## Workshop 6

EMTH1019

1. If  $\mathbf{a} = 2\mathbf{i} - \mathbf{j}$  and  $\mathbf{b} = \mathbf{i} + 3\mathbf{j} - 2\mathbf{k}$  find  $\mathbf{a} \times \mathbf{b}$ , then verify that  $\mathbf{a} \times \mathbf{b}$  is orthogonal to  $\mathbf{b}$ .

2. Find the area of the triangle PQR determined by the points P(1,-1,2), Q(2,0,-1) and R(0,2,1).

3. Find the area of the parallelogram formed by the two vectors  $\boldsymbol{u}$  and  $\boldsymbol{v}$ , if  $||\boldsymbol{u}|| = 16$ ,  $||\boldsymbol{v}|| = 4$  and the cosine of the angle between  $\boldsymbol{u}$  and  $\boldsymbol{v}$  is  $\frac{1}{2}$ .

4. Show that the vectors  $\boldsymbol{a}=[1,2,-1],$   $\boldsymbol{b}=[-2,0,3]$  and  $\boldsymbol{c}=[2,-4,-4]$  are coplanar.

5. Given the following matrices

$$A = \begin{bmatrix} 2 & 0 & -1 \\ 4 & -5 & 2 \end{bmatrix} \quad B = \begin{bmatrix} 7 & -5 & 1 \\ 1 & -4 & -3 \end{bmatrix} \quad C = \begin{bmatrix} 1 & 2 \\ -2 & 1 \end{bmatrix}$$

compute each of the following operations if it is defined. If an expression is undefined, explain why.

(i) 
$$A + B$$
 (ii)  $-4B$  (iii)  $AC$  (iv)  $CB$  (v)  $AB^T$  (vi)  $C - 3I_2$  (vii)  $C^2$ 

6. If a matrix A is 6 × 4 and the product AB is 6 × 8, what is the order (dimensions) of B?

7. How many rows does B have if BC is a  $4 \times 3$  matrix?

8. Let  $A=\begin{bmatrix}2&5\\-3&1\end{bmatrix}$  and  $B=\begin{bmatrix}4&-5\\3&k\end{bmatrix}$ . What value(s) of k, if any, will make AB=BA.

9. Verify that A and B are the inverse of one another, if  $A = \begin{bmatrix} 2 & 5 \\ -3 & -7 \end{bmatrix}$  and  $B = \begin{bmatrix} 2 & 5 \\ -3 & -7 \end{bmatrix}$ 

$$\left[\begin{array}{cc} -7 & -5 \\ 3 & 2 \end{array}\right].$$

10. Suppose that A and B are two square matrices such that AB = 0. Show that we must have B = 0 if A is invertible.