

2a

$$x^2 = 25 \quad * \quad x = 5$$

$$\underline{\Leftrightarrow} \quad -5$$

2c

$$a^2 + b^2 = 0 \quad * \quad ab = 0$$

$$\underline{\Rightarrow} \quad \begin{matrix} a=0 \\ b=1 \end{matrix}$$

2e

$$x^3 - x^2 - x + 1 = 0 \quad * \quad x = 1$$

$$-x^2(-x+1) + (-x+1)$$

$$(1-x^2)(1-x) = 0$$

$$\underline{\Leftrightarrow} \quad x = \pm 1$$

2i

$$|x| = x \quad * \quad x \geq 0$$

$$\underline{\Leftrightarrow}$$

2j

$$\sin 2x = \tan x \quad * \quad x = \frac{\pi}{4} + k\frac{\pi}{2}$$

↳ pattern
 $a = \frac{k}{2}$

$$\sin\left(2\left(\frac{\pi}{4} + a\pi\right)\right) = \sin\left(\frac{\pi}{2} + 2a\pi\right) = 1$$

$$\tan\left(\frac{\pi}{4} + a\pi\right) = 1$$

↳ pattern
 $a = \frac{k-1}{2}$

$$\sin\left(2\left(\frac{3\pi}{4} + a\pi\right)\right) = \sin\left(\frac{3\pi}{2} + 2a\pi\right) = -1$$

$$\tan\left(\frac{3\pi}{4} + a\pi\right) = -1$$

$\hookrightarrow 1 = 1 \quad \text{igaz}$
 $\hookrightarrow -1 = -1 \quad \text{igaz}$

$\Rightarrow \quad \Leftarrow \text{igaz}$

$$\sin 2x = \tan x$$

$$2 \sin x \cos x = \frac{\sin x}{\cos x}$$

$$2 \sin x \cos^2 x - \sin x = 0$$

$$\sin x (2 \cos^2 x - 1) = 0$$

$$\hookrightarrow \sin x = 0 \Rightarrow x = 0 + k\pi \quad \text{hamis}$$

$$2 \cos^2 x - 1 = 0 \Rightarrow \cos^2 x = \frac{1}{2} \Rightarrow \cos x = \pm \frac{1}{\sqrt{2}} \Rightarrow x = \frac{\pi}{4} + k\frac{\pi}{2}$$

$\xrightarrow{\text{igaz}} \Rightarrow \Rightarrow \text{hamis}$

$$* = \Leftarrow$$