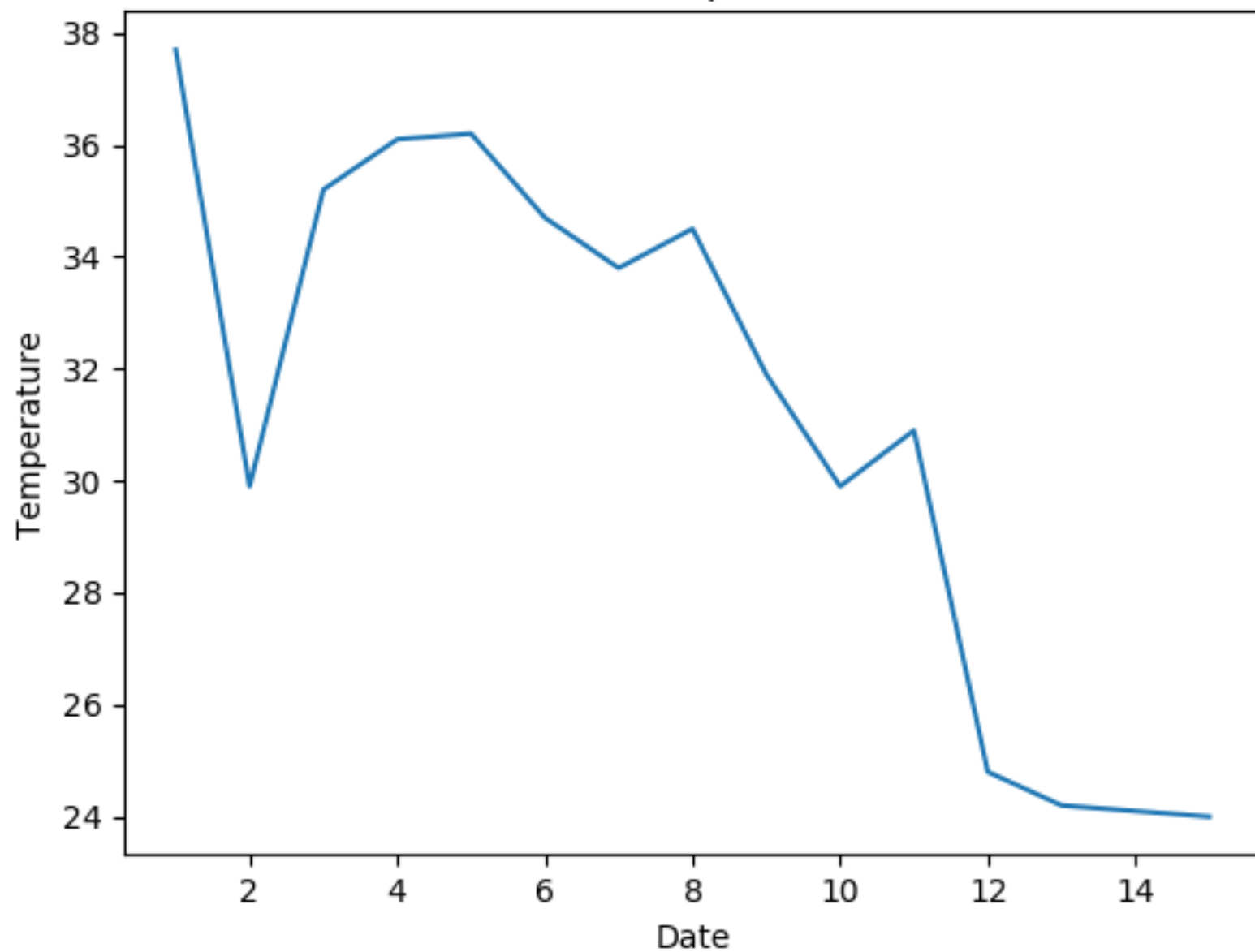
xlabel

# March Temperatures

```
import matplotlib.pyplot as plt
import numpy as np
march2017 = np.array([37.7, 29.9, 35.2,
36.1, 36.2, 34.7, 33.8, 34.5, 31.9, 29.9,
30.9, 24.8, 24.2, 24.1, 24.0])
dates = range(1, len(march2017)+1)
plt.plot(dates, march2017)
plt.title('March Temperatures')
plt.ylabel('Temperature')
plt.xlabel('Date')
plt.show()
.
```



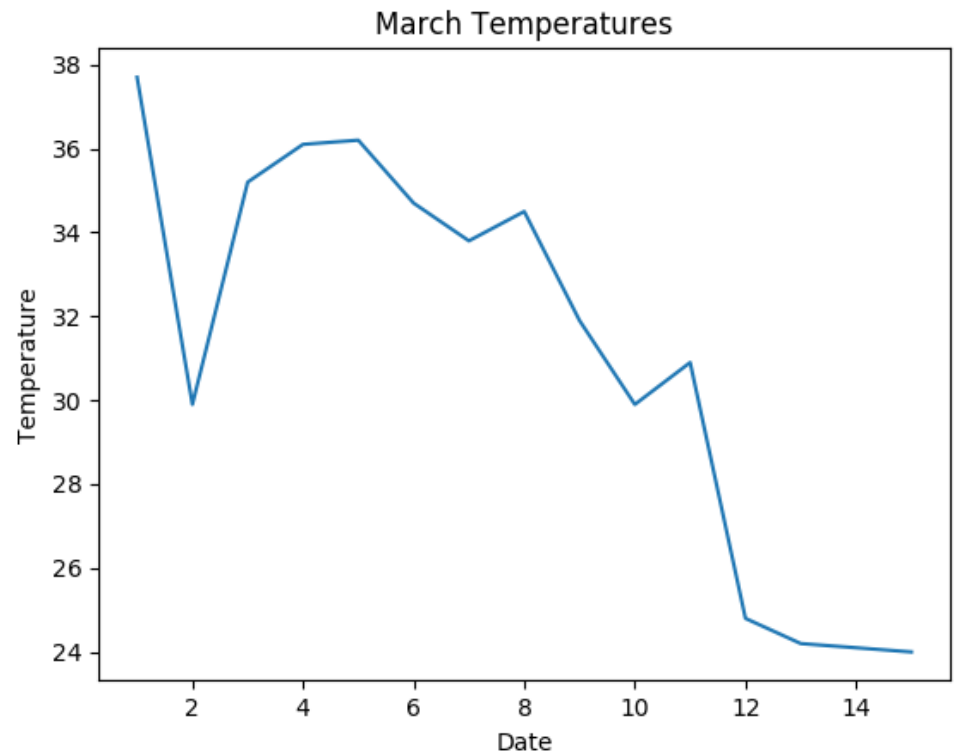
March Temperatures



# March Temperatures

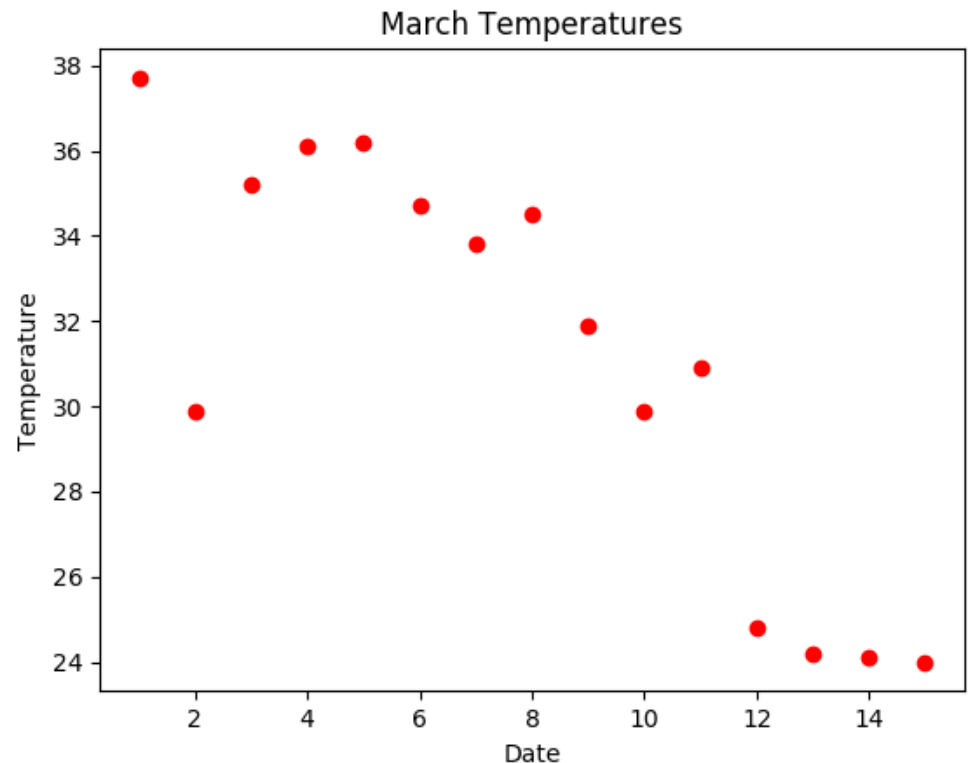
```
import matplotlib.pyplot as plt
import numpy as np
march2017 = np.array([37.7, 29.9, 35.2,
36.1, 36.2, 34.7, 33.8, 34.5, 31.9, 29.9,
30.9, 24.8, 24.2, 2
dates = range(1, 15)
plt.plot(dates, march2017)
plt.title('March Temperatures')
plt.ylabel('Temperature')
plt.xlabel('Date')
plt.show()
```

•



# March Temperatures – red dots

```
dates = range(1, len(march2017)+1)
plt.plot(dates, march2017, 'ro')
plt.title('March Temperatures')
plt.ylabel('Temperature')
plt.xlabel('Date')
plt.show()
```



# Multiple plots on an axis

```
import numpy as np
import matplotlib.pyplot as plt

# evenly sampled time at 200ms intervals
t = np.arange(0., 5., 0.2)
t2 = t**2
t3 = t**3

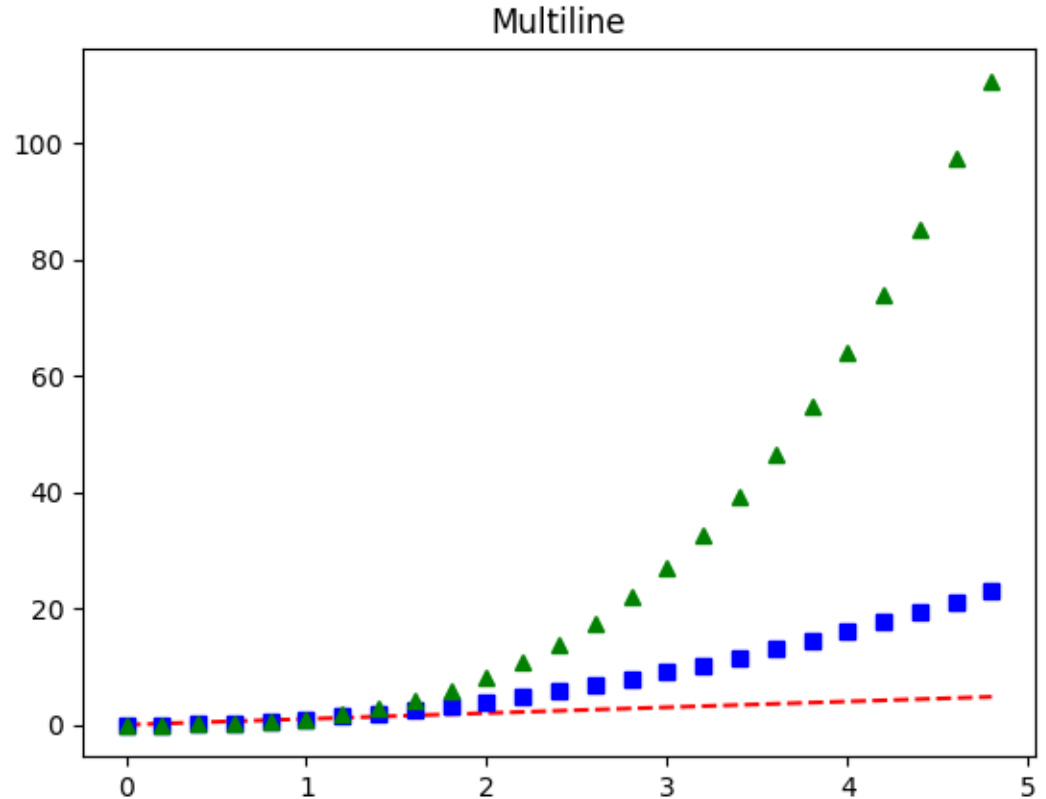
# red dashes, blue squares and green triangles
plt.title('Multiline')
plt.plot(t, t, 'r--', t, t2, 'bs', t, t3, 'g^')
plt.show()
```

# Multiple plots

```
import numpy as np
import matplotlib.pyplot as plt
```

```
# evenly sampled
t = np.arange(0., 5., 0.5)
t2 = t**2
t3 = t**3
```

```
# red dashes, blue squares and green triangles
plt.title('Multiline')
plt.plot(t, t, 'r--', t, t2, 'bs', t, t3, 'g^')
plt.show()
```



# Subplots

```
import matplotlib.pyplot as plt
import numpy as np
march2017 = np.array([37.7, 29.9, 35.2, 36.1, 36.2, 34.7,
33.8, 34.5, 31.9, 29.9, 30.9, 24.8, 24.2, 24.1, 24.0])
dates = range(1, len(march2017)+1)
```

```
plt.figure(1)
plt.subplot(211)
plt.plot(dates, march2017, '--')
plt.title('March Temperatures')
plt.ylabel('Temperature')
```

```
plt.subplot(212)
plt.plot(dates, march2017, 'ro')
plt.ylabel('Temperature')
plt.xlabel('Date')
```

```
plt.show()
```

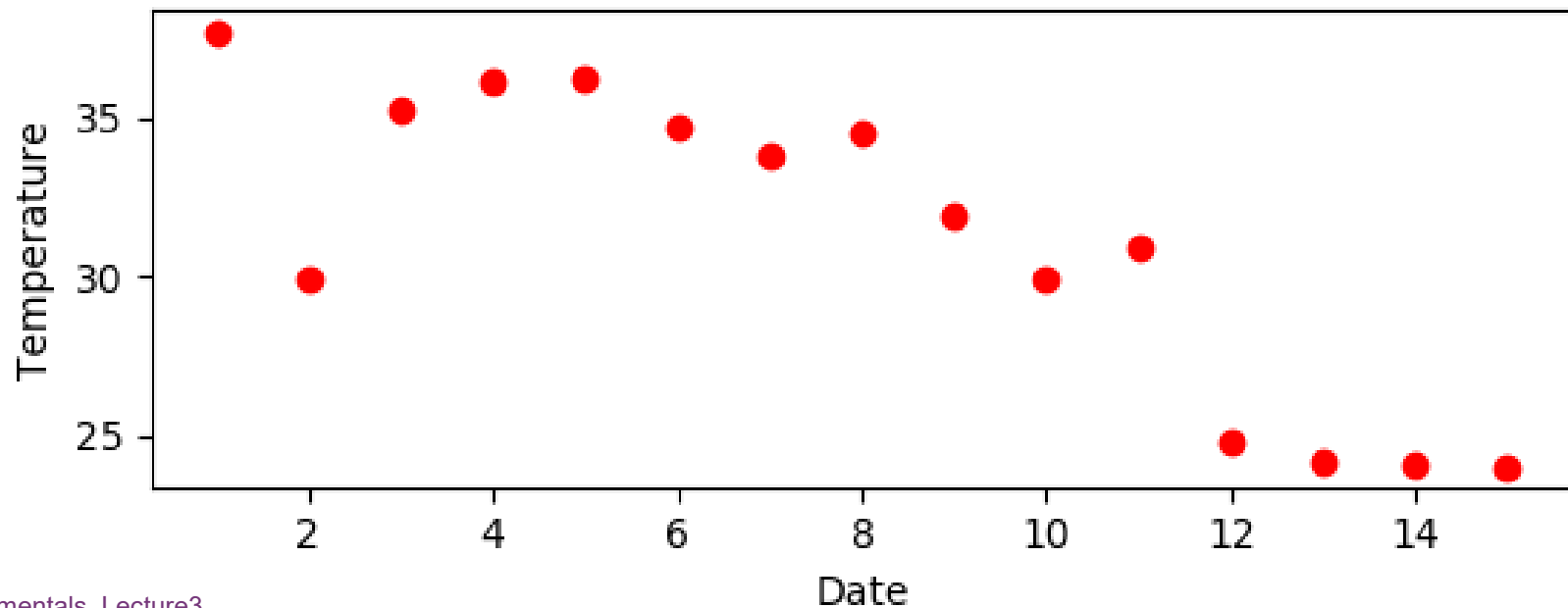
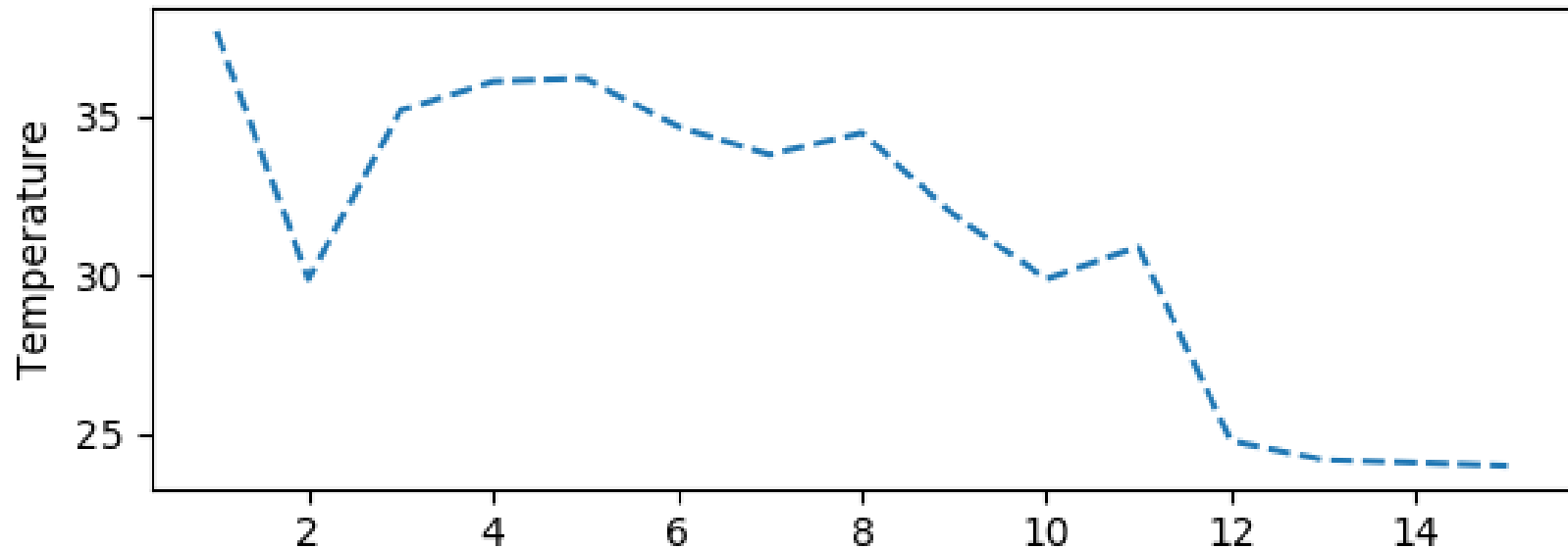
**plt.subplot(211)**

numrows

numcols

subplot #

## March Temperatures



```
plt.figure(1)
plt.subplot(221)
plt.plot(dates, march2017, '--')
plt.title('March Temperatures')
plt.ylabel('Temperature')
```

```
plt.subplot(222)
plt.plot(dates, march2017, 'ro')
plt.ylabel('Temperature')
plt.xlabel('Date')
```

```
plt.subplot(223)
plt.plot(dates, march2017, 'g^')
plt.ylabel('Temperature')
plt.xlabel('Date')
```

```
plt.subplot(224)
plt.plot(dates, march2017, 'bs')
plt.ylabel('Temperature')
plt.xlabel('Date')
```

```
plt.show()
```

# Subplots

## 2x2



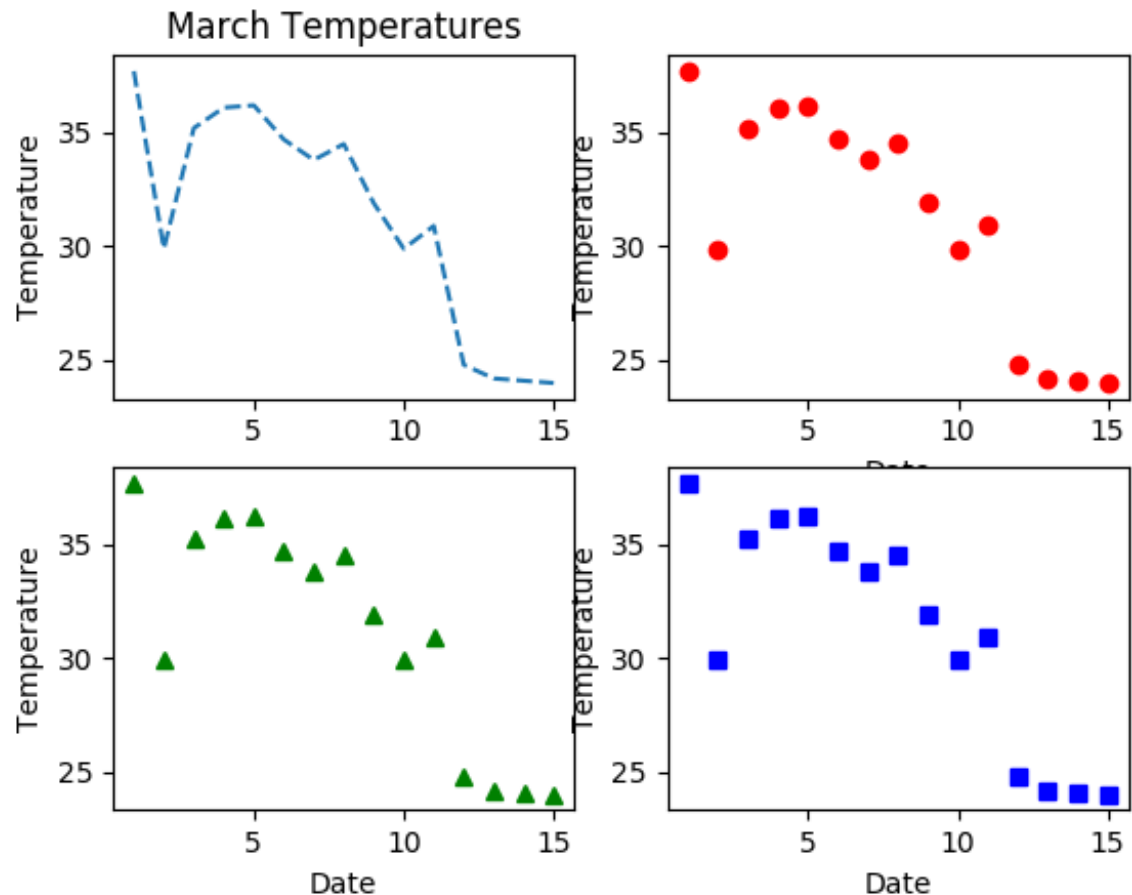
```
plt.figure(1)
plt.subplot(221)
plt.plot(dates, n
plt.title('March
plt.ylabel('Tempe
```

```
plt.subplot(222)
plt.plot(dates, n
plt.ylabel('Tempe
plt.xlabel('Date'
```

```
plt.subplot(223)
plt.plot(dates, n
plt.ylabel('Tempe
plt.xlabel('Date'
```

```
plt.subplot(224)
plt.plot(dates, march2017, 'bs')
plt.ylabel('Temperature')
plt.xlabel('Date')
```

```
plt.show()
```



# Subplots 2x2

# Line Colours, Styles and Markers

```
plt.plot(t,t, 'r--', t,t2, 'bs', t, t3, 'g^')
```

- linestyle or ls [ '-' | '--' | '-.' | ':' | 'steps' | ...]
- markers [ '+' | ',' | '.' | '1' | '2' | '3' | '4' ] s=square  
^=triangle
- colours (short names) ['b' | 'g' | 'r' | 'c' | 'm' | 'y' | 'k' | 'w']
- color='blue'
- color='pink'
- Lots of flexibility on colours – see <http://matplotlib.org/users/colors.html> for more information

# Named Colours

	black
	gray
	silver
	whitesmoke
	rosybrown
	firebrick
	red
	darksalmon
	sienna
	sandybrown
	bisque
	tan
	moccasin
	floralwhite
	gold
	darkkhaki
	lightgoldenrodyellow
	olivedrab
	chartreuse
	palegreen
	darkgreen
	seagreen
	mediumspringgreen
	lightseagreen
	paleturquoise
	darkcyan
	darkturquoise
	deepskyblue
	aliceblue
	slategray
	royalblue
	navy
	blue
	mediumpurple
	darkorchid
	plum
	m
	mediumvioletred
	palevioletred

	k
	grey
	lightgray
	w
	lightcoral
	maroon
	mistyrose
	coral
	seashell
	peachpuff
	darkorange
	navajowhite
	orange
	darkgoldenrod
	lemonchiffon
	ivory
	olive
	yellowgreen
	lawngreen
	lightgreen
	g
	mediumseagreen
	mediumaquamarine
	mediumturquoise
	darkslategray
	c
	cadetblue
	skyblue
	dodgerblue
	slategrey
	ghostwhite
	darkblue
	slateblue
	rebeccapurple
	darkviolet
	violet
	fuchsia
	deeppink
	crimson

	dimgray
	darkgray
	lightgrey
	white
	indianred
	darkred
	salmon
	orangered
	chocolate
	peru
	burlywood
	blanchedalmond
	wheat
	goldenrod
	khaki
	beige
	y
	darkolivegreen
	honeydew
	forestgreen
	green
	springgreen
	aquamarine
	azure
	darkslategrey
	aqua
	powderblue
	lightskyblue
	lightslategray
	lightsteelblue
	lavender
	mediumblue
	darkslateblue
	blueviolet
	mediumorchid
	purple
	magenta
	hotpink
	pink

	dimgrey
	darkgrey
	gainsboro
	snow
	brown
	r
	tomato
	lightsalmon
	saddlebrown
	linen
	antiquewhite
	papayawhip
	oldlace
	cornsilk
	palegoldenrod
	lightyellow
	yellow
	greenyellow
	darkseagreen
	limegreen
	lime
	mintcream
	turquoise
	lightcyan
	teal
	cyan
	lightblue
	steelblue
	lightslategray
	cornflowerblue
	midnightblue
	b
	mediumslateblue
	indigo
	thistle
	darkmagenta
	orchid
	lavenderblush
	lightpink

# Bar Charts

- Uses `plt.bar()` instead of `plt.plot()`

```
plt.bar(x_values,  
        y_values,  
        width,  
        other arguments)
```

- Can also add series' of bars in different colours

# Roll the Dice

```
import matplotlib.pyplot as plt
import random
dice = ['one','two','three','four','five','six']
one, two, three, four, five, six = 0,0,0,0,0,0

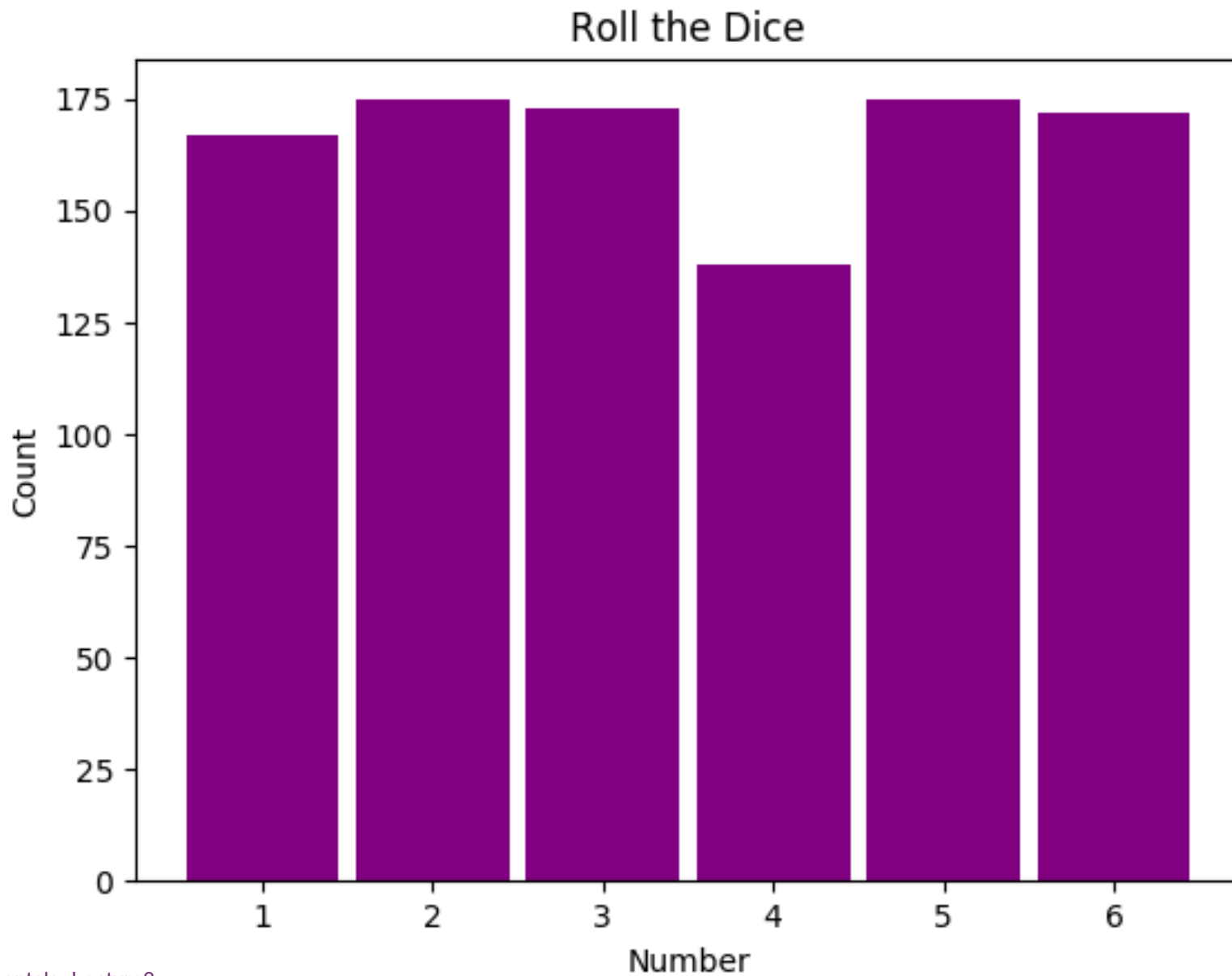
trials = 1000
print('\nDICE TOSS\n')
for index in range(trials):
    choice = random.choice(dice)
    if choice == 'one':
        one += 1
    elif choice == 'two':
        two += 1
    elif choice == 'three':
        three += 1
    elif choice == 'four':
        four += 1
    elif choice == 'five':
        five += 1
    else:
        six += 1
```

# Roll the Dice (continued)

```
print('\nRESULTS\n')
print('1: ', one)
print('2: ', two)
print('3: ', three)
print('4: ', four)
print('5: ', five)
print('6: ', six)
```

```
plt.title('Roll the Dice')
plt.xlabel('Number')
plt.ylabel('Count')
```

```
plt.bar([1, 2, 3, 4, 5, 6], [one, two, three, four,
                             five, six], 0.9, color='purple')
plt.show()
```



# Histograms

- Histograms give us a plot of the frequency of a value or event across a range of possible values
- For example, we could keep track of how many infinite loops occur per practical 😊
- Instead of `plt.plot()`, we use `plt.hist()`  
`plt.hist(data)`
- Default number of bins is 10

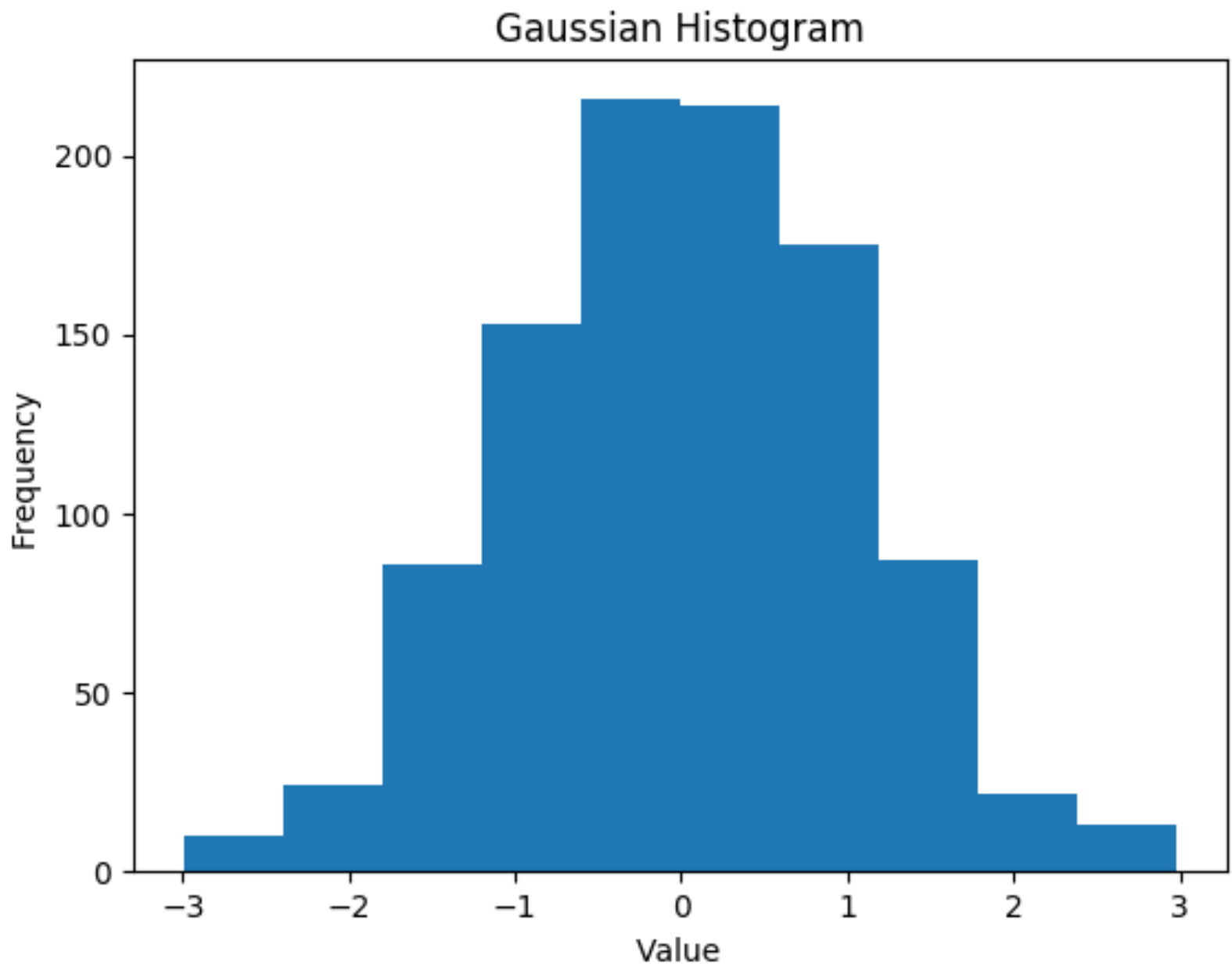


# Basic Histogram

```
import matplotlib.pyplot as plt
from numpy.random import normal

gaussian_numbers = normal(size=1000)

plt.hist(gaussian_numbers)
plt.title("Gaussian Histogram")
plt.xlabel("Value")
plt.ylabel("Frequency")
plt.show()
```



# Histograms

- Can normalize to convert to probabilities

```
plt.hist(data, bins=20, normed=True)
```

- Can make the graph cumulative, so then the probability of the values up to that value

```
plt.hist(data, bins=20, cumulative = True)
```

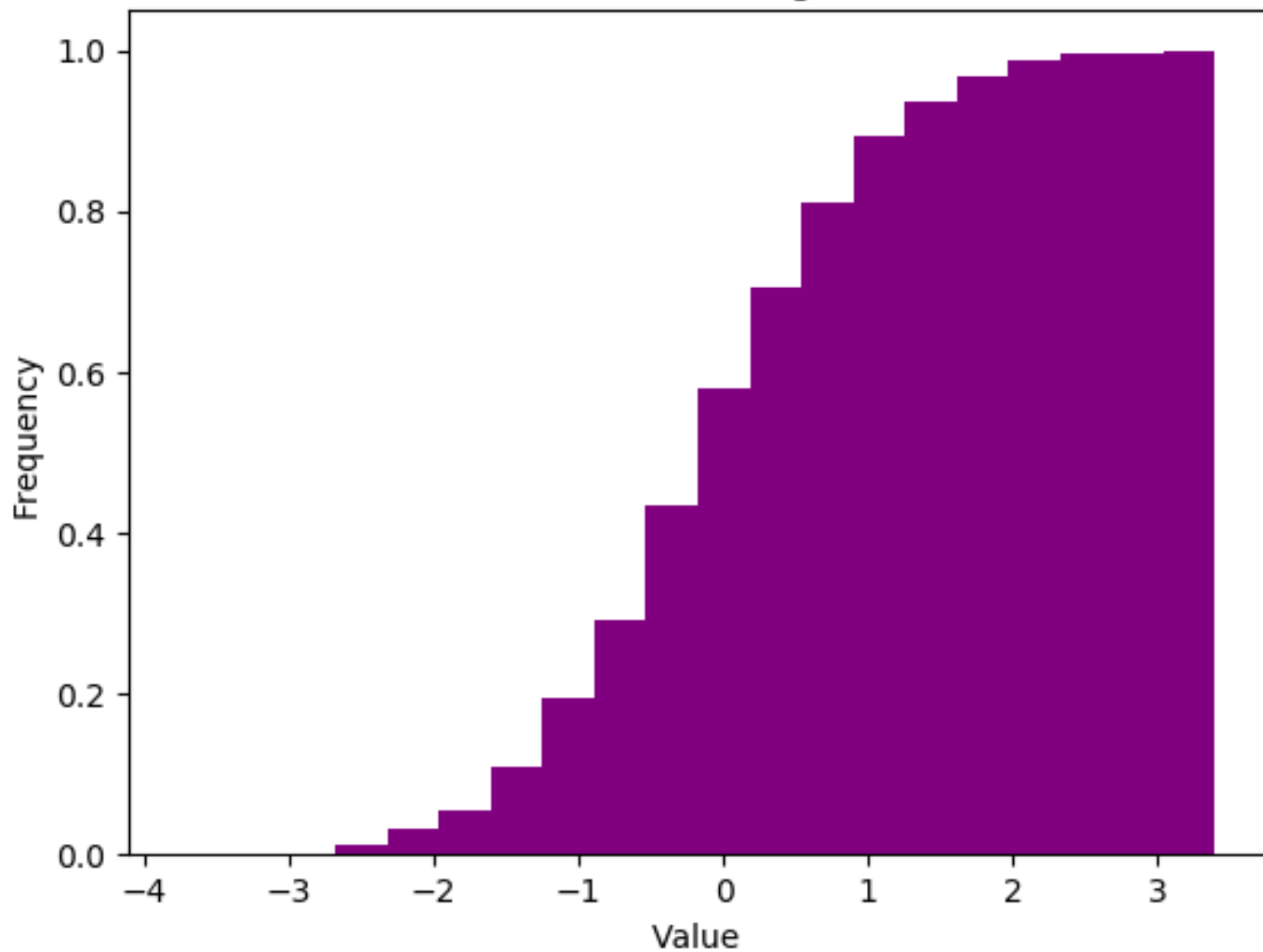
- Change the graph type to be a step outline rather than filled in

```
plt.hist(data, histtype='step', alpha=0.5)
```

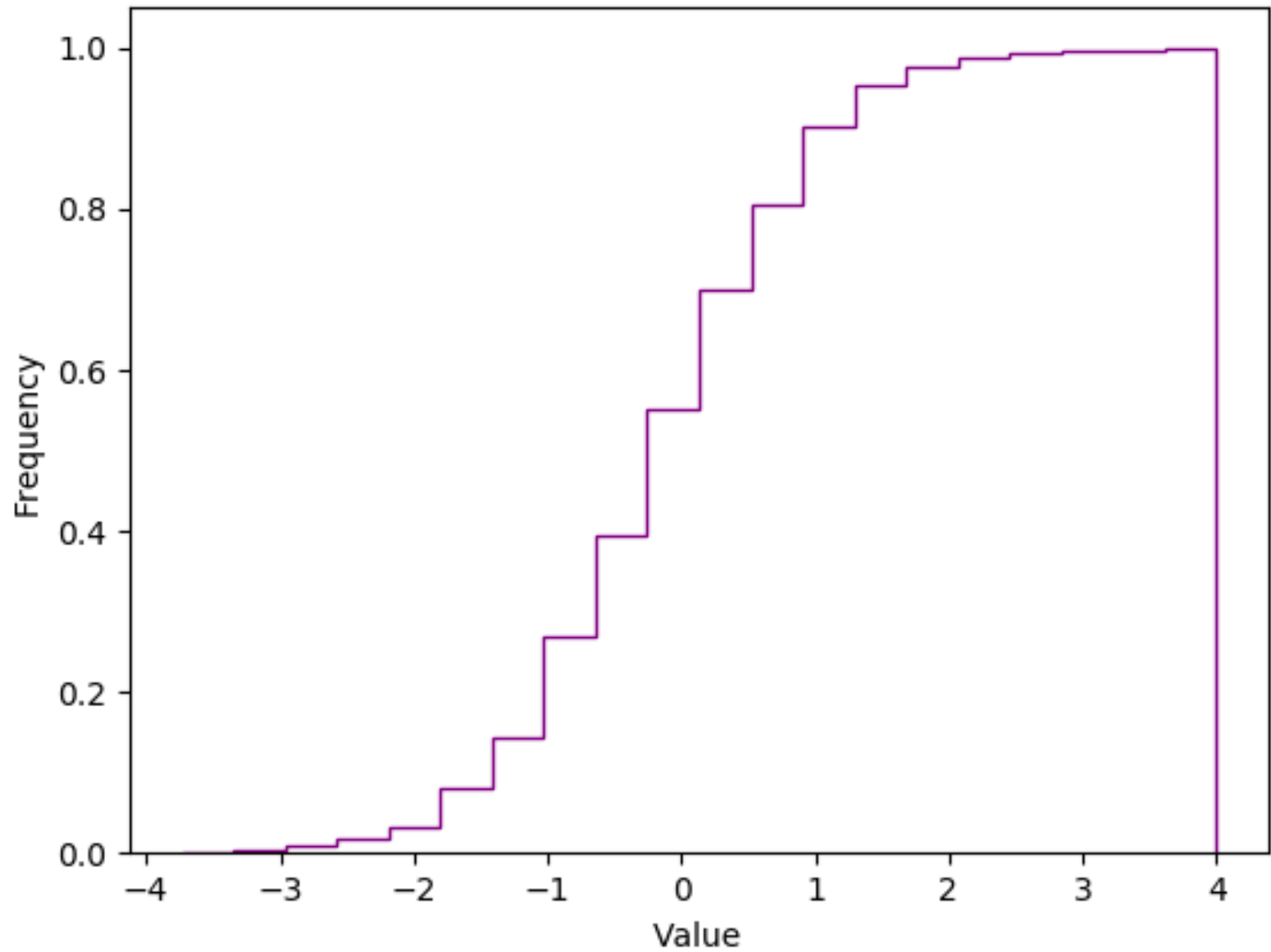
- And, of course, change the colour

```
plt.hist(gaussian_numbers, bins=20,  
         normed=True, cumulative=True,  
         color=['purple'])
```

Gaussian Histogram



## Gaussian Histogram



# EXAMPLE

Fundamentals of Programming  
Lecture 3

# growth.py

```
#  
# growth.py - simulation of unconstrained growth  
#  
import matplotlib.pyplot as plt  
  
print("\nSIMULATION - Unconstrained Growth\n")  
length = 100  
population = 100  
growth_rate = 0.1  
time_step = 0.5  
num_iter = length / time_step  
growth_step = growth_rate * time_step
```

# growth.py

```
print("INITIAL VALUES:\n")
print("Simulation Length (hours): ", length)
print("Initial Population: ", population)
print("Growth Rate (per hour): ", growth_rate)
print("Time Step (part hour per step): ", time_step)
print("Num iterations (length * timestep / hour):", num_iter)
print("Growth step (growthrate per timestep):", growth_step)

print("\nRESULTS:\n")
print("Time: ", 0, " \tGrowth: ", 0, " \tPopulation: ", 100)
times=[0]
pops=[100]
```

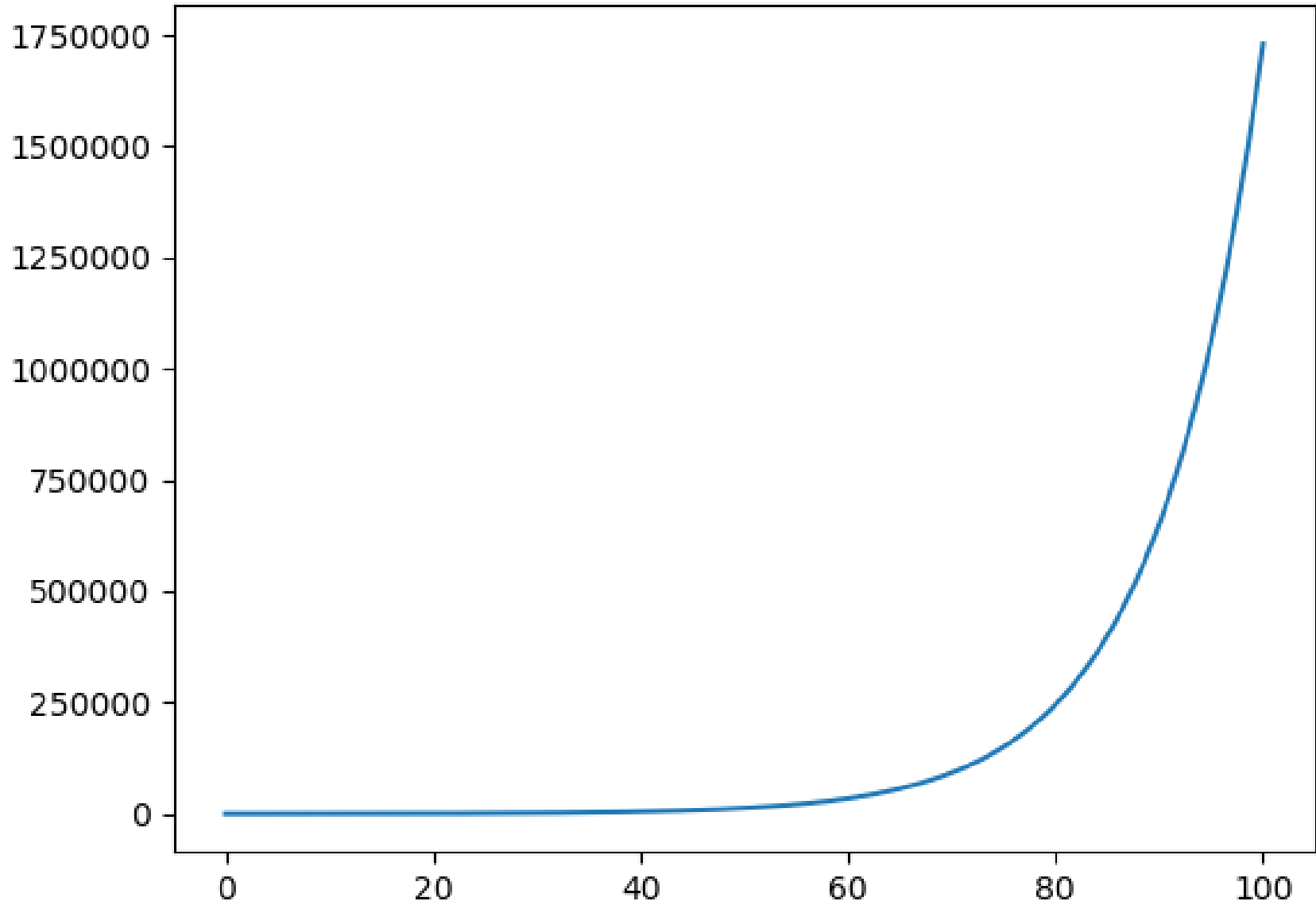


# growth.py

```
for i in range(1, int(num_iter) + 1 ):
    growth = growth_step * population
    population = population + growth
    time = i * time_step
    times.append(time)
    pops.append(population)
    print("Time: ", time, " \tGrowth: ", \
          growth, " \tPopulation: ", population)
print("\nPROCESSING COMPLETE.\n")

plt.title('Unconstrained Growth')
plt.plot(times, pops)
plt.show()
```

## Unconstrained Growth



# Summary

- We've looked at how to use Python arrays as implemented in the Numpy package
- We've looked at how to use simple plotting techniques from the matplotlib package
- We have applied arrays and plotting to more complex systems dynamics problems ... and we'll do more in the practicals

# Practical Sessions

- Practical 2 was quite challenging!
- You will need to spend time on the pracs beyond the 2 hour class
- Labs 218, 219, 220 and 221 are all available to you and have Linux/Python
- Take note of when the FOP practicals are on – you can come in and ask questions
- The Senior Tutors are available 3 hours per day to help students – office near rm 218

# Assessments

- The next assessment will be held during your assigned practical in Week 3/4 (Practical 3)
- It will be a short practical test using the lab computers
- Everyone should be able to get 100%!

# Practical Test 1 - Instructions

- Create files and directories as instructed
  - `mkdir`, `cd`, `vim`
- Create Python program to match the description given
  - e.g. `vim test.py`
- Capture your command history into a file within the `PracTest1` directory
  - e.g. `history > hist.txt`
- Zip your files and submit them through the assessment page
  - `zip PracTest1_12345678 *`

# References

- Weather data :  
<http://www.bom.gov.au/climate/dwo/201703/html/IDCJDW6111.201703.shtml>
- Retail trade figures:  
<http://www.abs.gov.au/AUSSTATS/abs@.nsf/DetailsPage/8501.0Jan%202017?OpenDocument>
- Pyplot tutorial:  
[http://matplotlib.org/users/pyplot\\_tutorial.html](http://matplotlib.org/users/pyplot_tutorial.html)
- Histograms:  
<https://bespokeblog.wordpress.com/2011/07/11/basic-data-plotting-with-matplotlib-part-3-histograms/>

# Next week...

- Multi-dimensional arrays
- More plotting